

CS529

# Fundamentals of Game Development

Lecture 6

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# Questions?

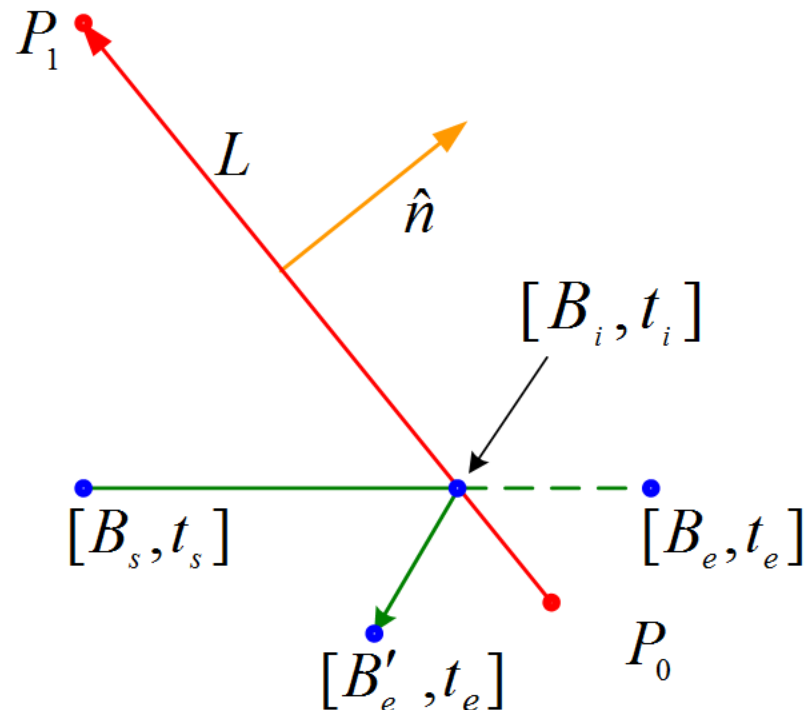
- Static Collision
  - Point/Circle
  - Circle/Circle
  - Point/Rectangle
  - Rectangle/Rectangle
- Review of Vector Algebra and Geometry
- Normal Line Equation
- Animated Point to Line Classification

# Overview

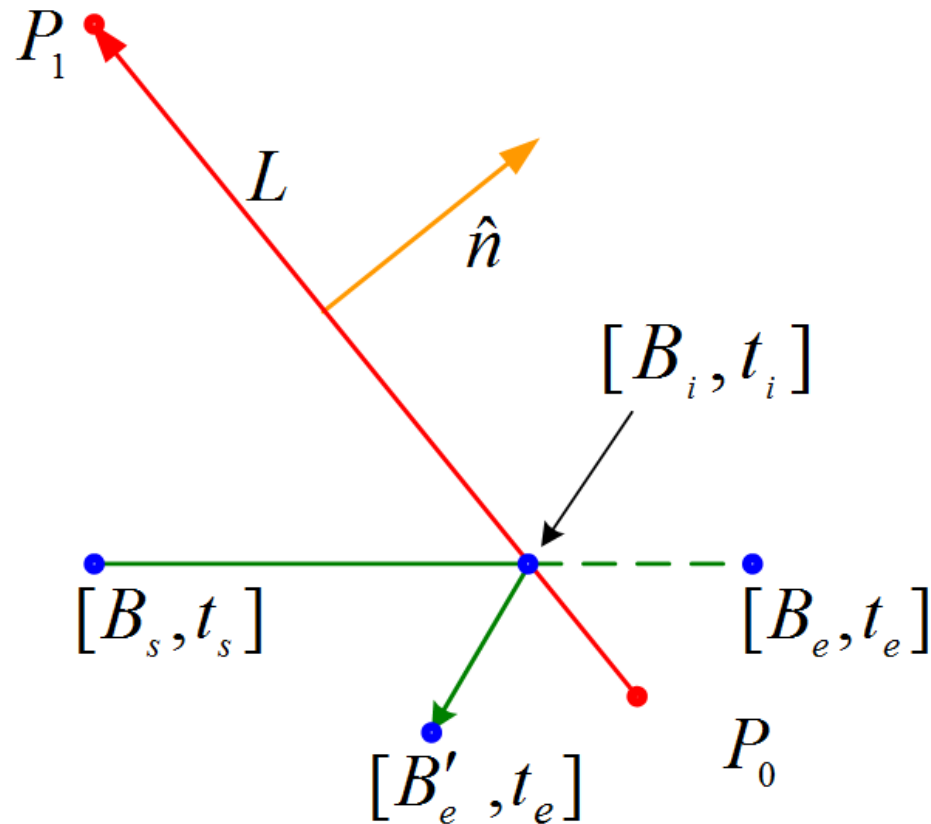
- Reflection
- Animated Circle to Line Segment

