Week 4: Statistical theory

1. The magic of randomness: causation

Stat 140 - 02

Mount Holyoke College

1. Questions?

2. This week: Randomness

3. Application 1: Identifying causality

- 1. Confounding factor
- 2. How to handle confounding factor
- 3. Gold standard of randomized experiments

4. Summary

1. Questions?

2. This week: Randomness

3. Application 1: Identifying causality

- 1. Confounding factor
- 2. How to handle confounding factor
- 3. Gold standard of randomized experiments

4. Summary

What do you think of when you hear the word Random

"The most decisive conceptual event of twentieth century physics has been the discovery that the world is not deterministic ... A space was cleared for chance"

lan Hocking, The taming of chance

Classic randomness example



Flip a coin

Classic randomness example



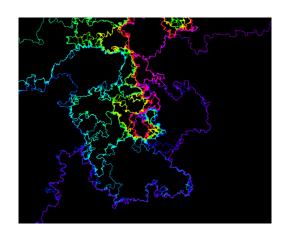
Toss a dice

Classic randomness example



Gambling

Classy randomness example



Random shapes

Classy randomness example



Mountain landscape

Classy randomness example



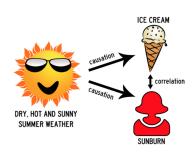
Gene mutation \rightarrow evolution

- 1. Questions?
- 2. This week: Randomness
- 3. Application 1: Identifying causality
 - 1. Confounding factor
 - 2. How to handle confounding factor
 - 3. Gold standard of randomized experiments
- 4. Summary

- 1. Questions?
- 2. This week: Randomness
- 3. Application 1: Identifying causality
 - 1. Confounding factor
 - 2. How to handle confounding factor
 - Gold standard of randomized experiments
- 4. Summary

In week 3, we looked at the relationship between two numerical variables.

Just because there is a linear relationship between two variables does not mean we have evidence that one variable causes the other.



Researchers observed from data that people who smoke get lung cancer at a higher rate than those who do not smoke. Does smoking cause lung cancer?

The tobacco lobby used to say no, arguing that:

- ▶ there might be a gene that predisposes people to both enjoy smoking and get cancer;
- people who like to smoke may tend to follow unhealthy lifestyles (e.g., alcohol use), and that may be the real cause of lung cancer;

The differences between lung cancer rates in the smokers and non-smokers may be due to smoking, or they may be due to a **confounding factor**. In this case, tobacco lobbies suggested two possible confounding factors: genes and lifestyle.

In seatbelt studies, one compares the fatality rates in accidents in which seatbelts were worn to the fatality rate in accidents without seatbelts.

But one has to worry about confounding factors.

What might be some confounding factors?

In seatbelt studies, one compares the fatality rates in accidents in which seatbelts were worn to the fatality rate in accidents without seatbelts.

But one has to worry about confounding factors. For example,

- ▶ People who don't wear seatbelts may drive more recklessly.
- ▶ People who don't wear seatbelts may prefer cars that are not designed with safety in mind.

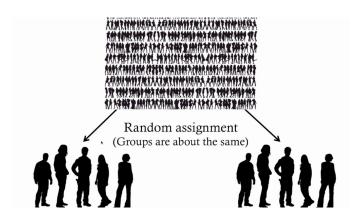
The two possible confounding factors here are: driving behaviors and car safety preference.

"The invalid assumption that correlation implies cause is probably among the two or three most serious and common errors of human reasoning."

Stephen Jay Gould

- 1. Questions?
- 2. This week: Randomness
- 3. Application 1: Identifying causality
 - 1. Confounding factor
 - 2. How to handle confounding factor
 - Gold standard of randomized experiments
- 4. Summary

How to handle confounding factor



Random assignment

In contrast, with a randomized design, the random assignment of people to the treatment and control groups ensures that there is almost no chance of a systematic difference between the groups. You are unlikely to get most of the people with good genes for lung cancer in one group and all those with bad genes in the other.

- ➤ A study found that elderly people who walked at least a mile a day had significantly higher brain volume (gray matter related to reasoning) and significantly lower rates of Alzheimer's and dementia compared to those who walked less
- ➤ The article states: "Walking about a mile a day can increase the size of your gray matter, and greatly decrease the chances of developing Alzheimer's disease or dementia in older adults, a new study suggests."

Poll question

Is this a valid conclusion?

- Yes
- 6 No

How would you design an experiment to determine whether exercise actually causes changes in the brain?

- A sample of mice were divided randomly into two groups.
 One group was given access to an exercise wheel, the other group was kept sedentary
- ► "The brains of mice and rats that were allowed to run on wheels pulsed with vigorous, newly born neurons, and those animals then breezed through mazes and other tests of rodent IQ" compared to the sedentary mice

Poll question

Is this evidence that exercise causes an increase in brain activity and IQ, at least in mice?

- Yes
- 6 No

If a randomized experiment yields a significant association between the two variables, we can establish causation from the explanatory to the response variable.

Randomized experiments are very powerful! They allow you to infer causality

- 1. Questions?
- 2. This week: Randomness
- 3. Application 1: Identifying causality
 - 1. Confounding factor
 - 2. How to handle confounding factor
 - 3. Gold standard of randomized experiments
- 4. Summary

The gold standard for a statistical study is the double-blind, randomized, controlled experiment.

A study is **controlled** if one group receives the treatment and another group does not. (In medicine, that group usually gets either a placebo, or standard medical care, or both.)

A study is **double-blind** if neither the subjects nor the scientists know who is assigned to which group until after the data are collected. This

- prevents subjects in different groups from behaving in different ways;
- prevents scientists from introducing any unconscious bias into the data collection process.

A study is **randomized** if the control group and the treatment group are chosen at random.

Without randomization, the groups may differ in a systematic way. For example, surgeons used to assign only the healthiest patients to receive an experimental new surgical treatment, since those patients could best withstand the invasive procedure. But the outcomes for those patients are not a reliable forecast for how normal patients would respond.

- 1. Questions?
- This week: Randomness
- 3. Application 1: Identifying causality
 - 1. Confounding factor
 - 2. How to handle confounding factor
 - 3. Gold standard of randomized experiments

4. Summary

Summary of main ideas

- 1. Confounding factor
- 2. How to handle confounding factor
- 3. Gold standard of randomized experiments