

## **DYNAMICAL PROCESSES IN COMPLEX** **NETWORKS**



**“SUDDEN TRANSITIONS IN COUPLED OPINION  
AND EPIDEMIC DYNAMICS WITH VACCINATION  
IN A NETWORK”**

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Citation:

MARCELO A PIRES, ANDRÉ L AND NUNO CROKIDAKIS.  
“SUDDEN TRANSITIONS IN COUPLED OPINION AND  
EPIDEMIC DYNAMICS WITH VACCINATION.”

# OBJECTIVES

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## **Understand Opinion Dynamics:**

- Use continuous opinion dynamics to model public attitudes on vaccination.
- Examine how opinions affect vaccination rates and disease transmission.

# OBJECTIVES

## **Model Epidemic Dynamics:**

- Apply the SIS model to simulate disease spread.
- Investigate how vaccination campaigns impact epidemic patterns.

# OBJECTIVES

## Explore Transition Points:

- Detect critical shifts in disease control influenced by public opinion and vaccine effectiveness.
- Utilize Monte Carlo simulations to explore sudden transitions in opinion and epidemic dynamics.

# **UNDERSTANDING OF THE PROJECT**

## **Approach:**

- Use the Susceptible-Infected-Susceptible (SIS) model with continuous opinion dynamics along with vaccination state to analyze their interaction.

The success or failure of a vaccination campaign is not solely reliant on factors like vaccine accessibility, vaccine effectiveness, and epidemiological variables. Public opinion about vaccination also plays a significant role. We address these opinions as a continuous factor.

While the use of discrete opinions (yes or no) is usually used, a continuous opinion is more appropriate because:

Reinforcing  
opinions based  
on interactions  
with peers

Opinions are not  
constant and  
change with time

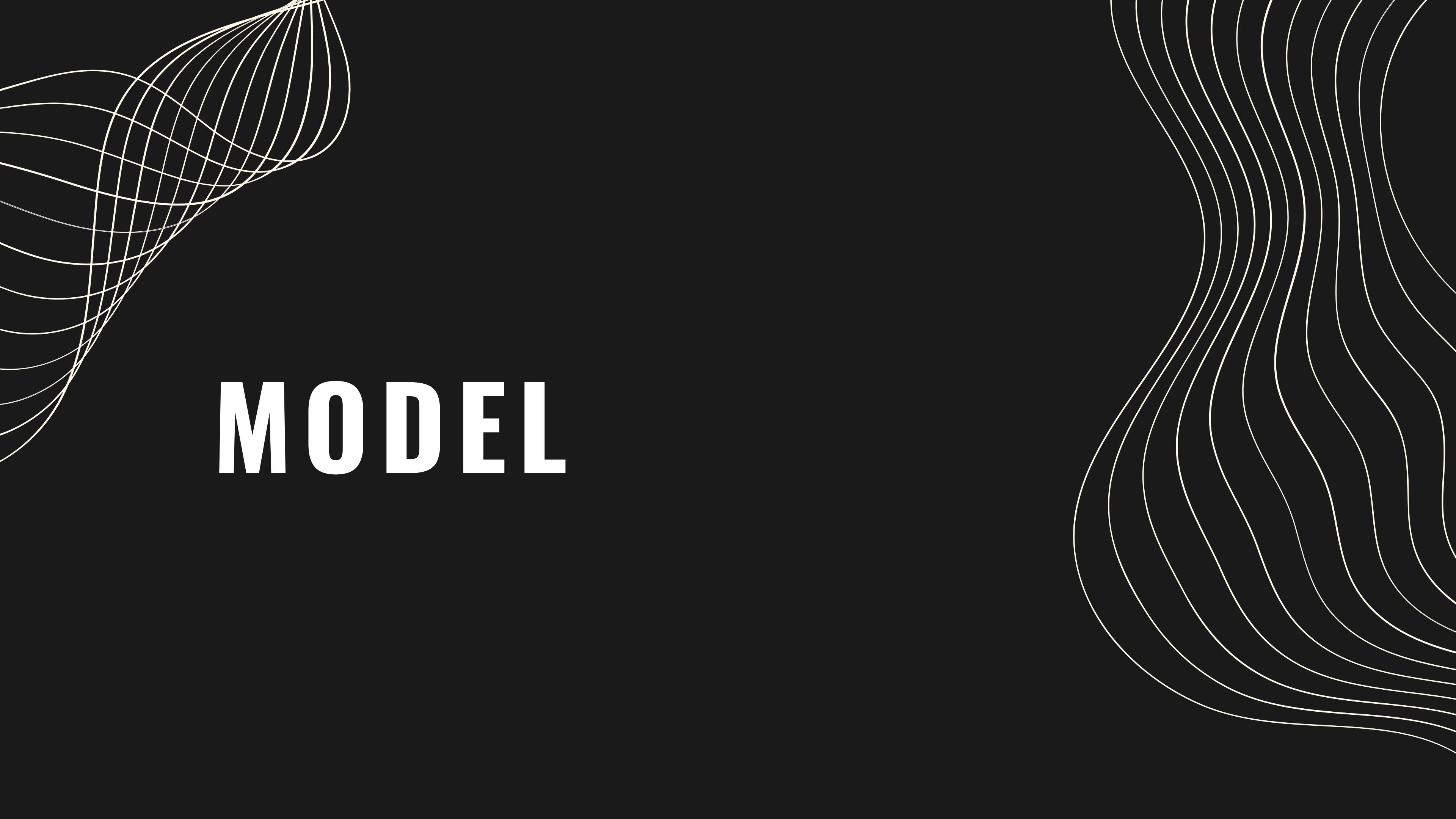
Real world opinions  
are more complex.  
Thus we need to  
incorporate  
extreme and  
moderate views.

We assume, based on kinetic models of collective opinion formation, that the opinion dynamics are governed by the equation:

$$o_i(t) = o_i(t - 1) + \epsilon o_j(t - 1) + w I(t - 1),$$

which considers that the opinion of each agent  $i$  at an instant  $t$  depends on:

1. His previous opinion
2. A peer pressure exerted by a randomly selected agent  $j$ , modulated by a stochastic variable  $\epsilon$  uniformly distributed in the interval  $[0, 1]$ , that introduces heterogeneity in the pairwise interactions
3. The proportion of Infected agents  $I(t - 1)$  modulated by an individuals' risk perception parameter  $w$ .