# Position of Ball After Collision (1 / 8)

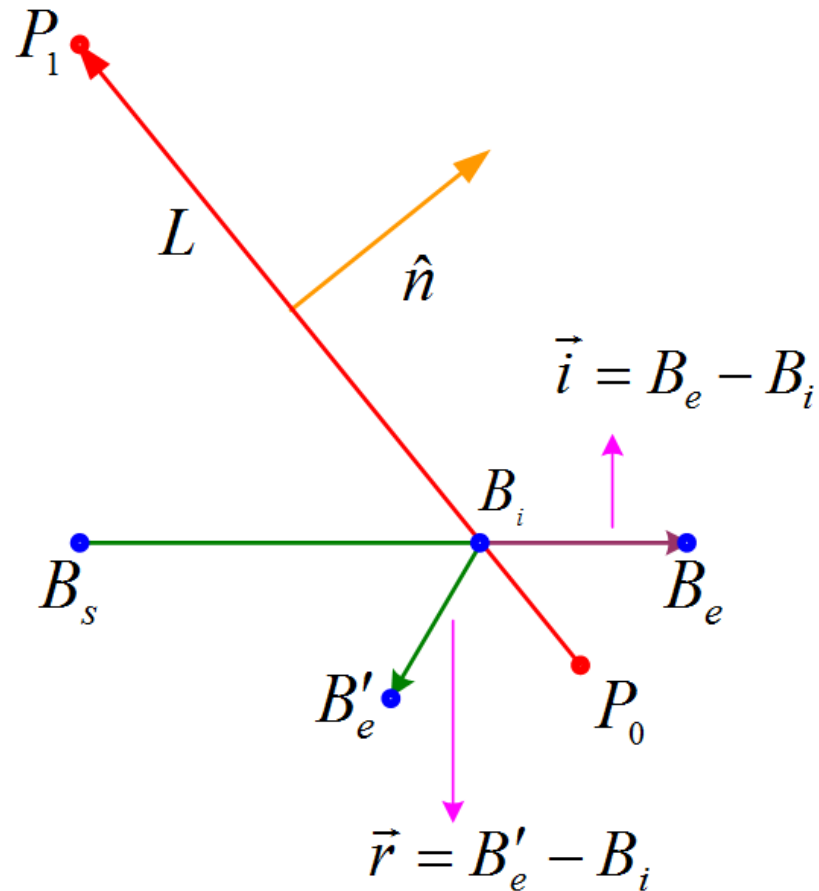
- Assuming elastic collision



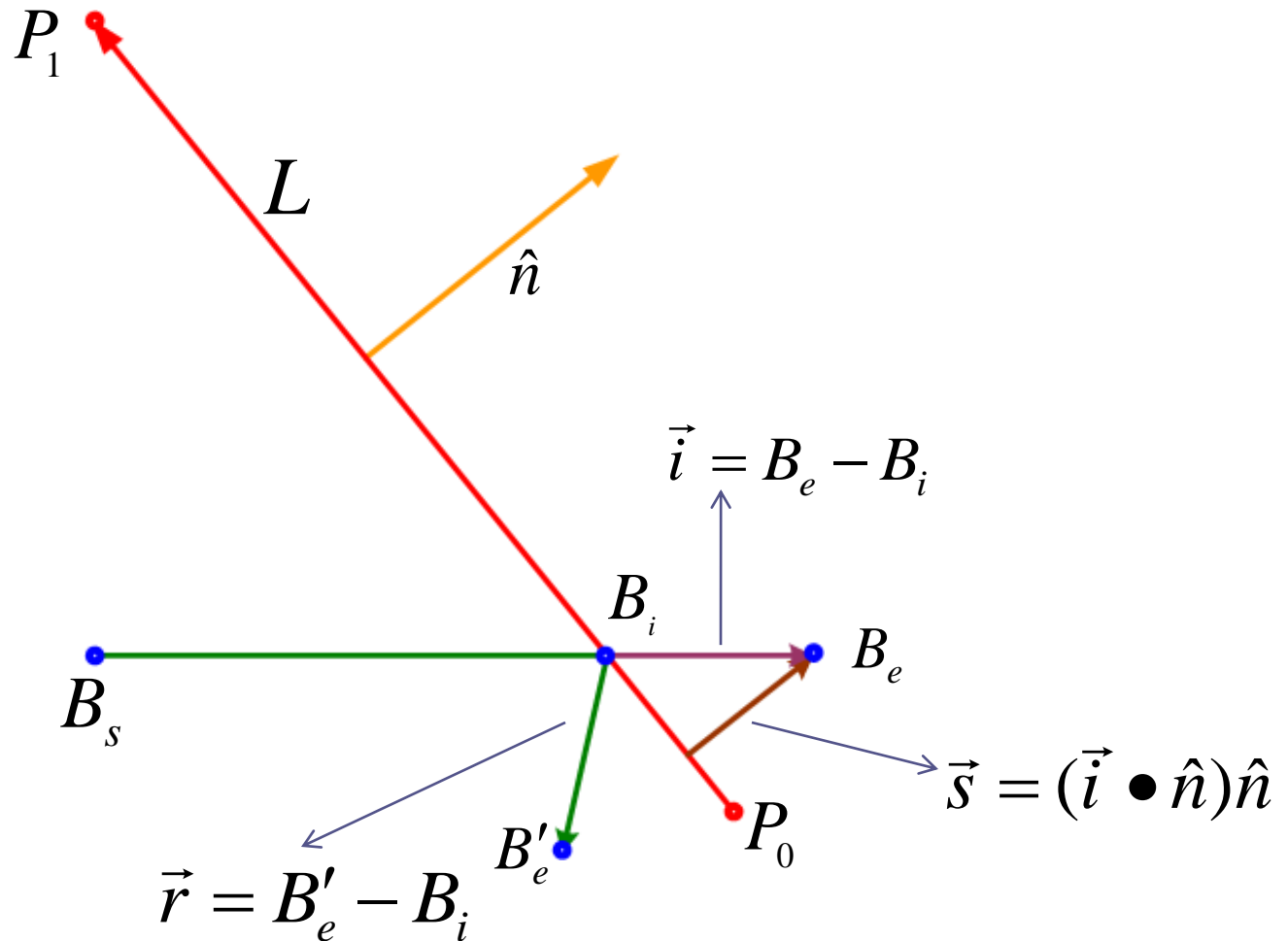
