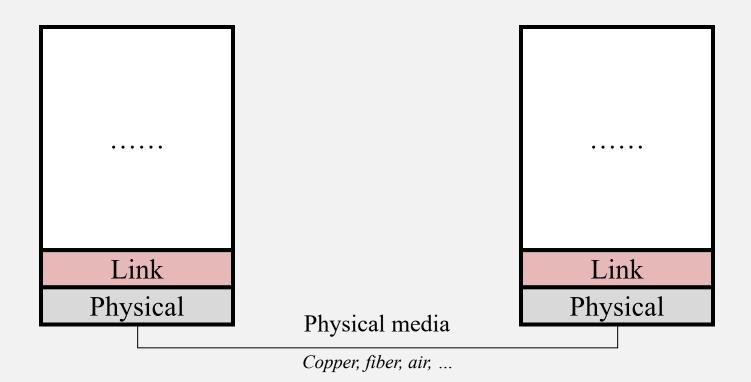
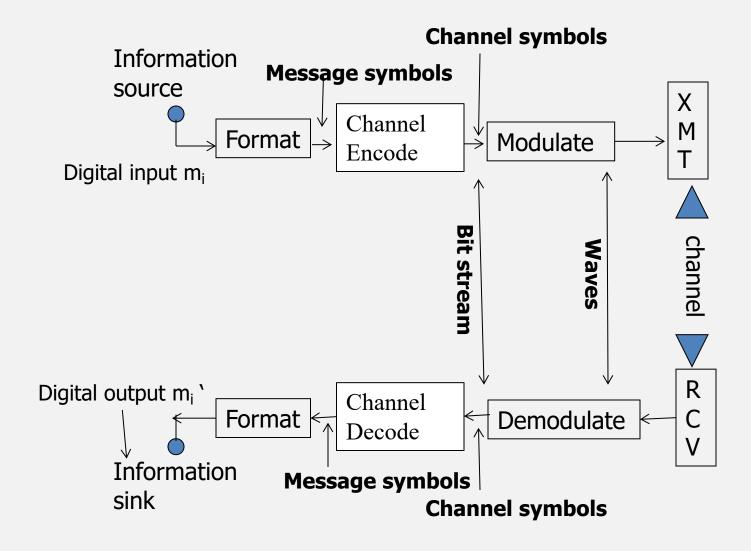


CSC/ECE 570 - Fall 2024, Section 002

## Where is PHY?



#### Block Diagram of a Digital Communication System



#### Bandwidth limited Bit rate

- Nyquist's theorem
  - Maximum bit rate =  $2H \log_2 V$  bits/sec
  - -H = bandwidth
  - -V = number of discrete states
- Shannon's theorem
  - Maximum bit rate =  $H \log_2 (1 + S/N)$  bits/sec
  - Note on application
    - SNR in Shannon's theorem ratio of power content  $(P_S/P_N)$
    - Usual unit of SNR dB, a logarithmic unit
    - $dB = 10 \log_{10} (P_S/P_N)$

## Question



#### **Shannon Capacity**

**Show Correct Answer** 

Based on the Shannon capacity formula, a client device sending application data to a server via a direct wireless link can always achieve H log2 (1 + S/N) bits/sec of application throughput, where H is the bandwidth, S is the signal strength, and N is the background noise.

Α

**TRUE** 

В

**FALSE** 

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# Question (consider Shannon Capacity)

Which of the following affect the theoretical limit of information that can be transmitted via a channel?

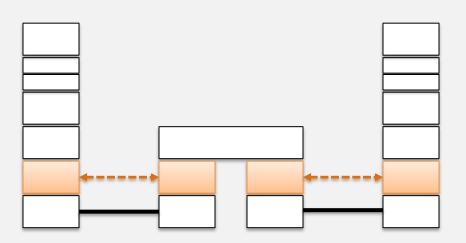
- **A** Bandwidth
- **B** Modulation
- **C** Noise
- D Interference
- E Overhead
- F Protocol
- **G** Distance



## Data Link Layer Perspective

- Second of the OSI Model
- Utilizes (unreliable) bitpipe from PHY layer
- Provides service to Networking layer
- Equipment: switch

• PDUs: "Frames"