# MODEL

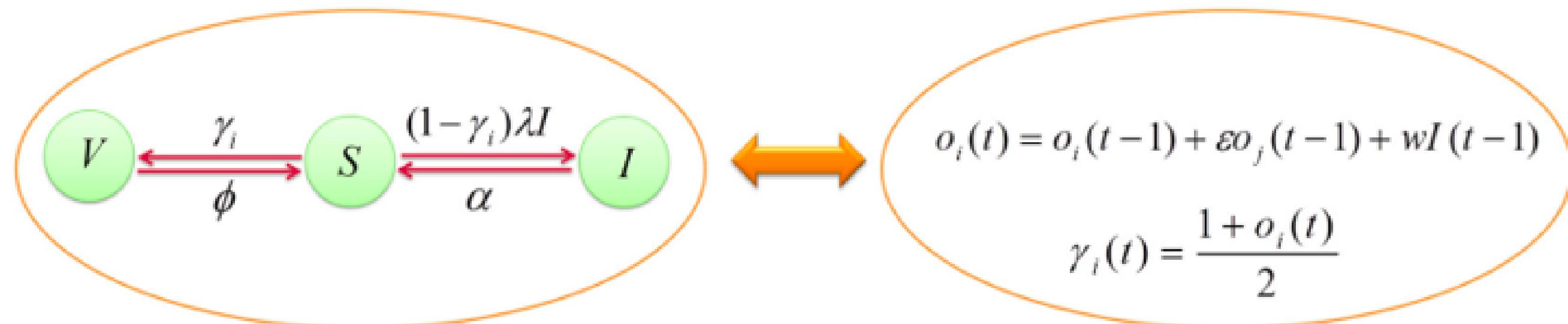
Individuals can undergo the following transitions among the epidemic compartments:

- $S \xrightarrow{\gamma_i} V$ : a Susceptible individual  $i$  becomes Vaccinated with probability  $\gamma_i$ ;
- $S \xrightarrow{(1-\gamma_i)\lambda} I$ : a Susceptible individual  $i$  becomes Infected with probability  $(1 - \gamma_i)\lambda$  if he is in contact with an Infected agent;
- $I \xrightarrow{\alpha} S$ : an Infected individual  $i$  recovers and becomes Susceptible again with probability  $\alpha$ ;
- $V \xrightarrow{\phi} S$ : a Vaccinated individual  $i$  becomes Susceptible again with the resusceptibility probability  $\phi$ .

Coupled vaccination and continuous opinion dynamics schematics.

The coupling between opinion and epidemic goes in both ways. The opinions influence the vaccination probability, by changing  $\gamma_i(t)$ .

The epidemic spreading increases the propensity of an agent getting vaccinated, through the term  $wI$