## Position of Ball After Collision (2/8)



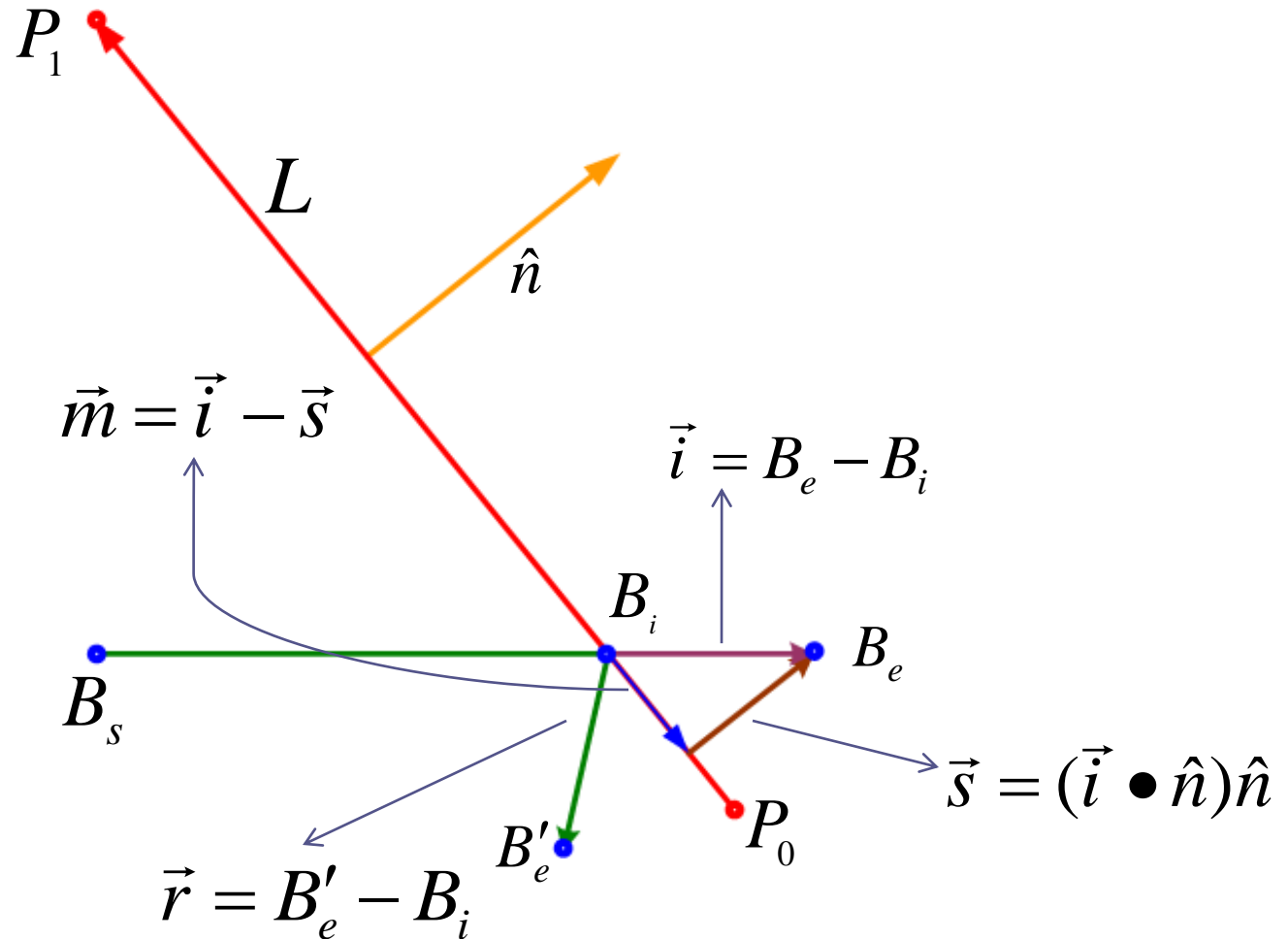
## Position of Ball After Collision (3/8)



