

METHODOLOGY

Building formal models of biological networks avoiding formal training

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Abstract

Background: The large amount of data with which an experimental biologist must deal makes it largely impossible to reason on the dynamics of complex systems without relying on computational support. In order to be fully profitable, computational modelling tools must be both accessible and powerful, providing a means to formalise and analyse experimental outcomes without requiring additional training.

Results: We show that the software tool ANIMO (Analysis of Networks with Interactive MOdelling) can be used in different modelling tasks, and illustrate how this can be an asset for the biological researcher. ANIMO models for *Drosophila melanogaster* circadian clock and signal transduction events downstream of TNF α and EGF in HT-29 human colon carcinoma cells are used as case studies to illustrate the possibilities offered by the tool.

Conclusions: The software tool ANIMO, recently updated to version 2, allows the biologist to develop a formal model through a user friendly interface, achieving useful insight without the need to study any new mathematical formalisms.

Keywords: modelling; signalling pathway; timed automata; dynamic behaviour

Background

In living cells, processes are regulated by networks of interacting molecules. Aberrations in these networks underlie a wide range of pathologies. The development of new therapies requires a thorough insight in the functioning of these networks. Obtaining such insight can be a challenging task. Feedback loops and crosstalk between pathways lead to an intricate wiring of the network. Hence, it is necessary to study the ensemble of molecules involved, because the behaviour of individual molecules is not sufficient for a complete understanding. Since the human brain is ill-suited to grasp the non-linear dynamics of these complex networks and the entailed emergent properties, the role of computational support is increasing in molecular biology.

A model plays a pivotal role in this cycle:

- 1 to organize data and store knowledge,
- 2 to structure reasoning and discussion
- 3 to perform *in silico* experiments and derive hypotheses.

An *in silico* model is always a simplified representation of biological reality and is never the aim in itself.

As models are a formalization of knowledge or theories, an underlying formalism is needed to express this knowledge. Different formal methods have been successfully

applied to construct representations of biological systems. Among these methods are Boolean logic [1, 2], ordinary differential equations (ODEs, reviewed by [3]), interacting state machines [4, 5], process calculi [6, 7], Timed Automata [8, 9, 10] and Petri nets [11, 12]. Most of these formal methods have been implemented into software tools to aid the process of modelling. Due to the lack of such a supporting tool, Timed Automata have remained a less frequently applied method.

Timed Automata have been developed to model the dynamic behaviour of systems with processes running in parallel [13]. As such, Timed Automata have been applied in communication protocols and industrial control engineering [14, 15, 16]. The parallels between these application areas and regulatory processes in cells have triggered the step towards their use in biology. [8] use Timed Automata to extend a classical modelling paradigm [17], allowing to add temporal dynamics to gene network models. [9] describe a model of biological oscillators and test synchronization properties in this dynamic system. A discretization of ODEs to Timed Automata is proposed by [10], applying a translation between the two formalisms to an example gene regulatory network. Two different approaches to transforming a Petri net model into Timed Automata are presented by [18], who also address the important issue of state space explosion in their paper. Finally, [19] propose an *ad hoc* Timed Automata model of a radiation treatment system, which is then validated through the analysis tool UPPAAL [20].

Each of these approaches has been successfully validated, demonstrating the potential of Timed Automata in biological applications. However, these approaches were all limited to simple or specific examples and none of these modelling methods has led to a tool implementation of the proposed method to encourage a broader use of Timed Automata in molecular biology. We have recently introduced the software tool ANIMO (Analysis of Networks with Interactive MOdelling, [21]), which aims at making available the power of Timed Automata to the experimental biologists without requiring them to be fluent in any mathematical formalism.

In this paper we present ANIMO 2.0, an updated version of ANIMO which allows for a considerably more efficient analysis of models. ANIMO 2.0 also introduces new features, such as the possibility to interrogate an ANIMO model with model checking queries represented as human language sentences instead of mathematical formulae. The case studies presented in the following sections are centered around possible usage scenarios for ANIMO, and aim at illustrating how a biologist can profit from the tool in its latest iteration. An installation manual for ANIMO 2.0 is available at <http://fmt.cs.utwente.nl/tools/animo/manual.html>.

Results

Modelling oscillation

Results obtained with ANIMO are comparable to results with other modeling approaches. To demonstrate this, Figure 3 represents an ANIMO model of the circadian clock in *Drosophila Melanogaster*, based on the work by [22], where ordinary differential equations (ODEs) were used. The cyclic behavior of the circadian clock is based on the alternating formation and destruction of the CYC/CLK protein complex. Concentration levels of this complex are in turn regulated by a series of proteins which are produced as a consequence of CYC/CLK formation. The CWO

protein is central to the functioning of the network, as it degrades the mRNA for most of the involved proteins. As such, CWO act as an inhibitor that counterbalances the effect of CYC/CLK. The positive influence of the light-regulated cryptochrome CRY on the degradation of TIM is a consequence of the passage between day and night, allowing the circadian clock to synchronize to a time zone (see Suppl. Sect. ??).

The output of the ANIMO model in Figure 3 closely matches the original ODE model. In particular, the oscillations in both models show the same periods and phases (see Suppl. Fig ??). Due to the compositional nature of Timed Automata ANIMO allows for intuitive *in silico* knock-out experiments, by right-clicking a node in the model and disabling it. Such experiments have been done before [22] and give similar results in our model.

Using ANIMO to generate hypotheses

In order to validate our modeling approach, we constructed a larger model of the signaling network downstream of $\text{TNF}\alpha$ and EGF, formalizing the crosstalk that takes place between the pathways at different levels of cellular regulation. We first modeled the two pathways in isolation (Suppl. Figs. ??, ??), using information on protein interactions from the KEGG [23] and phosphosite [24] databases. These models were fitted to experimental data from studies by [25] and [26]. We then merged the two pathways into a single model and added autocrine crosstalk between the pathways that has been described by [26]. Briefly, stimulation with $\text{TNF}\alpha$ leads to a rapid release of $\text{TGF}\alpha$ ($\text{TGF}\alpha$ in the model), which activates the EGF receptor (EGFR). This activation causes secretion of $\text{IL-1}\alpha$ (IL-1a) at later time points. The effect of $\text{IL-1}\alpha$ is down-regulated by the secretion of IL-1 receptor antagonist (IL-1ra) downstream of $\text{TNF}\alpha$. The resulting model (Fig. 4A) was compared to the experimental data for treatments with 100 ng/ml TNF alone and 100 ng/ml EGF alone (data not shown) [25].

