

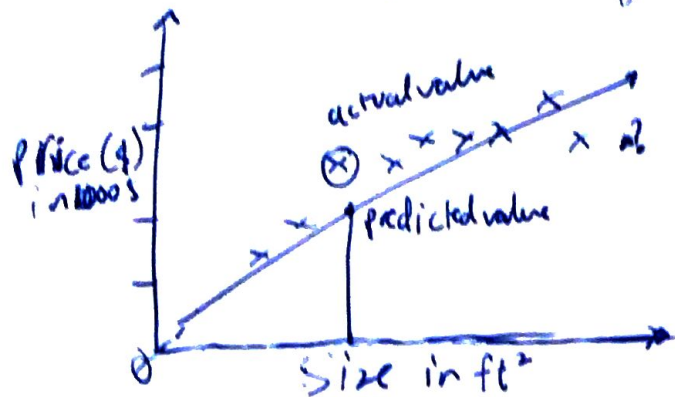
Linear Regression:

→ In Regression, $f(x)$ & $g(x)$ returns a continuous values.

→ let $g(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3 + \dots + \theta_D x_D$

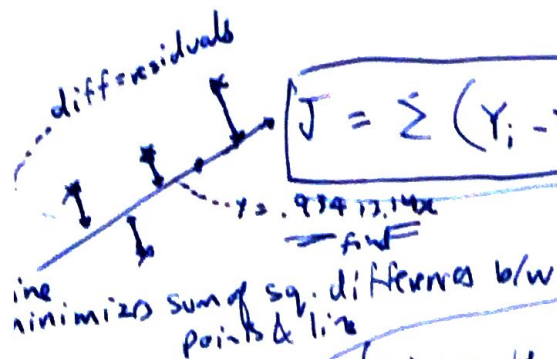
→ What are the params $\theta = [\theta_0, \theta_1, \theta_2, \dots, \theta_D]^T$ of model?

such that $g(x)$ works well in predicting target values?
 $(D+1)$ coefficients



error = $|y_i - g(x_i)|$
 in a value
 accumulated error = $\sum_{i=1}^N (|y_i - g(x_i)|)^2$
 we use (differentiable) squared value

$$\theta = [\theta_0, \theta_1]^T \text{ such that } g(x_i) \approx y_i \quad \forall (x_i, y_i)$$



$$J = \sum (y_i - \hat{y}_i)^2$$

we want to minimize J

$$\theta^* = \underset{\theta}{\operatorname{argmin}} \sum_{i=1}^N (y_i - \hat{y}_i)^2 \quad (\hat{y}_i = g(x_i, \theta))$$

bias = the 1st feature that we put to make a whole matrix

$$\begin{matrix} (Y - X\theta) \\ \uparrow \quad \uparrow \\ N \times 1 \quad N \times (D+1) \end{matrix} \quad (D+1) \times 1 \text{ col vector}$$

$$J = (Y - X\theta)^T (Y - X\theta)$$

minimize this?

→ take derivative wrt θ

→ set equal to 0 & solve for θ

$$\frac{\partial J}{\partial \theta} = 0$$