KCET 2022 Solved Paper

Mathematics

Question 1

If all permutations of the letters of the word MASK are arranged in the order as in dictionary with or without meaning, which one of the following is $19^{\, \rm th}$ word?

Options:

A. KAMS

B. AKMS

C. SAKM

D. AMSK

Answer: C

Solution:

Solution:

AKMS

 $A \rightarrow 3$!

 $K \rightarrow 3!$

 $M \rightarrow 3!$

 $SAKM \rightarrow \frac{1}{19}$

Question 2

If a_1 , a_2 , a_3 , ..., a_{10} is a geometric progression and $\frac{a_3}{a_1}=25$, then $\frac{a_9}{a_5}$ equals

Options:

A. $3(5^2)$

B. 5^{3}

C. 5^4

D. $2(5^2)$

Answer: C

$$\frac{a_3}{a_1} = 25$$

$$\frac{ar^2}{a} = 25$$

$$r^2 = 5^2$$

$$\frac{a_4}{a_5} = \frac{ar^8}{ar^4} = r^4 = 5^4$$

.....

Question 3

If the straight line 2x - 3y + 17 = 0 is perpendicular to the line passing through the points (7, 17) and (15, β), then β equals

Options:

- A. -5
- B. 29
- C. 5
- D. -29

Answer: C

Solution:

Solution:

The slope of the line 2x - 3y + 17 = 0 is m_1 .

The slope of line joining the points (7, 17) and (15, β) is $\frac{\beta-17}{15-7} = \frac{\beta-17}{8} = m_2$

From the question given,

$$m_1 m_2 = -1$$

Now,

$$\Rightarrow \frac{2}{3} \times \frac{\beta - 17}{8} = -1$$

$$\Rightarrow \beta - 17 = -12$$

Question 4

The octant in which the point (2, -4, -7) lies is

Options:

- A. Eighth
- B. Fourth

\sim	TT-1.
	Third
·	1 IIII U

D. Fift

Answer: A

Solution:

Solution:

Here x is positive, y is negative and z is negative.

So, it lies in VIII octant.

Question 5

If f (x) = $\begin{cases} x^2 - 1 & 0 < x < 2 \\ 2x + 3 & 2 \le x < 3. \end{cases}$ the quadratic equation whose roots are $\lim_{x \to 2^-} f(x)$

and $\lim_{x \to 2^+} f(x)$ is

Options:

A.
$$x^2 - 14x + 49 = 0$$

B.
$$x^2 - 6x + 9 = 0$$

C.
$$x^2 - 10x + 21 = 0$$

D.
$$x^2 - 7x + 8 = 0$$

Answer: C

Solution:

Solution:

$$\alpha = \lim_{x \to 2^{-}} f(x) = \lim_{x \to 2} x^{2} - 1 = 3$$

$$\beta = \lim_{x \to 2^{-}} f(x) = \lim_{x \to 2} 2x + 3 = 7$$

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2 - 10x + 21 = 0$$

.....

Question 6

If 3x + i(4x - y) = 6 - i where x and y are real numbers, then the values of x and y are respectively,

Options:

A. 3,9

B. 2,9

C.	2.4
◡.	2 , 1

D. 3,4

Answer: B

Solution:

Solution:

$$3x = 6$$

$$x = 2$$

$$4x - y = -1$$

$$8 - y = -1$$

9 = y

.....

Question 7

If the standard deviation of the numbers -1, 0, 1, k is $\sqrt{5}$ where k > 0, then k is equal to

Options:

A.
$$4\sqrt{\frac{5}{3}}$$

B.
$$2\sqrt{\frac{10}{3}}$$

D.
$$2\sqrt{6}$$

Answer: D

Solution:

$$\sigma^2 = 5, \bar{x} = \frac{k}{4}$$

$$\frac{1}{4}(1+0+1+k^2) - \frac{k^2}{16} = 5$$

$$\frac{k^2+2}{4} \frac{-k^2}{16} = 5$$

$$\frac{4k^2 + 8 - k^2}{16} = 5$$

$$\Rightarrow 3k^2 + 8 = 80$$

$$3k^2 = 72$$

$$1-2-24$$

$$k = \pm \sqrt{24} = 2\sqrt{6}$$

Question 8

If the set x contains 7 elements and set y contains 8 elements, then the number of bijections from x to y is

Options:

A. 0

B. 7!

C. 8P₇

D. 8!

Answer: A

Solution:

Solution:

 $n(A) \neq n(B)$

Number of bijections is zero

Question 9

If $f : R \rightarrow R$ be defined by

$$\mathbf{f(x)} = \begin{cases} 2x & : x > 3 \\ x^2 & : 1 < x \le 3 \\ 3x & : x \le 1. \end{cases}$$

then f(-1) + f(2) + f(4) is

Options:

A. 5

B. 9

C. 10

D. 14

Answer: B

Solution:

$$f(-1) = 3(-1) = -3$$

$$f(2) = 2^{2} = 4$$

$$f(4) = 2(4) = 8$$

$$f(-1) + f(2) + f(4)$$

=-3+4+8=9

.....

Question 10

Let the relation R is defined in N by aRb, if 3a + 2b = 27 then R is Options:

A. $\{(1, 12)(3, 9)(5, 6)(7, 3)\}$

B. $\{(1, 12)(3, 9)(5, 6)(7, 3)(9, 0)\}$

C. $\left\{ \left(0, \frac{27}{2}\right)(1, 12)(3, 9)(5, 6)(7, 3) \right\}$

D. $\{(2, 1)(9, 3)(6, 5)(3, 7)\}$

Answer: A

Solution:

Solution:

2b = 27 - 3a

$$b = \frac{27 - 3a}{2}$$

 $R = \{(1, 2), (3, 9), (5, 6), (7, 3)\}$

Question 11

$$\lim_{y \to 0} \frac{\sqrt{3 + y^3} - \sqrt{3}}{y^3} =$$

Options:

A.
$$\frac{1}{2\sqrt{3}}$$

B.
$$2\sqrt{3}$$

C.
$$\frac{1}{3\sqrt{2}}$$

D.
$$3\sqrt{2}$$

Answer: A

$$\lim_{y \to 0} \frac{3 + y^3 - 3}{y(\sqrt{3 + y^3} + \sqrt{3})} = \frac{1}{2\sqrt{3}}$$

Question 12

If A is a matrix of order 3×3 , then $(A^2)^{-1}$ is equal to

Options:

- A. $(-A^2)^2$
- $B. A^2$
- C. $(A^{-1})^2$
- D. $(-A)^{-2}$

Answer: C

Solution:

Solution:

$$(A^2)^{-1} = (A^{-1})^2$$

Question 13

If $A = \begin{bmatrix} 2 & -1 \\ 3 & -2 \end{bmatrix}$, then the inverse of the matrix A^3 is

Options:

- A. A
- B. 1
- C. -1
- D. -A

Answer: A

Solution:

$$A = \left[\begin{array}{cc} 2 & -1 \\ 3 & -2 \end{array} \right]$$

$$A^{-1} = \frac{1}{-1} \begin{bmatrix} -2 & 1 \\ -3 & 2 \end{bmatrix} = \begin{bmatrix} 2 & -1 \\ 3 & -2 \end{bmatrix} = A$$

$$A^2 = \left[\begin{array}{cc} 2 & -1 \\ 3 & -2 \end{array} \right] \left[\begin{array}{cc} 2 & -1 \\ 3 & -2 \end{array} \right]$$

$$= \begin{bmatrix} 4-3 & -2+2 \\ 6-6 & -3+4 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I$$

$$A^3 = A$$

$$(A^3)^{-1} = A^{-1} = \begin{bmatrix} 2 & -1 \\ 3 & -2 \end{bmatrix}^{-1} = \begin{bmatrix} -2 & 1 \\ -3 & 2 \end{bmatrix}$$

$$=-A$$

$$\therefore (A^3)^{-1} = -A$$

Question 14

If A is a skew symmetric matrix, then A^{2021} is

Options:

- A. Row matrix
- B. Symmetric matrix
- C. Column matrix
- D. Skew symmetric matrix

Answer: D

Solution:

Solution:

 $A^{T} = -A$ or A^{n} is slow symmetric if n is odd

$$P = A^{2021}$$

$$P^{T} = [A^{2021}]^{T} = [A^{T}]^{2021} = (-A)^{2021} = -P$$

Question 15

If
$$A = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}$$
 then $(aI + bA)^n$ is (where I is the identity matrix of order 2)

Options:

A.
$$a^2I + a^{n-1}b \cdot A$$

B.
$$a^nI + na^nbA$$

C.
$$a^n I + n \cdot a^{n-1} b \cdot A$$

D.
$$a^n I + b^n A$$

Answer: C

Solution:

Solution:

$$A = \left[\begin{array}{cc} 0 & 1 \\ 0 & 0 \end{array} \right]$$

$$[aI + bA]^{1} = \begin{bmatrix} a & 0 \\ 0 & a \end{bmatrix} + \begin{bmatrix} 0 & b \\ 0 & 0 \end{bmatrix} = \begin{bmatrix} a & b \\ 0 & a \end{bmatrix}$$

$$[aI + IA]^2 = \begin{bmatrix} a & b \\ 0 & a \end{bmatrix} \begin{bmatrix} a & b \\ 0 & a \end{bmatrix} = \begin{bmatrix} a^2 & 2ab \\ 0 & a^2 \end{bmatrix}$$

$$[aI + bA]^3 = \begin{bmatrix} a^2 & 2ab \\ 0 & a^2 \end{bmatrix} \begin{bmatrix} a & b \\ 0 & a \end{bmatrix} = \begin{bmatrix} a^3 & 3^2b \\ 0 & a^3 \end{bmatrix}$$

$$\therefore [aI + bA]^n = \begin{bmatrix} a^n & naa^{n-1}b \\ 0 & a^n \end{bmatrix}$$

$$= a^n I + n \cdot a^{n-1} b A$$

Question 16

If A is a 3×3 matrix such that $|5 \cdot adj A| = 5$ then |A| is equal to Options:

A.
$$\pm 1$$

B.
$$\pm 1 / 5$$

$$C. \pm 1 / 25$$

$$D. \pm 5$$

Answer: B

Solution:

$$A_{3\times3}$$
 matrix $|5. Adj A| = 5$

$$\Rightarrow 5^3 |A|^2 = 5$$

$$\Rightarrow |A^2| = \frac{1}{5^2}$$

$$|A| = \pm \frac{1}{5}$$

Question 17

If there are two values of 'a 'which makes determinant

$$\Delta = \begin{bmatrix} 1 & -2 & 5 \\ 2 & a & -1 \\ 0 & 4 & 2a \end{bmatrix} = 86 \text{ Then the sum of these numbers is}$$

Options:

- A. -4
- B. 4
- C. 9
- D. 5

Answer: A

Solution:

Solution:

$$\Delta = 1(2a^2 + 4) + 2(4a - 0) + 5(8) = 86$$

$$2a^2 + 8a + 44 - 86 = 0$$

$$2a^2 + 8a - 42 = 0$$

$$a^2 + 4a - 21 = 0$$

Sum of numbers $=-4\left(:-\frac{b}{a}=\alpha+\beta\right)$

Question 18

If the vertices of a triangle are (-2, 6)(3, -6) and (1, 5), then the area of the triangle is

Options:

- A. 40 sq. units
- B. 30 sq. units
- C. 15.5 sq. units
- D. 35 sq. units

Answer: C

Solution:

$$\Delta = \frac{1}{2} \begin{vmatrix} -2 - 3 & -2 - 1 \\ 6 + 6 & 6 - 5 \end{vmatrix} = \frac{1}{5} \begin{vmatrix} -5 & -3 \\ 12 & 1 \end{vmatrix}$$
$$= \frac{1}{2} \begin{vmatrix} -5 + 36 \end{vmatrix} = \frac{31}{2} = 15.5$$

Question 19

Domain of $\cos^{-1}[x]$ is, where [.] denotes a greatest integer function

Options:

- A. (-1, 2]
- B. [-1, 2]
- C. (-1, 2)
- D. [-1, 2)

Answer: D

Solution:

Solution:

 $\cos^{-1}[x]$

 $-1 \le [x] \le 1$

 $\Rightarrow [x] = \{-1, 0, 1\}$

 $x \in [-1, 2)$

Question 20

If $y = (1 + x^2) \tan^{-1} x - x$ then $\frac{dy}{dx}$ is

Options:

- A. $2xtan^{-1}x$
- B. $x^2 tan^{-1}x$
- C. $\frac{\tan^{-1}x}{x}$
- D. xtan⁻¹x

Answer: A

Solution:

$$y = (1+x^{2})\tan^{-1}x - x$$

$$\frac{dy}{dx} = \frac{(1+x^{2})}{1+x^{2}} + \tan^{-1}x \cdot (2x) - 1$$

$$= 2x\tan^{-1}x$$

Question 21

If $x = e^{\theta} \sin \theta$, $y = e^{\theta} \cos \theta$ where θ is a parameter, then $\frac{dy}{dx}$ at (1, 1) is equal to

Options:

A. 0

B.
$$-\frac{1}{2}$$

C. $\frac{1}{2}$

D.
$$-\frac{1}{4}$$

Answer: A

Solution:

Solution:

$$x = e^{\theta} \sin \theta = 1$$
$$y = e^{\theta} \cos \theta = 1, \ \frac{x}{y} = \tan \theta = 1$$

$$\Rightarrow \theta = \frac{\pi}{4}$$

$$\frac{dy}{dx} = \left| \frac{dy/d\theta}{dx/d\theta} \right| = \frac{-e^{\theta} \sin \theta + \cos \theta \cdot e^{\theta}}{e^{\theta} \cos \theta + \sin \theta e^{\theta}} = \frac{\cos \theta - \sin \theta}{\cos \theta + \sin \theta}$$

$$=\tan\left(\frac{\pi}{4}-\theta\right)=0$$

Question 22

If $y = e^{\sqrt{x\sqrt{x\sqrt{x}}}}x > 1$ then $\frac{d^2y}{dx^2}$ at $x = \log_e^3$ is

Options:

A. 3

B. 0

C. 5

D. 1

Answer: A

Solution:

$$e^{x^{\frac{1}{2}\left[1 - \frac{1}{2} + \frac{1}{4} + ...\right]}} = e^{x^{\frac{1}{2}}} = e^{x^{1}} = e^{x}$$

$$\frac{dy}{dx} = e^{x}$$

$$\frac{d^{2}y}{dxx^{2}} = e^{x}x\log_{e}^{3} = e^{\log_{e}^{3}} =$$

Question 23

If f(1) = 1, f'(1) = 3 then the derivative of $f(f(f(x))) + (f(x))^2$ at x = 1 is Options:

A. 10

B. 35

C. 33

D. 12

Answer: C

Solution:

Solution:

$$f(1) = 1, f'(1) = 3$$

$$\frac{d}{dx} [f(f(f(x))) + (f(x))^{2}]$$

$$[f'(f(f(x))) \cdot f'f(x) \cdot f'(x) + 2f(x) \cdot f'(x)]$$

$$= f'(f(f(1)))f'(f(1)) \cdot f'(1) + 2f(1) \cdot f'(1)$$

$$f'(f(1))f'(1) \cdot 3 + 2 \cdot (1)3$$

$$= f'(1) \cdot 3 \cdot 3 + 6$$

$$= 27 + 6 = 33$$

Question 24

If $y = x^{\sin x} + (\sin x)^x$ then $\frac{dy}{dx}$ at $x = \frac{\pi}{2}$ is

Options:

A. $\frac{4}{\pi}$

B. 1

C.
$$\pi \log \frac{\pi}{2}$$

D.
$$\frac{\pi^2}{2}$$

Answer: B

Solution:

Solution:

$$y = x^{\sin x} + (\sin x)^{x}$$

$$\frac{dy}{dx} = [x^{\sin x}] \left[\frac{\sin x}{x} + \cos x \cdot \log x \right] + (\sin x)^{x} [x \cos x + \log \sin x]$$

$$x = \frac{\pi}{2}$$

$$=\frac{\pi}{2}\left[\frac{2}{\pi}\right]+1[0+0]=1$$

.....