At this point, the behavior of the model deviated from the data for some of the nodes. This is an interesting situation, as it requires modifications to the model, that can be interpreted as new hypotheses. Below, we give two examples and show how adaptation of the model can be used to generate novel testable hypotheses.

Experimentally, treatment with $\text{TGF}\alpha$ alone does not lead to secretion of $\text{IL-1}\alpha$. Instead, a co-stimulation with $\text{TGF}\alpha$ and $\text{TNF}\alpha$ is required [26]. However, in the first version of the model, treatment with $\text{TGF}\alpha$ was sufficient for $\text{IL-1}\alpha$ expression (Fig. 4B). Given the time delay until secretion of $\text{IL-1}\alpha$, it can be expected that *de novo* synthesis of $\text{IL-1}\alpha$ is required and that both $\text{TNF}\alpha$ and $\text{TGF}\alpha$ are needed to activate transcription of the $\text{IL-1}\alpha$ gene. JNK1 and ERK signal downstream of $\text{TNF}\alpha$ and $\text{TGF}\alpha$, respectively, and are known to affect the activity of multiple transcription factors. We altered the model to make activation of $\text{IL-1}\alpha$ expression dependent on both JNK1 activity and ERK activity (Suppl. Fig. ??, arrows linking JNK1 and ERK to IL-1a gene). After this modification to the model, $\text{IL-1}\alpha$ was no longer secreted upon stimulation with $\text{TGF}\alpha$ alone, which greatly improved the fit between the measured $\text{IL-1}\alpha$ levels and the model (Fig. 5B). This hypothesis could now be used to design a new experiment to validate $\text{IL-1}\alpha$ as a target of combined JNK1 activity and ERK activity in HT-29 cells. For example, kinase

inhibitors specific to JNK1 and ERK could be used to confirm that activity of both kinases is required for expression and secretion of IL-1 α . Performing the experiment is beyond the scope of this study, but this hypothesis finds support in literature. Transcription factors c-Jun and c-Fos together form a heterodimer known as AP-1 and are activated by JNK1 and ERK, respectively [27, 28]. AP-1 has been reported to bind to the promoter of IL-1 α , providing evidence for a role in the regulation of IL-1 α expression [29]. Based on these findings in literature we included c-Jun and c-Fos in our model as transcriptional activators of IL-1 α (Fig.5A).

As a second example, we considered the behaviour of JNK1 and MK2. In the model, both proteins were located downstream of TNF α but not TGF α or EGF. Hence, the model did not show an effect of C225, a pharmacological inhibitor of ligand-EGFR binding, on activation of JNK1 or MK2 after stimulation with TNF α . However, experimental data show that C225 strongly reduces activation of JNK1 and MK2 upon stimulation with TNF α [26]. This fact is indicative of a role for EGFR in activation of JNK1 and MK2. Since both JNK1 and MK2 are located downstream of MEKK1, we hypothesized that activation of MEKK1 is dependent on both TNF α -signalling and TGF α -signalling. In the model we added a new hypothetical node **Hyp 2** (hypothesis 2) to link EGFR to MEKK1 (Suppl. Fig. ??). This addition led to an improved fit of the model to the data upon treatment with TNF α + C225: activation of both MK2 and JNK1 was strongly suppressed by C225 (Fig. 5C). Stimulation with EGF alone did not lead to activation of JNK1 and MK2. These data support the validity of the modification to the model. Further support for a link between EGFR and MEKK1 was found in literature. Specifically, Ras has been reported as a direct activator of MEKK1 [30]. EGFR is a well-known and potent activator of Ras, which is why it was already in our network [23]. Other studies also report activation of JNK1 and phosphorylation of c-Jun downstream of Ras, which is consistent with an interaction between Ras and MEKK1 [28, 31]. Based on these findings, we adapted our model by removing the **Hyp 2** node and creating a direct interaction between Ras and MEKK1 (Fig. 5A). Experimentally, the role of Ras could be confirmed by using a pharmacological inhibitor of Ras activity, and measuring the effect of this inhibitor on the activation of JNK1 and MK2. Together, our model suggests that EGFR activity is required but not sufficient for activation of JNK1 and MK2 in HT-29 cells.

There are other nodes for which the experimental data deviates from the model in one or more of the experimental conditions. A comparison between model and experimental data can be found in Figures ??, ?? and ??. A complete deciphering of the signalling events in this biological system is outside the scope of this paper. Instead, we illustrated how interactive modelling of the dynamic behaviour of a signal transduction network can be used to extend previous pathway topologies and can lead to the generation of novel hypotheses.

Exploiting formal methods: model checking

To show why one should use a formal model like Timed Automata, we demonstrate the application one of the biggest advantages of Timed Automata: state space-based analyses such as model checking [32] provided by UPPAAL [20].

The technique of model checking consists in verifying the truth of some properties that describe the behaviour of a model. This is usually done by exploring every

possible evolution of the model starting from an initial state. The set of all states that can be reached by a model is called *state space*, and formulae describing the evolution of a system are usually described by (a subset of) computation tree logic (CTL, [33]).

The case study we use as a testbed is the network model shown in the *Network* panel in Figure 6, which represents signaling events downstream of growth factors EGF (epidermal growth factor) and NGF (nerve growth factor) in PC12 cells (a cell line used to study neuronal differentiation). The model topology proposed in [?] was analyzed with an ANIMO model based on the reaction-centered approach, reproducing the experimentally observed ERK (extracellular signal-regulated kinase) activity changes [34]. In particular, a 10 minutes stimulation with EGF resulted in transient behavior (i.e. peak-shaped, see also the graph in Fig. 6), while NGF stimulation led to sustained activity (see Fig. 8).

This case study will also be used to evaluate the improvement in performances introduced by the new version of ANIMO, which is described in the Methods section.