# Position of Ball After Collision (4/8)

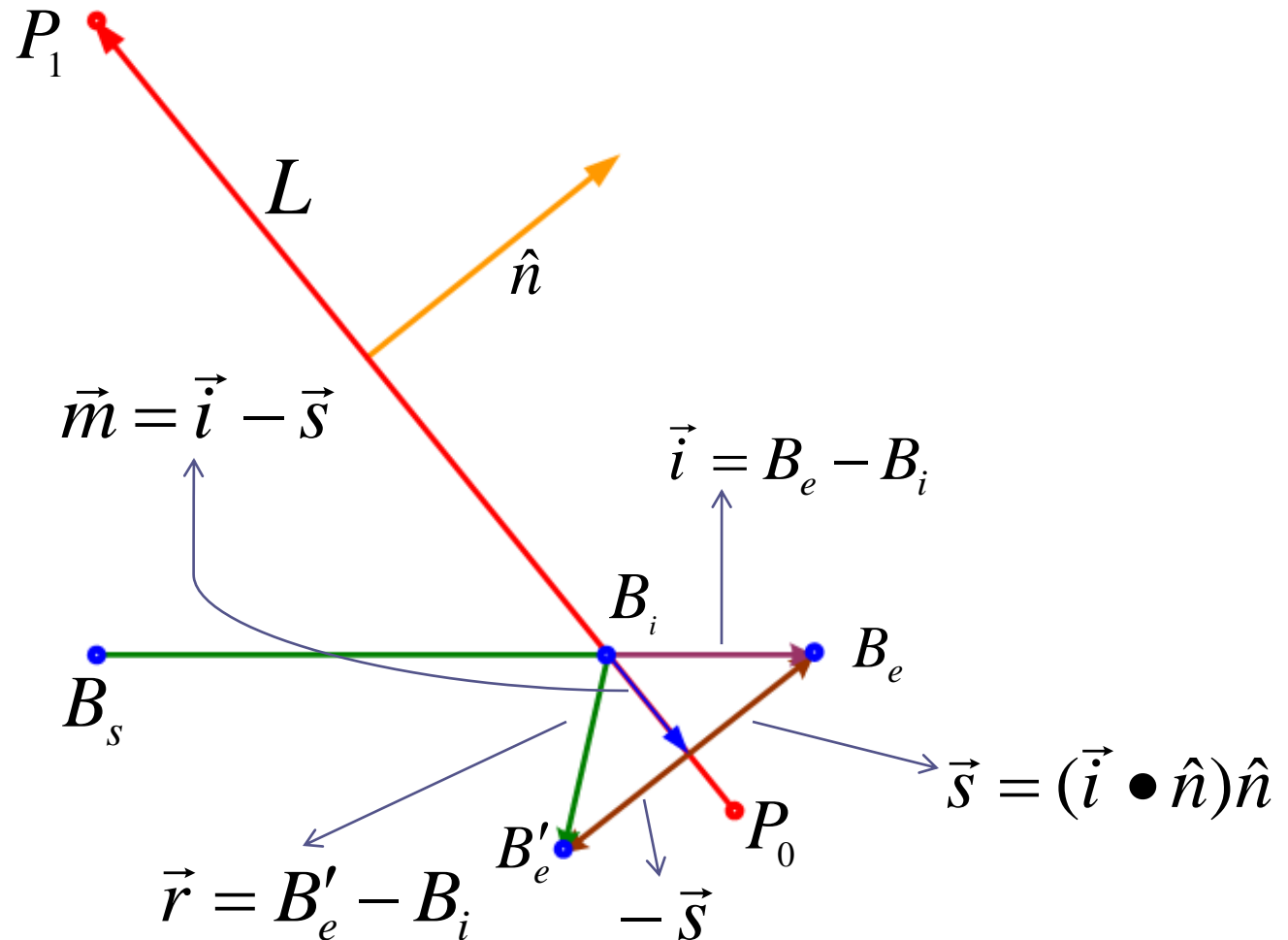


## Position of Ball After Collision (5/8)





# Position of Ball After Collision (6/8)



# Position of Ball After Collision (7/8)

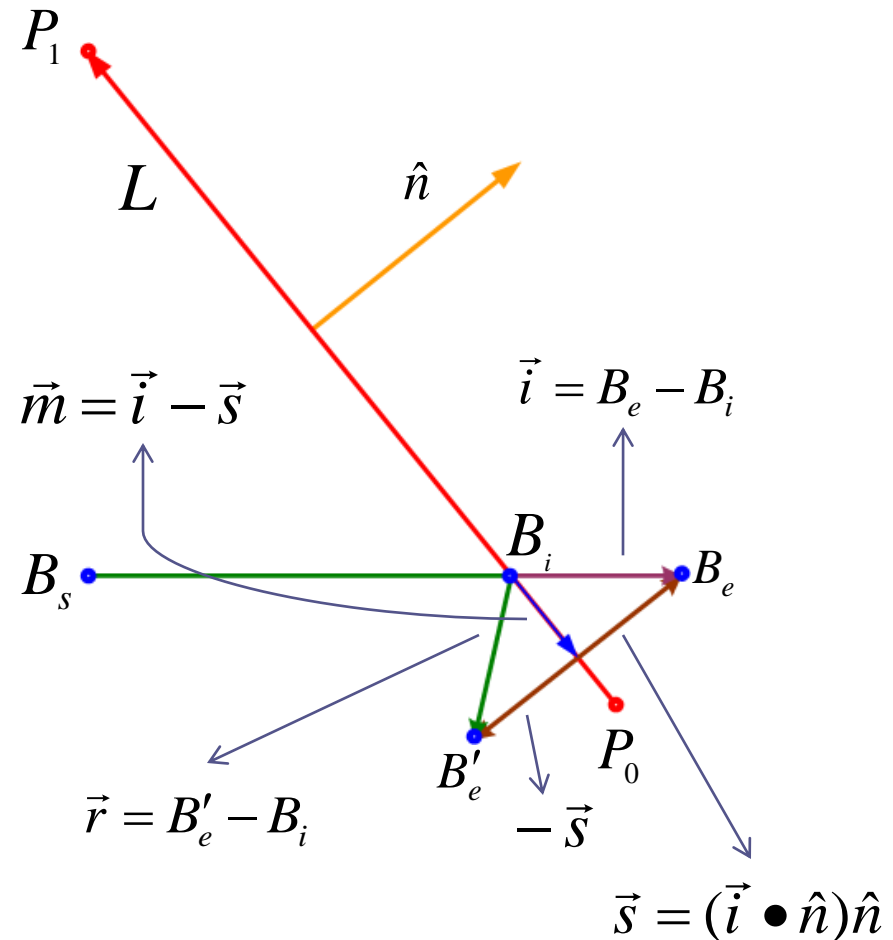
$$\vec{r} = \vec{m} - \vec{s}$$

$$\Rightarrow \vec{r} = \vec{i} - 2\vec{s}$$

$$\Rightarrow \vec{r} = \vec{i} - 2(\vec{i} \cdot \hat{n})\hat{n}$$

$$B'_e = B_i + \vec{r}$$

$$\Rightarrow B'_e = B_i + \vec{i} - 2(\vec{i} \cdot \hat{n})\hat{n}$$



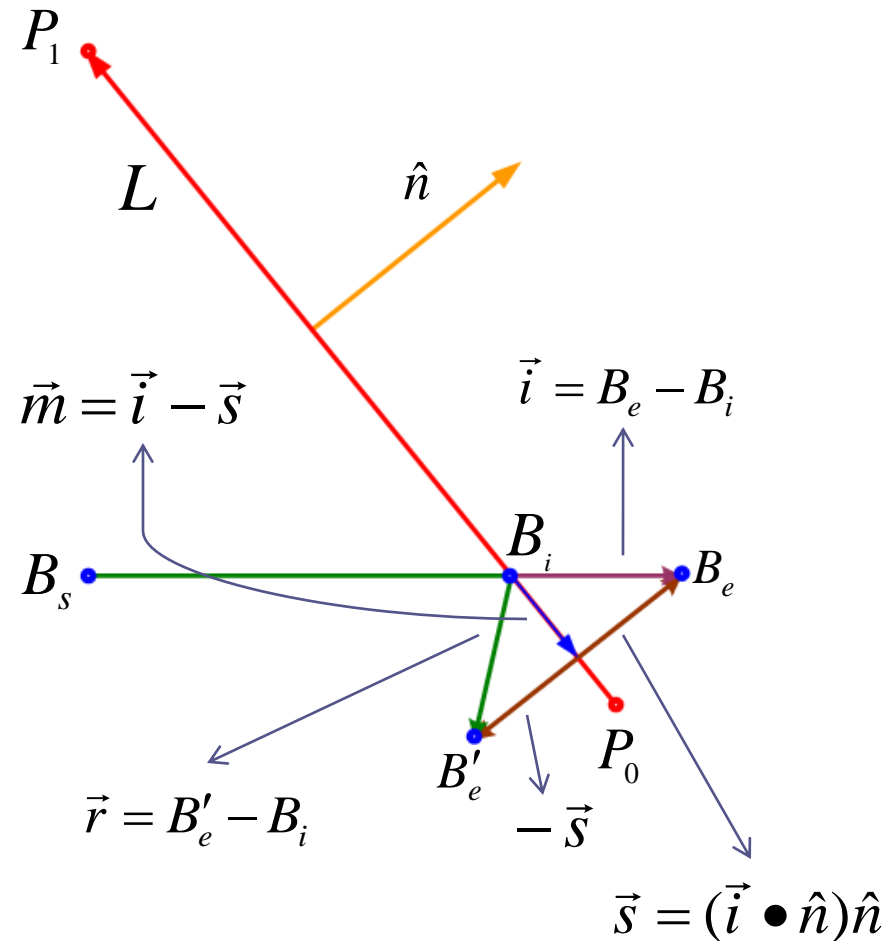
# Position of Ball After Collision (8/8)

