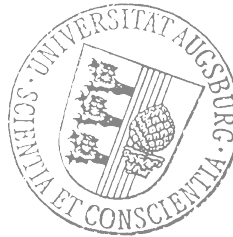


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University of Augsburg
Faculty of Applied Computer Science
Department of Computer Science
Master's Program in Computer Science



Master's Thesis

Brief Title

Full Title of the Thesis

submitted by
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Abstract

This paper aims at investigating the use of EEG signals in classifying a user's emotional state, as a first step of integrating into the SSI framework. The data corpus used is taken from the DEAP and used to solve four different binary classification problems relating to affectional state. First, different approaches for feature extraction and selection were researched, among those, the method of calculating the PSD (Power Spectrum Denisty), based on the FFT, was found to be the most widely used. This is due to the simplicity of implementation and the efficincy of using the resulted features for classification. Other, more complex methods, were used and then discarded as they seemed to offer no advantage in terms of classification accuracy. For classification, three standard classifier were tested for cross comparing accuracy as well as comparison with the classification results reported by pervious similar works with the DEAP. The tests consisited of two experiments, the first experiment used the data for each subject separatly for classification, before calculating the average classification accuracy over all subjects. This shows the expected rate of correct classification for a single user. The second experiment included the entire data of all subjects as a single coprus for classification. This is to demonsterate the generability of an EEG classifier for many users with different EEG patterns. Finally, a new classifier, previously proposed in the litereture for use in EEG classification, was implemented and tested, using the previous experiments, on the same data. The end of this paper reports a comparison between the resulting accuraccies of theses classifications as well as future recommendations for further improvements.

Acknowledgments

Acknowledgements writing allows an author to tell some words of gratitude to those, who turned out to be rather helpful during your thesis writing process. Of course, acknowledgements are not an integral part of a thesis and if you did all your work on your own, you can omit this part. Writing acknowledgements is not obligatory.

Statement and Declaration of Consent

Statement

Hereby I confirm that this thesis is my own work and that I have documented all sources used.

Max Mustermann

Augsburg, 00.00.0000

Declaration of Consent

Herewith I agree that my thesis will be made available through the library of the Computer Science Department.

Max Mustermann

Augsburg, 00.00.0000

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Chapter 1

Introduction

Affective computing is one of the rapidly growing fields of research in the disciplines of computer science, cognitive, psychology and physiology[13]. It aims at expanding computers with the human like ability of dealing with emotions. This involves a two sided effort, for one a computer needs to be able to gather information about the user's emotional state. This needs to be done implicitly, without the user needing to explicitly specify his current state. A computer must learn to process this information and adapt appropriately to the current emotional state. On the other side, affective computing can also imbue computers, and machines in general, with ability to portray or simulate emotions and emotional responses[12, 11].

While not all machines would benefit from such capabilities, many situations would be improved by making the machine simulate a human agent in being able to naturally adapt to the situation[11]. At the spear head of such application is human-computer interaction, which can be made much easier and more natural when an implicit channel of emotional information is introduced between the user and the machine. This is analagous to the large amount of information passed to and from a person in human-human interaction, simply through voice tones, facial expressions and body language[1]. For example, a computer able to detect a user's frustration towards a certain GUI feature, can perhaps modify itself to be more suitable to the user's need, or simply offer a human like response to alleviate their frustration such as an apology or an explanation. Other application that would benefit from affective computing include data gathering for psychological research, such as collecting data on frustration expressions, development of tools for training of social-emotional skills and building service robots able to

interact with people in a nursing or shopkeeping capacity[11].