Simulation-based analysis

We start by evaluating the cost in terms of time of simulations. This is a particularly important aspect to consider, as during the model building phase a user may need to perform a relatively large number of simulations, continuously adapting the topology or quantitative parameters of a network model. In order to make the modeling approach in ANIMO as interactive as possible, it is desirable to decrease dead times, and this translates into reducing the computational cost of model analysis as much as possible. UPPAAL's statistical model checking engine [?] is based on the generation of random walks (i.e., simulation runs) from a Timed Automata model. In this experiment, we query UPPAAL for simulation runs on the models generated by ANIMO applying the reaction- and reactant-centered modeling approaches to the case study. To define the initial state of the model, we consider the starting condition to be the treatment with 50 ng/ml NGF, which translates into setting the activity level of node NGF to 15/15, while changing EGF to be at 0/15 activity. We have chosen this configuration as the model is expected to continue reacting indefinitely (sustained ERK activity), without reaching a deadlock state where all reactions are inactive. This makes the model more demanding when generating the state space because having more reactions occur means having more states in the transition system underlying the Timed Automata model. Table 2 illustrates the computation time and memory usage when performing 100 simulation runs on each of the two considered models. Computing the simulation runs took about 92% less time with the reactant-centered model, using 87% less memory. This decrease in computation time for long simulation runs brings the approach nearer to the idea of interactive exploration of a network.

Model checking

Next, we set out to test the model checking performances using the old Timed Automata model used in ANIMO and the new one introduced in ANIMO 2. We will compare the execution times and memory requirements for a number of interesting queries:

- (1) and (2): $A[] \text{ not deadlock}$. The model continues to execute indefinitely (A refers to all possible paths in the transition system of the model, and $[]$ asks the property to always hold along a path).
- (3): $RKIP < 10 \rightarrow ERK \geq 40$. After RKIP (Raf kinase inhibitory protein) activity has been lowered, ERK activity increases. As in the model RKIP has 20 levels of granularity and ERK has 100 levels, $RKIP < 10$ means that RKIP is less than half active, and $ERK \geq 40$ means that ERK activity is at least 40%.
- (4): $E \langle \rangle RKIP < 10$. Find a point when RKIP is low (E asks for the existence of at least one path for which the property holds, while $\langle \rangle$ requires the property to hold at least once along a given path). This query is expected to generate a trace, the last point of which will be used as initial configuration for model checking queries (5) and (6).
- (5): $A[] ERK < 70$ and (6): $A[] ERK > 35$. Once RKIP activity has significantly decreased, ERK activity is sustained at an intermediate level.

The initial conditions are:

- (1): $EGF = 15/15$ and $NGF = 0/15$, all others as the original configuration, corresponding to the treatment condition with 100 ng/ml EGF.
- (2) - (4): $EGF = 0/15$, $NGF = 15/15$, all others as the original configuration, corresponding to the treatment condition with 50 ng/ml NGF^[1].
- (5) and (6): all activities as in the last state of the trace computed from query (4).

The analysis of query (1) returned false and all other queries returned true. In particular, query (1) confirms that under EGF treatment no other activity is observed in the model after the initial peak, while query (2) confirms that with NGF activity continues indefinitely. Moreover, queries (3) - (6) confirm the result of the simulations shown in [34], with NGF treatment leading to sustained ERK activity. The model checking performance of UPPAAL using the reaction- and reactant-centered model types is shown in Table 3.

Analysis of the results

Note that we focus most of our attention on the NGF treatment, as with this configuration the model was hypothesized to keep reacting permanently (sustained ERK activity). The results from queries (1) and (2) show that this is indeed the case, as EGF treatment leads to all reactions dying out after a number of steps (i.e., deadlock due to all automata being in the `not_reacting` location). This means that the queries (3) - (6) deal with a larger state space, leading to presumably lower model checking performances. Requesting a full inspection of the state space as we do when using a query of the type $A[] \phi$ returning true in cases (5) and (6), allows us to indirectly compare the state space size of the two model versions. As the hundreds-fold computation time improvements in Table 3 show, the reactant-centered model produces indeed a noticeably smaller state space, allowing for a higher level of interactivity also when performing non-trivial model checking.

Moreover, our experiments point out that the reactant-centered approach considerably lowers the memory requirements for the model. This is not only due to

^[1]In the laboratory experimental setting, NGF is used at a lower concentration than EGF, but it is still enough to saturate all NGF receptors, which are rarer than EGF receptors.

the absence of possibly large precomputed time tables, which can contain up to ten thousand elements each.^[2] Indeed, this point was further investigated by implementing a reaction-centered model which avoids the use of tables and instead makes on-the-fly computations of the time bounds with the same number representation as in the reactant-centered model. This resulted in improved performances in the cases of reachability and simulation-based queries, with memory requirements similar to the ones for the reactant-centered model. However, in all other cases a much larger amount of memory (more than 2 Gb) was used with respect to the table-based implementation of the same model, without leading to appreciable benefits in terms of execution time: in some cases performances were noticeably deteriorated. These findings support the intuitive idea that a reactant-centered approach leads in general to fewer events in a model, and to a smaller state space.

Note that while the network we consider for the case study is not particularly large, the gain in performances is still considerable and promising in the perspective of analyzing more complex networks.

User interface for model checking in ANIMO 2

In order to allow a non-expert user to profit from the power of model checking, we have implemented a template-based user interface to define queries directly inside the ANIMO Cytoscape plug-in: Figure 9 shows the interface for composing a model checking query in ANIMO. The mappings between user interface templates and actual model checking queries are inspired on the ones proposed in [?], and are shown in Table 4.

If the answer to a model checking query contains a (counter-) example trace, the trace is automatically parsed by ANIMO and presented to the user in form of a graph of activity levels, in the same fashion as is normally done with simulation runs. Finally, a button positioned near the time slider under a simulation graph allows the user to easily change the initial activity levels of the whole network by setting them as in the currently selected time instant. This feature was used after executing query (4) to set the initial conditions for queries (5)-(6). Such an addition makes it easier to inspect the behavior of a network by using a sequence of model checking interrogations.

Discussion

Comparison between ANIMO and other modelling tools

Different formalisms are in use in the field of computational modelling of biological systems, each with their specific characteristics. Many of these formalisms have been implemented into software tools to support modelling efforts. In order to compare ANIMO with existing tools, we have selected a number of mathematical formalisms, each connected to a supporting tool. With an emphasis on the modelling process rather than the final model, we compared these tools on the basis of the following parameters:

- 1 **Hidden formalism:** a knowledge of the underlying formalism is not required in order to use the tool

^[2]In the reaction-centered model, having a reaction depend on two 100-levels reactants leads to the generation of two time tables containing $100 \times 100 = 10\,000$ elements each.