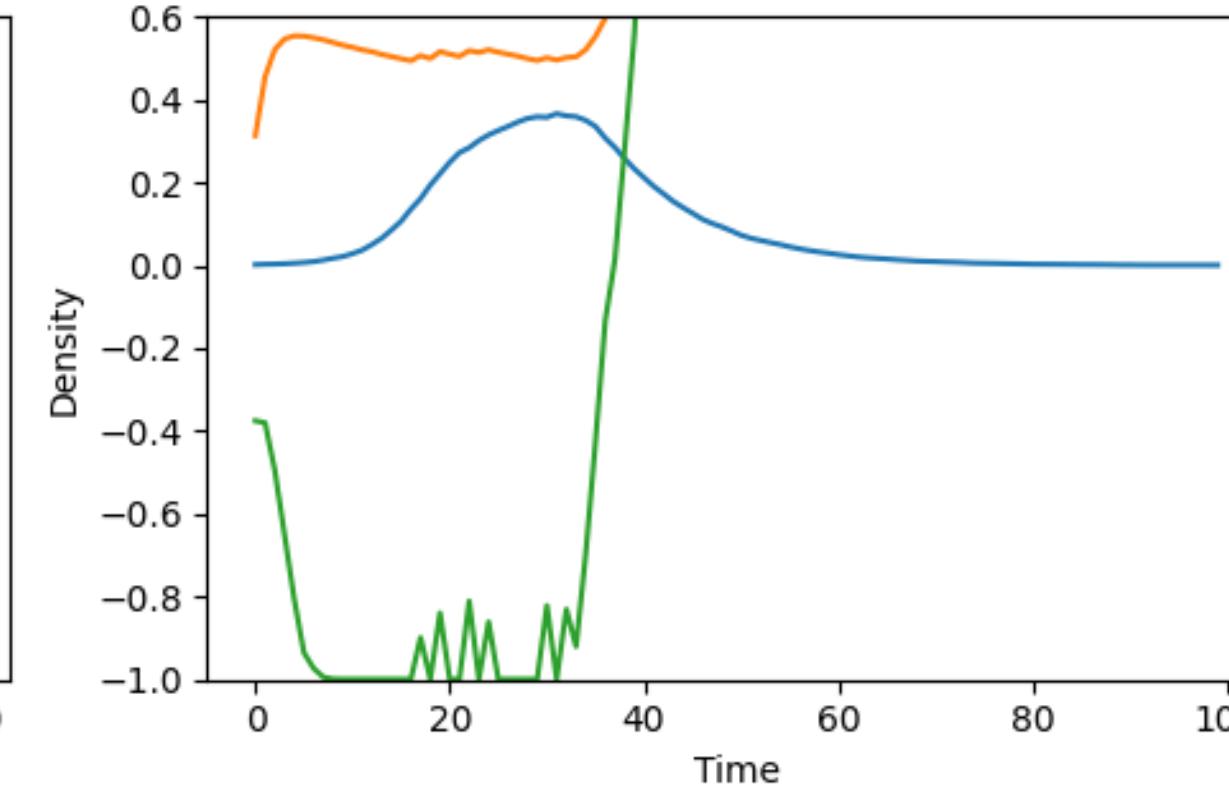
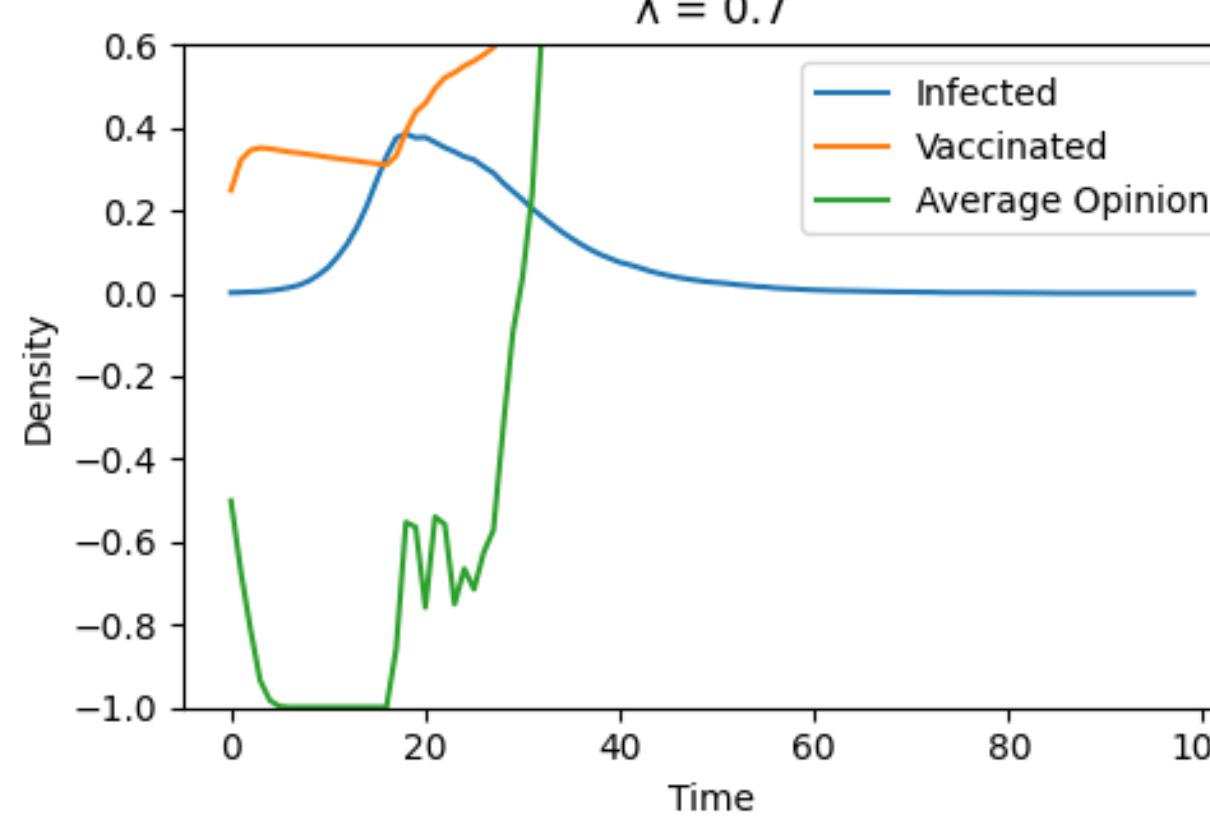
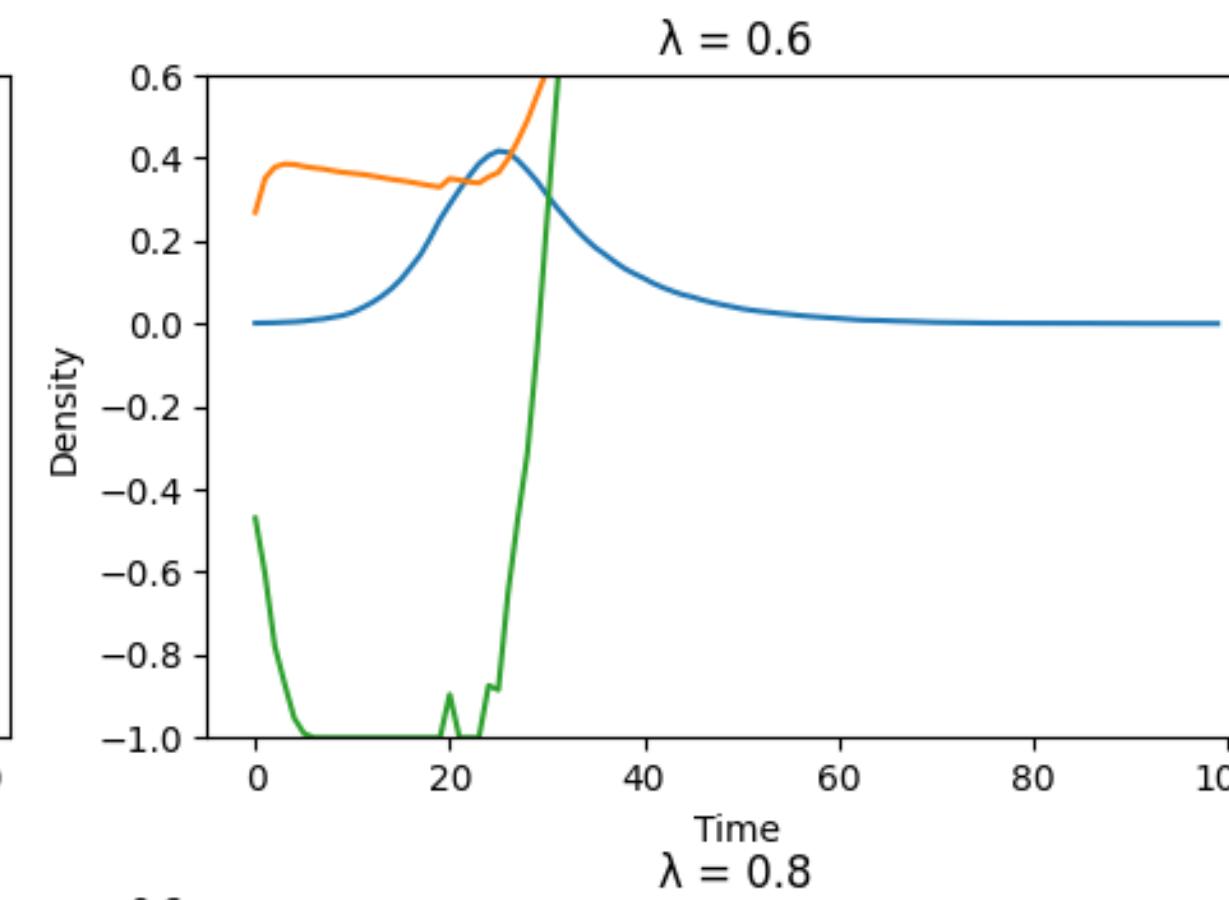
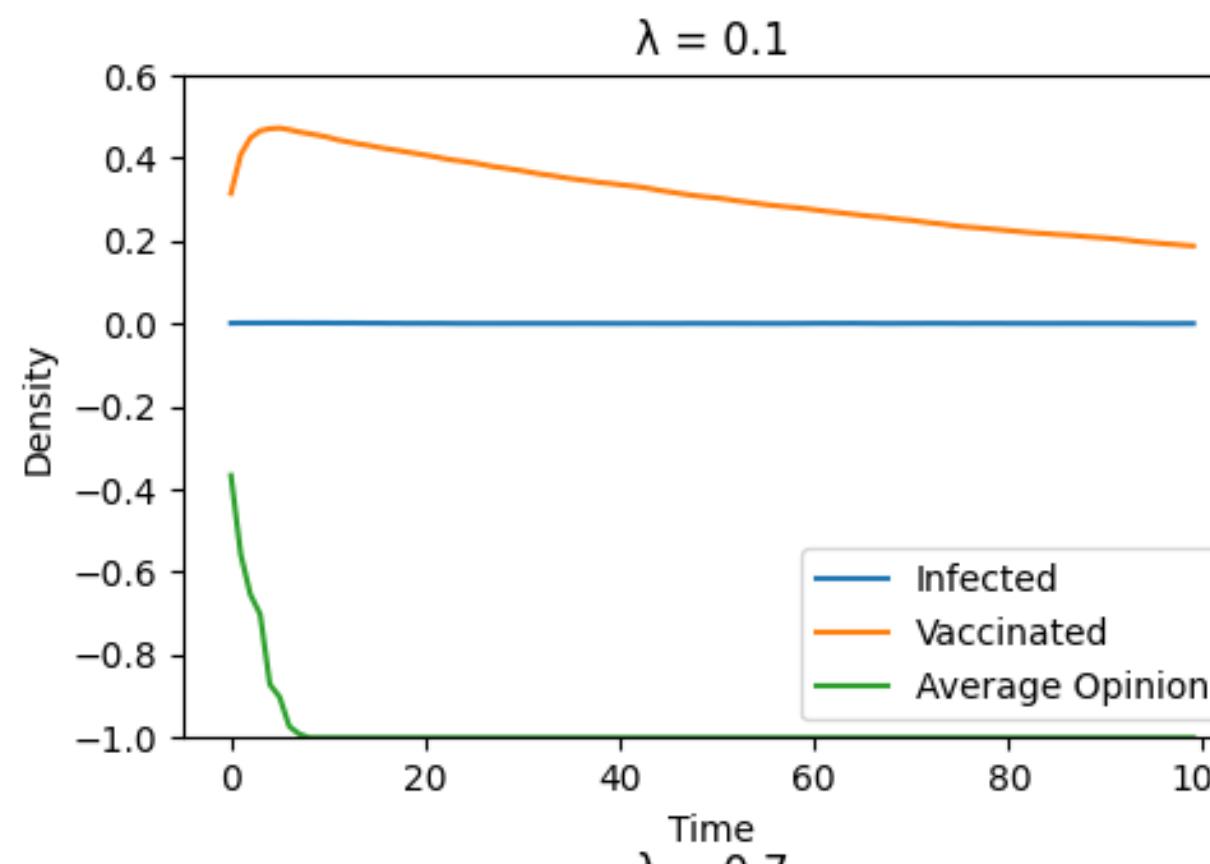