Modern Medecine uses a variety of techniques to capture and record different activities of the human body. One of those techniques, known as Electroencephalography (EEG), has undergone massive progress in recent years. The current procedure of EEG entails the use of electric conductive electrodes to detect electical activity produced by the brain. When a large number of brain cells are activated (synaptic excitation), a local current flow is produced which can cause weak electrical signals to manifest on the scalp. Once these signals are captured by the electrodes, they can be displayed on paper, or recorded to computer memory for further processing. Electroencephalographic reading can be done in two ways, called invasive and non-invasive procedures. The invasive form requires a surgical procedure to implant electrodes directly on the surface of the brain (subdural EEG) or withen the substance of the brain (depth EEG). In the non-invasive EEG procedure, electrodes are placed over the subjects scalp without the need for surgery or incision. While the non-invasive procedure requires more sensitive sensor and is more prone to noise and interference, it is much more practical than the invasive counter part. It can be applied many times to both adults and children without any risk of injury or brain damage[14]. For the purpose of this study, the term EEG will always refer to signals recorded by a non invasive procedure.

EEG signal recording has its long established uses in the fields of neurology and clinical neurophysiology. This is due its ability to reflect both normal and abnormal brain activity. It can also record the brain response to a stimuli withen fractions of a second of its occurance. This leads to a long list of applications including monitering brain alertness, coma, brain death and certain brain disorders such as epilepsy. However, recently, more focus has been given to the specific problem of computer classification of EEG signals using techniques such as machine learning. The main goal behind such research is the developement of Brain Computer Interfaces (BCIs)r These interfaces allow users to communicate simple commands to different machinery using nothing but brain singals. This can be invaliable to a disabled person with no motor skills (such as patients with spinal cord injury). EEG signal classification has aslo been used in the verification of theoratical hypotheses regarding the inner workings of the brain. Despite the major advances made in the field, however, there has been little attention given to use of EEG signals in determining the emotional state of a subject. This contribution aims at using new as well as previously developed techniques of EEG signal classification into affectional state detection (determining the emotional state of the user).

1.1 Motivation

This work is part of an ongoing effort to develop a framework, called the SSI (Social Signal Interpretation) for the recognition, analysis and recording of human behaviour. Here, we attempt to expand on the existing components by adding an extra channel of sensors for capturing EEG signal and using the new input for interpreting the affective state of the subject. The framework, including this contribution, is expected to benefit many applications, such as the use of humanoid avatars where advanced human computer interaction is required. It can also be used for studies regarding human psychology and emotional behaviours.

1.2 Objectives

This study aims at investigating the use of EEG signals for determining the emotional state of a subject. It uses popular machine learning techniques as well as newly developed algorithms for the recognition of affective state. The data used for the study is the DEAP dataset, the first dataset to recognize the physiological state as well as the self reported emotional response to certain music videos.

1.3 Outline

This study is divided into six chapters: introduction, dataset and preprocessing, feature extraction, classification, experimental results and a summary. These chapters are organised in the same order as what is normally the natural flow of machine learning problem. The fifth chapter, experimental results, reports the classification accuracies achieved in two experiments that were done during the course of the study and compares these results with previous experiments done with the same dataset. All implementations and experiments were done in matlab using the AuBT* (Augsburg Biosignal Toolbox).

Chapter 2

Theoretical Background

2.1 Electroencephalography

The discovery of electroencephalography was first made in 1875 by english physician, Richard Caton, who reported measuring what he described as “feeble currents of varying directions” from the exposed brains of rats and monkeys. The non-invasive procedure was then introduced by Hans Berger, a german neurologist, in 1924 who used ordinary radio equipement to amplify electrical activity produced by the brain on the human scalp. He used a strip of paper to show that EEG can be visually inspected without the need to open the skull.

Potential Difference is formed in brain neurons with the flow of Ca^{++} , K^+ , Na^+ and Cl^- -ions through membrane channels. The potential difference can either exceed a threshold making it an action potential or be subthreshold as postsynaptic potentials (PSPs). Action potentials are spike shaped with duration of 1 ms that when responding to stimuli that exceed a certain threshold, causes the neuron to fire. When action potentials reach a synapse, a connection between the firing neuron and other neurons, it forms a PSP with amplitude relative to the excitation of the input neuron. PSPs have typical amplitudes ranging from 5-10mV and spans between 10 and 50 ms. These potentials propagate throughout the brain neurons in same way. When that number of firing neurons causes a large enough PSP, extracranial electric field is formed. The contribution of action potentials to this field is negligible. The superimposiotion of postsynaptic potentials detected is known as EEG.