- 2 **Visual modelling:** the tool allows the user to model using a visual interface, and is not exclusively founded on formula-, text- or table-based input forms
- 3 **Qualitative parameters:** parameters for reactions can be input as approximated estimations, and not exclusively as numbers
- 4 **Tight coupling with topology:** models are tightly and clearly coupled to the networks they represent, showing the visual representation of the model in a shape similar or comparable to the representation currently used by biologists for signalling pathways
- 5 **User-chosen granularity:** if discretization is applied during the modelling process, the user can change the granularity with which such discretization is made, possibly for each component of the model separately

Table 1 shows the comparison between ANIMO and the selected tools.

Going beyond the user interface, there are a number of “pros and cons” for using ANIMO and Timed Automata in the biological context. First and foremost, being Timed Automata an executable formal language, a state space can be derived from a Timed Automata model. This means that state space-related analyses such as model checking can be performed on Timed Automata: as explained in the Results section, this can be done directly in ANIMO, bypassing the need for a deeper understanding of Timed Automata while indirectly applying a powerful model checking tool such as UPPAAL.

The smaller amount of parameters needed to build an ANIMO model, if compared e.g. to a differential equation-based approach, makes the modelling process faster, allowing the biologist to obtain interesting results in less time. However, a less parameter-intensive modelling approach is also less precise: in our case we abstract sequences of biochemical reactions into activation or inactivation interactions, simplifying any relation between two entities in a network as either activating or inhibiting. While this allows for some simplifications in the networks and the underlying formal models, it does not allow to represent in full detail more specific concepts as reactant concentration or reaction affinity. In case such concepts are of primary importance, we encourage the interested reader to turn to more precise modelling approaches, such as those based on differential equations. In particular, all reactants modelled in ANIMO are assumed to be present at the same (unitary) concentration. While this assumption is not always applicable, it encourages abstract thought: many biological processes can be represented as networks driven by *activity-based* interactions. Even if with a limited scope, ANIMO can be applied also in the analysis of metabolic processes, considering the production of protein *A* as the activation of node *A*, with degradation being represented as inhibition. As stated before, it cannot be expected from such models to be truly faithful to their respective biological processes, but they can still be an useful tool.

Final remarks

ANIMO is not the first modelling tool to provide an interface to a modelling formalism. Such interfaces exist in many other tools (see Suppl. Tab. 1). With its focus on user-friendliness and intuitive modelling, ANIMO’s main contribution lies in making computational modelling more accessible to experts in biology. Making use of the visual interface provided by Cytoscape, network representations subscribe to

biological conventions. Model parameters are kept to a minimum and can be directly accessed by mouse-clicking on nodes and edges. Because of the automatic translation of the network topology and user-defined parameters into an underlying formal model, training in the use of formal methods is not needed. In Supplementary Section , a more in-depth comparison between ANIMO and other modeling tools is given. For this comparison we selected a tool for each of the most commonly used formalisms, and used criteria with a strong focus on user-friendliness.

In Section , we described the construction of an ANIMO model of the circadian clock in *Drosophila Melanogaster*. This model captured the dynamics of the regulatory network and led to similar conclusions as an ODE model that had been published previously [22]. This finding supports the use of the series of modelling abstractions that we proposed. The biggest difference between the construction of these models is that the model by [22] is constructed by writing a system of mathematical equations, together with an algorithm for simulation. In ANIMO, instead, a number of network nodes is drawn for the molecules involved. These nodes are then linked by directed interactions that represent cause-and-effect relationships, with a single parameter that defines the strength of each interaction. This is a more intuitive approach to construct a model. Further contributing to an interactive modelling process is the compositionality of the model. Each node in the network can be disabled at any time by the user, or extra nodes can be added, without having to change any of the existing interactions.

In Section , we showed the construction of an executable model of signalling events downstream of $\text{TNF}\alpha$ and EGF in human colon carcinoma cells. This data set has been used for previous modelling studies, based on partial least-squares regression and fuzzy logic [35, 36]. The partial least-squares regression model describes an abstract data-driven model that uses statistical correlations to relate signal transduction events to various cellular decisions. This type of modelling is very useful in uncovering new and unexpected relations. It is also successful in making predictions, but gives little direct in the dynamic behaviour of the network. Fuzzy logic analysis led to a model that gave a better fit to the dynamic network behaviour than discrete logic (Boolean) models. Inspection of the inputs to the logical gates that were used to model protein behaviour led to the prediction of novel interactions between proteins, showing the usefulness of this approach. For most of the proteins, such as JNK1, time was used as an input parameter. For example, the logical gates “if $\text{TNF}\alpha$ is high *AND* time is low, then JNK1 is high” and “if $\text{TNF}\alpha$ is high *AND* time is high, then JNK1 is low” were used to describe the dynamic behaviour of JNK1. Although this leads to a representative description of the dynamic behaviour of JNK1, peaks in protein activity at early time points were not reproduced by the fuzzy logic model. Moreover, it gives no insight in the molecular interactions that are involved in activation or inhibition.

In this study, we used the same data set and performed a single round of the empirical cycle. This cycle starts off with the experiments carried out by [25]. We used the resulting experimental data, together with knowledge from curated databases [23, 24] to construct an executable model of the biological system. In contrast with the two approaches described above, ANIMO is aimed at the construction of more mechanistic models, mimicking biochemical interactions *in silico*.

This way of modelling gives a different type of insight. In the process of model construction, we extended a prior-knowledge network with time-dependent extra-cellular crosstalk that has been reported previously [26]. To come up with possible explanations for a disagreement between the model and the experimental data, two additional layers of crosstalk were introduced, at the signal transduction and transcriptional level. These modifications improved the fit of the model to the data and can be interpreted as novel testable hypotheses. Finally, we proposed new experiments that could be carried out to test these hypotheses, closing the empirical cycle. Together, our model sheds more light on the intricate entanglement between the TNF α and EGF pathways at multiple cellular levels. But above all, the model provides an excellent starting point for further investigation.

Conclusions

We have presented here how the ANIMO tool was improved to provide an interactive approach to model checking. Thanks to the increased performances of the new reactant-centered modeling approach, we are able to obtain answers to model checking queries in a matter of seconds. Coherently with the user friendliness of the tool, we ensure that the biologist can access the features of model checking without the need to directly deal with Timed Automata models. In this way, ANIMO acts as an intermediary between the biologist and a formal representation of biological signaling pathways, letting the experts concentrate on investigating the mechanisms of cellular responses.

