Principal Component Analysis (PCA)

Introduction

Principal component analysis (PCA) is a standard tool in modern data analysis - in diverse fields from neuroscience to computer graphics.

It is very useful method for extracting relevant information from confusing data sets.

Definition

Principal component analysis (PCA) is a statistical procedure that uses an orthogonal transformation to convert a set of observations of possibly correlated variables into a set of values of linearly uncorrelated variables called principal components.

The number of principal components is less than or equal to the number of original variables.

Goals

- The main goal of a PCA analysis is to identify patterns in data
- PCA aims to detect the correlation between variables.
- It attempts to reduce the dimensionality.

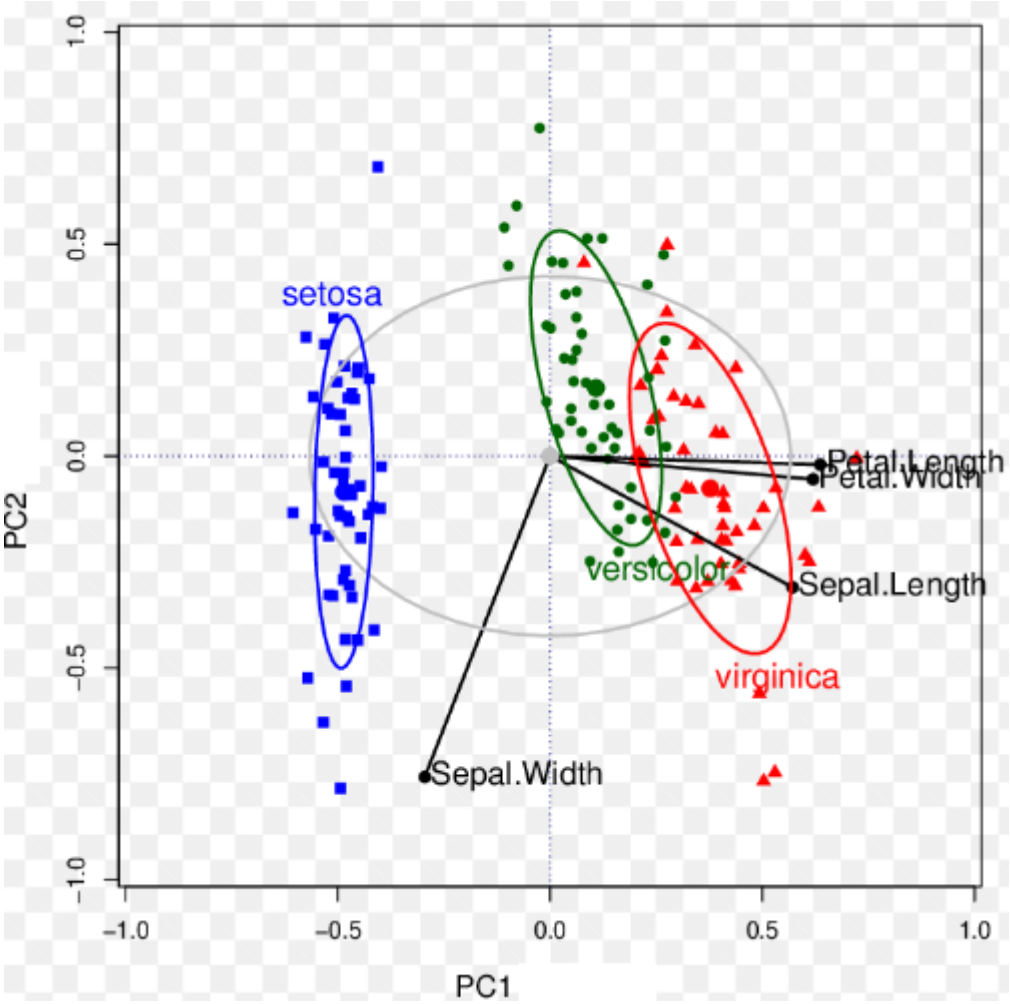
Dimensionality Reduction

It reduces the dimensions of a d-dimensional dataset by projecting it onto a (k)-dimensional subspace (where k<d) in order to increase the computational efficiency while retaining most of the information.

Transformation

This transformation is defined in such a way that the first principal component has the largest possible variance and each succeeding component in turn has the next highest possible variance.