EEG is recorded by means of conductive electrodes placed on the scalp.

Conductive paste and low resistance electrode can be used to boost recording quality. The need to interpret single recordings well as compare results call for standardized placement of electrodes. In 1958, a standard for electrode placement was introduced, called 10-20 electrode placement system. Using proportional distance from skull landmarks, the 10-20 system provides adequate coverage of the entire scalp. The name 10-20 stands for the percentage of distance between the ears and nose where electrode positions were chosen. Each electrode position is given a label based on the closest brain area: (F)rontal, (C)entral, (T)emporal, (P)osterior and (O)ccipital. On the left side of the brain, from the subjects perspective, labels are accompanied by an odd number and an even number on the right side.

The dedicated research effort behind EEG measurement is motivated by the very wide spectrum of applications it offers. EEG holds an advantage over other brain monitoring techniques which is speed, since it allows the recording of a stimuli response within fractions of a second of its occurrence. Clinical applications include anaesthesia, testing for drug effects, examining the brain for tumors or strokes and monitoring patients with coma or brain death. Certain variation of EEG signals can be used for specific applications. For example, evoked potentials can be used for cognitive related studies. Quantitative electroencephalography, the use of multi channel measurements of EEG, is typically used for topographic brain mappings. A popular application which has gained attention recently is Brain Computer Interfaces (BCI), which are computer interfaces designed to translate EEG signal of a user into a single command from a preprogrammed set. This allows users with no little or no mobility, such as patients with neck-down-paralysis, to control daily objects with nothing but brain commands.

2.2 Affective Computing

2.2.1 PseudoCode

If you want to show the implementation of some algorithm that is essential to the solution found in your thesis then do not write plain program code. Use an abstract pseudocode representation instead. No one wants to see C++ code or Java code in your thesis because it is presumed that you are able to write such a program as a computer scientist. Generally, writing program code is bad style and just blows up your thesis but will never be read by anyone but you. It is nothing scientific but your handwork while your thesis should show that you are able to do research as a scientist. A pseudocode example could look like the following:

Algorithm 2.1 The Dekker Algorithm

Require: $n \in \mathbb{N}$ **Require:** $0 \leq i, \text{turn} \leq n$ **Require:** $\forall 0 \leq j \leq n : (\text{interested}[j] = \text{false})$ **procedure** DEKKERALGORITHM(n, i) $\text{interested}[i] \leftarrow \text{true}$ **while** $\exists 0 \leq j \leq n : (j \neq i \wedge \text{interested}[j] = \text{true})$ **do** **if** $\text{turn} \neq i$ **then** $\text{interested}[i] \leftarrow \text{false}$ **while** $\text{turn} \neq i$ **do** **end while** $\text{interested}[i] \leftarrow \text{true}$ **end if** **end while****CRITICAL SECTION** $\text{turn} \leftarrow \text{Random}(n)$ $\text{interested}[i] \leftarrow \text{false}$ **end procedure**

Be sure that each pseudocode listing is listed in the list of algorithms at the end of your thesis.

Chapter 3

Data Used

3.1 Dataset Source and Construction

The continued research in the field of emotion recognition has called for the creation of many databases containing emotional information. These databases cover many different modalities such as facial expressions, body gestures and speech for visual and audio modalities. The dataset used for this study is a database called, DEAP (Database for Emotional Analysis using Physiological signals), that was first presented in 2012. It holds physiological recordings, including EEG signals, and facial expressions of several subjects while watching musical videos as emotional stimuli. The database also holds the rating of the subjects for each video with regards to: arousal, valence, dominance, liking and familiarity[6].