Question 25

If
$$A_n = \begin{bmatrix} 1-n & n \\ n & 1-n \end{bmatrix}$$
 then $A_1 | +A_2 | +... + A_{2021} | =$

Options:

A.
$$-2021$$

C.
$$-(2021)^2$$

D. 4042

Answer: C

Solution:

Solution:

$$A_n = \begin{bmatrix} 1-n & n \\ n & 1-n \end{bmatrix}$$
$$|A_n| = (1-n)^2 - n^2$$

$$=1+n^2-2n-n^2$$

Question 26

The function f (x) = $log(1 + x) - \frac{2x}{2 + x}$ is increasing on

Options:

A. $(-\infty, \infty)$

B. (-1, ∞)

C. $(\infty, -1)$

D. $(-\infty, 0)$

Answer: B

Solution:

Solution:

$$f'(x) = \frac{x^2}{(x+1)(2+x)^2} > 0$$
$$x+1 > 0 \Rightarrow x > -1$$

Question 27

The co-ordinates of the point on the $\sqrt{x} + \sqrt{y} = 6$ at which the tangent is equally inclined the axes is

Options:

A. (4, 4)

B. (9, 9)

C. (1, 1)

D. (6, 6)

Answer: B

Solution:

Solution:

$$\frac{dy}{dx} = -\sqrt{\frac{y}{x}} = -1$$

y = x

$$\sqrt{x} + \sqrt{x} = 6$$

x = 9, y = 9

Question 28

The function $f(x) = 4\sin^3 x - 6\sin^2 x + 12\sin x + 100$ is strictly

Options:

- A. decreasing in $\left[\begin{array}{c} -\pi \\ \overline{2} \end{array}, \begin{array}{c} \pi \\ \overline{2} \end{array} \right]$
- B. increasing in $\left(\pi, \frac{3\pi}{2}\right)$
- C. decreasing in $\left[0, \frac{\pi}{2}\right]$
- D. decreasing in $\left(\frac{\pi}{2}, \pi\right)$

Answer: D

Solution:

Solution:

```
f'(x) = (12\sin^2 x - 12\sin x + 12)\cos x
f'(x) = 12(\sin^2 x - \sin x + 1)\cos x
\sin^2 x - \sin x + 1 > 0
x \in \left(\frac{\pi}{2}, \pi\right)\cos x < 0
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Question 29

If [x] is the greatest integer function not greater than x then $\int_0^8 [x] dx$ is equal to

Options:

A. 28

B. 29

C. 30

D. 20

Answer: A

Solution:

Solution:

$$\int_{0}^{8} [x]dx = 1 + 2 + 3 + \dots + 7$$
$$= \frac{7(7+1)}{2} = 28$$

Question 30

Options:

A.
$$\frac{8}{23}$$

B.
$$\frac{8}{21}$$

C.
$$\frac{7}{23}$$

D.
$$\frac{7}{21}$$

Answer: B

Solution:

Solution:

Put $\sin \theta = t$

$$\int_0^1 t^{1/2} (1 - t^2) dt = \frac{8}{21}$$

Question 31

If $e^y + xy = e$ the ordered pair $\left(\frac{dy}{dx}, \frac{d^2y}{dx^2}\right)$ at x = 0 is equal to

Options:

A.
$$\left(\frac{1}{e}, \frac{1}{e^2}\right)$$

B.
$$\left(\frac{1}{e}, \frac{-1}{e^2}\right)$$

C.
$$\left(\frac{-1}{e}, \frac{-1}{e^2}\right)$$

D.
$$\left(\frac{-1}{e}, \frac{1}{e^2}\right)$$

Answer: D

Solution:

$$\frac{dy}{dx} = \frac{-y}{e^y + x}$$

$$\left(\frac{dy}{dx}\right)_{(0,1)} = -\frac{1}{e}$$

$$\left(\frac{d^2y}{dx^2}\right)_{(0,1)} = \frac{1}{e^2}$$

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Question 32

 $\int \frac{\cos 2x - \cos 2\alpha}{\cos x - \cos \alpha} dx \text{ is equal to}$

Options:

A. $2(\sin x - x \cos \alpha) + c$

B. $2(\sin x - 2x\cos\alpha) + c$

C. $2(\sin x + x \cos \alpha) + c$

D. $2(\sin x + 2x\cos\alpha) + c$

Answer: C

Solution:

Solution:

$$2\int \frac{\cos^2 x - \cos^2 \alpha}{\cos x - \cos \alpha} dx = 2\int (\cos x + \cos \alpha) dx$$

 $= 2[\sin x + x \cos \alpha]$

Question 33

 $\int_{0}^{1} \frac{xe^{x}}{(2+x)^{3}} dx \text{ is equal to}$

Options:

A.
$$\frac{1}{27}$$
, e - $\frac{1}{8}$

B.
$$\frac{1}{9} \cdot e + \frac{1}{4}$$

C.
$$\frac{1}{27} \cdot c + \frac{1}{8}$$

D.
$$\frac{1}{9} \cdot e - \frac{1}{4}$$

Answer: D

$$\int_{0}^{1} e^{x} \left[\frac{1}{(x+2)^{2}} - \frac{2}{(x+2)^{3}} \right] dx$$
$$= \left[\frac{e^{x}}{(x+2)^{2}} \right]_{0}^{1} = \frac{e}{9} - \frac{1}{4}$$

Question 34

If
$$\int \frac{dx}{(x+2)(x^2+1)} = a \log 1 + x^2 + b \tan^{-1} x + \frac{1}{5} \log |x+2| + c$$
, then

Options:

A.
$$a = \frac{-1}{10}b = \frac{2}{5}$$

B.
$$a = \frac{-1}{10}b = \frac{-2}{5}$$

C.
$$a = \frac{1}{10} b = \frac{2}{5}$$

D.
$$a = \frac{1}{10} b = \frac{-2}{5}$$

Answer: A

Solution:

Solution:

$$\frac{1}{(x+2)(x^2+1)} = \frac{A}{x+2} + \frac{Bx+C}{x^2+1}$$

$$A = \frac{1}{5}, B = \frac{-1}{5}, C = \frac{2}{5}$$

Question 35

Area of the region bounded by the curve $y = \tan x$, the x-axis and the line $x = \frac{\pi}{3}$ is

Options:

A.
$$\log_2 \frac{1}{2}$$

B. 0

C. log 2

D. -log 2

Answer: C

$$A = \int_{0}^{\pi/3} \tan x \, d \, x = \log \left| \sec x \right|_{0}^{\pi/3} = \log 2$$

Question 36

Evaluate $\int_2^3 x^2 dx$ as the limit of a sum

Options:

- A. $\frac{72}{6}$
- B. $\frac{25}{7}$
- C. $\frac{53}{9}$
- D. $\frac{19}{3}$

Answer: D

Solution:

Solution:

$$I = \left[\frac{x^3}{3}\right]_2^3 = \frac{1}{3}(27 - 8) = \frac{19}{3}$$

Question 37

$\int_{0}^{\pi/2} \frac{\cos x \sin x}{1 + \sin x} dx \text{ is equal to}$

Options:

- A. $\log 2 1$
- B. -log 2
- C. log 2
- D. $1 \log 2$

Answer: D

Solution:

$$\frac{\pi}{2} \frac{\cos x \sin x}{1 + \sin x} dx$$

$$\Rightarrow \int_0^1 \frac{t}{1+t} dt = 1 - \log 2$$

Question 38

If $\frac{dy}{dx} + \frac{y}{x} = x^2$, then 2y(2) - y(1) =

Options:

- A. $\frac{11}{4}$
- B. $\frac{9}{4}$
- C. $\frac{15}{4}$
- D. $\frac{13}{4}$

Answer: C

Solution:

Solution:

$$y \cdot x = \frac{x^4}{4} + C$$

$$2y(2) - y(1) = \frac{15}{4}$$

Question 39

The solution of the differential equation $\frac{dy}{dx} = (x + y)^2$ is

Options:

A.
$$tan^{-1}(x + y) = x + c$$

$$B. \cot^{-1}(x + y) = c$$

$$C. \tan^{-1}(x + y) = 0$$

D.
$$\cot^{-1}(x + y) = x + c$$

Answer: A

Solution:

$$x+y=z \Rightarrow \frac{dz}{dx} = 1+z^2$$

$$\int \frac{1}{1+z^2} dz = \int 1 dx$$

$$\tan^{-1}(x+y) = x+c$$

Question 40

If y(x) be the solution of differential equation $x \log x \frac{dy}{dx} + y = 2x \log x$, y(e) is equal to

Options:

A. e

B. 2

C. 0

D. 2e

Answer: D

Solution:

Solution:

I.F =
$$\log x$$

 $y \log x = 2x(\log x - 1) + c$
If $x = e$ then $y = c$ then $y(e) = 2e$

Question 41

If $|\vec{a}| = 2$ and $|\vec{b}| = 3$ and the angle between \vec{a} and \vec{b} is 120°, then the

length of the vector $\left| \begin{array}{c} \frac{1^{\overrightarrow{a}}}{2} - \frac{1^{\overrightarrow{b}}}{3} \end{array} \right|^2$ is

Options:

A. 2

B. $\frac{1}{6}$

C. 3

D. 1

Answer: C

$$\left| \frac{\overline{a}}{2} - \frac{\overline{b}}{3} \right|^2 = \frac{|\overline{a}|^2}{4} + \frac{|\overline{b}|^2}{9} - 2\frac{\overline{a}}{2} \cdot \frac{\overline{b}}{3} = 3$$

Question 42

If $|\vec{a} \times \vec{b}| + |\vec{a} \cdot \vec{b}|^2 = 36$ and $|\vec{a}| = 3$ then $|\vec{b}|$ is equal to

Options:

- A. 9
- B. 4
- C. 36
- D. 2

Answer: B

Solution:

Solution:

=
$$|\mathbf{a} \times \mathbf{b}|^2 + |\mathbf{a} - \mathbf{b}|^2 = 36$$

 $|\mathbf{a}|^2 |\mathbf{b}|^2 = 36 \Rightarrow \mathbf{b}^2 = 4, |\mathbf{b}| = 2$

Question 43

If $\vec{\alpha} = \hat{i} - 3\hat{j}$, $\vec{\beta} = \hat{i} + 2\hat{j} - \hat{k}$ then express $\vec{\beta}$ in the form $\vec{\beta} = \vec{\beta}_1 + \vec{\beta}_2$ where $\vec{\beta}_1$ is parallel to $\vec{\alpha}$ and $\vec{\beta}_2$ is perpendicular to $\vec{\alpha}$ then $\vec{\beta}_1$ is given by

Options:

A.
$$\frac{5}{8} \left(\stackrel{\land}{i} - 3 \stackrel{\land}{j} \right)$$

C.
$$\frac{5}{8} \left(\stackrel{\circ}{i} + 3 \stackrel{\circ}{j} \right)$$

D.
$$i + 3j$$

$$E. - \frac{1}{2} (\mathring{i} - 3\mathring{j})$$

Answer: E

$$\overrightarrow{\beta} = \left(\overrightarrow{\beta}_1 + \overrightarrow{\beta}_2\right)$$

$$\left(\overrightarrow{\beta} = \lambda \overrightarrow{\alpha} + \overrightarrow{\beta}_2\right) \cdot \overrightarrow{\alpha}$$

$$\overrightarrow{\alpha} \cdot \overrightarrow{\beta} = \lambda |\overrightarrow{\alpha}|^2 + 0$$

Question 44

The sum of the degree and order of the differential equation $(1+y_1^2)^{2/3}=y_2$ is

Options:

A. 4

B. 5

C. 6

D. 7

Answer: B

Solution:

Solution:

$$(1 + y_1^2) = (y_2)^3$$

2 + 3 = 5

Question 45

The co-ordinates of foot of the perpendicular drawn from the origin to the plane 2x - 3y + 4z = 29 are

Options:

A. (2, 3, 4)

B. (2, -3, 4)

C. (2, -3, -4)

D. (-2, -3, 4)

Answer: B

Solution:

Solution:

verification (2, -3, 4)

Question 46

The angle between the pair of lines $\frac{x+3}{3} = \frac{y-1}{5} = \frac{z+3}{4}$ and

$$\frac{x+1}{1} = \frac{y-4}{4} = \frac{z-5}{2}$$
 is

Options:

A.
$$\theta = \cos^{-1} \left[\frac{27}{5} \right]$$

B.
$$\theta = \cos^{-1} \left[\frac{19}{21} \right]$$

C.
$$\theta = \cos^{-1} \left[\frac{8\sqrt{3}}{15} \right]$$

D.
$$\theta = \cos^{-1} \left[\frac{5\sqrt{3}}{16} \right]$$

E.
$$\theta = \cos^{-1} \frac{31}{5\sqrt{42}}$$

Answer: E

Solution:

Solution:

$$\cos\theta = \frac{3 \times 1 + 5 \times 4 + 4 \times 2}{\sqrt{3^2 + 5^2 + 4^2} \times \sqrt{1^2 + 4^2 + 2^2}} = \frac{31}{5\sqrt{42}}$$

$$\theta = \cos^{-1} \frac{31}{5\sqrt{42}}$$

.....

Question 47

The corner points of the feasible region of an LPP are (0, 2), (3, 0), (6, 0), (6, 8) and (0, 5), then the minimum value of z = 4x + 6y occurs at

Options:

- A. finite number of points
- B. only one point
- C. infinite number of points
- D. only two points

Answer: D

At (0, 2), (3, 0), z = 12

Hence minimum at 2 points.

Question 48

A dietician has to develop a special diet using two foods X and Y. Each packet (containing 30g) of food. X contains 12 units of calcium, 4 4 units of cholesterol and 3 units of vitamin A. The diet requires at least 240 units of calcium, at least 460 units of iron and atmost 300 units of cholesterol. The corner points of the feasible region are

Options:

A. (2, 72), (40, 15), (15, 20)

B. (0, 23), (40, 15), (2, 72)

C. (2, 72), (15, 20), (0, 23)

D. (2, 72), (40, 15), (115, 0)

Answer: A

Question 49

The distance of the point whose position vector is $(2^{\hat{i}} + \hat{j} - \hat{k})$ from the plane $\vec{r} \cdot (\hat{i} - 2\hat{j} + 4\hat{k}) = 4$ is

Options:

A. $\frac{8}{\sqrt{21}}$

B. $\frac{-8}{\sqrt{21}}$

C. $8\sqrt{21}$

D. $\frac{-8}{21}$

Answer: A

Solution:

Solution:

Distance =
$$\frac{|2-2-4-4|}{\sqrt{1+4+16}} = \frac{(8)}{\sqrt{21}}$$

Find the mean number of heads in three tosses of a fair coin :	
Options:	

A. 1.5

B. 2.5

C. 4.5

D. 3.5

Answer: A

Solution:

Solution:

х	0	1	2	3
P(x)	1/8	3/8	3/8	1/8

Mean = $\frac{3}{8} + \frac{6}{8} + \frac{3}{8} = \frac{12}{8} = \frac{3}{2} = 1.5$

Question 51

If A and B are two events such that $P(A) = \frac{1}{2}$, $P(B) = \frac{1}{3}$ and $P\left(\frac{A}{B}\right) = \frac{1}{4}$, then $P(A \cap B)$ is

Options:

A. $\frac{1}{4}$

B. $\frac{1}{12}$

C. $\frac{3}{16}$

D. $\frac{3}{4}$

Answer: A

Solution:

$$P(A) = \frac{1}{2}, P(B) = \frac{1}{3}, P(A \cap B) = \frac{1}{4} \times \frac{1}{3} = \frac{1}{12}$$

$$P(A \cap B) = P(\overline{A \cup B})$$

$$P(A\cap B)=1-P(A\cup B)$$

$$P(A \cap B) = 1 - \left[\frac{1}{2} + \frac{1}{3} - \frac{1}{12} \right]$$

$$P(A \cap B) = 1 - \left[\frac{6+4-1}{12} \right]$$

$$P(A \cap B) = 1 - \frac{9}{12}$$

$$P(A \cap B) = \frac{1}{4}$$

Question 52

A pandemic has been spreading all over the world. The probabilities are 0.7 that there will be a lockdown, 0.8 that the pandemic is controlled in one month if there is a lockdown and 0.3 that it is controlled in one month if there is no lockdown. The probability that the pandemic will be controlled in one month is

Options:

A. 0.65

B. 1.46

C. 1.65

D. 0.46

Answer: A

Solution:

Solution:

 $P(E_1)$ = probability of there is lockdown = 0.7

 $P(E_2)$ = probability of there is lockdown = 0.3

A is the event controlled in one month

$$P(A / E_1) = 0.8$$
, $P(A / E_2) = 0.3$

$$P(A) = 0.7(0.8) + (0.3)(0.3)$$

$$= 0.56 + 0.09 = 0.65$$

Question 53

If A and B are two independent events such that $P(\overline{A}) = 0.75$, $P(A \cup B) = 0.65$, and P(B) = x, then find the value of x

Options:



B.
$$\frac{9}{14}$$

C.
$$\frac{8}{15}$$

D.
$$\frac{7}{15}$$

Answer: C

Solution:

Solution:

$$P(A) = \frac{1}{4}, P(B) = \frac{3}{4}, P(A \cup B) = \frac{13}{20}$$

$$\frac{1}{4} + x - \frac{1}{4} \cdot x = \frac{13}{20}$$

$$\frac{3}{4}x - \frac{13}{20} - \frac{5}{20} = \frac{8}{20}$$

$$x = \frac{8}{20} \times \frac{4}{3} = \frac{8}{15}$$

Question 54

Q54. Suppose that the number of elements in set A is p, the number of elements in set B is q and the number of elements in A \times B is 7 then $p^2 + q^2 =$

Options:

A. 50

B. 42

C. 51

D. 49

Answer: A

Solution:

Solution:

$$n(A) = p, \ n(B) = q$$

$$n(A\times B)=7$$

$$pq = 7$$

$$p^2 + q^2 = 7^2 + 1^2 \text{ or } 1^2 + 7^2$$

$$p^2 + q^2 = 50$$

Question 55

The domain of the function $f(x) = \frac{1}{\log_{10}(1-x)} + \sqrt{x+2}$ is

Options:

A. $[-2, 0) \cap (0, 1)$

B. [-2, 0)

C. [-2, 1)

D. $[-2, 0) \cup (0, 1)$

Answer: D

Solution:

Solution:

 $1 - x > 0, 1 - x \neq 1$ $x - 1 < 0 x \neq 0 x + 2 \ge 0$ $x < 1 x \ge -2$ $\therefore x \in [-2, 0) \cup (0, 1)$

.....

Question 56

The trigonometric function y = tan x in the II quadrant

Options:

A. decreases from 0 to ∞

B. increases from 0 to ∞

C. decreases from $-\infty$ to 0

D. increases from $-\infty$ to 0

Answer: D

Question 57

The degree measure of $\frac{\pi}{32}$ is equal to

Options:

A. 5°30′20″

B. 5°37[′]30[″]

C. 5°37′20″

D. 4°30′30″

Solution:

$$\frac{\pi}{32} = \frac{180^{\circ}}{32} = 5^{0}37'30''$$

Question 58

The value of $\sin \frac{5\pi}{12} \sin \frac{\pi}{12}$ is

Options:

A. 0

B. $\frac{1}{2}$

C. 1

D. $\frac{1}{4}$

Answer: D

Solution:

Solution:

$$\sin\frac{5\pi}{12}\cdot\sin\frac{\pi}{12}$$

$$= \frac{1}{2} \sin \frac{\pi}{6}$$

$$= \frac{1}{2} + \frac{1}{2} = \frac{1}{4}$$

Question 59

 $\sqrt{2 + \sqrt{2 + \sqrt{2 + 2\cos 8\theta}}} =$

Options:

A. $\sin 2\theta$

B. $2 \sin \theta$

C. $2\cos\theta$

D. $2\cos\frac{\theta}{2}$

Answer: C

Solution:

$$1 + \cos \theta = 2\cos^2\left(\frac{\theta}{2}\right)$$

$$\sqrt{2 + \sqrt{2 + \sqrt{2 + 2\cos \theta}}} = 2\cos \theta$$

Question 60

If $A = \{1, 2, 3, \dots 10\}$ then number of subsets of A containing only odd numbers is

Options:

A. 31

B. 32

C. 27

D. 30

Answer: B

Solution:

Solution:

Odd number = $\{1, 3, 5, 7, 9\}$ No. of sub sets = $2^5 = 32$

Physics

Question 1

The centre of mass of an extended body on the surface of the earth and its centre of gravity

Options:

- A. Can never be at the same point
- B. Centre of mass coincides with the centre of gravity of a body if the size of the body is negligible as compared to the size (or radius) of the earth
- C. Are always at the same point for any size of the body
- D. Are always at the same point only for spherical bodies

Answer: B

Question 2

A metallic rod breaks when strain produced is 0.2%. The Young's modulus of the material of the rod is 7×10^9N / m^2 . The area of section of support a load of 10^4N is

Options:

```
A. 7.1 \times 10^{-4} \text{m}^2
```

B.
$$7.1 \times 10^{-2} \text{m}^2$$

C.
$$7.1 \times 10^{-8} \text{m}^2$$

D.
$$7.1 \times 10^{-6} \text{m}^2$$

Answer: A

Solution:

Solution:

Stress = Strain \times Y Thus, maximum stress = $\frac{0.2}{100} \times 7 \times 10^9 = 1.4 \times 10^7$ Now, F orce = Stress \times Area Thus, $10^4 = 1.4 \times 10^7 \times$ A, or, A = 7.14×10^{-4} m²

.....

Question 3

A tiny spherical oil drop carrying a net charge q is balanced in still air, with a vertical uniform electric field of strength $\frac{81}{7}\pi \times 10^5 V$ / m. When the field is switched off, the drops is observed to fall with terminal velocity $2 \times 10^{-3} \text{ms}^{-1}$. Here $g = 9.8 \text{m} / \text{s}^2$, Viscosity of air is $1.8 \times 10^{-5} \, \text{Ns} / \text{m}^2$ and the density of oil is $900 \, \text{kg m}^{-3}$. The magnitude of ' q' is

Options:

A.
$$1.6 \times 10^{-19}$$
C

B.
$$3.2 \times 10^{-19}$$
C

$$C. 0.8 \times 10^{-19} C$$

D.
$$8 \times 10^{-19}$$
C

Answer: D

Here,

$$E = \frac{81\pi}{7} \times 10^5 \text{Vm}^{-1}$$

$$v = 2 \times 10^{-3} \text{ms}^{-1}$$

$$\eta = 1.8 \times 10^5 \text{Nsm}^{-2}$$

When the electric field is switched off, let the drop falls with terminal velocity v, then

$$v = \frac{2r^2(\rho - \sigma)g}{9\eta} \text{ or } r = \left[\frac{9v\eta}{2(\rho - \sigma)g}\right]^{\frac{1}{2}}$$

$$= \frac{7}{81\pi \times 10^5} \times \frac{4}{3} \times \pi \times 900 \times 9.8 \times \left[\frac{9 \times 8 \times 10^{-5} \times 2 \times 10^{-3}}{2 \times 900 \times 9.8} \right]^{\frac{3}{2}}$$

On solving we get, $q = 8 \times 10^{-19} C$

Question 4

"Heat cannot be itself flow from a body at lower temperature to a body at higher temperature". This statement corresponds to

Options:

- A. Conservation of mass
- B. First law of thermodynamics
- C. Second law of Thermodynamics
- D. Conservation of momentum

Answer: C

Solution:

C - I	lutio	
201	IIITIO	n:

Question 5

A smooth chain of length 2m is kept on a table such that its length of 60 cm hangs freely from the edge of the table. The total mass of the chain is 4 kg. The work done in pulling the entire chain on the table is, (Take $g = 10m / s^2$)

Options:

- A. 3.6J
- B. 2.0J
- C. 12.9J
- D. 6.3J

Answer: A

Solution:

Mass of the chain lying freely from the table = $M \frac{1}{L}$

$$= 4kg \times \frac{0.6}{2}$$
$$= 1.2kg$$

The distance of center of mass of chain from the table $=\frac{1}{2}\times 0.6m=0.3m$ Thus the work done in pulling the chain $=mgh=1.2\times 10\times 0.3J=3.6J$

.....

Question 6

The angular speed of a motor wheel is increased from 1200 rpm to 3120 rpm in 16 seconds. The angular acceleration of the moto wheel is

Options:

- A. $6\pi \, \text{rad} / \, \text{s}^2$
- B. $8\pi \, \text{rad} / \, \text{s}^2$
- C. $2\pi \operatorname{rad} / \operatorname{s}^2$
- D. $4\pi \, \text{rad} / \, \text{s}^2$

Answer: D

Solution:

Solution:

$$\alpha = \frac{W_2 - W_1}{t} = \frac{2\pi n_2 - 2\pi n_1}{t}$$

Question 7

Four charges +a, +2q, +q and -2q are placed at the corners of a square ABCD respectively. The force on a the positive charge kept the centre O is

Options:

- A. Along the diagonal AC
- B. Perpendicular to side AB
- C. Zero
- D. Along the diagonal BD

Answer: B

Force due to charge at D and B is along $\overrightarrow{F_0D}$ towards \overrightarrow{B} Force due to charge at A and C is along $\overrightarrow{F_AO}$ towards \overrightarrow{A} . \therefore Resultant

displacement will be along \overrightarrow{F} which is perpendicular to AB.

Question 8

An electric dipole with dipole moment 4×10^{-9} Cm is aligned at 30° with the direction of a uniform electric field of magnitude $5 \times 10^{4} N \, \text{C}^{-1}$, the magnitude of the torque acting on the dipole is

Options:

- A. 10^{-5} N m
- B. $10 \times 10^{-3} \,\text{Nm}$
- C. 10^{-4} Nm
- D. $\sqrt{3} \times 10^{-4} \,\mathrm{Nm}$

Answer: C

Solution:

Solution:

 $\tau = P.E. \sin \theta$

Question 9

A charged particle of mass 'm' and charge 'q' is released from rest in an uniform electric field \vec{E} . Neglecting the effect of gravity, the kinetic energy of the charged particle after 't' seconds is

Options:

- A. $\frac{Eqm}{t}$
- B. $\frac{E^2q^2t^2}{2m}$
- C. $\frac{2E^2t^2}{mq}$
- D. $\frac{E^2q^2m}{2t^2}$

Answer: B

$$\begin{split} K \cdot E &= \frac{1}{2} m v^2 \\ &= \frac{1}{2} m \left(0 + \frac{E q}{m} t \right)^2 \end{split}$$

Question 10

The electric field and the potential of an electric dipole vary with distance r as

Options:

- A. $\frac{1}{r^2}$ and $\frac{1}{r^3}$
- B. $\frac{1}{r^3}$ and $\frac{1}{r^2}$
- C. $\frac{1}{r}$ and $\frac{1}{r^2}$
- D. $\frac{1}{r^2}$ and $\frac{1}{r}$

Answer: B

Solution:

Solution:

$$E = K \frac{2p}{r^3} \propto \frac{1}{r^3}$$

$$V = K \frac{p \cos \theta}{r^2} \propto \frac{1}{r^2}$$

Question 11

The displacement of a particle executing SHM is given by $X = 3 \sin \left[2\pi t + \frac{\pi}{4} \right] \text{ where '} x \text{ 'is in meters and '} t \text{ 'is in seconds. The amplitude and maximum speed of the particle is}$

Options:

- A. $3m, 6\pi ms^{-1}$
- B. 3m, 8πms⁻¹
- C. 3m, $2\pi ms^{-1}$
- D. 3m, $4\pi \text{ms}^{-1}$

Answer: A

$$A = 3m$$

$$V_{max} = A\omega = 3 \times 2\pi = 6\pi$$

Question 12

Electric as well as gravitational affects can be thought to be caused by fields. Which of the following is true for an electrical or gravitational field?

Options:

- A. Fields are useful for understanding forces acting through a distance
- B. There is no way to verify the existence of a force field since it is just a concept
- C. The field concept is often used to describe contact forces
- D. Gravitational or Electric fields does not exist in the space around an object

Answer: A

Solution:

Solution:

Question 13

A charged particle is moving in an electric field of $3\times10^{-10}Vm^{-1}$ with mobility $2.5\times10^{-6}m^2$ / v / s, its drift velocity is

Options:

A.
$$2.5 \times 10^4$$
 m / s

B.
$$1.2 \times 10^{-4}$$
m / s

C.
$$7.5 \times 10^{-4}$$
m / s

D.
$$8.33 \times 10^{-4}$$
m / s

Answer: C

Solution:

Solution:

$$\mu = \, \frac{V_d}{E} \Rightarrow V_d \, = \mu E$$

Wire bound resistors are made by

Options:

- A. Winding the wires of an alloy of Ge, Au, GA
- B. Winding the wires of an alloy of Manganin, constantan, Nichrome
- C. Winding the wires of an alloy of Cu, Al, Ag
- D. Winding the wires of an alloy of Si, Tu, Fe

Answer: B

Solution:

Solution:

Question 15

Ten identical cells each of potential 'E' and internal resistance 'r', are connected in series to form a closed circuit. An ideal voltmeter connected across three cells, will read

Options:

A. 13E

B. 7E

C. 10E

D. 3E

Answer: D

Solution:

Solution:

 $\begin{array}{l} \text{10 identical cells connected in series.} \\ \text{Potential of each cell} &= E \\ \text{Internal resistance of each cell} &= r \\ \text{Total voltage of ten cells} &= 10E \\ \text{Total resistance of ten cells} &= 10r \\ \text{Current in the circuit, I} &= \frac{10E}{10r} = \frac{E}{r} \\ \end{array}$

Potential difference across 3 cells, $V = I \times 3r = \frac{E}{2} \times 3r = 3E$

Hence, ideal voltmeter will read 3E.

Question 16

In an atom electron revolve around	l the nucleus along a path of radius
0.72° making 9.4×10^{18} revolutions	s per second. The equivalent current
is [Given $e = 1.6 \times 10^{-19} C$]	

A. 1.4A

B. 1.8A

C. 1.2A

D. 1.5A

Answer: D

Solution:

Solution:

$$i = \frac{e}{T} = ef$$

Question 17

When a metal conductor connected to left gap of a meter bridge is heated, the balancing point

Options:

- A. Remains unchanged
- B. Shifts to the center
- C. Shifts towards right
- D. Shifts towards left

Answer: C

Solution:

Solution:

$$\frac{R}{\ell} = \frac{S}{100 - \ell}$$

If temperature increases, resistance increases.

As R increases, balancing length also increases. It will shift towards Right

Question 18

Two tiny spheres carrying charges 1.8 μC and 2.8 μC are located at 40 cm apart. The potential at the mid-point of the line joining the two charges is

Options:A. 4.3×10^{4} V B. 3.6×10^{5} V

C.
$$3.8 \times 10^4 V$$

D.
$$2.1 \times 10^5 V$$

Answer: D

Solution:

Solution:

$$V \; = \; \frac{k q_1}{r_1} \; + \; \frac{k q_2}{r_2}$$

Question 19

A parallel plate capacitor is charged by connecting a 2V battery across it. It is then disconnected form the battery and a glass slab is introduced between plates. Which of the following pairs of quantities decrease?

Options:

- A. Energy stored and capacitance
- B. Capacitance and charge
- C. Charge and potential difference
- D. Potential difference and energy stored.

Answer: D

Solution:

50	۱.	.+	in	n	

Question 20