PCA Example


setosa
versicolor
virginica
Petal.Length
Petal.Width
Sepal.Length
Sepal.Width
PC1
PC2
1.0
0.5
0.0
−0.5
−1.0
−1.0
−0.5
0.0
0.5
1.0

PCA Approach

- Standardize the data.
- Compute the Eigenvectors and Eigenvalues.
- Sort eigenvalues in descending order and choose the k-eigenvectors
- Construct the projection matrix from the selected k-eigenvectors.
- Transform the original dataset via projection matrix to obtain a k-dimensional feature subspace.

Limitation of PCA

The results of PCA depend on the scaling of the variables.

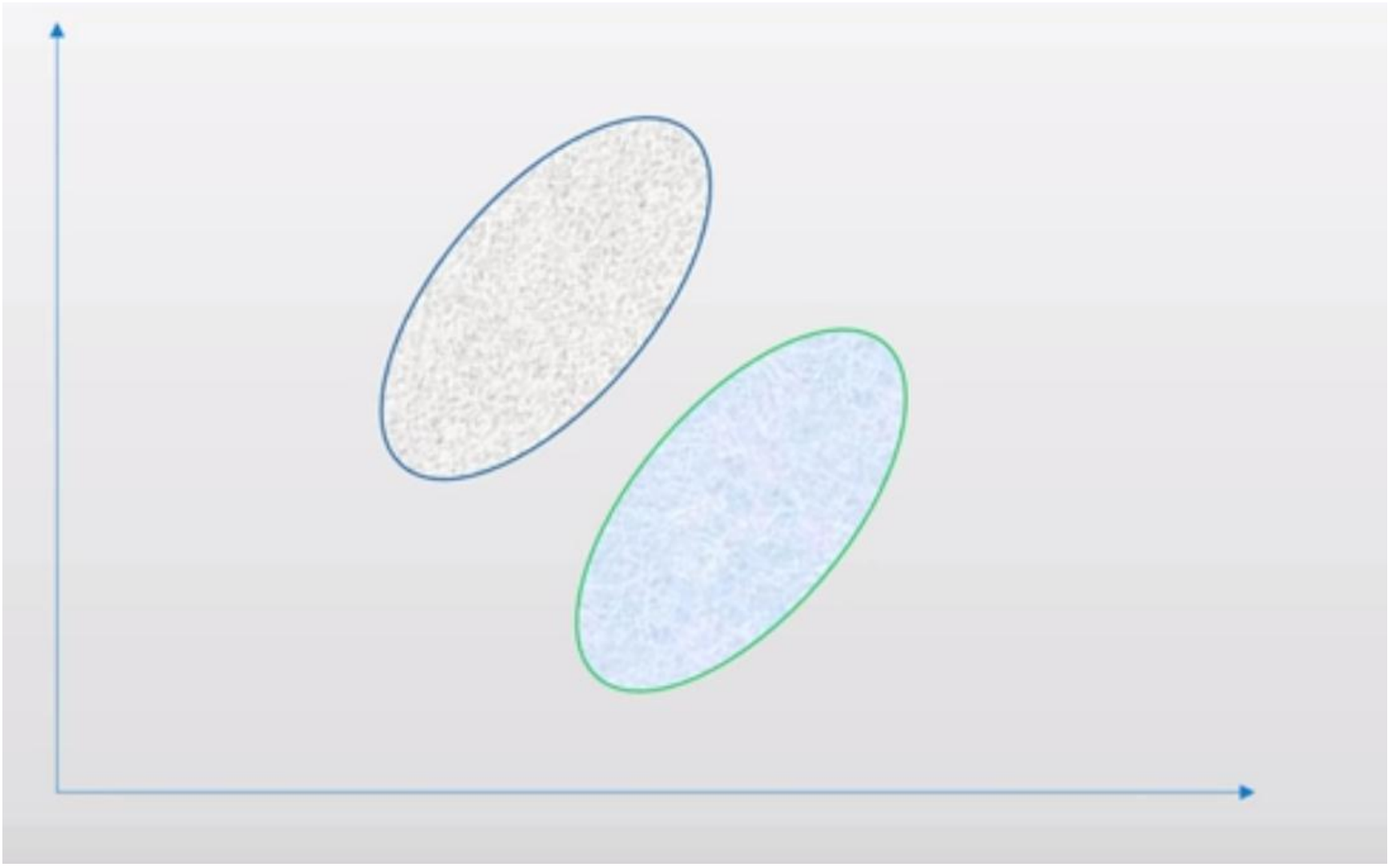
A scale-invariant form of PCA has been developed.

