

$\log_5 a = \log_5 a$

$\log_5 a$

$\log_a b = 2.5752$ and $\log_{10} b = 1.8$

Therefore, $\log_{10} a$ must equal to $\frac{1.8}{2.5752} = 0.69897$

Treating both sides of equation $\log_{10} a = 0.69897$ as exponents of 10 gives $a = 10^{0.69897} = 5$

10. An investment of 1,600 is worth 7,400 after 8.5 years. What is the continuously compounded rate of return of this investment?

- ☒ 18.02%
☐ 19.01%
☐ 17.01%
☐ 20.01

☒ correct
 $\ln \frac{7400}{1600} = 0.18017$
8.5

11. A pearl grows in an oyster at a continuously compounded rate of .24 per year. If a 25-year old pearl weighs 1 gram, what did it weigh when it began to form?

- ☐ 0.02478
☐ 0.2478
☐ 0.0002478
☒ 0.002478

☒ correct
 $e^{(0.24 \times 25)} = \frac{1}{x}$
 $x = \frac{1}{(e^{0.24 \times 25})}$
 $x = \frac{1}{403.4288}$
 $x = 0.002478$

12. $\log_2 z = 6.754$. What is $\log_{10}(z)$?

- ☐ 1.3508
☐ 0.82956
☐ 0.49185
☒ 2.03316

☒ correct
 $\frac{\log_2 z}{\log_2 10} =$
 $(\log_{10} z) \times (\log_2 10) = 3.321928$
Therefore, $\log_{10} z = \frac{6.754}{3.321928} = 2.0316$

13. Suppose that $g : \mathbb{R} \rightarrow \mathbb{R}$ is a function, and that $g(1) = -10$. Suppose that $g'(x)$ is negative for every single value of x . Which of the following could possibly be $g(1.5)$?

- ☒ $g(1.5) = 9.7$
☐ $g(1.5) = 10.1$
☐ $g(1.5) = 11$
☐ $g(1.5) = 103.4$

☒ correct
Since the slope of the tangent line to the graph of g is negative everywhere on the graph, we know that g is decreasing function! And therefore we must have $g(1.5) < g(1)$. That is the case here, so this value is at least possible.