A proton moves with a velocity of $5 \times 10^{6 \text{\^{j}}} ms^{-1}$ through the uniform electric field, $\vec{E} = 4 \times 10^6 \left[2^{\hat{i}} + 0.2^{\hat{j}} + 0.1^{\hat{k}} \right] V m^{-1}$ and the uniform magnetic field $\vec{B} = 0.2 \left[\hat{i} + 0.2^{\hat{j}} + \hat{k} \right] T$. The approximate net force acting on the proton is

A galvanometer of resistance 50Ω is connected to with a resistance 2950Ω in series. A full scale def	
Question 22	
Solution:	
Solution:	
Answer: C	
D. 6.28×10^{-4} T	
C. 3.14×10^{-4} T	
B. 9.42×10^{-4} T	
A. 1.57×10^{-4} T	
Options:	
A solenoid of length 50 cm having 100 turns carri The magnetic field at one end of the solenoid is	es a current of 2.5A.
Question 21	
Solution:	
Solution:	
Answer: D	
D. none	
$C. 5 \times 10^{-13} N$	
B. 20×10^{-13} N	

is obtained in the galvanometer. In order to reduce this deflection to 20

divisions, the resistance in series should be

Options:

A. 5050Ω

B. 4450Ω

 $C.6050\Omega$

D. 5550Ω

A. 2.2×10^{-13} N

Solution:

$$R = (n-1)(G+R)$$

= $\left(\frac{30}{20} - 1\right)3000 = 1500\Omega$
Total resistance = $2950 + 1500 = 4450\Omega$

Question 23

A circular coil of wire of radius ' r ' has ' n ' turns and carries a current ' I '. The magnetic induction ' B ' at a point on the axis of the coil at a distance $\sqrt{3}$ r from its centre is

Options:

- A. $\frac{\mu_0 nI}{16r}$
- B. $\frac{\mu_0 nI}{4r}$
- C. $\frac{\mu_0 nI}{32r}$
- D. $\frac{\mu_0 nI}{8r}$

Answer: A

Solution:

Solution:

$$B = \frac{\mu_0 nir^2}{2(x^2 + r^2)^{3/2}}$$

Question 24

If voltage across a bulb rated 220V, 100W drops by 2.5% of its rated value, the percentage of the rated value by which the power would decrease is

- A. 5%
- B. 10%
- C. 20%
- D. 2.5%

Solution:

$$P = \frac{V^{2}}{R}$$

$$P \propto V^{2}$$

$$\frac{\Delta P}{P} \times 100 = 2 \frac{\Delta V}{V} \times 100$$

$$= 2 \times 2.5 = 5\%$$

Question 25

A wore of certain material is stretched slowly by 10%. Its new resistance and specific resistance becomes respectively

Options:

A. 1.21 times, same

B. both remains the same

C. 1.1 times, 1.1 times

D. 1.2 times, 1.1 times

Answer: A

Solution:

Solution:

Let
$$1_1 = 100$$
, $1_2 = 110$
 $R \propto 1^2$
 $\frac{R_2}{R_1} = \left(\frac{1_2}{1_1}\right)^2 = \left(\frac{110}{100}\right)^2 = 1.21$
 $R_2 = 1.21R_1$
Specific resistance remains same

Question 26

A fully charged capacitor ' C´ with initial charge ' \mathbf{q}_0 ' is connected to a coil of self inductance ' L ' at t=0. The time at which the energy is stored equally between the electric and the magnetic field is

B.
$$\frac{\pi}{4}\sqrt{LC}$$

C.
$$2\pi\sqrt{LC}$$

Answer: B

Solution:

Solution:

$$\frac{1}{2}LI_{max}^{2} = \frac{q^{2}}{2C}$$

$$\frac{1}{2}LI^{2} = \frac{1}{2} \times \frac{1}{2}LI_{max}^{2}$$

$$I = \frac{I_{max}}{\sqrt{2}}$$

$$I_{max} \sin \omega t = \frac{I_{max}}{\sqrt{2}}$$

$$\omega t = \frac{\pi}{4}$$

$$t = \frac{\pi}{4}\sqrt{LC}$$

Question 27

A magnetic field of flux density $1.0\,\mathrm{Wbm\,m^{-2}}$ acts normal to a 80 turn coil of $0.01\mathrm{m^2}$ area. If this coil is removed from the field in 0.2 second, the emf induced in it is

Options:

A. 0.8V

B. 5V

C. 4V

D. 8V

Answer: C

Solution:

Solution:

$$\phi_1 = BAN = 1 \times 0.01 \times 80$$

$$\phi_1 = 0.8wb$$

$$\phi_2 = 0$$

$$e = -\frac{(\phi_2 - \phi_1)}{t}$$

$$= -\left(\frac{0 - 0.8}{2}\right) = 4V$$

Question 28

An alternating current is given by $i = i_1 \sin \omega t + i_2 \cos \omega t$. The r.m.s current is given by

Options:
A. $\sqrt{\frac{i_1^2 + i_2^2}{2}}$
B. $\sqrt{\frac{i_1^2 + i_2^2}{\sqrt{2}}}$
C. $\frac{i_1 + i_2}{\sqrt{2}}$
D. $\frac{i_1 - i_2}{\sqrt{2}}$
Answer: A
Solution:
Solution:
Question 29
Which of the following statements proves that Earth has a magnetic field?
Options:
A. Earth is surrounded by ionosphere
B. A large quantity of iron-ore is found in the Earth
C. The intensity of cosmic rays stream of charged particles is more at the poles than at the equator.
equator.
equator. D. Earth is a planet rotating about the North south axis
equator. D. Earth is a planet rotating about the North south axis Answer: C

A long solenoid has 500 turns, When a current of 2A is passed through it, the resulting magnetic flux linked with each turn of the solenoid is 4×10^{-3} Wb, then self induction of the solenoid is

Options:

A. 2.0 henry

B. 1.0 henry
C. 4.0 henry
D. 2.5 henry
Answer: B
Solution:
Solution: $\varphi = 500 \times 4 \times 10^{-3} = 2 \text{W b}$ $\text{Li} = \text{N } \varphi$ $\text{L} = \frac{2}{2} = 1 \text{H}$
Question 31
Which of the following radiations of electromagnetic waves has the highest wavelength?
Options:
A. IR-rays
B. Microwaves
C. X-rays
D. UV-rays
Answer: B
Solution:
Solution:
Question 32
The power of a equi-concave lens is -4.5 and is made of an material of R.I. 1.6, the radii of curvature of the lens is
Options:
A. -2.66cm
B. 115.44 cm
C26.6 cm
D. +36.6 cm
Answer: C

Solution:

$$p=\,\frac{1}{f}=(\mu-1)\left(\,\,\frac{1}{-R}-\,\frac{1}{R}\right)$$

Question 33

A ray of light passes through an equilateral glass prism in such a manner that the angle of incidence is equal to the angle of emergence and each of these angles is equal to $\frac{3}{4}$ of the angle of the prism. The angle of deviation is

Options:

- A. 20°
- B. 30°
- C. 45°
- D. 39°

Answer: B

Solution:

Solution:

Question 34

A convex lens of focal length ' f ' is placed somewhere in between an object and a screen, the distance between the object and the screen is ' x '. If the numerical value of the magnification produced by the lens is ' m ', then the focal length of the lens is

Options:

A.
$$\frac{(m+1)^2x}{m}$$

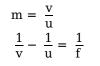
B.
$$\frac{(m-1)^2x}{m}$$

C.
$$\frac{mx}{(m+1)^2}$$

D.
$$\frac{mx}{(m-1)^2}$$

Answer: C

Solution: Solution: u + v = x



Question 35

A series resonant ac circuit contains a capacitance $10^{-6} F$ and an inductor of $10^{-4} H$. The frequency of electrical oscillations will be

Options:

- A. $\frac{10^5}{2\pi}$ Hz
- B. $\frac{10}{2\pi}$ H z
- $C. 10^5 Hz$
- D. 10 Hz

Answer: A

Solution:

Solution:

Question 36

In a series LCR circuit R = 300 Ω , L = 0.9H , C = 2.0 μF and ω = 1000 rad / sec, then impedance of the circuit is

Options:

- Α. 500Ω
- Β. 400Ω
- C. 1300Ω
- D. 900Ω

Answer: A

Solution:

Question 37 For light diverging form a finite point source **Options:** A. The wave front is parabolic B. The intensity at the wave front does not depend on the distance C. the wave front is cylindrical D. the intensity decreases in proportion to the distance squared. **Answer: D Solution: Solution:** **Question 38** The fringe width for red colour as compared to that for violet colour is approximately **Options:** A. 4 times B. 8 times C. 3 times D. Double **Answer: D Solution: Solution:**

Question 39

In case of Fraunhoffer diffraction at a single slit the diffraction pattern on the screen is correct for which of the following statements?

- A. Central dark band having uniform brightness on either side.
- B. Central bright band having dark bands on either side.

C. Central dark band having alternate dark and bright bands of decreasing intensity on same side.
D. Central bright band having alternate dark and bright bands of decreasing intensity on either side.
Answer: D
Solution:
Solution:
Question 40
When a Compact Disc (CD) is illuminated by small source of white light coloured bands observed. This due to
Options:
A. Interference
B. Reflection
C. Scattering
D. Diffraction
Answer: D
Solution:
Solution:
Question 41
Consider a glass slab which is silvered at one side and the other side is transparent. Given the refractive index of the glass slab to be 1.5. If slal is
Options:
A. 120°
B. 45°
C. 90°
D. 180°
Answer: C

Focal length of a convex lens will be maximum for

Options:

- A. Green light
- B. Red light
- C. Blue light
- D. Yellow light

Answer: B

Solution:

Solution:

Question 43

The de-Broglie wavelength of a particle of kinetic energy ' K ' is λ ; the wavelength of the particle, if its kinetic energy is $\frac{K}{4}$ is

Options:

- A. $\frac{\lambda}{2}$
- Β. 4λ
- С. λ
- D. 2λ

Answer: D

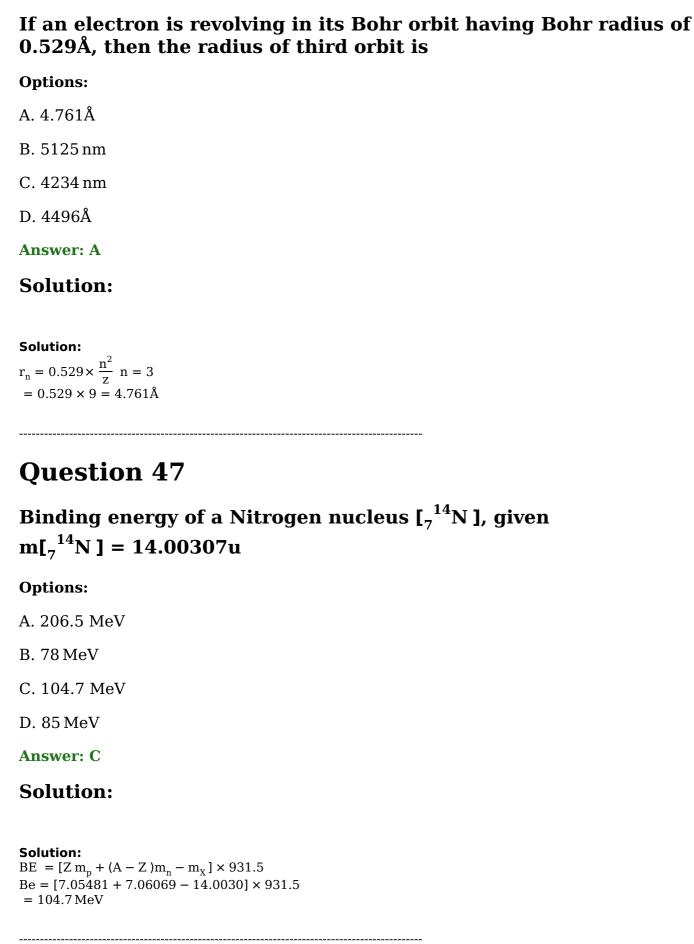
Solution:

$$\lambda \propto \frac{1}{\sqrt{k}}$$

$$\frac{\lambda_1}{\lambda_2} = \sqrt{\frac{k_2}{k_1}}, = \sqrt{\frac{k}{4k}} = \frac{1}{2}$$

$$\lambda_2 = 2\lambda$$

The radius of hydrogen atom in the ground state is 0.53Å. After collision with an electron, it is found to have a radius of 2.12Å, the principle quantum number ' n ' of the final state of the atom is
Options:
A. $n = 3$
B. $n = 4$
C. $n = 1$
D. $n = 2$
Answer: D
Solution:
Solution: $r \propto n^2$ $\frac{r_1}{r_2} = \left(\frac{n_1}{n_2}\right)^2$ $0.25 = \frac{1}{n_2^2}$ $n_2^2 = \frac{1}{0.25} = \frac{100}{25} = 4$ $n_2 = 2$