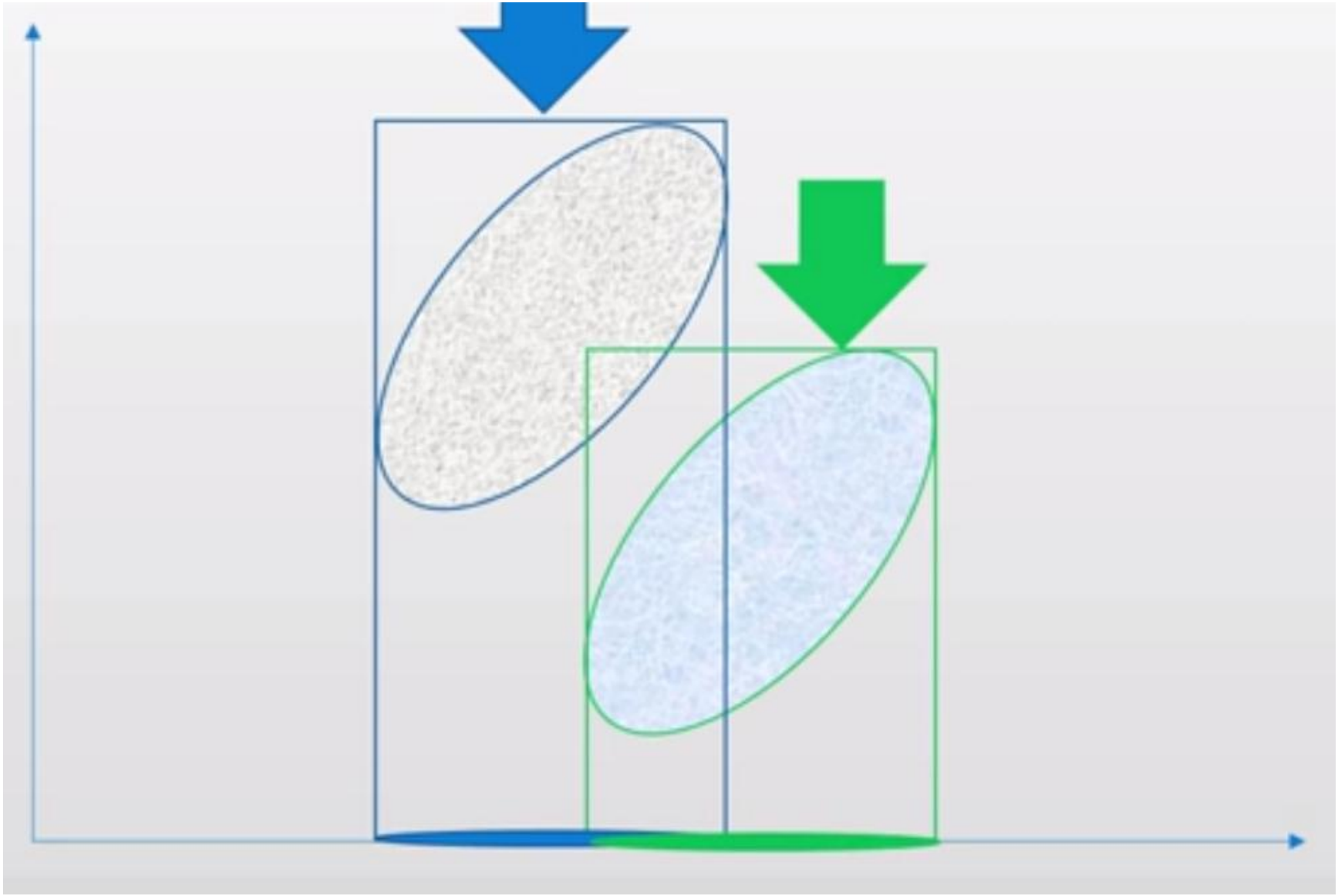
Linear Discriminant Analysis (LDA)

