

## Model Predictive Control -Reflections

### The model

The model used is Kinematic model as described in the class. Following are the equations used:

$$x_{t+1} = x_t + v_t * \cos(\psi_t) * dt$$

$$y_{t+1} = y_t + v_t * \sin(\psi_t) * dt$$

$$\psi_{t+1} = \psi_t + \frac{v_t}{L_f} * \delta * dt$$

$$v_{t+1} = v_t + a_t * dt$$

$$cte_{t+1} = cte_t + v_t * \sin(e\psi_t) * dt$$

$$e\psi_{t+1} = e\psi_t + \frac{v_t}{L_f} * \delta_t * dt$$

The steering angle here is **delta** and throttle is **alpha**. Throttle here is a combination of brake and acceleration with values -1 and 1 respectively. Delta is kept between -25 to +25 degrees. This model gives us the prediction of the next state quite accurately using the equations above.

**Lf** is a pre-determined constant denoting the center of gravity of the vehicle.

**x,y,psi and velocity** are used to model the state of the car and errors **cte** and **psi\_error** are the cross-track and orientation errors respectively. The vehicle coordinates x and y are in global co-ordinates which are converted to car co-ordinates.

### Timestep length(N) and elapsed duration(dt)

Initially, I started with N = 25 and dt = 0.05 as given in quiz. I thought 1.25 secs would be a good starting point, but I realized soon that higher N tended to swerve the car out of the track. I tried experimenting with lower values of N keeping dt constant. But keeping dt constantly low, the speed was very slow, and I thought as I will be incorporating latency, I should probably increase dt. After some experimentation, I settled for following values:

$$N = 10$$

$$dt = 0.1$$

### **Polynomial Fitting and MPC Preprocessing**

To make calculations simple, the waypoints are converted from global to car's coordinates using the following equations:

$$\text{Waypoint\_x} = (\text{ptsx} - \text{px}) * \cos(-\text{psi}) - (\text{ptsy} - \text{py}) * \sin(-\text{psi});$$

$$\text{Waypoint\_y} = (\text{ptsx} - \text{px}) * \sin(-\text{psi}) + (\text{ptsy} - \text{py}) * \cos(-\text{psi});$$

This is run in a loop for the length of the ptsx. This makes sure the vehicles coordinates are now at origin and psi is zero. The polynomial is fitted using 3<sup>rd</sup> degree equation and cross track error is obtained by evaluation at this "fitted" coefficients

### **Model Predictive Control with Latency**

Latency is introduced in the model as there will always be a delay between the command (brake, steering etc) and the action to be performed. To account for this, I predicted the car's positions and state using a 0.1sec delay on top of added 100 ms delay by default. I initially tried a value of 0.2s for latency, but it immediately became clear that latency > dt does not make much sense. I modified the state equations to account for this delay and fed it to my mpc.solve()