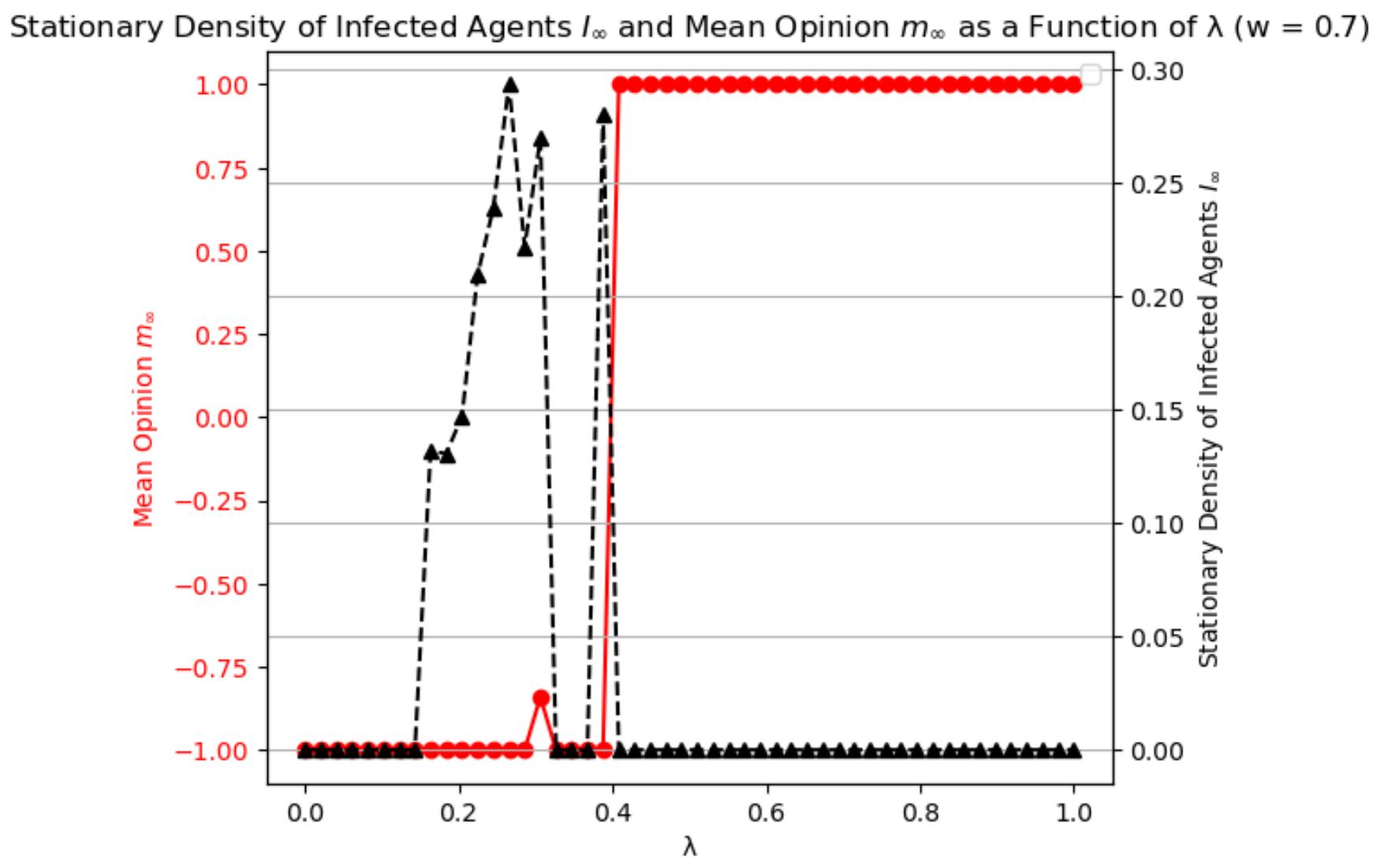
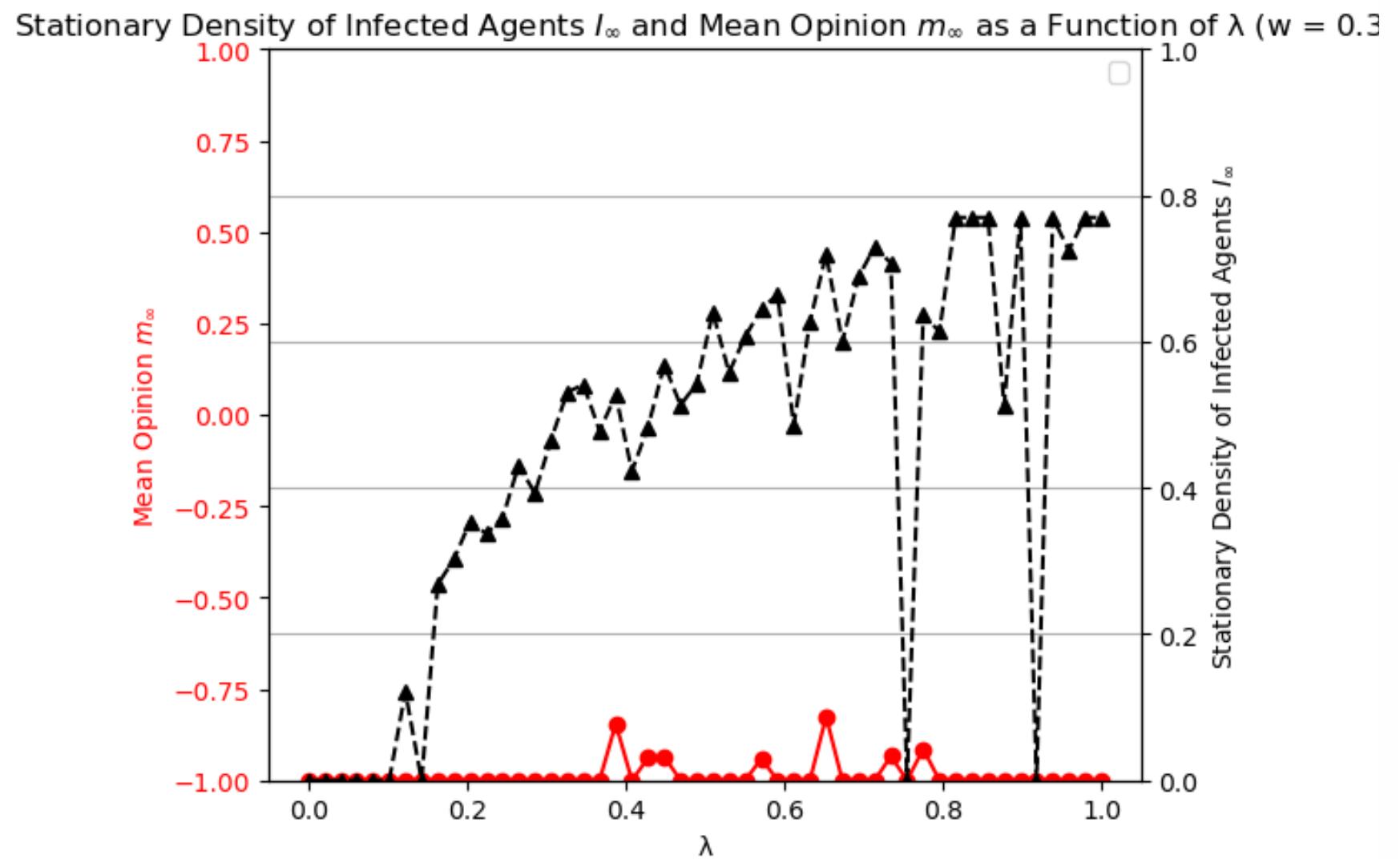
# RESULTS