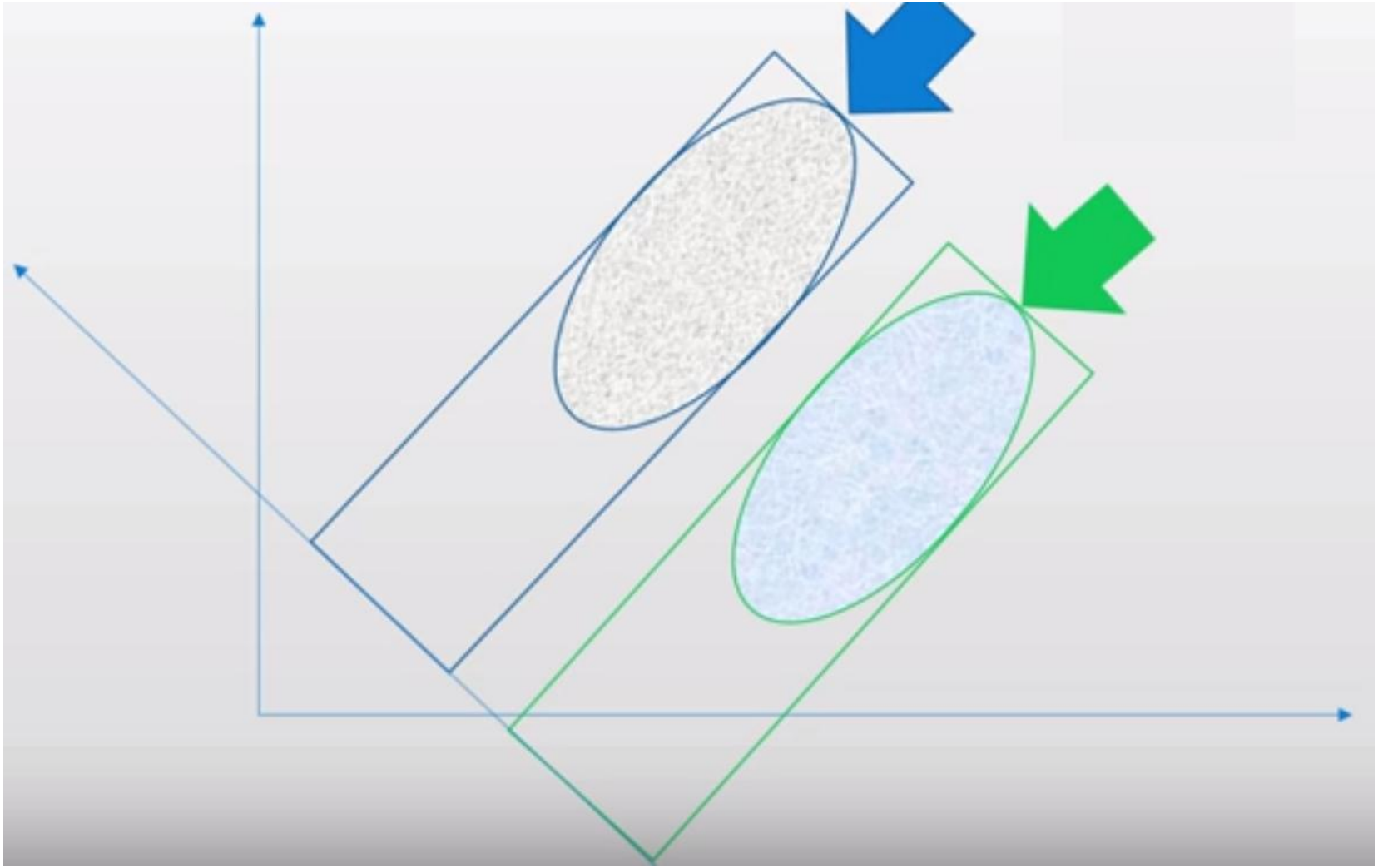
Introduction

Linear Discriminant Analysis (LDA) is used to solve dimensionality reduction for data with higher attributes

- Pre-processing step for pattern-classification and machine learning applications.
- Used for feature extraction.
- Linear transformation that maximize the separation between multiple classes.
- “Supervised” - Prediction agent







LDA steps:

1.Compute the d-dimensional mean vectors.

2.Compute the scatter matrices

3.Compute the eigenvectors and corresponding eigenvalues for the scatter matrices.

4.Sort the eigenvalues and choose those with the largest eigenvalues to form a d×k dimensional matrix

5.Transform the samples onto the new subspace.