## Data Link Layer Services

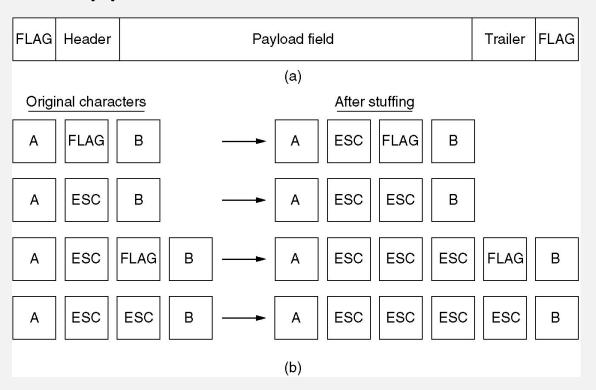
- Services Provided to the Network Layer
  - Framing
    - Logical bit groupings (header/trailers) more use at higher layers
  - Error Control
    - Error control overlaps with physical layer (bit errors 0->1)
    - DLC retransmission strategies
  - Flow Control
    - Matches dissimilar endpoint processing speeds (overwhelm)
    - Slow receiver should not be swamped by fast sender
    - Also a backward error correction mechanism
  - Optionally, mediate contention for shared medium
    - Such as Ethernet

## Utilizing Unreliable Bitpipe - Framing

- "Sometimes sender sends bits, sometime not"
- How does the receiver (receiving DLC) know when bits are being received, and when not?
  - Must create own (DLC layer) convention (protocol) about transmission of bits
  - Start with preamble, end with conclusion
  - Creates logical groups at DLC layer "frames"
  - Also serves as logical groups to encapsulate higher layer PDUs
    - Higher layers want service in multiple-byte chunks
    - Logical units determined by the logic of the higher layers
- Frame delineation 1) must start with (and end with) an easily recognizable set of bits 2) that are unlikely to arise randomly due to noise

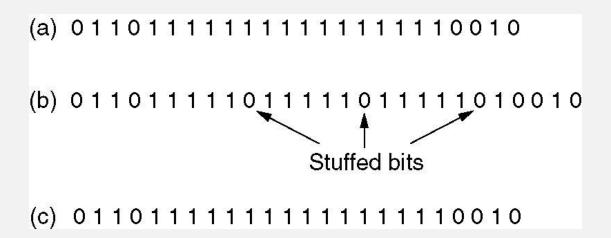
# Framing with FLAGs (1st way)

- FLAG is a distinctive bit pattern
  - Such as 01111110 (01<sup>6</sup>0)
  - Must not appear inside data

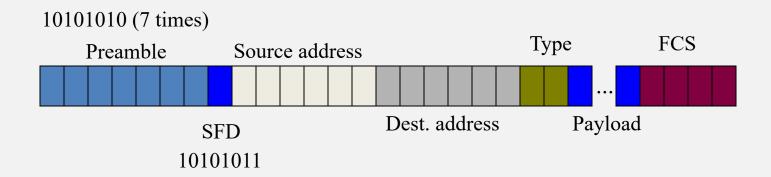


# Bit Stuffing (2<sup>nd</sup> way)

- Bit stuffing method
  - Delineate by pattern of many bits
  - Prevent pattern from occurring in data by few bits
  - Must be completely reversible, i.e. destuffable



## **Ethernet Frame**



## Data Link Layer Services

- Services Provided to the Network Layer
  - Framing
    - Logical bit groupings more use at higher layers
  - Error Control
    - Error control overlaps with physical layer (bit errors 0->1)
    - DLC retransmission strategies
  - Flow Control
    - Matches dissimilar endpoint processing speeds (overwhelm)
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  - Optionally, mediate contention for shared medium
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#### **Error Control**

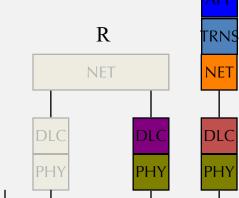
- Errors happen
- Detection
  - Can at least catch errors
  - ARQ strategies may come in
- Correction (Forward Error Correction FEC)
  - Better if we can
  - Sometimes essential due to link characteristics
- Involves error codes
  - Coding, not encryption

### Flow Control

 Potential data generation and transmission may be faster than consumption

Receiver might be "overwhelmed"

- Fast sender, slow receiver (root cause)
  - Also at E2E layer (transport, or app)
- Realistically, must stop and wait during transmission
  - Channel idle for some fraction of time
  - Possible to proactively use some of this time
  - Windowed flow control



D

### Flow Control vs. Error Control

- Flow control if sender "gets ahead" of receiver, must retransmit
- Error control 
   may need to retransmit because of error in channel as well
  - Error must be detected
  - Only non-erroneous copy at the sender
  - Receiver must request a repeat
  - Automatic Repeat ReQuest (ARQ)
- But sender needs to know
  - Requests are sometimes implicit

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#### **Error Control**

- Errors happen
- Detection
  - Can at least catch errors
  - ARQ strategies may come in
- Correction (FEC)
  - Better if we can
  - Sometimes essential due to link characteristics
- Involves error codes
  - Coding, not encryption