Following is a summary of the procedure that went into the creation of the database*. It started with 120 musical videos, half of which were selected automatically and the rest manually. To ensure diversity, the manually selected videos were chosen such that each 15 videos belonged to a different quadrant in the valence/arousal space (LALV, LAHV, HALV, HALV). Then for each video, a one minute highlight segment was extracted automatically through a linear regression method used in [?] to maximize the emotional content. An online subjective emotion assessment interface allowed users to evaluate the videos for arousal and valence. The final 40 videos were selected from the ones having the highest rating in terms of valence/arousal. These videos were viewed, in random order, by 32 subjects while their physiological state was recorded. For 22 subjects, facial

*For more details the reader is referred to [6]

expressions were also recorded. For each video, the subject provided a self assessment of their emotional state using self-assessment manikins (SAMs) in terms of valence, arousal, dominance and liking[6].

3.2 Recorded Signals and Preprocessing

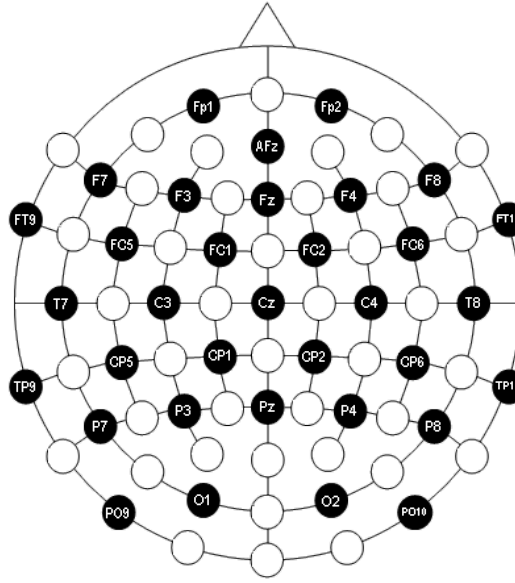


Figure 3.1: The 10/20 placement of electrodes from the DEAP dataset

The DEAP dataset was selected for its abundance in physiological information. The database holds recordings of 40 physiological signals, of which 32 are EEG channels. Figure 3.1 shows the 32 EEG channels including and their positions on the scalp. The label of each channel and position are defined by the 10 - 20 system. While other physiological signals are included in the database, only EEG signals are considered in this study. As well as, the many data channels, the database large number of subjects is a big advantage. As it has been noted that EEG signal patterns vary greatly among different individuals, the presence of data from that many subjects allow for testing emotional recognition techniques for generalizability and accommodation of diversity. The database also provides preprocessed versions of the raw data to allow for a quick implement-and-test approach. Preprocessing used included downsampling from the original 512Hz to 128Hz, removal of EOG artefacts, bandpass frequency filtering between 4.0hz and 45.0hz and averaging the data to the common reference.

Chapter 4

Feature Extraction

4.1 Challenges and Typical Approaches

Feature extraction is usually the first step in a classification problem. It is also the most crucial step as classification accuracy is naturally dependent on the quality of features used. This means that features need to be informative, discriminative between classes and descriptive of each class. The difficulty in feature extraction lies in the nature of an EEG signal which challenges most of the standard feature extraction techniques. The first complication that can be observed in an EEG signals is the signal-to-noise ratio since they tend to be very noisy with large number of outliers. Second, EEGs are non stationary signals and experience sharp variation over time. This makes time related information, while essential to the recognition of stimuli related changes, very difficult to extract. Also, EEG classification lends itself easily to the curse of dimensionality and overfitting. This is caused by the large number of features extracted from multi channel sensor recordings that are later combined into one feature vector. Adding to the problem, is the small size of the datasets available for training[8].

Many techniques have been developed in order to improve the quality of extracted features. Commonly used, are the parametric methods such as the autoregressive(AR) and the adaptive autoregressive(AAR). These methods assume that the signal follows a mathematical model, where its exact form is determined by estimating values for its free coefficients. The difference between the adaptive and the non-adaptive method is that an adaptive model is updated for each new sample[10]. Other features include time frequency features, inverse model features and Band Powers(BP). Selected

for this study, is the Power Spectrum Density (PSD) method which was found to be most popular in the review literature.