In order to enforce the concept of user interaction as a primary focus of the tool, we plan to extend ANIMO by adding support for parameter sensitivity analysis and automatic parameter sweeps. We already allow for only one numeric parameter per reaction, but an automatic way of adjusting such parameters to fit experimental data will allow the user to concentrate more on defining a sensible topology for a pathway. Such an automatic search could be limited by setting specific bounds on reaction rates based on previous knowledge, or on a trade-off with performances. Moreover, inspired by works on automata learning [?], we plan to add also the possibility to automatically derive a network topology based on experimental data and user-defined restrictions based on previous knowledge.

We aim at widening the available set of model checking queries, in order to allow biologists to perform *in silico* experiments on an already fitting model and to obtain answers to more relevant questions. This would increase the usefulness of a model as a help to drive wet-lab investigation. In order to allow for meaningful *in silico* experiments, we plan to purposefully introduce user-defined non-deterministic parts in our models, which would allow for drug dosage investigations through model checking. This can be done e.g. through the definition of intervals for the values of some reaction kinetic constants, adding considerable uncertainty in the timing of those reactions. A model of this type could then be interrogated with queries like “How much X, Y and Z do we need to provide, and at which time points, in order to obtain targets A, B and C to be active?”. More useful results can be achieved through proper application of the statistical model checking part of UPPAAL [?] to an extended version of our model to include realistically significant stochastic behavior. Finally, in order to further improve performances, the applicability a

multi-core model checking approach based on the works by Dalsgaard et al. [?] is under study.

Methods

A new way of modeling signaling pathways with Timed Automata

We propose here a novel model to represent signaling pathways with Timed Automata. We define the model currently used in ANIMO to be *reaction-centered*, as for each reaction in the network an instance of a Timed Automaton template is generated to mimic the occurrences of that reaction. Observing that signaling networks tend to be highly connected, containing noticeably more reactions than reactants, we propose to shift the focus on reactants instead, achieving what we call a *reactant-centered* model. This change of view is inspired by the classical way in which biological events are modeled with ordinary differential equations (ODEs) [?].

Reactant-centered model

The reactant-centered model presented here is based on the concept of *net effect* of a set of reactions on a reactant: instead of considering each reaction in isolation, we consider their combined influence on each reactant. As an example, consider a reactant A activated by reactions R_1 and R_2 , and inhibited by reaction R_3 (see Fig. 7A). The net effect of these three reactions on A defines the *net reaction* $R_A = R_1 + R_2 - R_3$. Applying a concept similar to the definition of an ODE, where the rate of change of each reactant depends on the rate of the reactions influencing it, the rate of R_A is computed as the sum of the rates of the reactions influencing A :

$$r_A = r_1 + r_2 - r_3$$

where r_i is the rate of reaction R_i and is defined as follows. Consider R_1 to be the reaction $B \rightarrow A$ with kinetic constant k_1 . Suppose the settings in the ANIMO network for R_1 make its rate depend only on the activity level of B . Then we compute the rate of R_1 as $r_1 = [B] \times k_1$, with $[B]$ the current activity level of B . We do similarly for the reactions R_2 and R_3 .

As with ODEs, if r_A is positive the activity level of A will increase; otherwise, A will decrease its activity level. The absolute value of r_A determines the speed with which such change happens. The value of the reaction rate is thus translated into a time value to be used as time bound in the Timed Automaton representing R_A (see Fig. 7B) by computing

$$T_A = \frac{1}{\text{abs}(r_a)}$$

with $\text{abs}(r_a)$ the absolute value of r_a . In order to represent a natural variability in the timing of reactions, we relax the exact value of T_A by defining bounds of $\pm 5\%$:

$$\begin{aligned} \text{tL} &= T_A \times 0.95 \\ \text{tU} &= T_A \times 1.05 \end{aligned}$$

Analogously to the reaction-centered model of [34], we will call **tL** the *lower time bound* and **tU** the *upper time bound*.

Timed Automata model

The behavior of the Timed Automaton representing the net reaction R_A is defined as follows: after a number of seconds variable inside the continuous interval $[tL, tU]$ (measured with the local clock c), the activity level of A will increase or decrease by one step, depending on the sign of r_A ; then new values for r_A , tL and tU will be computed based on the (possibly) changed conditions.

The process described in Section to compute the values of tL and tU is an instance of the function called `update()` in the Timed Automaton template of Figure 7B. The computation of `update()` is the first step taken when initializing a new model taking the transition from the initial location `start` (identified by two concentric circles) to `updating`. Location `updating` is then used to decide whether R_A can be executed or not (functions `can_react()` and `cant_react()` used as guards for the transitions exiting from `updating`). This decision is based on the computed value for r_A and the current activity level of A : if $r_A > 0$ and A is already completely active (or $r_A < 0$ and A is completely inactive), no update to A can be applied, so the automaton switches to location `not_reacting`. Moreover, r_A can be 0: this means that the reactions influencing A balance each other to complete cancellation, so also in this case R_A cannot occur and the next location will be `not_reacting`. Otherwise (i.e. if `can_react()` is true), the activity level of A can be changed, so the next location will be the one labeled `waiting`, which is reached after having made sure that its clock invariant is respected (committed location between `updating` and `waiting`).

When in location `waiting`, the local clock c is let run until enough time has passed for the reaction to occur: this is obtained by using $c \geq tL$ as guard for the transition from `waiting` to `updating`. Because of the invariant $c \leq tU$ on `waiting`, we ensure that the reaction occurs after no more than tU seconds have passed. The transition to `updating` leads to an update to the activity level of A (call to `react()`), together with the computation of new values for r_A , tL and tU (function `react()` calls `update()`). Moreover, we see in Figure 7B that a communication is sent on channel `reacting[0]` (0 is the index assigned to reactant A): this is used to warn the other automata that the activity level of A has just changed, possibly changing the conditions for other reactions.

During the course of a model simulation, one of the reactants influencing a reaction on which A depends may change its activity level before R_A can occur: this event may have an influence on the value of r_A , so a re-computation of r_A , tL and tU is needed. In the template of Figure 7B, the indexes of the influencing reactants are 1, 2 and 3, corresponding respectively to B , C , D in Figure 7A. Whenever a communication on one of the channels corresponding to an influencing reactant is received while in location `waiting`, the automaton moves to location `stubborn`. This location was introduced to avoid unwanted non-deterministic behavior^[3] in the model. In the example, this could happen when the activity level of B is updated concurrently (in the same instant) with the activity level of A . As B influences A through reaction R_1 , any change in the activity level of B causes a change in r_1 , thus requiring a recomputation of r_A , tL and tU . Due to the interleaving nature of Timed Automata semantics, only one automaton may change location for the Timed

^[3]The term *unwanted* refers to a non-determinism that is not related to actual biological concepts, but to the semantics of the modeling paradigm.