# **BASELINE SIMULATION**

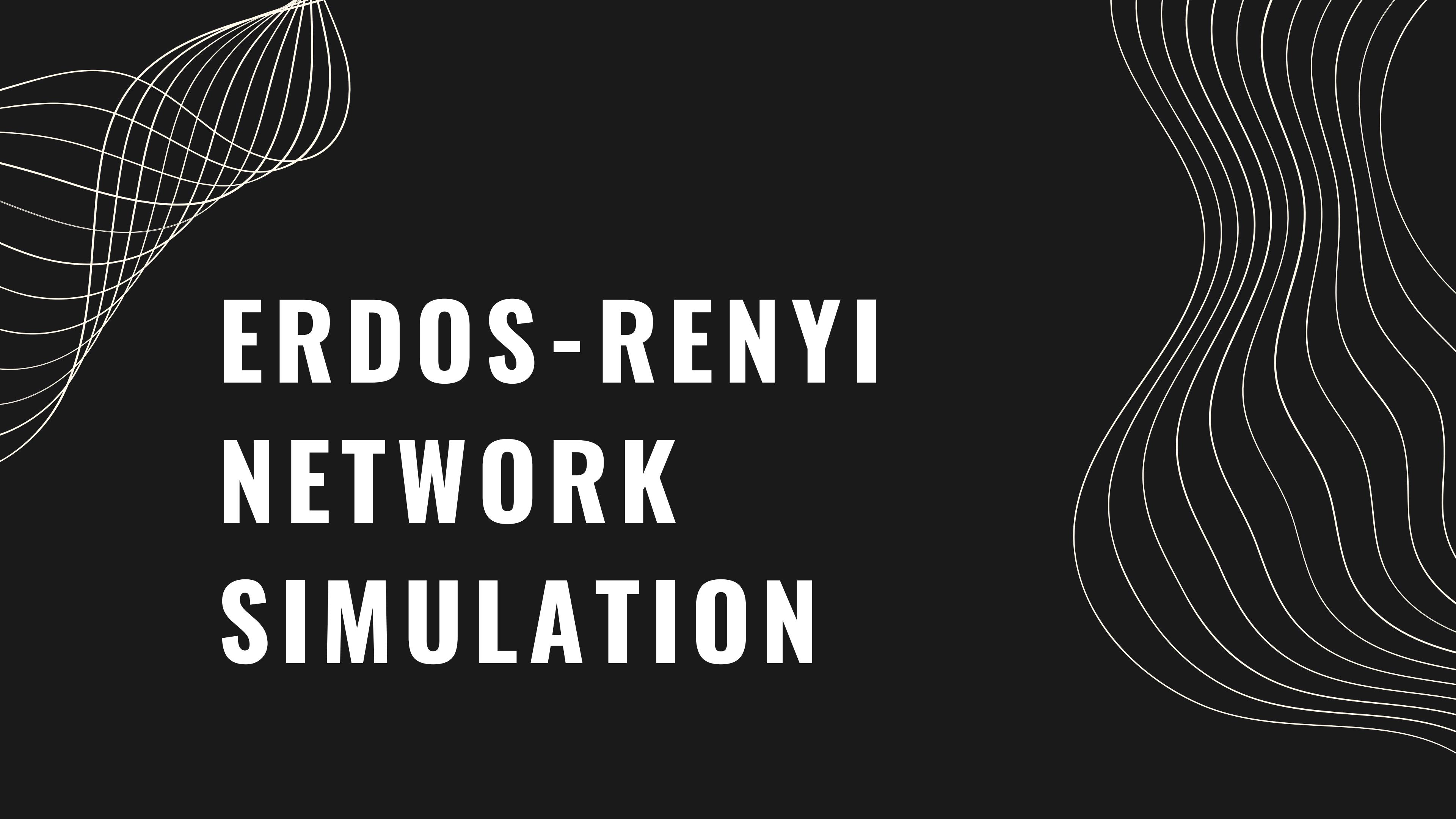
Tuning  $\lambda$  and plotting different temporal evolutions for  $I(t)$  ,  $V(t)$  and  $m(t)$  .