Question 45
In accordance with the Bohr's model, the quantum number that characterises the Earth's revolution around the sun in orbit of radius 1.5×10^{11} m with orbital speed 3×10^{4} ms ⁻¹ is [given mass of Earth = 6×10^{24} kg]
Options:
A. 8.57×10^{64}
B. 2.57×10^{74}
$C. 5.98 \times 10^{86}$
D. 2.57×10^{38}
Answer: B
Solution:
Solution:



In a photo electric experiment, if both the intensity and frequency of the incident light are doubled, then the saturation photo electric current

A.	Is	doubled

B. Becomes four times

C. Remains constant

D. Is halved

Answer: A

Solution:

Question 49

The kinetic energy of the photoelectrons increases by 0.52 eV when the wavelength of incident light is changed from 500 nm to another wavelength which is approximately

Options:

A. 1250 nm

B. 1000 nm

C. 700 nm

D. 400 nm

Answer: C

Solution:

Solution:

$$KE_{1} - KE_{2} = \frac{hc}{\lambda_{1}} - \frac{hc}{\lambda_{2}}$$
$$\Delta KE = hc \left[\frac{1}{\lambda_{1}} - \frac{1}{\lambda_{2}} \right]^{2}$$

Question 50

The resistivity of a semiconductor at room temperature is in between

A.
$$10^6$$
 to $10^8 \Omega$ cm

B.
$$10^{10}$$
 to $10^{12}\Omega$ cm

C.
$$10^{-2}$$
 to $10^{-5}\Omega$ cm

D.
$$10^{-3}$$
 to $10^6 \Omega\, cm$

Answer: I)
-----------	---

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	lutio	LL

Question 51

The forbidden energy gap for 'Ge crystal at '0 'K is

Options:

A. 2.57 eV

B. 6.57 eV

C. 0.071 eV

D. 0.71 eV

Answer: D

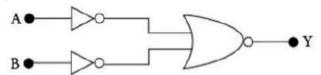
Solution:

Solution:

.....

Question 52

Which logic gate is represented by the following combination of logic gates?



Options:

A. AND

B. NOR

C. OR

D. NAND

Answer: A

Solution:

Question 53

A metallic rod of mass unit length 0.5 kg m⁻¹ is lying horizontally on a smooth inclined plane which makes an angle of 30° with the horizontal. A magnetic field of strength 0.25T is acting on it in the vertical direction. When a current 'T' is flowing through it, the rod is not allowed to slide down. The quantity of current required to keep the rod stationary is

Options:

A. 14.76A

B. 11.32A

C. 7.14A

D. 5.98A

Answer: B

Solution:

Solution:

F = BiI $BiI \cos \theta = mg \sin \theta$ $0.25 \times I \times \frac{\sqrt{3}}{2} = 0.5 \times 10 \times \frac{1}{2}$ $I = \frac{5 \times 100}{25 \times \sqrt{3}} = \frac{20}{\sqrt{3}}A$ I = 11.32A

Question 54

A nuclear reactor delivers a power of 10^9W , the amount of fuel consumed by the reactor in one hour is

Options:

A. 0.72g

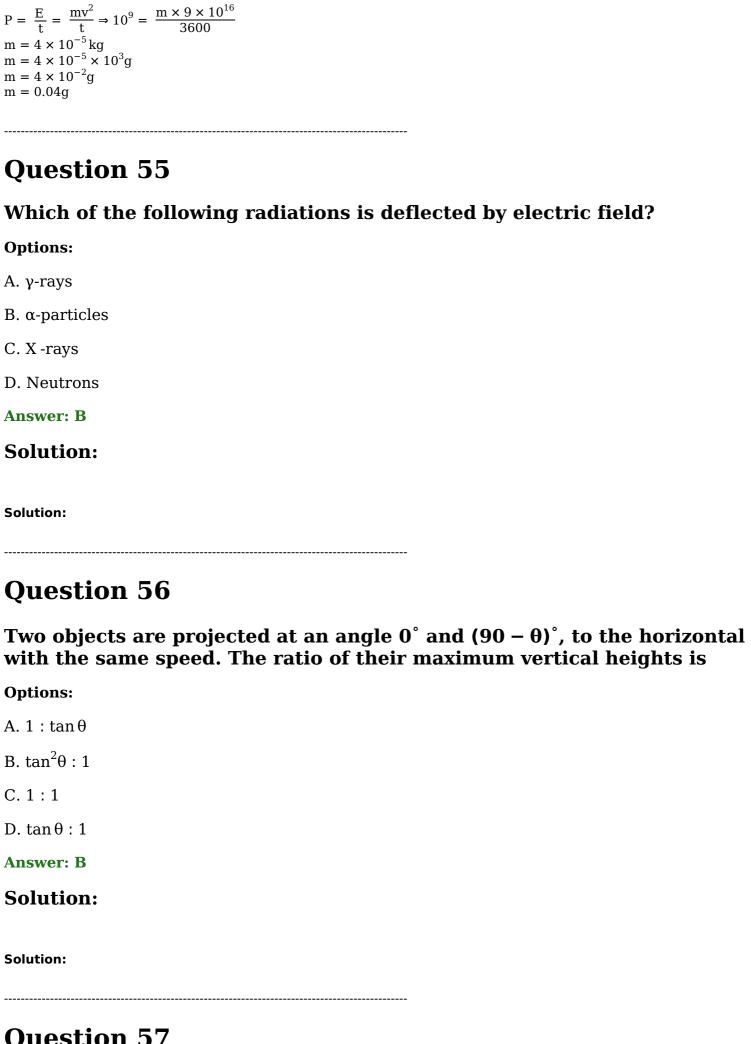
B. 0.96g

C. 0.04g

D. 0.08g

Answer: C

Solution:



A car is moving in a circular horizontal track of radius 10m with a

constant speed of 10ms^{-1} . A bob is suspended from the roof of the car by a light wire of length 1.0m. The angle made by the wire with the vertical is (in radian)

Options:

A. 0

B. $\frac{\pi}{3}$

C. $\frac{\pi}{6}$

D. $\frac{\pi}{4}$

Answer: D

Solution:

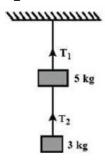
Solution:

$$\tan \theta = \frac{V^2}{2g} = \frac{10 \times 10}{10 \times 10} = 1$$

$$\theta = \frac{\pi}{4}$$

Question 58

Two masses of 5 kg and 3 kg are suspended with the help of massless inextensible strings as shown in figure, when whole system is going upwards with acceleration $2m / s^2$, the value of T_1 is (use $g = 9.8m / s^2$)



Options:

A. 23.6N

B. 59N

C. 94.4N

D. 35.4N

Answer: C

Solution:

Question 59

The Vernier scale of a travelling microscope has 50 divisions which coincides with 49 main scale divisions. If each main scale division is 0.5 mm, then the lease count of the microscope is

Options:

A. 0.01 mm

B. 0.5 cm

C. 0.01 cm

D. 0.5 mm

Answer: A

Solution:

Solution:

L. C = 1M SD - 1V SD or L.C = $\frac{1M \text{ SD}}{\text{No.of.vernier scale division}} = \frac{0.05 \text{ mm}}{50} \text{ L.C } = 0.01 \text{ mm}$

Question 60

The displacement 'x' (in meter) of a particle of mass 'm' (in kg) moving in one dimension under the action of a force, is related to time 't' (in sec) by, $t = \sqrt{x} + 3$. The displacement of the particle when its velocity is zero, will be

Options:

A. 6m

B. 2m

C. 4m

D. 0m

Answer: D

Solution:

$$t = \sqrt{x} + 3$$

$$\Rightarrow x = (t - 3)^{2}$$

$$v = \frac{dx}{dt} = 2(t - 3)$$

$$v = 0 \Longrightarrow t = 3$$
At $t = 3$, $x = (3 - 3)^{2} = 0$

Chemistry

Question 1

A first order reaction is half completed in 45 min. How long does it need 99.9% of the reaction to be completed?

Options:

A. 10 Hours

B. 20 Hours

C. 5 Hours

D. 7.5 Hours

Answer: D

Solution:

Solution:

 $t_{99.9\%} = 10t_{50\%}$ = 10 × 45 min = 450 min = 7.5 hours

Question 2

The rate of the reaction $CH_3COOCC_2 + NaOH \rightarrow CH_3COONa + C_2H_5OH$ is given by the equation, Rate = K[CH₃COOC₂H₅][NaOH]. If concentration is expressed in mol L⁻¹, the unit of K^{is}

Options:

A.
$$Lmol^{-1}s^{-1}$$

B.
$$s^{-1}$$

C.
$$mol^{-2}L^2s^{-1}$$

D.
$$mol L^{-1} s^{-1}$$

Answer: A

Solution:

Solution:

2 nd order reaction

Colloidal solution commonly used in the treatment of skin disease is

Options:

A. Colloidal Gold

B. Colloidal Antimony

C. Colloidal Sulphur

D. Colloidal Silver

Answer: C

Solution:

Solution:

Question 4

Specific conductance of $0.1 MHNO_3$ is $6.3 \times 10^{-2} ohm^{-1} cm^{-1}$. The molar conductance of the solution is

Options:

A. $6.300 \text{ ohm}^{-1} \text{cm}^2 \text{mol}^{-1}$

B. 63.0ohm⁻¹cm²mol⁻¹

C. $630 \text{ohm}^{-1} \text{cm}^2 \text{mol}^{-1}$

D. $315 \text{ohm}^{-1} \text{cm}^2 \text{mol}^{-1}$

Answer: C

Solution:

Solution:

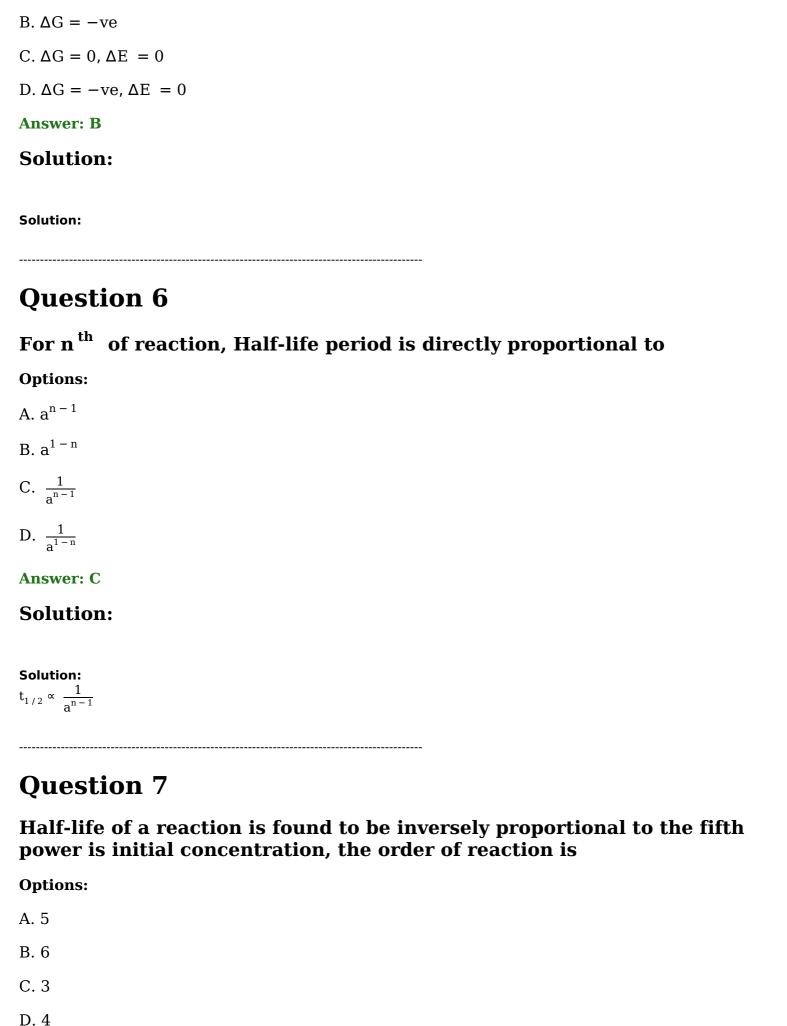
$$\lambda_{\rm m} = \frac{1000 \text{k}}{\text{C}} = \frac{1000 \times 6.3 \times 10^{-2}}{0.1}$$
$$= 630 \text{ohm}^{-1} \text{cm}^2 \text{mol}^{-1}$$

Question 5

For spontaneity of a cell, which is correct?

Options:

A. $\Delta G = +ve$, $\Delta E = +ve$



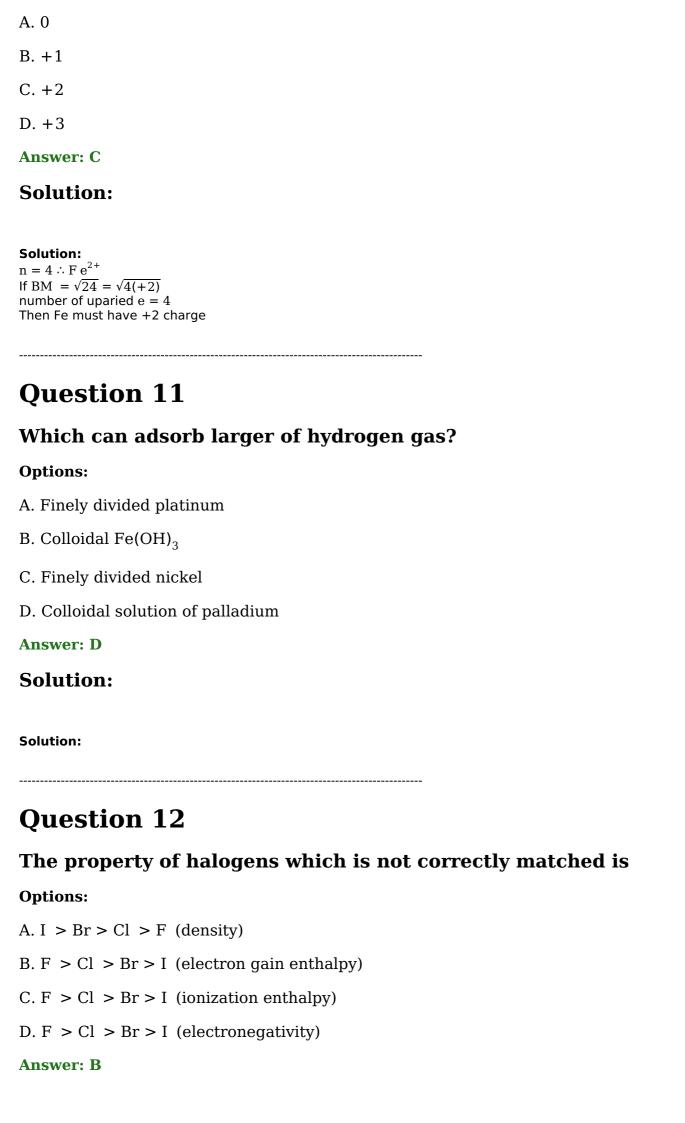
Answer: B

Solution: $t_{1/2} \propto \frac{1}{a^{n-1}}$; n = 6**Question 8** The strong reducing property of hypophosphorous acid is due to **Options:** A. Two P-H bonds B. Presence of phosphorus in its highest oxidation state C. Its concentration D. The positive valency of phosphorus **Answer: A Solution: Solution: Question 9** A transition metal exists in its highest oxidation state. It is expected to behave as **Options:** A. An oxidizing agent B. A reducing agent C. A chelating agent D. A central metal in a co-ordination compound **Answer: A Solution:**

Solution:

Question 10

What will be the value of x in F e^{x^+} , if the magnetic moment $\mu = \sqrt{24}BM$?



Solution:					
Question	13				
Which noble	gas has least t	tendency to	o form con	npounds?	
Options:					
A. Ar					
B. Kr					
C. He					
D. Ne					
Answer: C					
Solution:					
Solution:					
	14				
Question			 s. The san	ne gas will	be obtained
Question $(NH_4)_2Cr_2O_7$	14		 s. The san	ne gas will	be obtained
Question (NH ₄) ₂ Cr ₂ O ₇ by	14 on heating lib		 s. The san	ne gas will	be obtained
Question (NH $_4$) $_2$ Cr $_2$ O $_7$ by Options:	14 on heating lib with NaNO $_2$		 s. The san	ne gas will	be obtained
Question $(NH_4)_2Cr_2O_7$ by Options: A. Treating H_2O_2	$f 14$ on heating lib with NaNO $_2$ N $_2$ with H $_2$ O		 s. The san	ne gas will	be obtained
Question $(NH_4)_2Cr_2O_7$ by Options: A. Treating H_2O_2 B. Treating Mg_3N_1	14 on heating lib with NaNO ₂ N_2 with H_2O N_3		 s. The san	ne gas will	be obtained
Question $(NH_4)_2Cr_2O_7$ by Options: A. Treating H_2O_2 B. Treating Mg_3N C. Heating NH_4N	14 on heating lib with NaNO ₂ N_2 with H_2O N_3		s. The san	ne gas will	be obtained
Question $(NH_4)_2Cr_2O_7$ by Options: A. Treating H_2O_2 B. Treating Mg_3N C. Heating NH_4N D. Heating NH_4N	14 on heating lib with NaNO ₂ N_2 with H_2O N_3		 s. The san	ne gas will	be obtained

The complex hexamine platinum (IV) chloride will give number of ions on ionization.

Options:

A. 3

B. 2

C. 5

D. 4

Answer: C

Solution:

Solution:

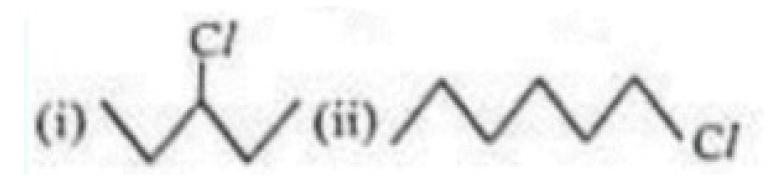
 $[Pt(NH_3)_6]Cl_4 \rightarrow [Pt(NH_3)_6]^{+4} + 4Cl^-$ Five ions are produced

Question 16

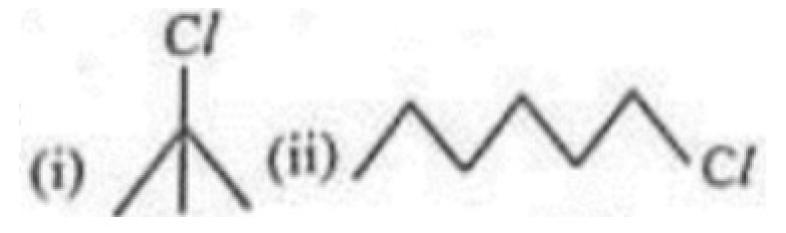
In the following pairs of halogen compounds, which compound undergoes faster SN $^{\rm 1}$ reaction?

Options:

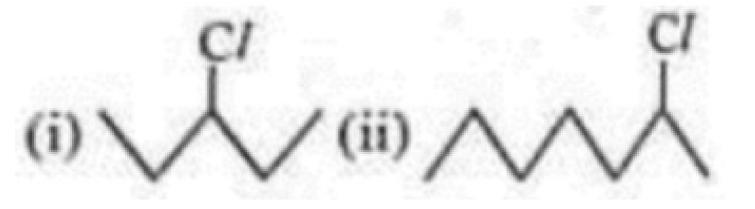
A.



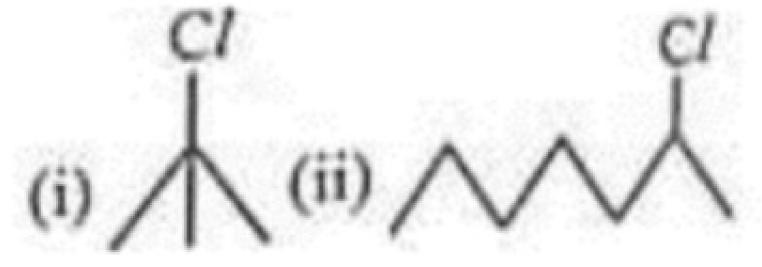
В.



C.



D.



Answer: D

Solution:

Solution:

 $S_N 1$ reaction proceeds via formation of carbocation. In option B, the alkyl halide (1) is 3° while (2) is 2°.

Therefore greater the stability of the carbocation, faster is the rate of $S_{\rm N}{\rm 1}$ reaction.

Therefore option D, the compound pair of 2-chloro-2 methylpropane and 2chloroheptane is the correct option.

