

## Summary of Coordinate Transformations

Cartesian to Cylindrical  
Cylindrical to Cartesian

Cartesian to Spherical  
Spherical to Cartesian

## Divergence Theorem and Curl

Gradient - Scalar Field  
Divergence - Vector Field

If  $\nabla \cdot \vec{A} = 0$  then  $\vec{A}$  = solenoidal vector field (whatever goes in comes out)

Divergence Theorem

$$\int_V \nabla \cdot \vec{A} \, dV = \oint_S \vec{A} \cdot \vec{dS}$$
$$\int_V \nabla \cdot \vec{D} \, dV = \oint_S \vec{D} \cdot \vec{dS}$$

Circulation of  $\vec{A}$  around contour C

$$\Delta \oint_C \vec{A} \cdot d\vec{l}$$

\*\*\*  $\Delta$  is underlined in Nguyen's notation. Look into this.

Curl

$$\nabla \times \vec{A} = \frac{1}{\Delta s} \lim_{\Delta s \rightarrow 0} \oint_S \vec{A} \cdot d\vec{l}$$

Stoke's Theorem

$$\int_S \nabla \times \vec{A} \cdot d\vec{s} = \oint_C \vec{A} \cdot d\vec{l}$$

Two Null Identities

$$\nabla \times (\nabla V) \equiv 0$$

$$\nabla \cdot (\nabla \vec{A}) \equiv 0$$

## Maxwell's Equations

$$\vec{E}(x, y, z, t), \vec{H}, \vec{D}, \vec{B}, \vec{J}, \varphi_v$$

Faraday

$$\nabla \times \vec{E} = \frac{-\delta \vec{B}}{\delta t}$$

Ampere

$$\nabla \times \vec{H} = \vec{J} + \frac{-\delta \vec{D}}{\delta t}$$

Gauss

$$\nabla \cdot \vec{D} = \varphi_v$$

No Magnetic Charges

$$\nabla \cdot \vec{B} = 0$$

Modified Ampere's Law

$$\frac{\delta \vec{D}}{\delta t}$$

**Special Cases of Maxwell's Equations: Static  $\vec{E}$  and  $\vec{H}$**

$$\vec{E}, \vec{H} = f(x, y, z) \neq f(t) \rightarrow \frac{\delta}{\delta t} = 0$$

Faraday

$$\nabla \times \vec{E} = 0 \qquad \oint_C \vec{E} \cdot d\vec{l} = 0$$

Ampere

$$\nabla \times \vec{H} = \vec{J} \qquad \oint_C \vec{H} \cdot d\vec{l} = I$$

Gauss

$$\nabla \times \vec{D} = \varphi_v \qquad \oint_C \vec{D} \cdot d\vec{s} = Q$$

No Magnetic Charges

$$\nabla \times \vec{B} = 0 \qquad \oint_C \vec{B} \cdot d\vec{s} = 0$$

Modified Ampere's Law

$$\frac{\delta \vec{D}}{\delta t}$$

\*\*\* AUTHOR'S NOTE - MAKE VAR/CONST KEY \*\*\* - stopped reference on page 49 lecture notes