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NOTE 100%

## Graded quiz on Sets, Number Line, Inequalities, Simplification, and Sigma Notation

NOTE DE LA SOURCESON LA PLUS RÉCENTE 100%

1. Let  $B = \{3, 5, 10, 11, 14\}$ . Is the following statement true or false:  $3 \notin B$  1 / 1 point

☐ True

☒ False

Correct

The symbol  $\notin$  stands for "is not an element of." Since 3 is in an element of the set  $B$ , the given statement is not true.

2. Let  $A = \{1, 3, 5\}$  and  $B = \{3, 5, 10, 11, 14\}$ . Which of the following sets is equal to the union  $A \cup B$ ? 1 / 1 point

☐  $\{1, 10, 18\}$

☐  $\{3, 5, 10, 11, 14\}$

☒  $\{1, 3, 5, 10, 11, 14\}$

☐  $\{1, 3, 5, 3, 5, 10, 11, 14\}$

Correct

The union of two sets consists precisely of the elements that are in at least one of the two sets. That is precisely what is listed here.

3. How many real numbers are there between the integers 1 and 4? 1 / 1 point

☐ 2

☒ Infinitely many

☐ None

☐ 4

Correct

There are in fact infinitely many real numbers between any pair of distinct integers, or indeed any pair of distinct real numbers!

4. Suppose I tell you that  $x$  and  $y$  are two real numbers which make the statement  $x \geq y$  true. Which pair of numbers cannot be values for  $x$  and  $y$ ? 1 / 1 point

☐  $x = 2$  and  $y = 1$

☐  $x = 10$  and  $y = 10$

☒  $x = -1$  and  $y = 0$

☐  $x = 5$  and  $y = 3.3$

Correct

Recall that the statement  $x \geq y$  means that  $x$  is either equal to  $y$  or  $x$  is to the right of  $y$  on the real number line. Since  $-1$  is actually to the left of  $0$ , these cannot be values for  $x$  and  $y$ .

5. Suppose that  $z$  and  $w$  are two positive numbers with  $z < w$ . Which of the following inequalities is false? 1 / 1 point

☒  $-5z < -5w$

☐  $z + 3 < w + 3$

☐  $-z > -w$

☐  $w - 7 > z - 7$

Correct

If we start with  $z < w$  and multiply both sides by  $-5$ , we need to flip the less-than sign, which would give  $-5z > -5w$ . For an example, try  $z = 1$  and  $y = 2$  and see what happens!

6. Find the set of all  $x$  which solve the inequality  $-2x + 5 \leq 7$  1 / 1 point

☐  $x = -1$

☐  $x \geq -6$

☐  $x \leq -1$

☒  $x \geq -1$

Correct

Subtracting 5 from both sides of the given inequality gives  $-2x \leq 2$ . Then we divide both sides by  $-2$ , remembering to flip the inequality sign, and we obtain this answer

7. Which of the following real numbers is not in the closed interval  $[2, 3]$  1 / 1 point

☒ 1

☐ 2.1

☐ 2

☐ 3

Correct

Recall that the closed interval  $[2, 3]$  consists of all real numbers  $x$  which satisfy  $2 \leq x \leq 3$ . Since  $2 \leq 1$  is false,  $1 \notin [2, 3]$

8. Which of the following intervals represents the set of all solutions to:  $-5 \leq x + 2 < 10$ ? 1 / 1 point

☐  $[-7, 8]$

☒  $[-7, 8)$

☐  $[-5, 10)$

☐  $(7, 8)$

Correct

Subtracting 2 from all sides of the inequalities gives  $-7 \leq x < 8$ , and the set of all real numbers  $x$  which make that true is exactly the half-open interval  $[-7, 8)$ .

9. Which of the numbers below is equal to the following summation:  $\sum_{k=2}^5 2k$ ? 1 / 1 point

☐ 10

☐ 4

☒ 28

☐ 14

Correct

We compute  $\sum_{k=2}^5 2k = 4 + 6 + 8 + 10 = 28$ .

10. Suppose we already know that  $\sum_{k=1}^{20} k = 210$ . Which of the numbers below is equal to  $\sum_{k=1}^{20} 2k$ ? 1 / 1 point

☒ 420

☐ 210

☐ 2

☐ 40

Correct

By applying one of our Sigma notation simplification rules, we can rewrite the summation in question as  $2 \sum_{k=1}^{20} k = 2 \times 210 = 420$ .

11. Which of the numbers below is equal to the summation  $\sum_{j=2}^{10} 7$ ? 1 / 1 point

☐ 70

☐ 48

☐ 7

☒ 63