



Resolution

Conversion to CNF :-

1) $\text{IsProf}(\text{Alice})$

2) $\forall x (\text{IsProf}(x) \rightarrow \text{IsPerson}(x))$

$$\boxed{\sim(\text{IsProf}(x)) \vee (\text{IsPerson}(x))} \quad \left[\begin{array}{l} \text{Remove implication, drop universal} \\ \text{quantifier} \end{array} \right]$$

3) $\text{IsDean}(\text{John})$

4) $\forall x (\text{IsDean}(x) \rightarrow \text{IsProf}(x))$

$$\boxed{\sim(\text{IsDean}(x)) \vee (\text{IsProf}(x))} \quad \left[\begin{array}{l} \text{Remove implication, drop universal} \\ \text{quantifier} \end{array} \right]$$

5) $\forall x (\forall y (\text{IsProf}(x) \wedge \text{IsDean}(y)) \rightarrow \text{IsFriendOf}(y, x) \vee \sim \text{knows}(x, y))$

$$\sim(\text{IsProf}(x) \wedge \text{IsDean}(y)) \vee (\text{IsFriendOf}(y, x) \vee \sim \text{knows}(x, y))$$

$$\boxed{\sim \text{IsProf}(x) \vee \sim \text{IsDean}(y) \vee \text{IsFriendOf}(y, x) \vee \sim \text{knows}(x, y)}$$

$$6.) \forall x (\exists y (\text{IsFriendOf}(y, x)))$$

$$\boxed{\text{IsFriendOf}(F(x), x)} \quad [\text{Skolemization, Dropping universal quantifier}]$$

$$7.) \forall x (\neg \exists y (\text{IsPerson}(x) \wedge \text{IsPerson}(y) \wedge \text{Criticizes}(x, y) \rightarrow \neg \text{IsFriendOf}(x, y)))$$

$$\neg (\text{IsPerson}(x) \wedge \text{IsPerson}(y) \wedge \text{Criticizes}(x, y)) \vee (\neg \text{IsFriendOf}(x, y))$$

$$\boxed{(\neg \text{IsPerson}(x)) \vee (\neg \text{IsPerson}(y)) \vee (\neg \text{Criticizes}(x, y)) \vee (\neg \text{IsFriendOf}(x, y))}$$

$$8.) \text{Criticizes}(\text{Alice}, \text{John})$$

Alpha:-

$$\neg \text{IsFriendOf}(\text{John}, \text{Alice})$$

Not alpha:-

$$\text{IsFriendOf}(\text{John}, \text{Alice})$$

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