Question 17

The only Lanthanoid which is radioactive

Options:
A. Promethium
B. Praseodymium
C. Lanthanum
D. Cerium
Answer: A
Solution:
Solution:
Question 18
All Cu(II) halides are known, except the iodide, the reaction for it is that
Options:
A. Cu ⁺² has much more negative hydration enthalpy
B. Cu ⁺² ion has smaller size
C. lodide is bulky ion
D. Cu ⁺² oxidises iodide to iodine
Answer: D
Solution:
Solution: All Cu (II) halides are known except the iodine because Cu^{2+} oxidizes iodine to iodine $2Cu^{2+} + 4I^{-1} \rightarrow 2CuI_{(S)} + I_2$
Question 19
The correct IUPAC name of cis-platin is
Options:

- A. Diammine dichloride platinum (O)
- B. Dichlorido diammine platinum (IV)
- C. Diammine dichlorido platinum (II)
- D. Diammine dichloride platinum (IV)

Answer: C

Solution:

 $[Pt(NH_3)_2 Cl_2] = cis-platin$

Question 20

Crystal Field Splitting Energy (CFSE) for $[CoCl_6]^{4-}$ is $18000cm^{-1}$. The Crystal Field Splitting Energy (CFSE) for $[CoCl_4]^{2-}$ will be

Options:

A. 8000cm^{-1}

B. 10, 000cm⁻¹

C. 18, 000cm⁻¹

D. 16, 000cm⁻¹

Answer: A

Solution:

Solution

 $\Delta_{\rm t} = \frac{4}{9} \Delta_0 = \frac{4}{9} \times 18000 \,{\rm cm}^{-1} = 8000 \,{\rm cm}^{-1}$

Question 21

The major product obtained when ethanol is heated with excess of conc. $\rm H_2SO_4$ at at 443K is

Options:

A. ethane

B. methane

C. ethene

D. ethyne

Answer: C

Solution:

$$CH_3 - CH_2 - OH \xrightarrow{Conc. H_3SO_4} CH_2 = CH_2$$

Question 22

Among the following, the products formed by the reaction of anisole with H I are

Options:

A. Benzene + Methanol

B. Phenol + Methane

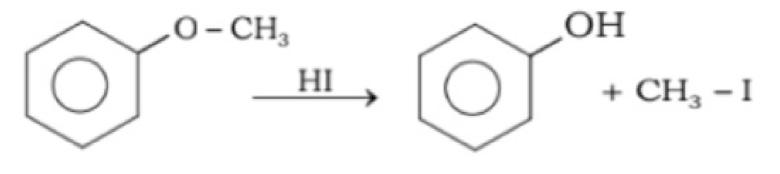
C. Phenol + lodomethane

D. Sodium phenate + Methanol

Answer: C

Solution:

Solution:



Question 23

Which one of the following Chlorohydrocarbon readily undergoes solvolysis?

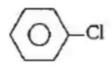
Options:

A.

В.

$$C. CH_2 = CHCl$$

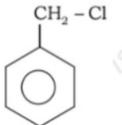
D.



Answer: A

Solution:

Solution:



on solvolysis give more stable benzyl carbocation

Question 24

Identify the products A and B in the reactions:

 $R - X + AgCN \rightarrow A + AgX$

 $R - X + KCN \rightarrow B + KX$

Options:

A. A = RN C; B = RCN

B. A = RN C; B = RN C

C. A = R - CN; B = RCN

D. A = RCN ; B = RN C

Answer: A

Solution:

Solution:

$$R - X + AgCN \rightarrow R - NC + AgX$$

 $R - X + KCN \rightarrow R - CN + KX$

Question 25

An organic compound with molecular formula $\rm C_7H_{8}O$ dissolves in N aOH and gives a characteristic colour with F el $_3$. On treatment with bromine, it gives a tribromo derivative $\rm C_7H_{5}OB_{3}$. The compound is

A. m - Cresol

B. p-Cresol

C. Benzyl alcohol

D. o-Cresol

Answer: A

Solution:

Solution:

Phenols gives characteristic colour with $\mbox{FeCl}_{\mbox{\scriptsize 3}}$

$$\begin{array}{c|c} OH & OH \\ \hline \\ Br \\ Br_2 \\ \hline \\ Br \\ CH_3 \\ \hline \\ Br \\ CH_3 \\ \hline \\ Br \\ \end{array}$$

Meta-derivative of phenol only gives tribromo derivative

Question 26

In Kolbes reaction the reacting substances are

Options:

A. Sodium phenate and CCl $_{\rm 4}$

B. Phenol and CHCl_3

C. Sodium phenate and CO₂

D. Phenol and CCl₄

Answer: C

Solution:

ONa
$$CO_2$$
 CO_2 $COOH$

In Carby	ylamine	test for	primary	amines	the	resulting	foul	smelti	ing
product	is		_						



A. CH₃ NC

B. COCl₂

C. CH₃NCl₂

D. CH₃CN

Answer: A

Solution:

Solution:

Carbylamine test for primary amines the resulting isocyanide $\rm CH_3-NH_2 \xrightarrow[NaOH3]{CH_3}CH_3NC$

.....

Question 28

Ethanoic acid undergoes Hell-Volhard Zelinsky reaction but Methanoic acid does not, because of

Options:

A. absence of α – H atom in ethanoic acid

B. higher acidic strength of ethanoic acid than methanoic acid

C. presence of $\alpha-H\,$ atom in methanoic acid

D. presence of α – H atom in ethanoic acid

Answer: D

Solution:

Solution:

Carboxylic acid with alpha hydrogen undergoes HVZ reaction

Question 29

The general name of the compound formed by the reaction between aldehyde and alcohol is

- A. Glycol
- B. Acetate
- C. Ester
- D. Acetal

Answer: D

Solution:

Solution:

O OH OR
$$R-C-H+R-OH \rightarrow R-CH-OR \xrightarrow{R-OH} R-CH-OR$$
 Hemiacetal acetal

Question 30

Reaction by which benzaldehyde can not be prepared is

Options:

A. Toulene
$$\frac{\text{(i)CrO}_2\text{Cl}_2\text{inCS}_2}{\text{(ii)H}_3\text{O}^+}$$

B. Benzoyl chloride
$$+H_2 \frac{\text{Pd} - \text{BaSO}_4}{\Delta}$$

C. Benzene +CO + HCl
$$\xrightarrow{\text{anhydrous AlCl}_3}$$

D. Benzoic acid $\xrightarrow{\text{Zn - Hg and Conc. HCl}}$

Answer: D

Solution:

a)
$$CH_{3}$$

$$(i) Cro_{2}Cl_{2} inCS_{2}$$

$$(ii) H_{3}O'$$

$$CHO$$

$$COOH$$

$$C$$

The test to differentiate between pentan-2-one and pentan-3-one is Options:

A. Fehling's test

B. Iodoform test

C. Baeyer's test

D. Benedict's test

Answer: B

Solution:

Solution:

$$[CH_3 - \overset{\circ}{C} - CH_2 - CH_2 - CH_3]$$

 $CH_3 - CH_2 - \overset{\circ}{C} - CH_2 - CH_3]$

A secondary amine is

Options:

- A. a compound with an NH_2 group on the carbon atom in number 2 position
- B. a compound in which 2 of the hydrogen of N $_{3}$ have been replaced by organic groups
- C. an organic compound with two NH₂ group
- D. a compound with two carbon atom and an NH₂ group

Answer: B

Solution:

Solution:

Question 33

Which of the following is correctly matched?

Options:

- A. Bakelite Novolac
- B. Polyster tetrafluoroethene
- C. Nylon acrylonitrile
- D. Teflon copralactum

Answer: A

Solution:

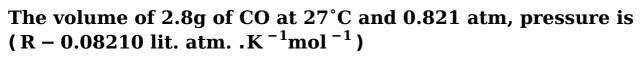
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Question 34

Which institute has approved the emergency use of 2 -deoxy-D-Glucose as additive therapy for COV I D - 19 patients?

- A. Ministry of Health and Family Welfare
- B. Drug Controlled General of India
- C. Indian Council of Medical Research

D. World Health Organisation
Answer: B
Solution:
Solution:
Question 35
A Nucleic acid, whether DNA or RNA gives on complete hydrolysis, two purines bases, two pyrimidine bases, a pentose sugar and phosphoric acid. Nucleotides which are intermediate products in the hydrolysis contain
Options:
A. purine or pyrimidine base and orthophosphoric acid
B. purine or pyrimidine base, a pentose sugar and ortho-phosphoric acid
C. purine or pyrimidine base and pentose sugar
D. a purine base, pentose sugar and orthophosphoric acid
Answer: B
Solution:
Solution:
Question 36
Which is most VISCOUS?
Options:
A. Ethylene glycol
B. Glycerol
C. Methanol
D. Ethanol
Answer: B
Solution:
Solution:



Options:

A. 3 litres

B. 30 litres

C. 0.3 litres

D. 1.5 litres

Answer: A

Solution:

Solution:

Question 38

The work done when 2 moles of an ideal gas expands reversibly and isothermally from a volume

Options:

A. 0.115 kJ

B. 58.5 kJ

C. 11.5 kJ

D. 5.8 kJ

Answer: C

Solution:

Solution:

 $W = -2.303 \, \text{nRT} \log V_2 / V_1$

Question 39

An aqueous solution of alcohol contains 18g of water and 414g of ethyl alcohol. The mole fraction of water is

Options:

A. 0.7

C. 0.1

D. 0.4

Answer: C

Solution:

Solution:

Molecular weight of $C_2H_5OH = 24 + 5 + 16 + 1 = 46$

Molecular mass of $H_2O = 18$

414 g of C_2H_5 OH has $\frac{414}{46}$ = 9 mole (i.e. n_1 = 9 mole) 18g of H_2 O has = $\frac{18}{18}$ = 1 mole (i.e. n_2 = 1 mole)

 $\text{mole fraction of water } = \frac{n_2}{n_1 + n_2} = \frac{1}{1 + 9}$

$$=\frac{1}{10}=0.1$$

Question 40

If wavelength of photon is $2.2 \times 10^{-11} m$ and $h = 6.6 \times 10^{-34} Js$, then momentum of photon

Options:

A. $1.452 \times 10^{-44} \,\mathrm{kg} \,\mathrm{ms}^{-1}$

B. $6.89 \times 10^{43} \text{kgms}^{-1}$

C. $3 \times 10^{-23} \text{kg ms}^{-1}$

D. $3.33 \times 10^{-22} \text{kgms}^{-1}$

Answer: C

Solution:

Solution:

$$\lambda = \frac{h}{mv} = \frac{h}{p}$$

$$p = \frac{h}{\lambda} = \frac{6.6 \times 10^{-34}}{2.2 \times 10^{-11}} = 3 \times 10^{-23}$$

Question 41

Elements X, Y and Z have atomic number 19,37 and 55 respectively. Which of the following statements is true about them?

Options:

A. Z would have the highest ionization potential

B. Y would have the highest ionization potential
C. Their ionization potential would increase with increasing atomic number
$D.\ Y$ would have an ionization potential between those of X and Z
Answer: D
Solution:
Solution:
Question 42
In oxygen and carbon molecule the bonding is
Options:
A. O_2 : 1σ, 1π; C_2 : 0σ, 2π
B. O_2 : 0σ, 2π; C_2 : 2σ, 0π
С. О $_2$: 1 σ , 1 π ; С $_2$: 1 σ , 1 π
D. O_2 : 2σ, 0π; C_2 : 0σ, 2π
Answer: A
Solution:
Solution:
Question 43
Amphoteric oxide among the following:
Options:
A. Ag_2O
${\rm B.~SnO}_2$
C. BeO
D. CO ₂
Answer: B,C
Solution:
Solution:

Question 44 Which property of ${\rm CO_2}$ makes it biologically and geo-chemically important? **Options:** A. Its low solubility in water B. Its high compressibility C. Its acidic nature D. Its colourless and odourless nature **Answer: A Solution: Solution: Question 45** The IUPAC name for $\overset{\text{O}}{\text{CH}_3} - \overset{\text{O}}{\text{C}} - \overset{\text{O}}{\text{CH}_2} - \overset{\text{O}}{\text{CH}_2} - \overset{\text{O}}{\text{C}} - \overset{\text{O}}{\text{O}} - \overset{\text{O}}{\text{H}} \, \text{is}$ **Options:** A. 1-carboxybutan-3-one B. 4-oxopentanoic acid C. 1 -hydroxy pentane-1, 4-dione D. 1,4-dioxopentanol **Answer: B Solution: Solution:**

Question 46

1 mole of HI is heated in a closed container of capacity of 2L. At equilibrium half a mole of HI is dissociated. The equilibrium constant of the reaction is

Options: A. 0.25 B. 0.35 C. 1 D. 0.5 **Answer: A Solution: Solution:** $2 \text{ HI} \rightleftharpoons \text{H}_2 + \text{I}_2$ 0.5 0.25 0.25 $K_{C} = \frac{[H_{2}][I_{2}]}{[HI]^{2}}$ $K_{C} = \frac{\frac{0.25 \times 0.25}{2}}{\frac{0.5 \times 0.5}{2}} = \frac{1}{4} = 0.25$ **Question 47** Which among the following has highest pH? **Options:** A. 1MH₂SO₄ B. 0.1 MNaOH C. 1 MHCl D. 1 MNaOH **Answer: D Solution:**

Solution:

Question 48

In which of the following compounds, an element exhibits two different oxidation states?

A.	N ₂ H
В.	N ₃ H
C.	NH_2
D	NH

CONH₂

D. NH₄NO₃

Answer: D

Solution:

Solution:

Question 49

Which of the following hydrides is electron deficient?

Options:

A. CH₄

B. B_2H_6

C. NaH

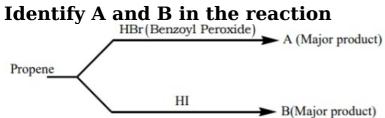
D. CaH_2

Answer: B

Solution:

Solution:

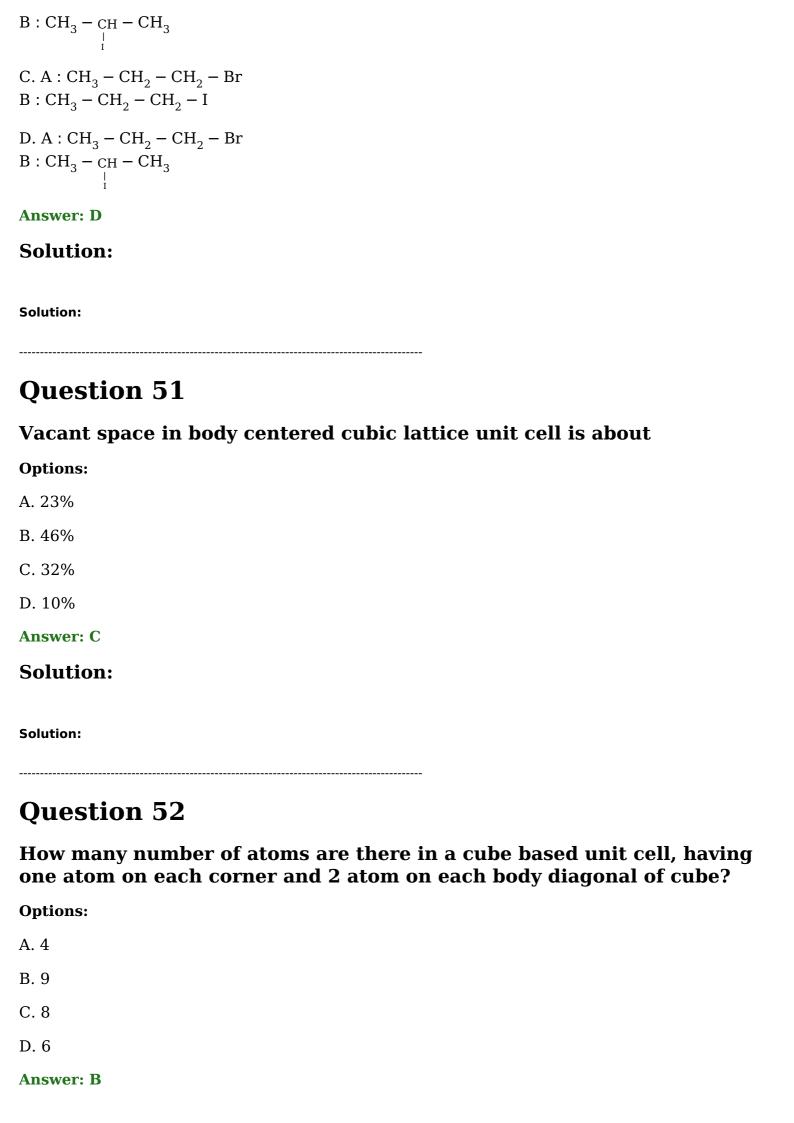
Question 50



$$\begin{aligned} &\text{A. A: } \text{CH}_3 - \underset{\text{Br}}{\text{CH}} - \text{CH}_3. \\ &\text{B: } \text{CH}_3 - \text{CH}_2 - \text{CH}_2 - \text{I} \end{aligned}$$

$$B : CH_3 - CH_2 - CH_2 - I$$

$$B. A: CH_3 - CH_3 - CH_3,$$



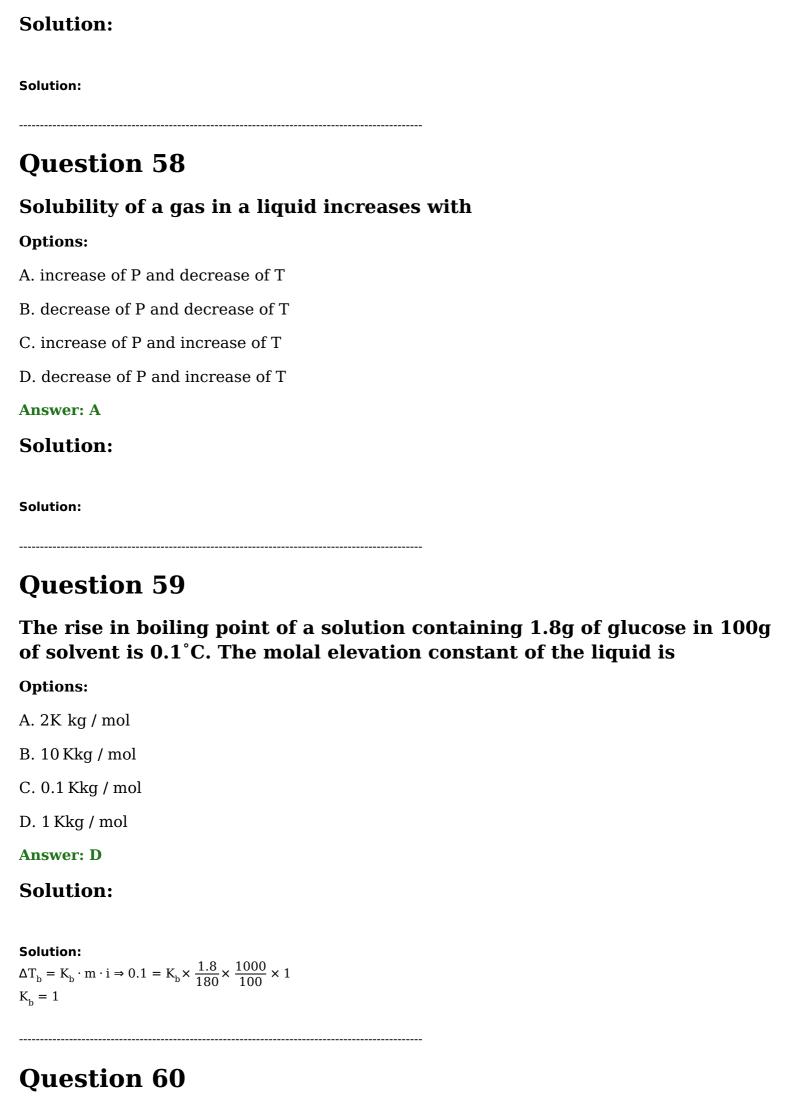
Solution:
Solution:
Question 53
Which of the following is NOT true about the amorphous solids?
Options:
A. Amorphous solids can be moulded by heating
B. They are anisotropic in nature
C. On heating they may become crystalline at certain temperature
D. They may become crystalline on keeping for long time.
Answer: B
Solution:
Solution:
Question 54
Which of the following colligative properties can provide molar mass of proteins, polymers, and colloids with greater precision?
Options:
A. Depression in freezing point
B. Osmotic pressure
C. Relative lowering of vapour pressure
D. Elevation in boiling point
Answer: B
Solution:
Solution:
Question 55
In Fuel cells are used as catalysts.

Options:
A. Zinc - Mercury
B. Lead - Manganese
C. Platinum - Palladium
D. Nickel - Cadmium
Answer: C
Solution:
Solution:
Question 56
The molar conductivity is maximum for the solution of concentration
Options:
A. 0.005 M
B. 0.001 M
C. 0.004 M
D. 0.002 M
Answer: B
Solution:
Solution: $\Delta_m = \frac{k \times 1000}{M}$ Lower the molarity higher the molar conductivity
Question 57
Alkali halides do not show dislocation defect because
Options:
A. Cations and anions have almost equal size
B. There is large difference in size of cations and anions

C. Cations and anions have low co-ordination number.

D. Anions cannot be accommodated in vacant spaces.

Answer: B



If 3g of glucose (molar mass = 180g) is dissolved in 60g of water at 15°C, the osmotic pressure of the solution will be
Options:
A. 6.57 atm
B. 5.57 atm
C. 0.34 atm
D. 0.65 atm
Answer: A
Solution:
Solution: $T = C \cdot R \cdot T = \frac{w_2}{M_2} \frac{1000}{V(m\ell)} \times R \cdot T$ $\Rightarrow \frac{3}{180} \times \frac{1000}{60} \times 0.0821 \times 288 = 6.568 \text{ atm}$
Biology
Question 1
A series of experiments were conducted by Frederick Griffith in 1928, on transforming principle with
Options:
A. Streptococcus pneumoniae
B. Escherichia coli
C. Bacillus thuringiensis
D. Salmonella typhimurium
Answer: A
Solution:
Solution:
Question 2
The number of codons effective in coding twenty amino acids:

- A. 20
- B. 61
- C. 32
- D. 64

Answer: B

Solution:

Solution:

George Gamow in 1954, pointed out the possibility of a three-letter code i.e. triplet codon. This will give $4 \times 4 \times 4 = 64$ codons which are more than enough to code for twenty amino acids. Out of these 64 codons, 3 codons are stop codons. Hence, 61 effective codons are there for the synthesis of twenty amino acids.

Question 3

Which aspect forms the basis of DNA finger-printing?

Options:

- A. The amount of DNA found in samples of blood, saliva and skin.
- B. The ratio of purines and pyrimidines present in DNA.
- C. The Sequence of DNA present in the ridges and grooves of finger-prints.
- D. The Satellite DNA showing high degree of repetition in DNA segments.

Answer: D

Solution:

Solution:

Variable Number of Tandem Repeat (VNTR) polymorphism is the basis of DNA fingerprinting which are short nucleotide repeats. DNA of each organism has specific sequences called restriction fragments that can be cleaved by restriction endonuclease enzymes to produce fragments of different lengths.

Question 4

Identify the most infectious and fatal type of malarial parasite:

Options:

- A. Plasmodium ovale
- B. Plasmodium vivax
- C. Plasmodium malariae
- D. Plasmodium falciparum

Answer: D

Solution:
olution:
Question 5
The type of antibodies produced during the allergic reaction
Options:
A. IgM
B. Ig A
C. lg E
D. IgG
Answer: C
Solution:
olution:
Question 6
One of the side-effect of the use of anabolic steroids in females
Options:
A. Masculinisation
B. Loss of memory
C. Hallucination
D. Cirrhosis of liver
Answer: A
Solution:
folution:
Ouestion 7

Which one of the following is a opiate narcotics?

A. LSD
B. Barbiturates
C. Morphine
D. Amphetamines
Answer: C
Solution:
Solution:
Question 8
The large holes in 'Swiss - Cheese' are made by a
Options:
A. Fungus that releases a lot of gases during metabolic activities
B. Machine
C. Bacterium that produces methane gas
D. Bacterium producing a large amount of CO_2
Answer: D
Solution:
Solution:
Question 9
Which vitamin is increased by "LAB' in curd?
Options:
Δ Vitamin F

A. Vitamin E

B. Vitamin C

C. Vitamin B

D. Vitamin ${\bf B}_{12}$

Answer: D

colution:
Question 10
Enzyme which is useful to remove the oily stains in laundry
Options:
a. Lipase
3. Renin
C. Protease
D. Amylase
Answer: A
Solution:
olution:
Question 11
ONA replicates semi conservatively was first shown in :
Options:
A. Higher animals
B. Escherichia coli
C. Human cell
D. Plants
Answer: B
Solution:
folution:
Question 12
What does the sample of given base sequence represent? 5 - GAATTC - 3 6 - CTTAAG - 5

B. Initiator codon at S' end
C. Deletion mutation
D. Completion of replication
Answer: A
Solution:
Solution:
Question 13
Gel electrophoresis is used for
Options:
A. Cutting of DNA into fragments.
B. Construction of recombinant DNA by joining with cloning vectors.
C. Isolation of DNA molecule.
D. Separation of DNA fragments according to their size.
Answer: D
Solution:
Solution:
Question 14
An antibiotic resistance gene in a vector usually helps in the selection of
Options:
A. Non-competent cells
B. Competent cells
C. Transformed cells
D. Non-recombinant cells
Answer: C

A. Palindromic sequence

Solution:

Question 15
Silencing of specific mRNA in RNAi is by
Options:
A. dsDNA
B. SsRNA
C. dsRNA
D. ssDNA
Answer: C
Solution:
Solution:
Question 16
Cry-IAC effectively controls,
Options:
A. Ring worm
3. Cotton bollworms
C. Corn borer
D. Root nematode
Answer: B
Solution:
Solution:
Question 17
ADA deficiency can be cured by

- A. Heart Transplantation
- $B.\ Bone-marrow\ Transplantation$
- $C.\ Liver\ Transplantation$

D. Kidney Transplantation
Answer: B
Solution:
Solution:
Question 18
Average natality rate in our village is 25, average mortality is 24, immigration 2 and emigration 3 and the net increase in population is
Options:
A. 27
B. 0
C. 5
D. 10
Answer: B
Solution:
Solution:
Question 19
The term "Molecular Scissors" refers to
Options:
A. Tag polymerase
B. Polymerase-I
C. Polymerase-I
D. Restriction enzyme
Answer: D
Solution:
Solution:

Question 20 The animals which are active during day time: **Options:** A. Cresporal B. Diurnal C. Auroral D. Vesporal **Answer: B Solution: Solution:** **Question 21** Which of the following statement is incorrect related to biomes? **Options:** A. Low temperature and less rainfall is a characteristics of Tundra biomes. B. Variation in temperature and mean precipitation accounts for the major biomes, C. More rainfall and low temperature is the characteristics of deserts. D. High temperature and minimum rainfall help to form grasslands. **Answer: C Solution: Solution: Question 22**