## Fundamental Concepts - Redundancy

- Some data is actual data for error control
  - Transmitted data: Could be data + metadata
  - More data introduced expressly for the purpose of error control
  - "Metadata" for error control
  - Data and metadata must be distinguished
    - Usually a framing issue
  - Metadata introduces overhead
  - Only data is "useful" outside error control



## Fundamental Concepts - Rate

- Overhead → "rate" of a coding scheme
  - Rate of useful data per encoded data, < 1.0</li>
- Higher rate is more efficient
- Unfortunately, less likely to be good coding
- Expressed as a ratio of bits
  - Over long periods, if not constant



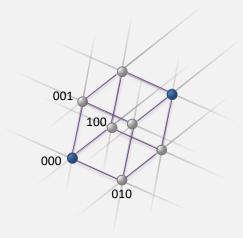
## Fundamental Concepts – Block

- If a coding scheme always codes n bits to n+m bits,
  - We speak of *n* bit blocks that are independently coded
  - The code is called a block code

- Alternative "stream" type coding
  - Convolution

## Fundamental Concepts - Distance

- Data given to error control can be anything
  - 2<sup>n</sup> "datawords"
  - For each, a unique m bit code
  - "Codeword" (encoded data) is n+m bits
- Hamming distance is a measure of strength
- d<sub>min</sub> = minimum Hamming distance between any two codewords
- To guarantee detection of t errors
  - $-d_{min} > t$
- To guarantee correction of t errors
  - $-d_{min} > 2t$



Goal: maximize d<sub>min</sub>

## Efficient Use of Rate

- Lower rate means more overhead bits
  - But does not necessarily translate into higher distance
- Choosing appropriate codewords "smartly" can increase distance

$$0 \rightarrow 00, 1 \rightarrow 10$$
 (does not increase robustness)

$$0 \rightarrow 00, 1 \rightarrow 11$$
 (does)

$$n = 1, m = 1$$

$$n = 2, m = 1$$

$$00 \rightarrow$$

$$01 \rightarrow$$

$$10 \rightarrow$$

$$11 \rightarrow$$

?

# Simple Repeat (coding example)

- Correction is possible, but rate suffers
- "k out of 2k-1" kind of voting process
- E.g., if each bit is sent seven times,
  - 1 bit blocks
  - 2¹ datawords ('0' and '1')
  - Only 2 valid codewords ('0000000' and '1111111')
  - Hamming distance  $d_{min} = 7$
  - t < 7 if only detection is attempted (up to 6)</li>
  - Up to 3 if correction is attempted from any seven-bit combination

## **Parity**

- XOR all bits of the message
- Append the resultant bit to the word (m = 1)
- Detects all single bit errors
  - In fact, can detect all odd number of bits errors
  - But can not correct
- Unfortunately, chances of errors increases

$$\xrightarrow{\mathbf{S}_1 \ \mathbf{S}_2 \ \dots \ \mathbf{S}_n} \qquad \xrightarrow{\mathbf{C}} \qquad \xrightarrow{\mathbf{S}_1 \ \mathbf{S}_2 \ \dots \ \mathbf{S}_n} \qquad \xrightarrow{\mathbf{C}}$$

$$\mathbf{c} = \mathbf{s}_1 \oplus \mathbf{s}_2 \oplus \ldots \oplus \mathbf{s}_n$$
, the modulo-2 sum

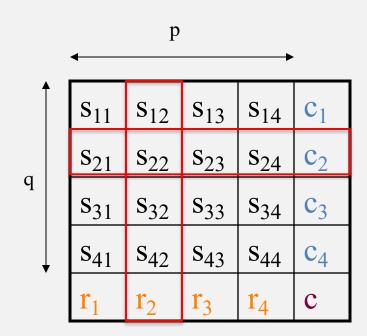
# Horizontal and Vertical Parity

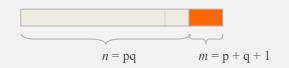
- Arrange message bits in a grid
- Parity bits for each row, each column
- Detects all single, double, triple errors
- Some but not all quadruple errors
  - Which ones?
- Can it correct errors?(up to 1)

$$Message = [ s_{ij}]$$

$$\mathbf{c}_i = \mathbf{s}_{i1} \oplus \mathbf{s}_{i2} \oplus \ldots \oplus \mathbf{s}_{ip}$$

$$\mathbf{r}_{j} = \mathbf{s}_{1j} \oplus \mathbf{s}_{2j} \oplus \ldots \oplus \mathbf{s}_{qj}$$

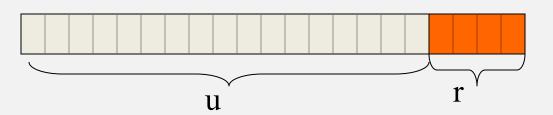




Trade-off? Rate is decreased ... (efficiency)