**NOVELTY**



# **ERDOS-RENYI NETWORK SIMULATION**

Mathematical model that explores how public opinion can influence the course of an epidemic. Essentially, the equation tracks how the opinion of an individual can be influenced by:

- Their own current opinion ( $O_i(t)$ )
- The influence of their neighbors ( $\sum_{j=1}^N A_{ij} O_j(t)$ ) weighted by the adjacency matrix ( $A_{ij}$ )
- A general influence term ( $\sum_{j=1}^N W K_j A_{ij}(t)$ ) modulated by the risk perception parameter ( $W$ )

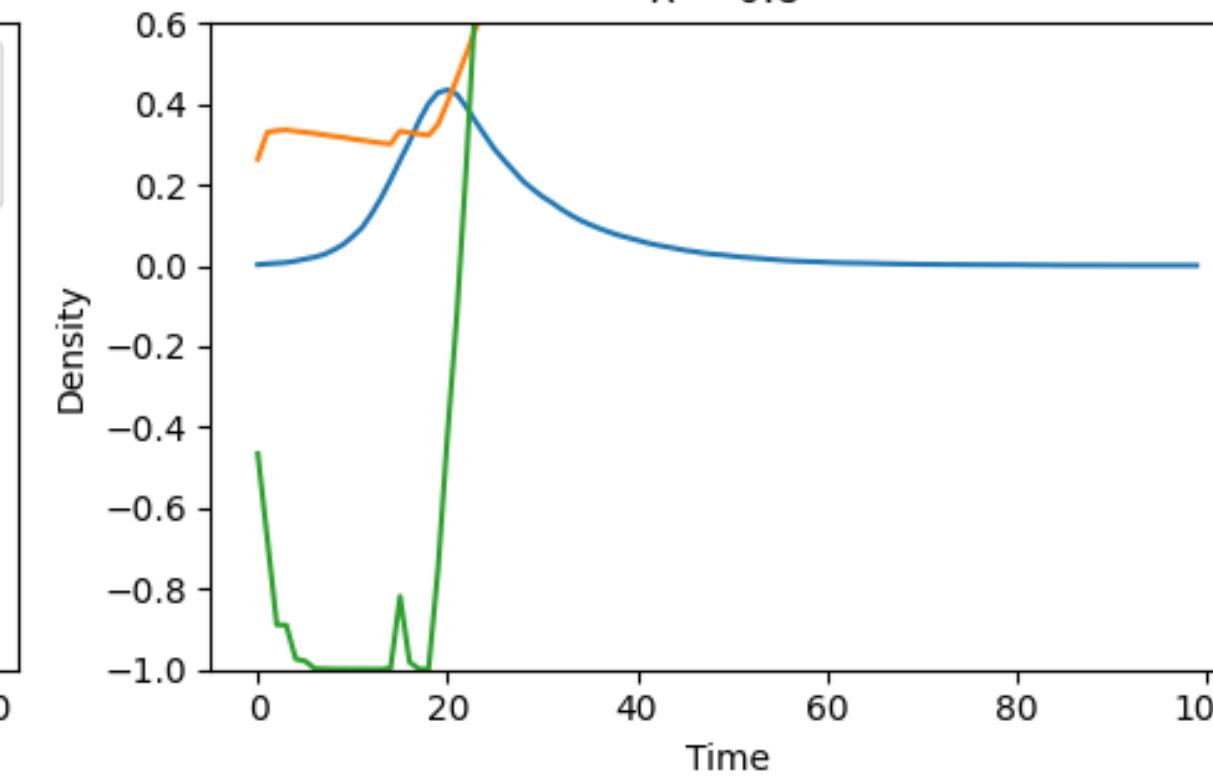
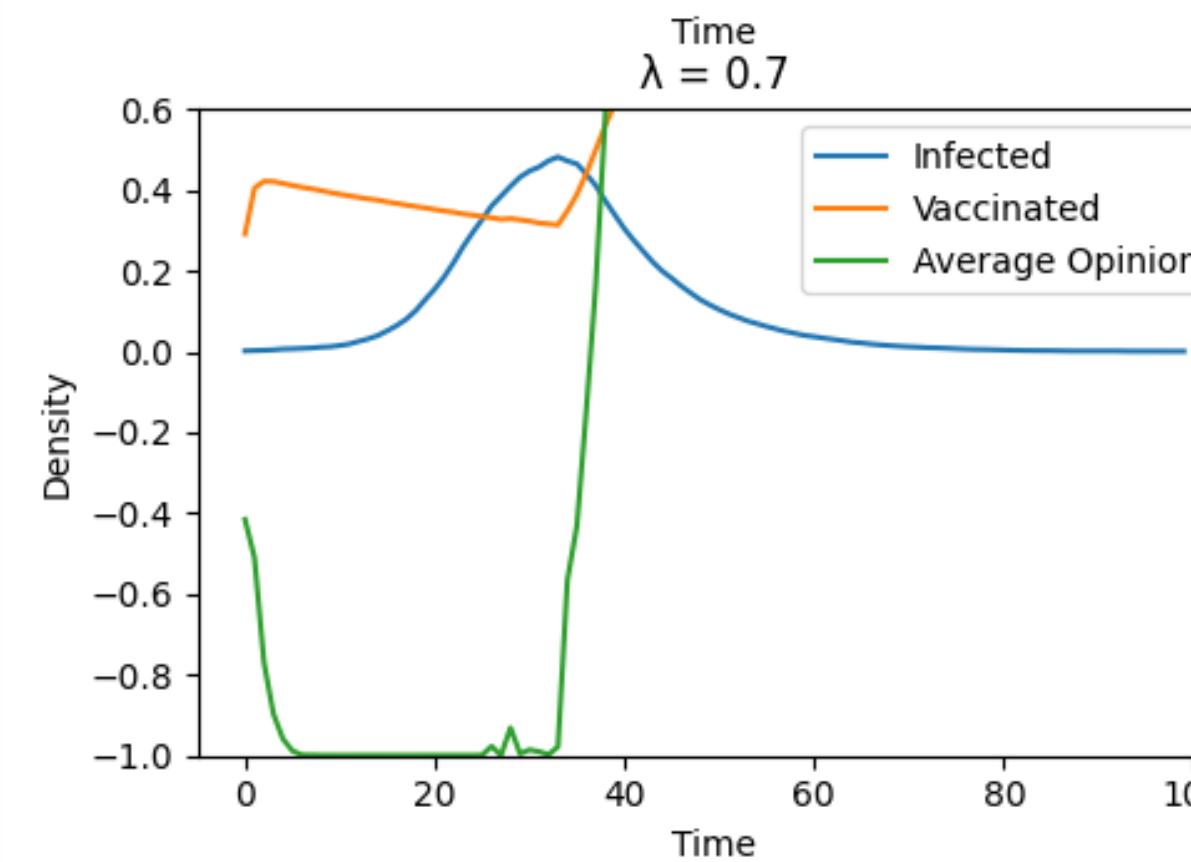
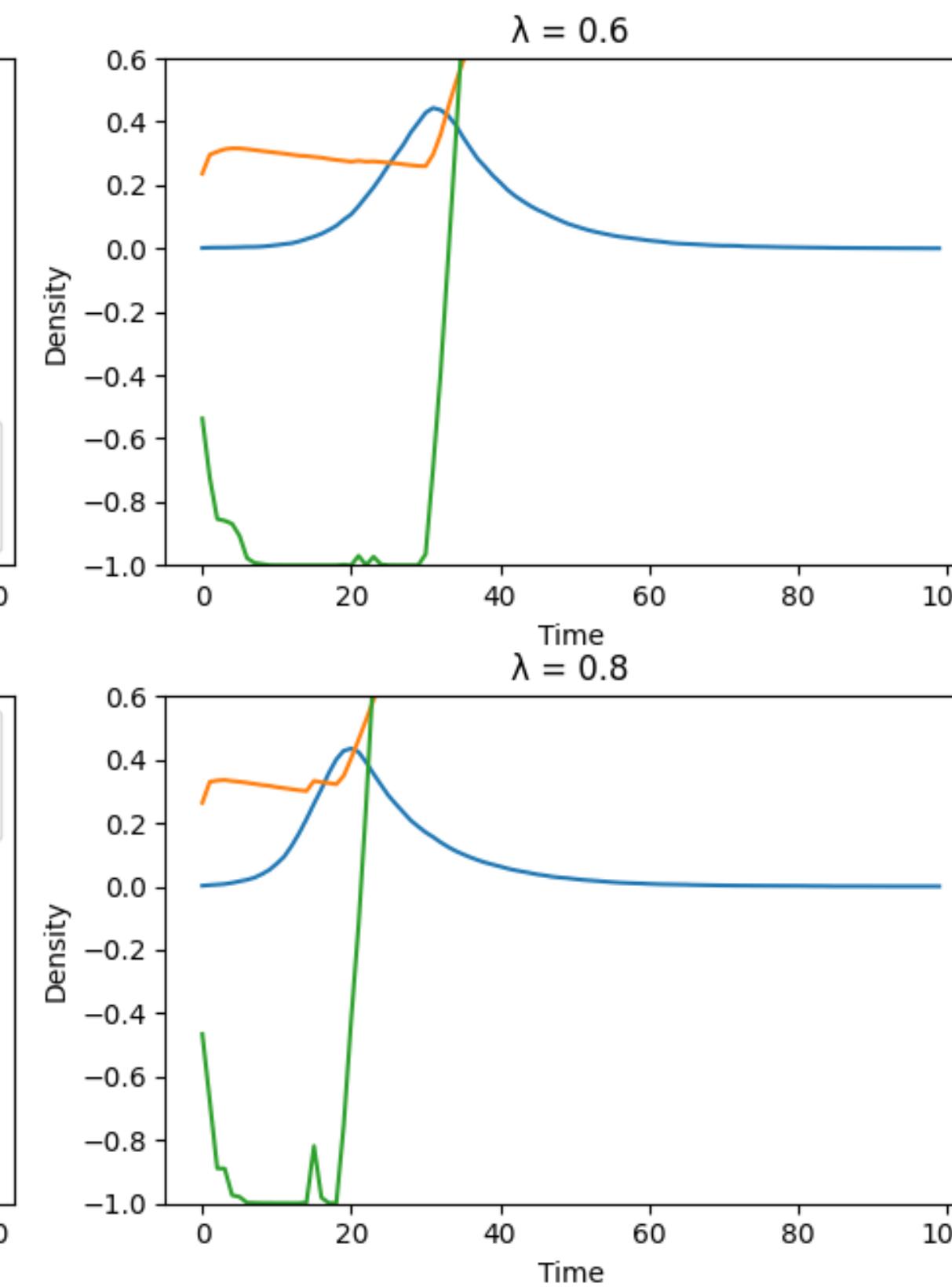
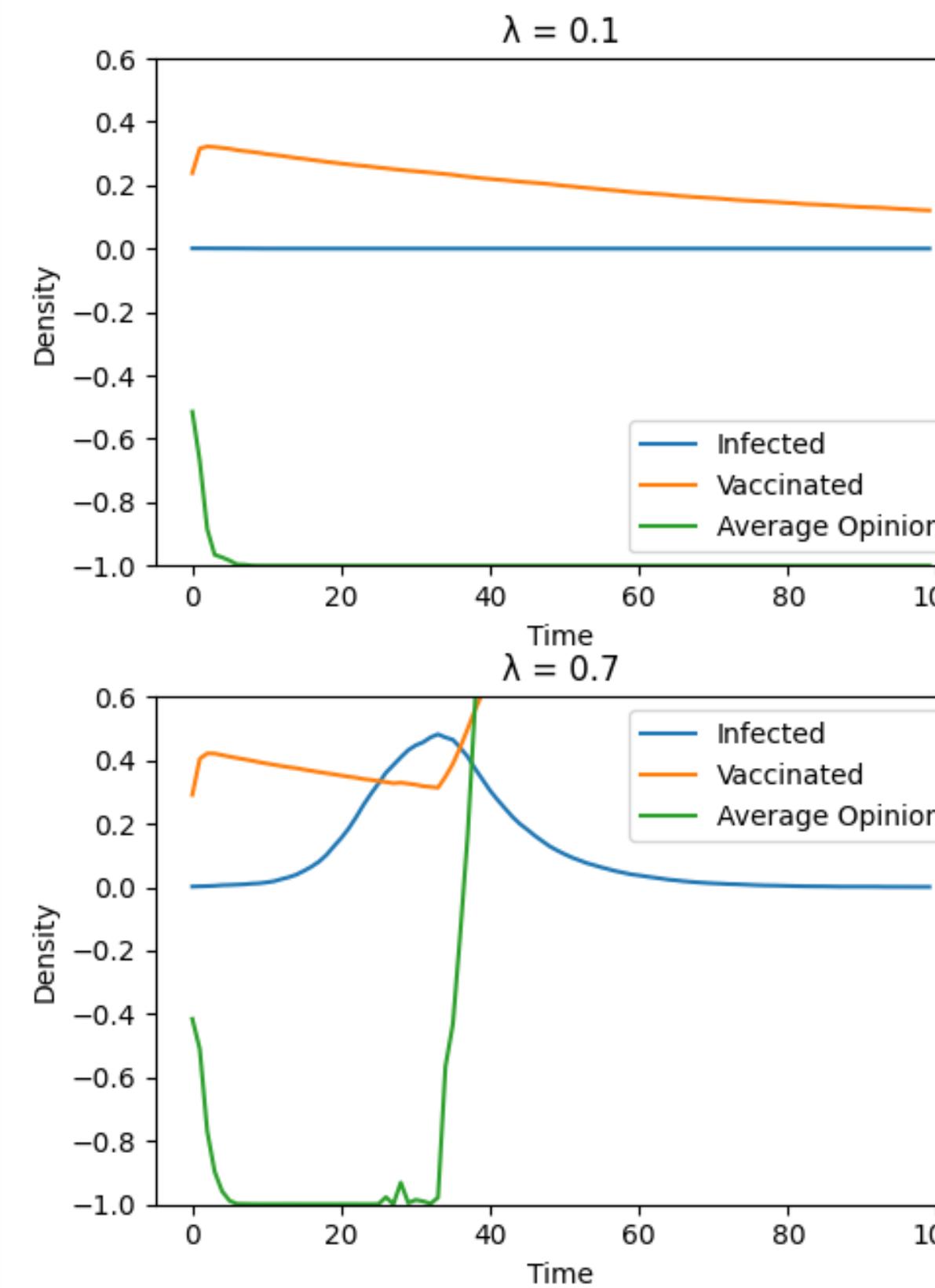
Overall, the model suggests that an individual's opinion about a certain topic can be impacted by their own perspective, how those around them view it, and their perceived risk associated with the topic.

