## Linear Regression

## Print slope, intercept & line

#### Linear regression

In linear regression, the equation that describes the factor-response relationships is Y=mX+C where Y and X are vectors that describe the response variable and the factor variable respectively.

### Multiple regression

In a multiple regression case, we're interested in the impact of not only one, but many different factors, on the response variable.

The equation can be written as  $Y=m_1X_1+m_2X_2+C$  where m1 and m2 are the coefficients of factors X1 and X2 respectively.

## Polynomial Regression

For polynomial regression, we might use higher powers of X to describe Y, as described in

$$Y = m_1 X + m_2 X^2 + C$$

where m1 and m2 are coefficients of the first and second powers of the factor.

### Logistic regression

Logistic regression is a statistical method for analysing a dataset in which there are one or more independent variables that determine an outcome.

The outcome is measured with a variable in which there are only two possible outcomes. It is used to predict a binary outcome (1 / 0, Yes / No, True / False) given a set of independent variables.

### **Applications**

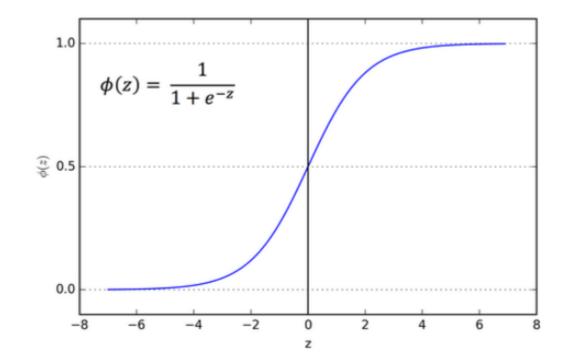
- Spam Detection : Predicting if an email is Spam or not
- Credit Card Fraud: Predicting if a given credit card transaction is fraud or not
- Health: Predicting if a given mass of tissue is benign or malignant
- Marketing: Predicting if a given user will buy an insurance product or not
- Banking: Predicting if a customer will default on a loan

### sigmoid/logistic function

In logistic regression, the goal is to determine a mathematical equation that can be used to predict the probability of event

The sigmoid/logistic function is given by the following

equation.



#### **Metrics for Performance Evaluation**

- Focus on the predictive capability of a model
  - Rather than how fast it takes to classify or build models, scalability, etc.
- Confusion Matrix:

	PREDICTED CLASS		
CLASS		Class=Yes	Class=No
	Class=Yes	а	b
	Class=No	С	d

a: TP (true positive)

b: FN (false negative)

c: FP (false positive)

d: TN (true negative)

# Metrics for Performance Evaluation...

	PREDICTED CLASS		
CLASS		Class=Yes	Class=No
	Class=Yes	a (TP)	b (FN)
	Class=No	c (FP)	d (TN)

Most widely-used metric:

Accuracy = 
$$\frac{a+d}{a+b+c+d} = \frac{TP+TN}{TP+TN+FP+FN}$$

# Metrics for Performance Evaluation...

	PREDICTED CLASS		
CLASS		Class=Yes	Class=No
	Class=Yes	a (TP)	b (FN)
	Class=No	c (FP)	d (TN)

$$precision = \frac{tp}{tp + fp},$$

$$recall = \frac{tp}{tp + fn},$$

#### Precision and Recall

**Precision** is the fraction of information retrieved that are relevant.

**Recall** is the fraction of relevant information that are retrieved.

	PREDICTED CLASS		
CLASS		Class=Yes	Class=No
	Class=Yes	a (TP)	b (FN)
	Class=No	c (FP)	d (TN)

$$ext{precision} = rac{tp}{tp+fp},$$

$$ext{recall} = rac{tp}{tp + fn},$$

#### F1 Score

Harmonic mean of precision and recall

$$F_1 = 2 * \frac{precision * recall}{precision + recall}$$