

### Practice quiz on Types of Functions

TOTAL: 100 POINTS

1. Suppose that  $A = \{1, 2, 10\}$  and  $B = \{4, 8, 40\}$ . Which of the following formulae do **not** define a function  $f: A \rightarrow B$ ?

- ☐  $f(a) = 4a$ , for each  $a \in A$
- ☐  $f(1) = 4, f(2) = 40$ , and  $f(10) = 8$ .
- ☒  $f(1) = 5, f(2) = 8$ , and  $f(10) = 40$ .
- ☐  $f(1) = 4, f(2) = 4$ , and  $f(10) = 4$ .

Correct

A function  $f: A \rightarrow B$  is a rule which assigns an element  $f(a) \in B$  to each  $a \in A$ . In this case, unfortunately,  $f(1) = 5 \notin B$ .

2. Suppose that  $A$  contains every person in the VHS study (see the second video in the course if you're confused here). Suppose that  $Y = \{+, -\}$  and  $Z = \{H, S\}$ .

Suppose that  $T: A \rightarrow Y$  is the function which gives  $T(a) = +$  if person  $a$  tests positive and  $T(a) = -$  if they test negative.

Suppose that  $D: A \rightarrow Z$  is the function which gives  $D(a) = H$  if person  $a$  actually has VHS, and  $D(a) = S$  if the person actually has VHS.

Which of the following must be true of person  $a$  if we have a false positive?

- ☐  $T(a) = -$  and  $D(a) = H$
- ☐  $T(a) = -$  and  $D(a) = S$
- ☒  $T(a) = +$  and  $D(a) = H$
- ☐  $T(a) = +$  and  $D(a) = S$

Correct

Suppose that a false positive is a positive test result for  $T(a) = +$  which is misleading because the person actually does not have the disease ( $D(a) = H$ ).

3. Consider the function  $g: \mathbb{R} \rightarrow \mathbb{R}$  defined by  $g(x) = x^2 - 1$ . Which of the following points are not on the graph of  $g$ ?

- ☐  $(1, 0)$
- ☒  $(2, -1)$
- ☐  $(0, -1)$
- ☐  $(-1, 0)$

Correct

Remember that the graph of  $g$  consists of all points  $(x, y)$  such that  $y = g(x)$ . Here  $g(2) = 3 \neq -1$ , so the point  $(2, -1)$  is **not** on the graph of  $g$ .

4. Let the point  $A = (2, 4)$ . Which of the following graphs does **not** contain the point  $A$ ?

- ☐ The graph of  $g(x) = x + 2$
- ☐ The graph of  $h(x) = x^2$
- ☐ The graph of  $f(x) = 2x$
- ☒ The graph of  $k(x) = x - 1$

Correct

The graph of  $k$  consists of all points  $(x, y)$  such that  $y = k(x)$ . Here  $k(2) = 1 \neq 4$ , so the point  $(2, 4)$  is **not** on the graph of  $k$ .

5. Suppose that  $h(x) = -3x + 4$ . Which of the following statements is true?

- ☐  $h$  is neither a strictly increasing function nor a strictly decreasing function.
- ☐ All statements are correct.
- ☒  $h$  is a strictly decreasing function.
- ☐  $h$  is a strictly increasing function.

Correct

A function  $h$  is called strictly decreasing if whenever  $a < b$ , then  $h(a) > h(b)$ . Since the graph of  $h$  is a line with negative slope, this is in fact true!

6. Suppose that  $f: \mathbb{R} \rightarrow \mathbb{R}$  is a strictly increasing function, with  $f(3) = 15$ .

Which of the following is a possible value for  $f(3.7)$ ?

- ☐ 14.7