Lagrange polynomial to interpolate through points (1,1)= (-1,6), (0,2) (1,4) KI YI WE YE KIY P(n) = 1 yilila)

Pn-1 = 4, 1, (n) +4, 12(n) +4, 2 (n)

$$L_{1}(x) = \frac{x-x_{2}}{x_{1}-x_{2}} \times \frac{x-x_{3}}{x_{1}-x_{3}} = \frac{x-0}{-1-0} \times \frac{x-1}{-1-1} = \frac{x(x-1)}{2}$$

$$I_{2}(n) = \frac{x - x_{1}}{x_{2} - x_{1}} \times \frac{x - x_{3}}{x_{2} - x_{3}} = \frac{x + 1}{0 + 1} \times \frac{x - 1}{0 - 1} = (x + 1)(n - 1) - (x + 1)(n - 1)$$

$$(3(x)) = \frac{x-x_1}{x_2-x_1} + \frac{x-x_2}{x_2-x_2} = \frac{x+1}{1+1} \times \frac{x-0}{1-0} = 2(x+1)$$

$$P_2 = 91 \times (N-1) + 92 (-1)(N+1)(N-1) + 93 (N)(N+1)$$

= 
$$\frac{3}{8}(\tilde{x}-x)$$
 -  $2(\tilde{x}-1)$  +  $\frac{1}{4}(\tilde{x}+x)$  =  $3\tilde{x}-3x-2\tilde{x}+2\tilde{x}+2\tilde{x}$ 

2)a) Newton polynomial to interpolate through point (1,5)=(-1,6) (0,2) (1,4) Pr(n) = 91+ (n-n1) 92 + (n-n1) (n-n2) 93

41 = 91

$$92 = 91 + (x_2 - x_1) + (x_3 - x_1) + (x_3 - x_2) + (x_3$$

$$M = 6 - 8 + 2a_3$$
  $\Rightarrow 2a_3 = 6 \Rightarrow a_3 = 3$ 

1 bo +2 Co +3 do = b1

$$S_{1}^{4}(0) = 2(0+6d_{1}(0+1)) = 2(0+6d_{1})$$

$$S_{1}^{4}(0) = 2(1+6d_{1}(0+0)) = 2(1)$$

$$S_{0}^{4}(1) = 2(0+6d_{1}(0+0)) = 2(1)$$

$$S_{0}^{4}(1) = 2(0+6d_{1}(0+1)) =$$

$$S_{0}(x) = \frac{3}{2}x^{2} + \frac{9}{2}x^{2} - x + 2$$

$$S_{1}(x) = 2 - 1(x - 0) + \frac{9}{2}(x - 0)^{2} - \frac{3}{2}(x - 0)^{2}$$

$$= 1 - x + \frac{9}{2}x^{2} - \frac{3}{2}x^{2}$$

$$S_{1}(x) = \frac{3}{2}x^{2} + \frac{9}{2}x^{2} - x + 2$$

- 2.9) Newton interpolation is prefuelle due to its simplicity and direct fishing properties when he data is smooth and Evenly distributed
  - Piecesse Culicisphus are prefered as they provide usbust interpolation when the date is noisely and has irregular intervals
  - In one problem data is smooth and has no noise missing value we would pufu newton polynomial interpolation.