Automata system to change state. This means that, should the activity level of B be changed first, the conditions for R_A would be recomputed, possibly preventing the update to A to occur. Vice versa, should the activity level of A be changed first, both A and B could change their activity levels. In such a situation, the non-deterministic order in which the updates are computed decides the behavior of the model. To avoid this, we ensure that if a reaction can occur in a given instant (i.e. $c \geq tL$), it will not consider the concurrent updates to influencing reactants (in the example, having the clock reach tL ensures that R_A occurs, independently from any concurrent update to B). Performing a check on the current value of the clock c with respect to the reaction lower time bound allows an automaton to detect the case of a concurrent update, remaining “stubborn” in its resolution of reacting with the current configuration: the guard $c \geq tL$ on the transition returning from **stubborn** to **waiting** is the same as the guard on the transition from **waiting** to **updating** and implies that the transition could occur in the current time instant. If no conflict is found, i.e. $c < tL$, a new time limit for the reaction is computed via function `update()` while moving to location **updating**. Note that the clock c is not reset when moving from **stubborn** to **updating**: should the new conditions only change the value of tL and tU without disabling the reaction, the “partial work” of the reactions is not discarded.

Finally, location **not_reacting** is used to avoid reacting when not necessary (see the description of `cant.react()` above), and to respond to changes in those reactants which can influence the value of r_A . Should one of such reactants change its activity level, the conditions are updated and the local clock is reset, moving to **updating** to check whether the reaction can now occur.

Computations on the fly

Reaction rates are all computed at run-time by function `update()`, and are based on the user-chosen scenarios, their kinetic constant k and the activity level of the involved reactants. As such computations require floating-point precision but UPPAAL only provides integer variables and operators, we use a significand-and-exponent notation with 4 significant figures, which allows for an error in the order of 0.1% while avoiding integer overflow in UPPAAL’s engine. As an example of such a notation, consider the two floating-point numbers $a = 1.23456$ and $b = 0.00023456$, and their sum $c = a + b = 1.23479456$. The corresponding representations in our integer-based notation will be:

$$\begin{aligned} a = \langle 1235, -3 \rangle &= 1235 \times 10^{-3} \\ b = \langle 2346, -7 \rangle &= 2346 \times 10^{-7} \\ a + b = \langle 1237, -3 \rangle &= 1237 \times 10^{-3} \end{aligned}$$

In this case, the number representing the sum $a + b$ differs from the exact result by $c - 1237 \times 10^{-3} = 0.001456$. The interested reader can find the UPPAAL definitions and functions needed to compute rate and time values for the Timed Automata templates inside any UPPAAL model file generated by ANIMO with a reactant-centered model type.

Notes on the Timed Automata model

We note that replacing all the existing reactions with the net reactions relative to each reactant in a model does change the behavior of the model in the sense that continuous oscillations of activity levels around an equilibrium point are less frequent. However, this does not mean that the behavior of two models using the two different approaches will diverge: the equilibrium points are still the same. From the user's point of view, graphs will look smoother while still exhibiting the same qualitative behavior, as can be seen in Figure 8. The Timed Automata templates in Figure 7 show that the main difference between the two approaches is indeed due to the choice of lumping all the reactions influencing A into the single reaction R_A . In the next session we will show that having less oscillations leads in practice to better analysis performances.

Experimental setup for simulations and model checking

All experiments described in the Results section were carried out on an Intel® Core™ i7 CPU at 2.80GHz equipped with 4 Gb RAM and running Ubuntu GNU/Linux 12.10 64bit. UPPAAL version 4.1.11 was used to compute the result of the queries, asking for “some trace” with random depth-first search order when an execution trace was expected to be produced. For the simulation queries using the statistical model checking engine, we left all options at their default values.

Competing interests

The authors declare that they have no competing interests.

Author's contributions

S.S. designed and performed the experiments, developed the Cytoscape integration, wrote the manuscript; J.S. conceived, designed and performed the experiments, wrote the manuscript; B.W. developed the Cytoscape integration, and designed and developed the time slider UI; P.E.vdV. initiated the study, conceived the Cytoscape implementation, supervised the project; R.A.U.C. performed experiments; M.K. designed experiments, analyzed data and wrote the manuscript; R.L. Contributed to the methodology and supervised the project; J.vdP. contributed to the strategy and methodology in the manuscript, in particular the connection with formal methods; J.N.P. designed experiments, analyzed data sets, contributed in particular to the application of ANIMO for large biological data, wrote the manuscript, and supervised the project.

