## Homework 7

October 24, 2018

## 1 Binary tree

The following questions use the following datatype definition.

```
datatype 'data tree =
   Empty |
   Node of 'data tree * 'data * 'data tree;
```

- A full binary tree is one in which every Node has either two Empty children or two Node children but not one of each. Write a function isFull of type 'a tree -> bool that tests whether a tree is full or not. Empty tree is full.
- 2. Write a function makeBST of type

```
'a list -> ('a * 'a -> bool) -> 'a tree
```

that organizes the items in a list into a binary search tree. The tree needs not to be balanced and you may assume that no items in the list is repeated.

The 2nd parameter of makeBST is a comparison function that compares two items and determine whether the first one is less than the second one or not.

A binary search tree is either empty or it has two subtrees and a data item x, where the items in the left subtree are all smaller than x, the items in the right subtree are greater than x, and the two subtrees are binary search tree as well.

For example,

```
- makeBST [1,3,2] (op <);
val it = Node (Node (Empty,1,Empty),2,Node (Empty,3,Empty)) : int tree</pre>
```

Note that depending on your implementation, the shape of the tree may look different though it should contain the same elements.

## 3. Write a function searchBST of type

```
''a tree -> (''a * ''a -> bool) -> ''a -> bool
```

that searches a binary search tree for a given data element and returns true if it is found and false otherwise. Your solution should only search subtrees that may contain the element you are looking for.

If we apply the function in the following way searchBST tree f e, then searchBST should first compare e with the tree data d using = to see if e and d are equal. If they are equal, then return true. Otherwises, searchBST should check if f(e, d) is true or false, if true, then search the left subtree and if false, it should search the right subtree.

For example, in the following program, the variable  ${\tt isFound}$  should be true.