#### CRC – In Plain Words

- Let dataword bits be U (viewed as a binary number)
- Define a generator bit sequence G of t+1 bits
   Both sender and receiver knows G
- Compute a trailer R of t bits based on U and G, s.t.
   <U, R> is exactly divisible by G (using modulo-2 arithmetic)
- Can detect all up to t bits bursty errors...
  - ... but not the generator sequence itself
    - => **Bursty**: consecutive bit flippings (frequent on Internet)



# Calculating CRC Example

#### want:

 $U \cdot 2^t \oplus R = nG$ 

#### equivalently:

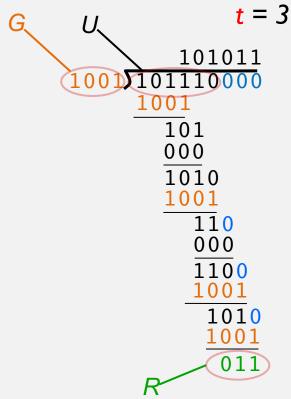
 $U \cdot 2^t = nG \oplus R$ 

#### thus:

if we divide U·2t by G, the remainder is R

$$R = remainder\left[\frac{U \cdot 2^t}{G}\right]$$

Long Division – but addition & subtraction are XOR



$$XOR$$

$$1 \oplus 1 = 0$$

$$1 \oplus 0 = 1$$

$$0 \oplus 1 = 1$$

$$0 \oplus 0 = 0$$

$$G = 101, t = 2, U = 111011$$

## CRC – Polynomial View

#### Message polynomial

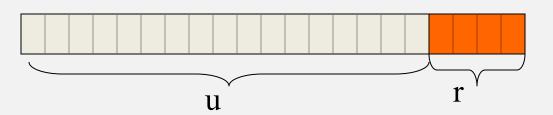
$$\mathbf{u}(x) = u_0 + u_1 x + u_2 x^2 + \dots + u_{n-1} x^{n-1}$$

#### **CRC** polynomial

$$\mathbf{r}(x) = r_0 + r_1 x + r_2 x^2 + \dots + r_{m-1} x^{m-1}$$

#### Code polynomial

$$c(x) = u(x) x^m + r(x)$$



### CRC as Remainder of a Division

#### Generator polynomial:

$$g(x) = 1 + g_1x + ... + g_{m-1}x^{m-1} + x^m$$

#### **Encoding Rule:**

$$\mathbf{r}(x) = \text{Rem } \left\{ \begin{array}{c} \mathbf{u}(x) \ x^m \\ \mathbf{g}(x) \end{array} \right\}$$

Divisible by g

## Long Division Example

$$n=3$$
 and  $m=3$   
 $g(x) = 1 + x^2 + x^3$   
 $u(x) = 1 + x^2$   
 $c(x) = ?$ 

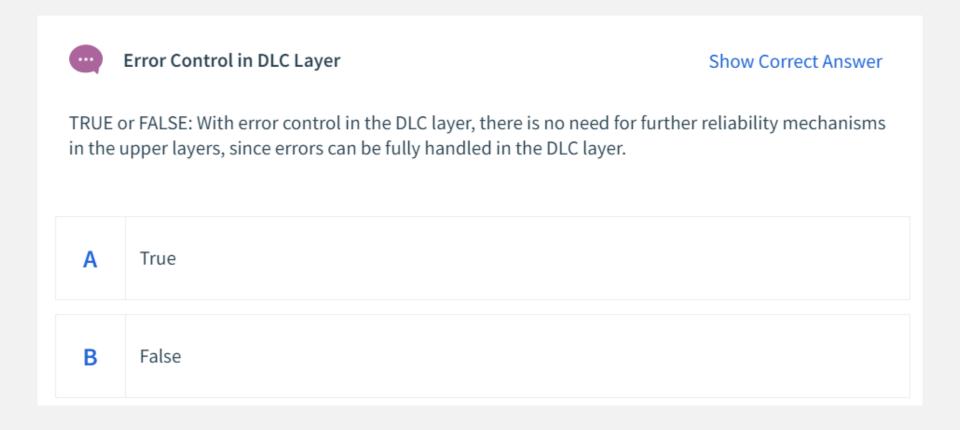
$$x^3 + x^2 + 1$$

$$x^5 + x^4 + x^2$$

$$x^4 + x^3 + x^2$$

$$x^4 + x^3 + x$$
Remainder





## Review: CRC Bits



## **Running Summary**

- DLC framing, flow control, error control
  - Optionally medium access
- Error control
  - Metadata must be added to enable error detection/correction
  - May be integrated with encoding of data overlap with physical layer
  - Block codes
- Encapsulates error detection/correction largely within DLC and physical layers