

Name: _____
MATH55 Section ____
Homework 2
Due Thursday 1/31

Give an example of a relation on a set that is both symmetric and transitive but not reflexive. Explain what is wrong with the following proof.

Statement: If R is symmetric and transitive, then R is reflexive.

Proof: Suppose R is symmetric and transitive. Symmetric means that $x R y$ implies $y R x$. We apply transitivity to $x R y$ and $y R x$ to give $x R x$. Therefore R is reflexive.

15.16 There is only one possible equivalence relation on a one-element set: If $A = \{1\}$, then $R = \{(1, 1)\}$ is the only possible equivalence relation. There are exactly two possible equivalence relations on a two-element set: If $A = \{1, 2\}$, then $R_1 = \{(1, 1), (2, 2)\}$ and $R_2 = \{(1, 1), (1, 2), (2, 1), (2, 2)\}$ are the only equivalence relations on A .

How many different equivalence relations are possible on a three-element set? ... on a four-element set?

16.8 Continued from the previous problem. Suppose six of these people are men, and the other six are women. In how many ways can they join hands for a circle dance, assuming they alternate in gender around the circle?

(Last problem: Twelve people join hands for a circle dance. In how many ways can they do this?)

16.13 One hundred people are to be divided into ten discussion groups with ten people in each group. In how many ways can this be done?