4.2 Power Spectral Density

The Power Spectrum Density (PSD) approach has been shown to outperform most other feature extraction techniques[3]. That and the simplicity of implementation are the reasons for choosing it as the feature extraction method. The process of calculating the power spectrum density is known as spectral power estimation. It means determining the power of the signal at each of several frequency bands. This splits the raw EEG signal into several much more informative values. Spectral estimation can be done in two ways. One is to apply a bandpass filter with the required bandwidth to the signal. The calculated power of the output signal divided by the bandwidth of the filter is the spectral density for that particular band. While straight forward, this approach is impractical for situations with prerecorded digitized signals or in the case of considering a large number of frequency bands. Several other approaches exist and split into two groups, parametric and non-parametric methods[?].

The parametric approach requires a model be fitted to the data. That is to say that the parametric approach requires the assumption that the signal is produced by linear system driven by white noise. In the cases where the data truly follows the fitted model, the parametric approach can provide more accurate results. In other cases, however, this approach is quite sensitive to misspecification. In the non-parametric approach, the PSD is estimated directly from the signal. The most basic of the non-parametric methods is the Periodogram. This method uses the discrete-time Fourier transform of the signal, using the Fast Fourier Transform (FFT). The PSD in this case is the appropriately scaled magnitude squared of the result. For a signal of L samples, the periodogram is

$$P_{xx} = \frac{1}{LF_s} \left| \sum_{n=0}^{L-1} x_L^{(n)} e^{-j2\pi f n / F_s} \right|^2$$

Where F_s is the sampling frequency. The method used here is a variation of the periodogram, known as the Welch Periodogram. Instead of calculating a periodogram for the whole signal, the signal is first divided into segments that and then a periodogram is calculated for each segment separately. The results are then averaged to calculate the final PSD. This reduces variation and provides a smoother periodogram[5].

4.3 Extracted Features

Spectral density estimation was applied to each channel of EEG sparately. The frequency bands considered are standard wave patterns that have been observed to give strong indications of brain state. These are six frequency bands that are part of the standard EEG nomenclature. Each of these bands have been shown to have strong corelation with a specific change in the mental state of the subject. They are the following:

Delta Waves Frequency range lies between 0.1 and 4 Hz. It is clearly observed during episodes of deep sleep, known as slow-wave sleep, with large amplitudes, commonly between 75 and 200 μV .

Theta Waves These are more commonly observed in children, and are rare in case of adults. They have tied to states of light sleep or meditation. Its frequency range is between 4 and 8 Hz.

Alpha Waves These waves mostly originate in the postorior part of the brain. They are observed during alertness of the brain. They can be more easily seen with the eyes closed. It was observed that alpha waves are slightly blocked by mental effort or spiked attention. Frequency range lies between 8 and 12 Hz.

Slow Alpha Waves Also known as the alpha delta waves, they are a special type of alpha waves. Their frequency range is restricted between 8 and 10 Hz and are dominant in the anterior-posterior gradient.

Beta Waves With a much wider frequency than other waves, between 12 and 30 Hz, their spikes are related to increased attention, alertness and focus. Beta waves are supressed right before and during physical motions.

Gamma Waves Frequency range is above 30 Hz but rarely exceeds 45 Hz. Gamma waves are associated with higher mental functions, specifically the processing of information and voluntary movements.

The power values of these six frequency bands were calculated for each of the 32 recorded channel and then concatenated into a single feature vector. This give a feature vector of 192 features.

Other than the power spectral density, spectral asymmetry was also used as features. Spectral power asymmetry is defined as the difference in power between the channels on the left and right hemispheres of the brain.