$$\vec{r} = \vec{m} - \vec{s}$$

$$\Rightarrow \vec{r} = \vec{i} - 2\vec{s}$$

$$\Rightarrow \vec{r} = \vec{i} - 2(\vec{i} \bullet \hat{n})\hat{n}$$

$$\hat{v} = \frac{\vec{r}}{\|\vec{r}\|}$$



# Overview

- Reflection
- **Animated Circle to Line Segment**

# Modeling Pinball as Circle

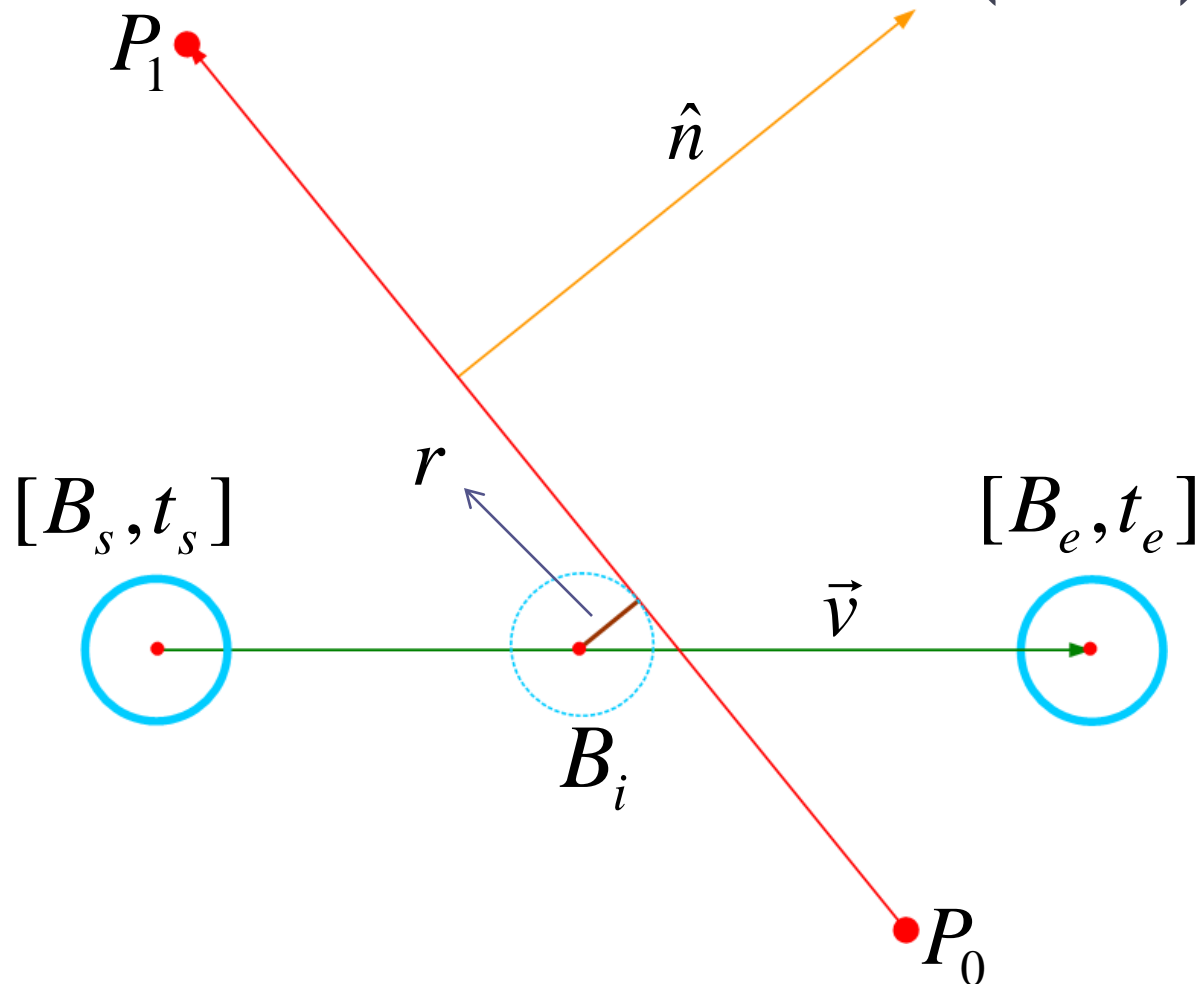
- Pinball modeled by a circle with center and radius  $r$
- Located at center point  $B_s$  at top of frame
- Moving in direction given by normalized vector  $\vec{v}$  and speed  $k$  units

$$\mathbf{B}(t) = \mathbf{B}_s + \overrightarrow{k\hat{v}t}, t \in [0,1]$$

- Velocity per frame  $\vec{v} = \mathbf{B}_s \mathbf{B}_e$

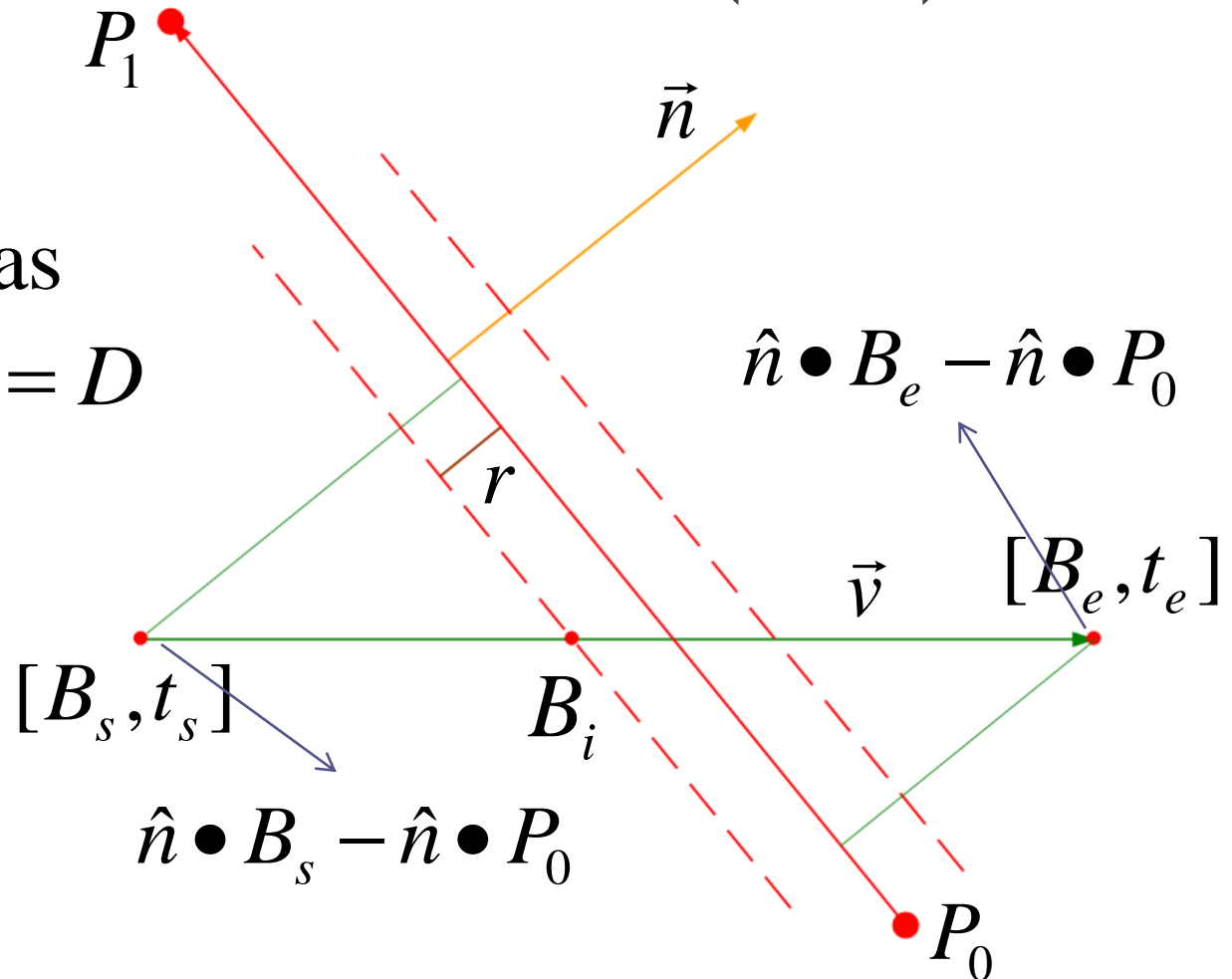
$$\Rightarrow \mathbf{B}(t) = \mathbf{B}_s + \vec{v}t, t \in [0,1]$$