The amount of Photosynthetically active radiation captured by plants is

- A. 12-20 percent
- B. 20-30 percent
- C. 2-10 percent
- D. 60-70 percent

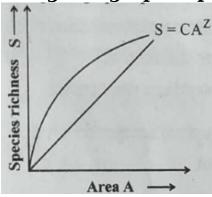
Answer: C

Solution:

Solution:

Question 23

The given graph represents



Options:

A. Population growth

B. Enzyme activity

C. Species area relationship

D. Growth of organisms

Answer: C

Solution:

Solution:

Question 24

Cuscuta is an example of

Options:

A. Predation

B. Broad Parasitism

C. Endoparasitism

D. Ectoparasitism

Answer: D

Solution:
Question 25
Particulates of size pose greatest risk to human health.
Options:
A. Less than 7.5 micrometers in diameter
B. Less than 2.5 micrometers in diameter
C. Less than 4.5 micrometers in diameter
D. Less than 3.5 micrometers in diameter
Answer: B
Solution:
Solution:
Question 26
Maintenance of constant internal environment is called as
Options:
A. Osmoregulation
B. Metastasis
C. Homeostasis
D. Thermoregulation
Answer: C
Solution:
Solution:
Question 27
Bovine spongiform encephalopathy is caused by

- A. Fungi
- B. Viroids

C. Prions
D. Virus
Answer: C
Solution:
Solution:
Question 28
Phycoerythrin and Floridian starch is found in
Options:
A. Red algae
B. Blue - green algae
C. Green algae
D. Brown algae
Answer: A
Solution:
Solution:
Question 29
Different types of respiratory organs like gills, book gills, book lungs and trachea are present in
Options:
A. Annelids
B. Sponges
C. Molluses
D. Arthropods
Answer: D
Solution:
Solution:

Q 11 2 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Which of the following plant is used to extract Colchicine?
Options:
A. Tulip
B. Colchicum
C. Aloe
D. Asparagus
Answer: B
Solution:
Solution:
Question 31
Rows of S-shaped setae in the body of earthworm are present in all the segments, except
Options:
A. the first segment
B. the last segment
C. the first and last segment
D. the first, last and clitellum
Answer: D
Solution:

Solution:

Question 32

Cell theory was formulated by

- A. Schwann and Robert Brown
- B. Schleiden and Schwann
- C. Robert Hook and Robert Brown

D. Schleiden and Robert Brown
Answer: B
Solution:
Solution:
Question 33
The type of Polysaccharide present in a cotton fibre
Options:
A. Glycogen
B. Starch
C. Insulin
D. Cellulose
Answer: D
Solution:
Solution:
Question 34
Enzyme involved in crossing over
Options:
A. Ligase
B. Recombinase
C. Polymerase
D. Endonuclease
Answer: B
Solution:
Solution:
Question 35

Options:	
A. Maize	
B. Tomato	
C. Potato	
D. Pea	
Answer: A	
Solution:	
Solution:	
Question 36	
Respiratory quotient of glucose is	
Options:	
A. 1.0	
B. 0	
C. 0.7	
D. 0.9	
Answer: A	
Solution:	
Solution:	
Question 37	
A person suddenly starts coughing while swa would have been due to improper movement	
Options:	
A. Tongue	
B. Epiglottis	
C. Diaphragm	

Kranz anatomy can be seen in

D. Neck

Answer: B

Solution:
olution:
Question 38
Binomial nomenclature is introduced by
Options:
A. John Ray
3. Carolus Linnaeus
C. Lamarck
D. Bentham and Hooker
Answer: B
Solution:
solution:
Question 39
Filtration of blood during urine formation takes place in
Options:
A. Glomerulus
B. DCT
C. PCT
D. Collecting duct
Answer: A
Solution:
folution:
Ouestion 40

Corpus Callosum connects the

A. Spinal cord with the brain
B. Two lobes of cerebellum
C. Two cerebral hemispheres
D. Cerebrum and cerebellum
Answer: C
Solution:
Solution:
Question 41
Menstrual cycle is exhibited by:
Options:
A. Tiger
B. Cow
C. Rat
D. Apes
Answer: D
Solution:
Solution:
Question 42
An example of dioecious plant :
Options:
A. Papaya
B. Cucurbita
C. Coconut
D. Mango
Answer: A
Solution:

Question 43
talk of the Stamen is:
ptions:
. Peduncle
. Filament
. Pedicel
. Petiole
nswer: B
olution:
olution:
Question 44
The ovule of angiosperm is technically known as :
ptions:
. Megaspore
. Megasporangium
. Megasporophyll
. Megaspore mother cell
nswer: B
olution:
olution:
Question 45
ypical mature embryosae of angiosperm is

- A. 8 nucleated 1 celled structure
- B. 8 nucleated 8 celled structure
- C. 8 nucleated 7 celled structure

D. 7 nucleated 8 celled structure
Answer: C
Solution:
Solution:
Question 46
One of the 2000 years old viable seed, discovered during the archeological excavation at King Herold's near dead sea.
Options:
A. Lupin
B. Sunflower
C. Phoenix dactylifera
D. Maize
Answer: C
Solution:
Solution:
Question 47
The testis are situated outside the abdominal cavity in scortum as it helps to $ \\$
Options:
A. Regulates hormone secretion
B. Store sperm
C. Release sperm
D. Maintain the low temperature
Answer: D
Solution:
Solution:

Identify the odd one from the following:

Options:

A. Isthamus

B. Fimbriae

C. Labia minora

D. Infundibulum

Answer: C

Solution:

Solution:

"Isthmus," "Fimbriae," and "Infundibulum" are anatomical terms related to the female reproductive system.

The isthmus refers to a narrow portion or constriction, often found in the fallopian tubes.

Fimbriae are finger-like projections at the end of the fallopian tubes, responsible for capturing the released egg during ovulation and guiding it into the fallopian tube.

The infundibulum is the funnel-shaped opening of the fallopian tube near the ovary, which receives the egg from the ovary.

On the other hand, "Labia minora" is a term related to the external genitalia of the female reproductive system. It refers to the inner folds of skin located on either side of the vaginal opening. It is different from the other options, which are specific anatomical structures within the reproductive system.

Question 49

In which month of gestation, the first movements of foetus and appearance of hair on its head is observed?

Options:

A. 8th month

B. 1st month

C. 4th month

D. 5th month

Answer: D

Solution:

Solution:

The first movements of the fetus, known as "quickening," and the appearance of hair on its head, occur at different times during gestation.

The first movements of the fetus are usually felt by the mother between 18 to 25 weeks of gestation. This can vary from woman to woman and pregnancy to pregnancy. Initially, the movements may feel like flutters or gentle taps, and as the fetus grows, the movements become more pronounced and noticeable.

As for the appearance of hair on the fetus's head, it typically occurs around the 14th to 16th week of gestation. This is a developmental milestone when the hair follicles start forming, and fine hair, known as lanugo, begins to grow on the fetus's body, including the scalp. The lanugo hair helps regulate the fetus's body temperature and usually sheds before birth.

herefore, the appearance of hair on the fetus's head is observed earlier in gestation compared to the first movement which are felt later in the second trimester.		
Question 50		
The most abundant type of WBC cells		
Options:		
A. Monocytes		
B. Basophils		
C. Neutrophils		
D. Eosinophils		
Answer: C		
Solution:		
Solution:		
Question 51		
Which of the following is correctly matched ?		
Options:		
A. Spores - Sponge		
B. Conidia - Hydra		
C. Gemmules - Amoeba		
D. Bulbil - Agave		
Answer: D		
Solution:		
Solution:		
Question 52		
The technique advised by a doctor to overcome the problem of infertility :		

A. RTI

B. MTP						
C. ART						
D. RCH						
Answer: C						
Solution:						
Solution:						
Question 53						
Amniocentesis is a process to:						
Options:						
A. Determine the sex of the foetus						
B. Determine any disease of heart						
C. Know about the disease of brain						
D. To grow cell on culture medium						
Answer: A						
Solution:						
Solution:						
Question 54						
The first human like being is						
Options:						
A. Homo menthus						
B. Homo erectus						
C. Homo habilis						
D. Homo sapiens						
Answer: C						
Solution:						
Solution:						

XO type of sex determination and XY type of sex determination are the examples of

- A. Female Homogamety
- B. Male Heterogamety
- C. Female Heterogamety
- D. Male Homogamety

Answer: B

Solution:

So	ılı	ut	i	or	1:

Question 56

Example for Non-Mendelian disorder:

Options:

- A. Cystic fibrosis
- B. Haemophilia
- C. Down's syndrome
- D. Thalassemia

Answer: C

Solution:

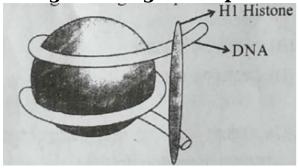
Solution:

Question 57

Gynecomastia is a symptom of

- A. Cri-du-chat syndrome
- B. Down's syndrome
- C. Kline Felter's syndrome

D. Turner's syndrome			
Answer: C			
Solution:			
Solution:			
Question 58			
The affected male in	the pedigree cha	rt is symbolized by:	
(A)	(B)	(C)	(D) O
Options:			
A. (A)			
B. (B)			
C. (C)			
D. (D)			
Answer: A			
Solution:			
Solution:			
Question 59			
The given diagram re	presents :Biology	Question Image	



- A. Mesosome
- B. Chromosome
- C. Ribosome
- D. Nucleosome

secreted by human placenta?