That is to say that for each sensor channel on the right brain hemisphere, the corresponding symmetrical channel on the left hemisphere is identified. Then the power of the signals coming from both sensors is subtracted from each other. This is known as their spectral asymmetry and is calculated for each of the above mentioned frequency bands. Spectral asymmetry has been shown to be effective features in the recognition of certain mental disorders and tumors. With 14 symmetrical channels present in the data, the number of added features is 84 which extends the feature vector to 276 total features.

4.4 Feature Selection

Following feature extraction, feature selection is applied. Feature selection is the process of selecting a subset of the available features to be actually used in classification. There are several benefits to feature selection. First, it can eliminate noisy features which merely confuse the classifier. It can improve the efficiency of classification by reducing storage space and training time. It can also remove features that non discriminative between classes making them ineffectual to classification. Feature selection can greatly reduce the effect of the curse of dimensionality. This can be very important in EEG classification due to the normally small datasets. Many algorithms exist for feature selection. The method used here is called the Analysis of Variance (ANOVA). This is a statistical method commonly used to investigate the relations between a sample and the data. Here, it shows the contribution of each feature to the overall variance of the data. This allows the feature set to be restricted to the highest contributing features. This study compares between the accuracies of different classifiers with and without the use of feature selection.

Chapter 5

Classification

5.1 Standard Classifiers

For classification of the selected features, three standard classifiers were used: linear discriminant analysis (LDA), k nearest neighbours (KNN) and neural networks. These classifiers have been used in many works relating to EEG classification and are described below:

LDA The LDA is a statistical method that was introduced by RA Fisher[4]. When applied to a binary classification problems (containing two classes), the means of both classes, μ_1 and μ_2 , and the covariances, Σ_1 and Σ_2 , are calculated from the training set. The mean and covariance of each class serves as representation of that class. The LDA makes the assumptions that both classes are normally distributed, and that both variances are equal ($\Sigma_1 = \Sigma_2 = \Sigma$). With that the decision function for class 1 becomes

$$\vec{w} \cdot \vec{x} > T$$

Where \vec{x} is a feature vector, T is a constant threshold and

$$\vec{w} \propto \sum_{i=1}^{-1} (\mu_1 - \mu_2)$$

LDA can be applied to classification problems with more than 2 classes using the 1-vs.-all method[?].

KNN This algorithm uses a form of majority vote to form a decision regarding classification. To classify a feature vector \vec{x} , a set of the K closest

vectors is created and \tilde{x} is assigned to the most occurring class in the set. The determination of the closest vectors can be done using several distance metrics. The most commonly used distance measure is the mahalanobis distance which, for two vectors \tilde{x} and \tilde{y} , is equal to

$$d^2 = (\tilde{x} - \tilde{y}) \sum^{-1} (\tilde{x} - \tilde{y})^T$$

Where \sum is the covariance matrix. KNN has the advantage of non linear decision boundary as it can approximate any function, providing K is large enough. It benefits the most from feature selection as it is highly susceptible to the curse of dimensionality[8].

Neural Networks Neural Networks are a technique of classification that simulate the brain neurons. They are formed of several connected nodes, where each connection has a weight. The input nodes receive the values of the feature vector, normalize them between 0 and 1 and then pass them to the next connected nodes. The values are multiplied by the connection weight before the process is repeated at the next node. Information propagates through the network using the same way until it reaches the output nodes. The output nodes produce the final values that determine the decision of the network. Neural networks are known as universal approximators for their ability to approximate any function. This makes them somewhat sensitive to noise. Despite that, neural networks have been shown to be a very efficient classification technique and have been used in many BCI implementations.

5.2 Gaussian Classifier

5.2.1 Classifier Implementation

The gaussian classifier is the fourth classifier implemented to compare its performance with the other standard classifiers in EEG recognition. This classifier was developed specifically for use in brain computer interfaces for EEG classification. It was introduced in the work of Millán et al. (2000)[9]. It was termed a “a local neural classifier”. While its correct recognition rate can be outdone by other more standard classifiers, it holds two advantages that make it more appropriate to online classification. First, it has very small resolution time (half a second) which can be essential for the classification of a continuous stream of data. Second, the classifier has a lower wrong

response rate than most other classifiers which can be important if the cost of recovery from a wrong classification is much higher than the cost of rejecting an uncertain sample. It is worth mentioning that this advantage is more prominent in application of EEG based control than in EEG based emotional recognition.