# Pinball-Wall Intersection (1 / 3)



# Pinball-Wall Intersection (2/3)

Wall modeled as  
 $L: \vec{n} \bullet P - \vec{n} \bullet P_0 = D$



# Pinball-Wall Intersection (3/3)

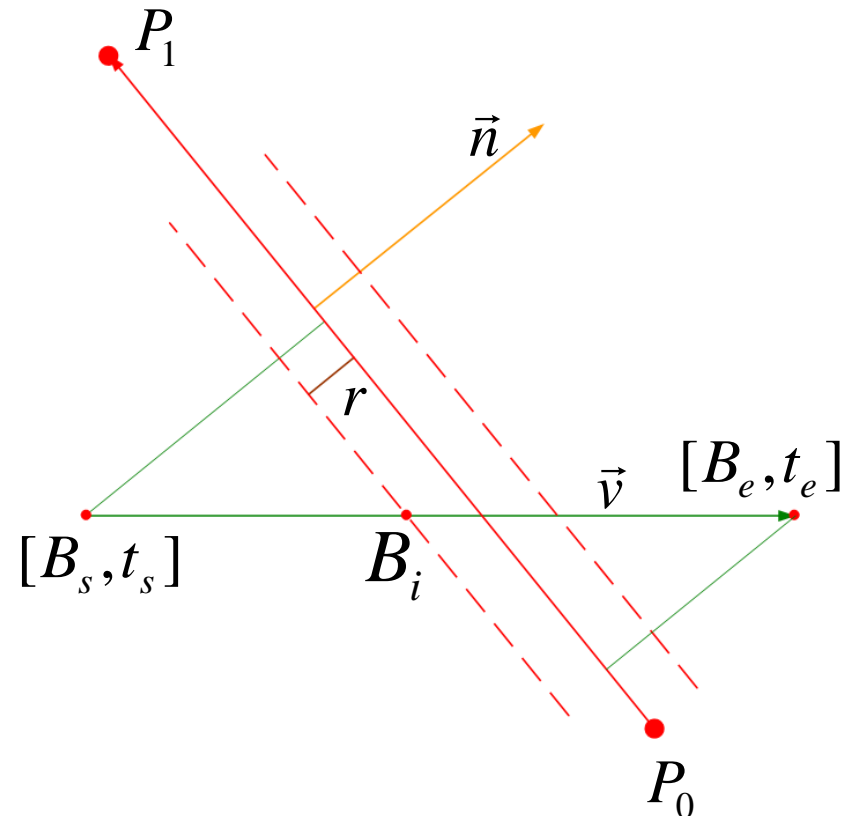
Pinball is inside at  $t_s$  and outside at  $t_e$

$$t_i = \frac{\hat{n} \bullet P_0 - \hat{n} \bullet B_s + D}{\hat{n} \bullet \vec{v}}$$

where  $t_i \in [0,1]$

$$B_i = B_s + \vec{v} \left( \frac{\hat{n} \bullet P_0 - \hat{n} \bullet B_s + D}{\hat{n} \bullet \vec{v}} \right)$$

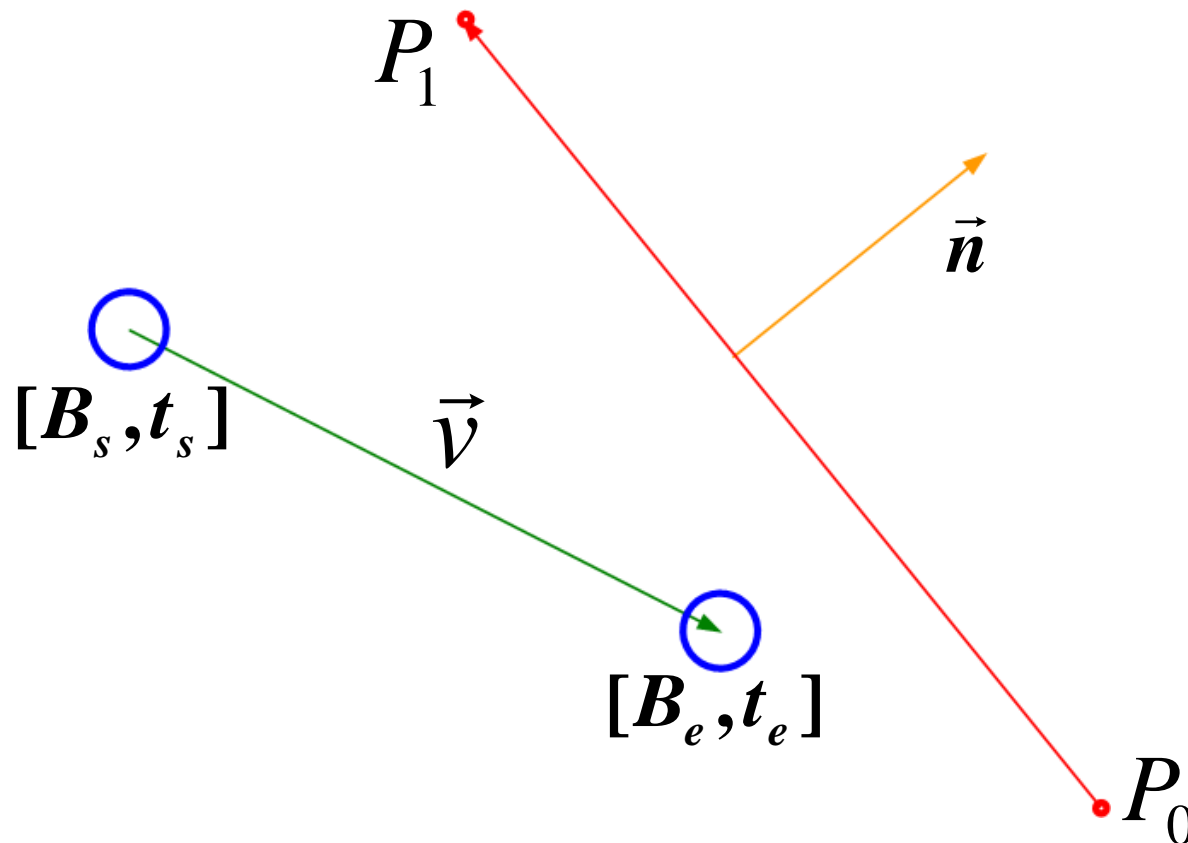
**Note:**  $D = -r$  when  $B_s$  is inside  
 $D = r$  when  $B_s$  is outside