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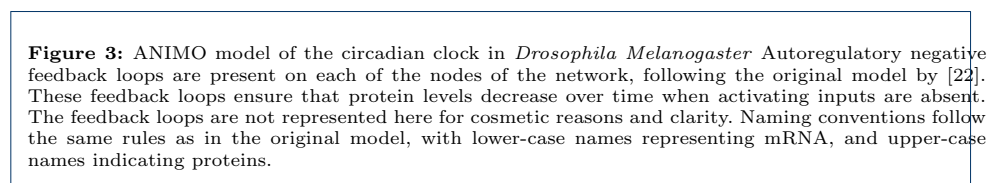
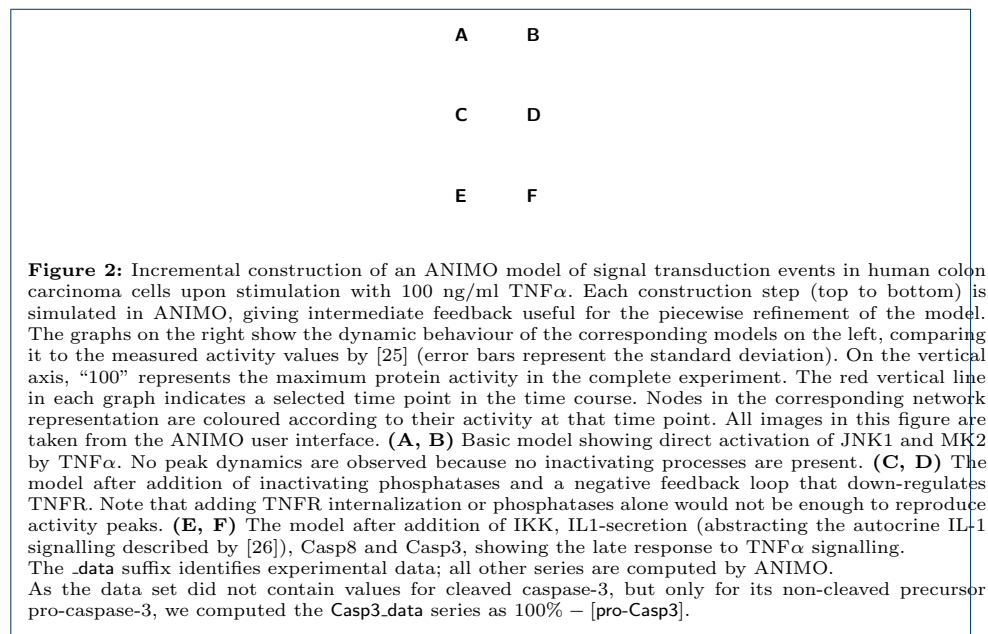
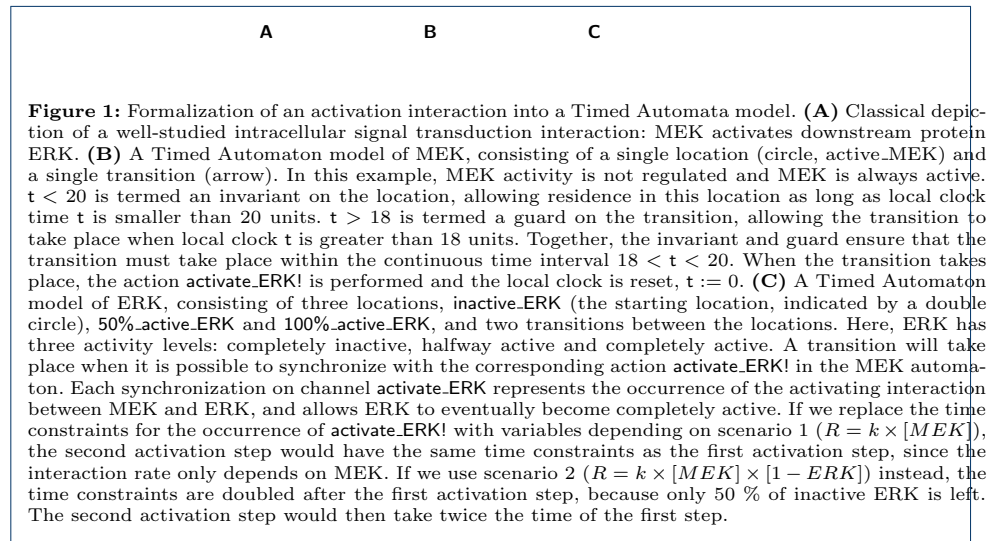
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Figures



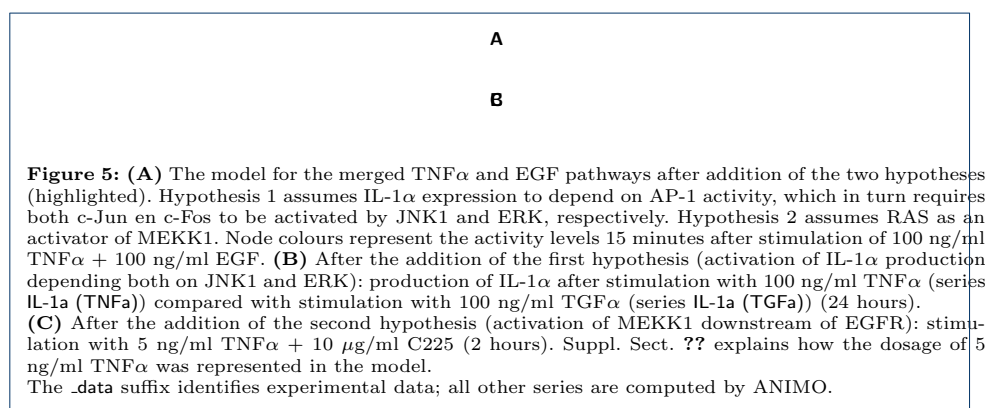
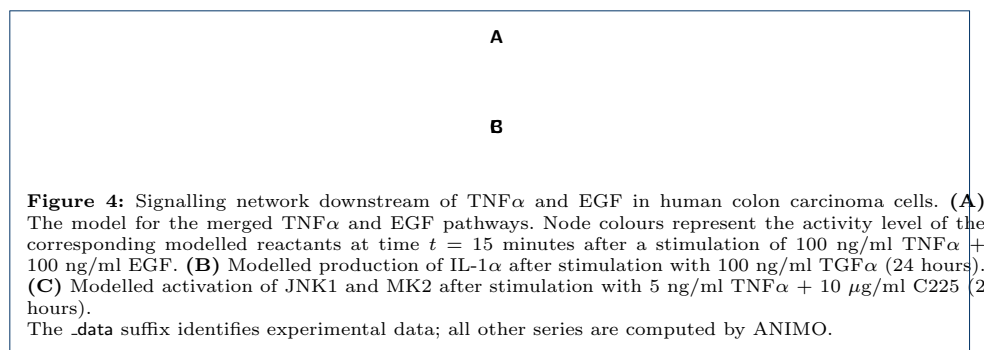
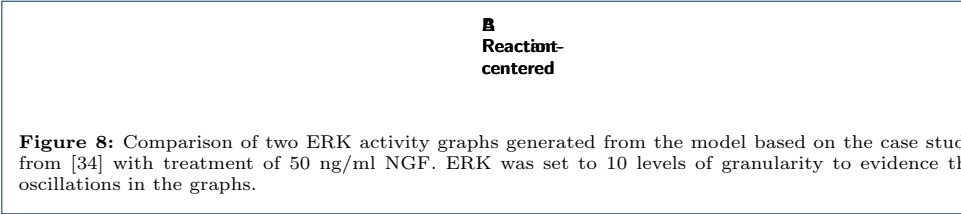
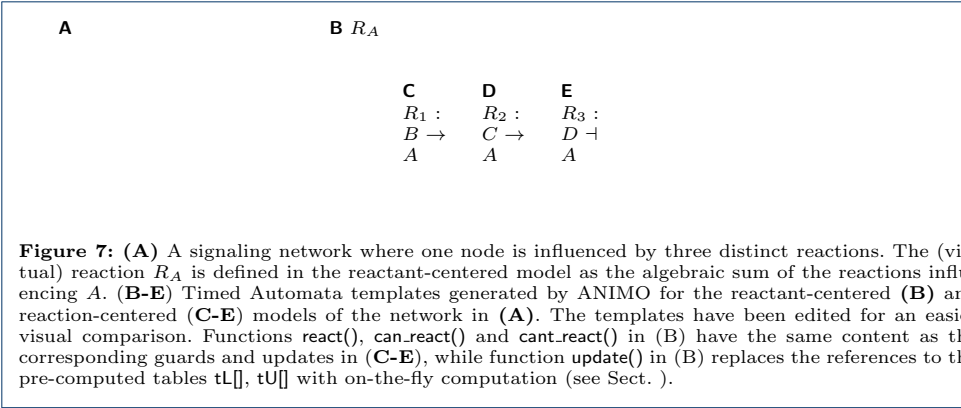