For N_k class classification problem, the algorithm for the gaussian classifier starts by calculating the initial mean μ_k and covariance matrix \sum_k of each class C_k using the maximum likelihood approach

$$\mu_k = \frac{1}{N_k} \sum_{n=1}^{N_k} x^n \quad (5.1)$$

$$\sum_k = \frac{1}{N_k} \sum_{n=1}^{N_k} (x^n - \mu_k)(x^n - \mu_k)^T \quad (5.2)$$

With the assumption that each class has an independent normal distribution and using the values calculated above, the discriminant function for the classifier becomes

$$y_k(x) = \frac{-1}{2} (x - \mu_k)^T \sum_k^{-1} (x - \mu_k) - \frac{1}{2} \ln |\sum_k| + \ln P(C_k) \quad (5.3)$$

Where $P(C_k)$ is the prior probability of class C_k . Here, the classes are considered to have equal probability of $\frac{1}{N_k}$. The discriminant function follows from the Bayesian rule

$$y_k(x) = P(C_k|x) = \frac{p(x|C_k)P(C_k)}{p(x)}$$

after dropping constant terms.

Practically, what this means is that the mean μ_k and covariance \sum_k form a prototype for class C_k . During classification the sample x is assigned to the closest prototype which is determined based on the mahalanobis distance. During training the values of μ_K and \sum_k are optimized iteratively using gradient descent to minimize the mean square error function. With the additional assumption of diagonal covariance matrices, the update function of μ_k for each feature vector x^n becomes

$$\Delta\mu_k = \alpha [t_k(x^n) - y_k(x^n)] \sum_k^{-1} (x^n - \mu_k) y_k(x^n) y_j(x^n) \quad (5.4)$$

Where t_k is the K^{th} component of the target vector of the form 1-of-c, y_k is the probability of class C_k calculated using 5.3 and y_j the probability of other classes. The values of the covariance matrices are reevaluated using 5.2 after every full iteration over the training set.

5.2.2 Shrunk Covariance

A complication that arises from the large dimensionality of the feature vector, is the accuracy of covariance matrix estimation. With the number of features much greater than the number of samples in the dataset, calculated covariance matrix tend to be singular. The problem with a singular covariance matrix is that the inverse Σ^{-1} , which is required by for the calculation of y_k given by 5.3, does not exist. The solution that was implemented is the shrunk covariance matrix. The concept of a shrunk covariance matrix reduces the estimation errors by pushing the matrix towards a more structured matrix, the target matrix, whose diagonal elements are the sample variances[2]. The advantage of the target matrix is that it is guaranteed to be non singular (invertible), however, it can be a much worse estimation for the covariance matrix than the maximum likelihood estimation. For covariance matrix S , the shrunk covariance matrix Σ_{shrunk} is

$$\Sigma_{shrunk} = \delta F + (1 - \delta)S \quad (5.5)$$

Where F is the target matrix and δ is a number between 0 and 1 called the shrinkage factor. The shrinkage factor effectively determines the contributions of the maximum likelihood estimation matrix S and the target matrix F to the final covariance matrix Σ_{shrunk} . The shrinkage factor here is empirically determined to be 0.2. The elements of the target matrix F can be calculated by

$$f_{ii} = s_{ii}f_{ij} = \bar{r}\sqrt{s_{ii}s_{jj}} \quad (5.6)$$

and \bar{r} is the sample correlation given by

$$\bar{r} = \frac{2}{(N-1)N} \sum_{i=1}^{N-1} \sum_{j=i+1}^N \frac{s_{ij}}{\sqrt{s_{ii}s_{jj}}} \quad (5.7)$$

N is the number of samples in the dataset[7].