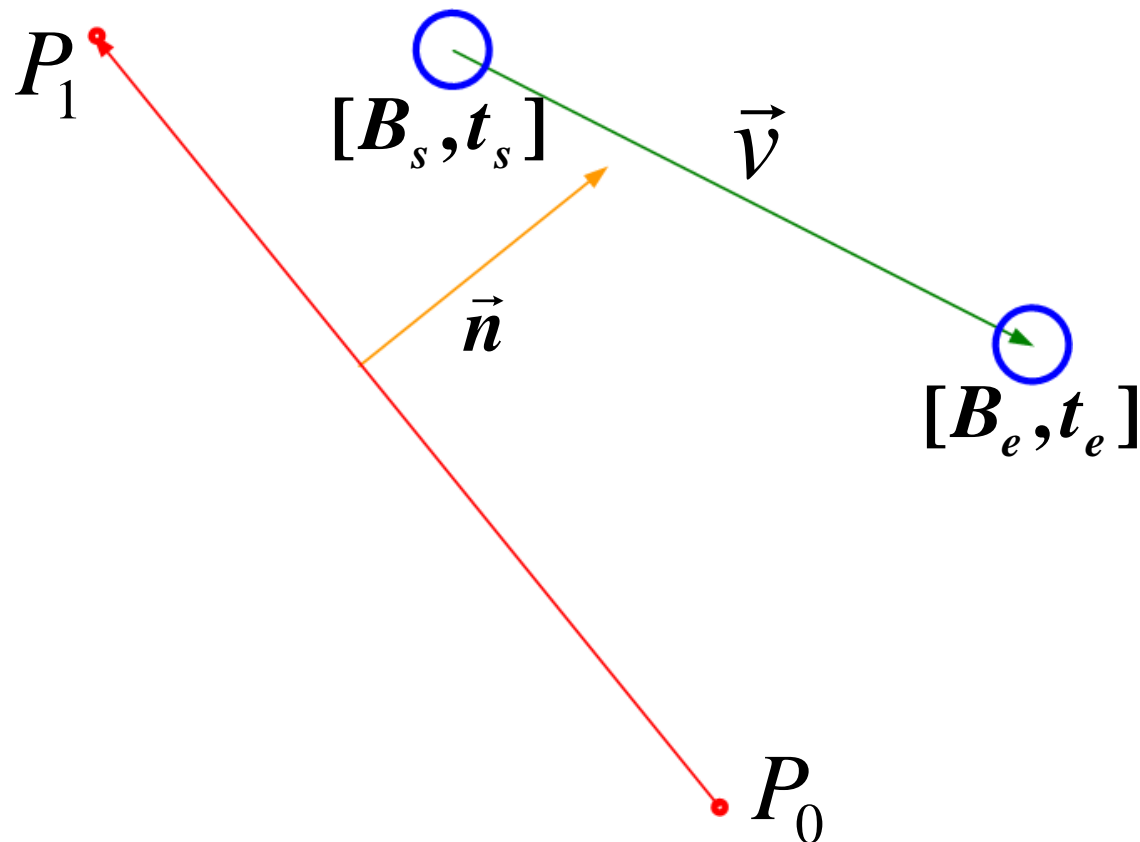
# Test for Non-Collision (1 / 4)

$$(\hat{n} \bullet B_s - \hat{n} \bullet P_0 < -r) \& \& (\hat{n} \bullet B_e - \hat{n} \bullet P_0 < -r)$$



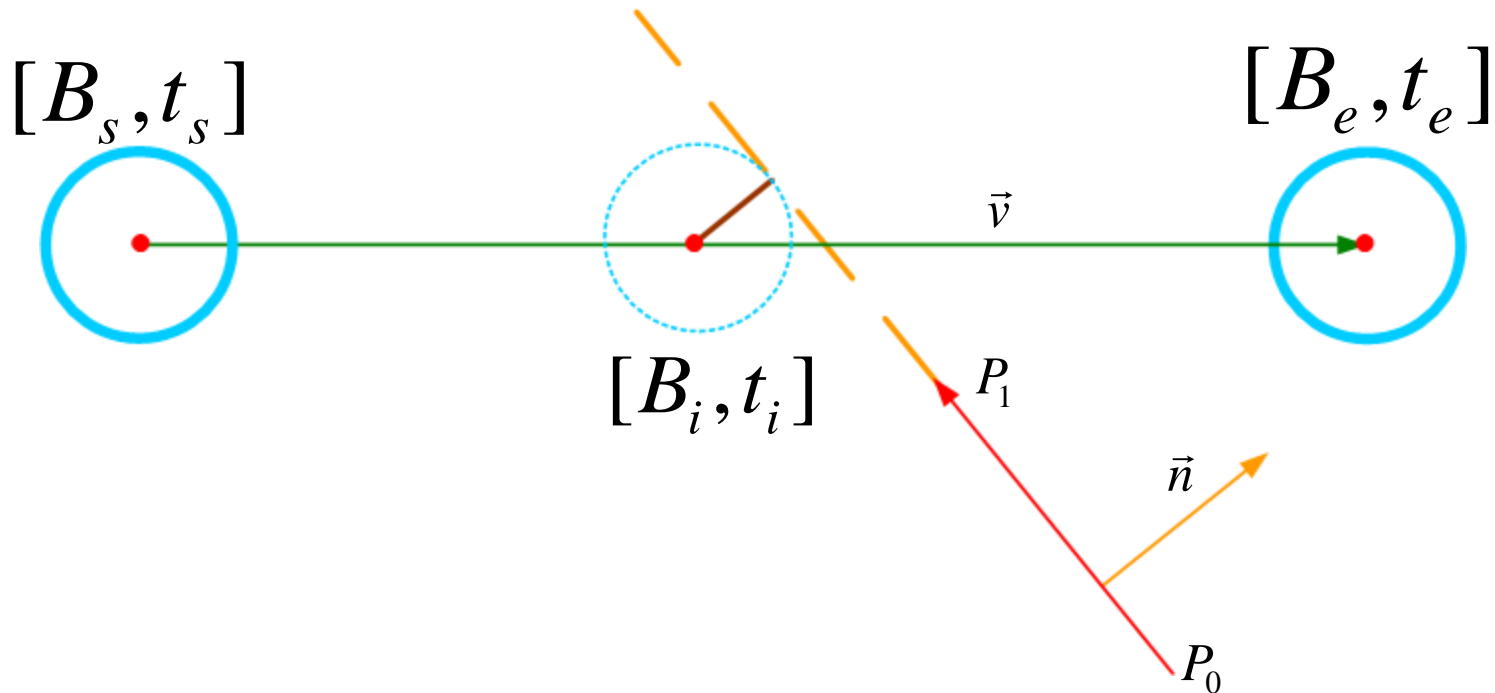
## Test for Non-Collision (2/4)

$$(\hat{n} \bullet B_s - \hat{n} \bullet P_0 > r) \& \& (\hat{n} \bullet B_e - \hat{n} \bullet P_0 > r)$$