$$O_i(t+1) = O_i(t) + \frac{\epsilon}{K_i} \sum_{j=1}^N A_{ij} O_j(t) + \frac{w}{K_i} \sum_{j=1}^N A_{ij} I_j(t)$$

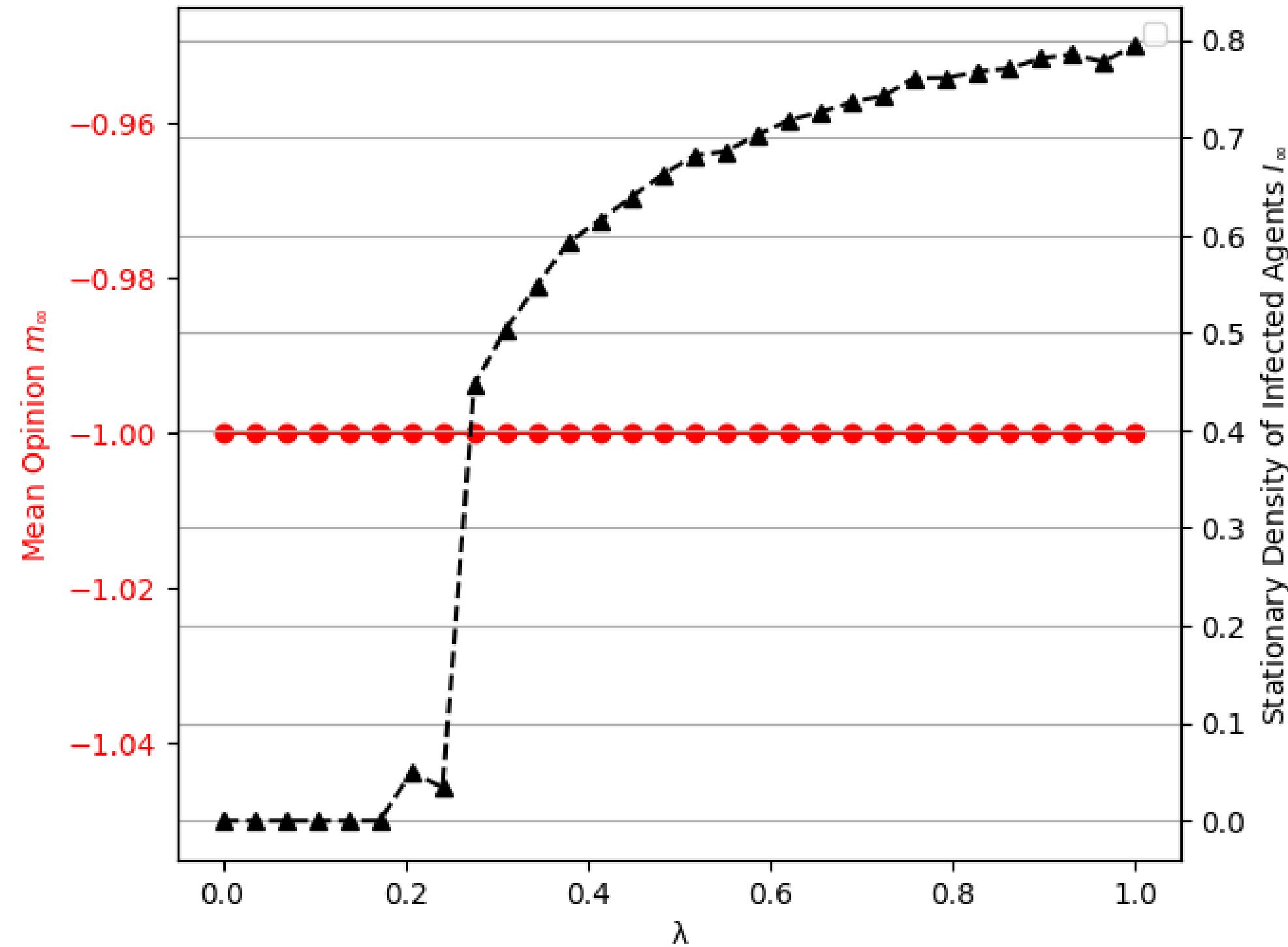


# **ER NETWORK RESULTS**

Tuning  $\lambda$  and plotting different temporal evolutions for  $I(t)$  ,  $V(t)$  and  $m(t)$  .



Stationary Density of Infected Agents  $I_\infty$  and Mean Opinion  $m_\infty$  vs  $\lambda$



D = 0.20  
w = 0.8  
alpha = 0.1  
phi = 0.01  
N = 10000  
mcs = 100

# THANK YOU

## *TEAM REWARD*

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