Figure 6: The Cytoscape user interface running the ANIMO plug-in (image from [34]). The *Network* panel in the center contains the nodes-edges model of the cross-talking signaling pathways of NGF and EGF, with colors indicating node activity levels and shapes representing different protein categories (see the *Legend* on the left). The *Results Panel* on the right contains a graph plotting activity levels of selected nodes during the first hour of evolution of the model. The slider under the graph allows the user to select the time instant (marked as a vertical red line in the graph) on which the colors nodes in the *Network* are based. The series with the `_data` suffix is experimental data from [?], considering a treatment with 100 ng/ml EGF.



Tables

Additional Files

Additional file 1 — Sample additional file title

Additional file descriptions text (including details of how to view the file, if it is in a non-standard format or the file extension). This might refer to a multi-page table or a figure.

Additional file 2 — Sample additional file title

Additional file descriptions text.

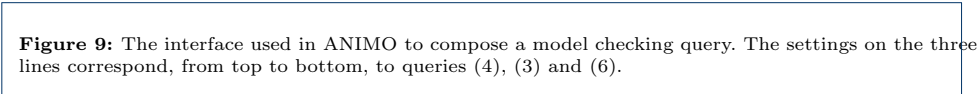


Table 1: Comparison between ANIMO and some existing approaches to modelling biological systems. A “Yes” under a column indicates that the modelling tool (mostly) fulfils the parameter, “No” indicates very limited or no fulfilment.

| Tool | Formalism | Hidden formalism | Visual modelling | Qualitative parameters | Tight coupling with topology | User-chosen granularity |
|-------------------------|------------------------|------------------|------------------|------------------------|------------------------------|-------------------------|
| ANIMO [34] | Timed Automata | Yes | Yes | Yes | Yes | Yes |
| Bio-PEPA Workbench [37] | Bio-PEPA | No | No | No | No | Yes |
| Cell Illustrator [38] | Petri Nets | Yes | Yes | No | Yes | No |
| COPASI [39] | ODE, stochastic models | No | No | No | No | No |
| COSBI LAB ¹ | BlenX | Yes | Yes | No | Yes | No |
| GINsim [40] | Boolean Networks | No | Yes | Yes | Yes | Yes ² |
| GNA [41] | ODE | No | Yes | Yes | Yes | No ³ |
| Rhapsody ⁴ | Statecharts | No | Yes | Yes | No ⁵ | No |

¹ COSBILab web page <http://www.cosbi.eu/index.php/research/cosbi-lab>

² The user can choose the number of levels for each reactant, allowing to define multi-level models based on Boolean reaction dynamics.

³ When discretizing an ODE model, the granularity depends on the mathematical features of the model, and not directly on the user’s choice.

⁴ IBM Rational Rhapsody web page <http://www-01.ibm.com/software/rational/products/rhapsody/designer>

⁵ Statecharts represent more closely the so-called *transition system* of the model as opposed to the components and interactions occurring among them.

| Model type | Time (s) | Memory (peak KB) |
|-------------------|----------|------------------|
| Reaction-centered | 37.14 | 257,928 |
| Reactant-centered | 2.83 | 33,464 |

Table 2: UPPAAL processor time and memory usage for reaction- and reactant-centered modeling approaches when computing the query `simulate 100 [36000] { R1, R2, ..., R11 }` on the model from [34] with starting condition $NGF = 15/15$, $EGF = 0/15$, corresponding to a treatment with 50 ng/ml NGF. The query asks for 100 time series of the activity levels of all reactants in the model over the first 60 minutes of execution.

| Query | Reaction-centered | | Reactant-centered | | Improvement | |
|-------|----------------------|------------------------|----------------------|------------------------|---------------|-----------------|
| | Computation time (s) | Memory usage (peak KB) | Computation time (s) | Memory usage (peak KB) | Time (n-fold) | Memory (n-fold) |
| (1) | 127.248 | 351 804 | 1.415 | 25 716 | 90 | 14 |
| (2) | 167.635 | 269 932 | 1.932 | 26 112 | 87 | 10 |
| (3) | 150.901 | 318 460 | 1.439 | 26 136 | 105 | 12 |
| (4) | 2.154 | 216 920 | 0.113 | 25 316 | 19 | 9 |
| (5) | 470.560 | 311 568 | 2.223 | 26 648 | 212 | 12 |
| (6) | 453.900 | 357 980 | 2.229 | 26 652 | 204 | 13 |

Table 3: UPPAAL processor time and memory usage for reaction- and reactant-centered modeling approaches when computing the given queries on the case study from [34].

| ANIMO template | UPPAAL formula |
|---|------------------------------------|
| It is possible for state ϕ to occur | $E\langle\phi$ |
| State ϕ never occurs | $E\langle\neg(\phi)$ |
| If a state ϕ occurs, then it is necessarily followed by a state ψ | $\phi \rightarrow\rightarrow \psi$ |
| A state ϕ can persist indefinitely | $E\Box\phi$ |
| A state ϕ must persist indefinitely | $A\Box\phi$ |

Table 4: Mapping between queries as presented in ANIMO user interface and the corresponding model checking queries in UPPAAL syntax. State formulas indicated by ϕ and ψ are all in the form $R \bowtie n$, with R the identifier of a reactant in the model, $\bowtie \in \{<, \leq, =, \geq, >\}$ and $n \in [0, g(R)]$ a valid activity level value between 0 and the granularity (number of discrete levels) of R .