Chapter 6

Experimentation and Results

6.1 Setup

Throughout the course of this study, two classification experiments were carried out in order to compare the performance of different classifiers and procedures on EEG signals. The setup of the two experiments closely resembles that which is used in [6]. Specifically, the first experiment follows the exact same procedure, while using different classifiers, to allow comparison of the produced results with the results reported in their work. To prepare for the experiments the signals are split into one minute segments, representing the recording of an EEG signal from a single subject while watching one musical video. This gives 40 segments for each of the 32 subjects making a total of 1280 segments. Each segment is considered a single sample in the dataset. Classification of a sample in this context indicates the overall emotion of the subject during a single musical video. This is preferable to the more common practice of using one second segments, as it provides a more meaningful classification rather than just indicate the fluctuations of the emotional state. Both experiments include three binary classification problems: arousal, valence and liking. Each sample in the dataset is classified into the three categories as either high or low. Since the DEAP dataset provides numerical values between 0 and 9 for the three categories, values higher than 4.5 are considered high.

6.2 Experiment One

The first experiment is a standard classification experiment. The EEG samples from each of the 32 subjects is treated as a single training corpus. The four classifiers are then applied to the corpus for each of the three classification problems. The resulting correct classification and percentage accuracy is recorded. This procedure is then repeated for the 32 subjects, and the average accuracy of the four classifiers overall is calculated. This showcases the expected performance of each classifier when integrated into real life applications. The procedure of this experiment matches the single trial classification experiment carried out in [6] using a naïve bayes classifier. This is why the results reported in their work was included in the comparison of the results reported here. Only results that made use of feature selection were reported in their study.

Emotion	LDA	KNN	MLP	Gaussian	NB
Arousal (without feature selection)	53.77%	58.30%	59.66%	57.62%	n/a
Arousal (with feature selection)	48.19%	50.66%	54.90%	50.00%	62.00%
Valence (without feature selection)	51.62%	56.24%	55.90%	52.99%	n/a
Valence (with feature selection)	49.46%	51.29%	54.50%	50.00%	57.00%
Liking (without feature selection)	51.03%	56.85%	60.36%	53.93%	n/a
Liking (with feature selection)	49.46%	51.29%	54.50%	50.00%	55.40%

Table 6.1: Averages of correct classification percentages for experiment one

6.3 Experiment Two

One of the recurring problems in EEG classification is the sharp variation between different samples, which can greatly reduce the generalizability of results. This is not only true for data from different subjects, but also applies for data from the same subject that was acquired in different recording sessions. This has made it a standard practice to use classifier systems that are optimized for specific individuals. This may have had its uses in an academic environment, despite the added cost to calibration times and reproducibility. However, all attempts of applying such techniques to practical commercial applications remain highly unlikely without the development of more general solutions. To that end, this experiment was designed to com-

pare the robustness of different classifiers, and to test the generalizability of their accuracies. The experiment uses the data of all 32 subjects as a single training corpus, with no indication of the different sources. The four classifiers are applied to the corpus in the same way as the previous experiment, for the three emotions with and without using feature selection.

Emotion	LDA	KNN	MLP	Gaussian
Arousal (without feature selection)	50.56%	57.65%	57.10%	57.38%
Arousal (with feature selection)	61.49%	58.09%	59.31%	56.86%
Valence (without feature selection)	48.89%	60.89%	56.84%	55.13%
Valence (with feature selection)	54.38%	59.78%	54.96%	55.75%
Liking (without feature selection)	48.95%	54.20%	52.49%	52.60%
Liking (with feature selection)	50.57%	57.29%	53.11%	52.75%

Table 6.2: Percentages of correct classifications for experiment two.

Table 6.2 summarizes the results obtained from experiment two.

Chapter 7

Summary

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Appendices

Appendix A

First Appendix

This is the place where the appendices are supposed to be. Appendices are everything that would just blow up your thesis but are still of some interest for a reader that wants to get a deeper grasp on the details of your work.

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