# Test for Non-Collision (3/4)

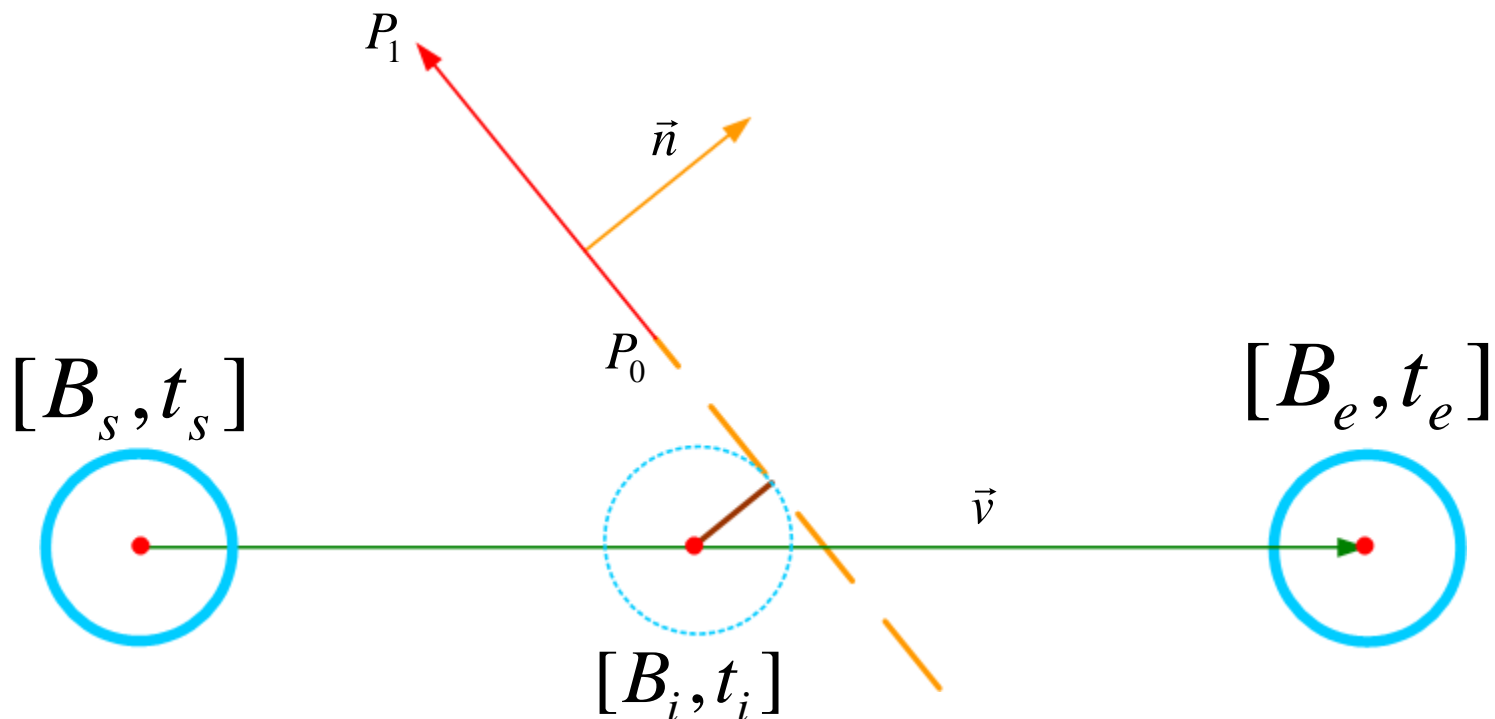
$$(B_i - P_1) \bullet (P_0 - P_1) < 0$$



Ball collides with infinite extension of wall... not finite wall!

# Test for Non-Collision(4/4)

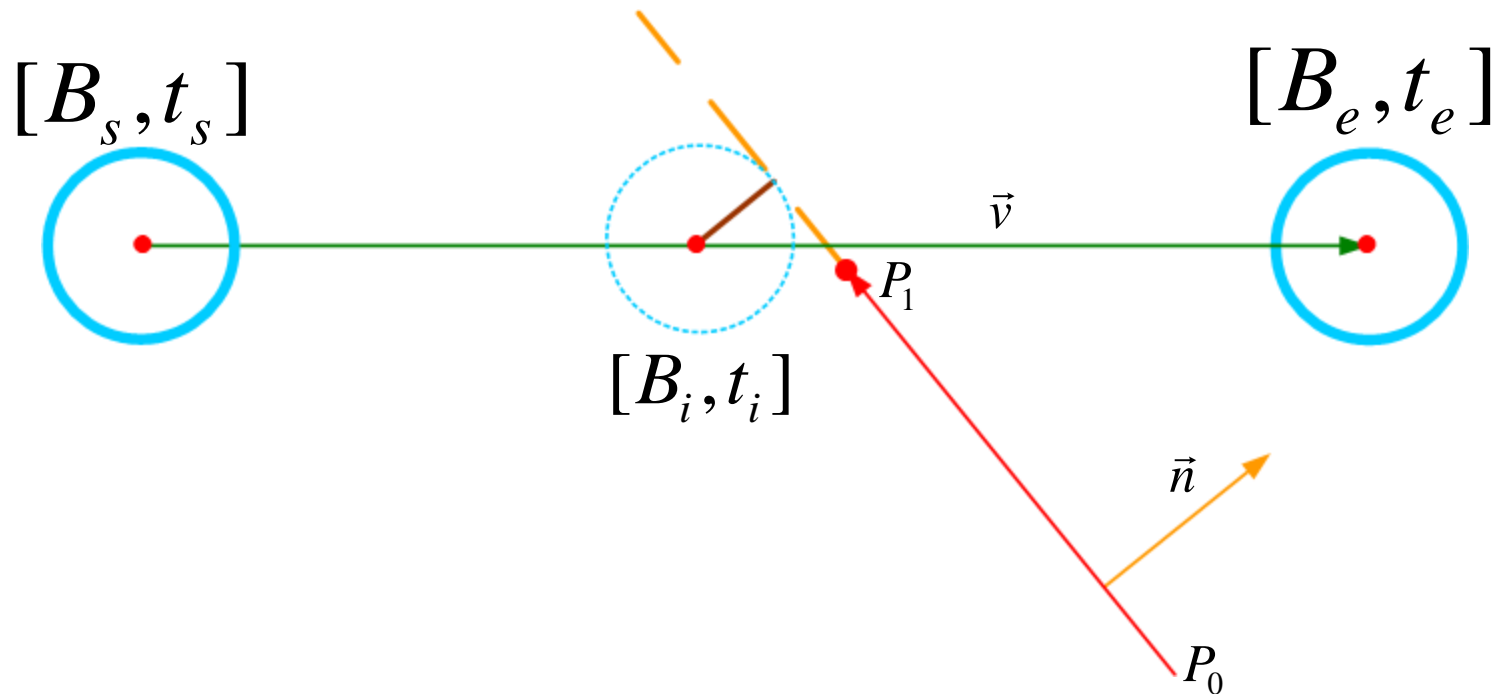
$$(B_i - P_0) \bullet (P_1 - P_0) < 0$$



Ball collides with infinite extension of wall... not finite wall!

# But! We have a Problem

The intersection point  $B_i$  is not on the line, but the ball collides with the wall.



# Steps

- Check for trivial rejection
  - $B_s, B_e$  inside or both outside
  - Going from inside to outside and the collision type of the line segment is outside, and vice versa.
- Calculate the point and time of intersection
  - Check if the time is between  $t_s$  and  $t_e$
- Check if the point of intersection is on the line segment