## EE23BTECH11054 - Sai Krishna Shanigarapu\*

## **GATE EE 2023**

54. The circuit shown in the figure is initially in the steady state with the switch K in open condition and  $\overline{K}$  in closed condition. The switch K is closed and  $\overline{K}$  is opened simultaneously at the instant  $t = t_1$ , where  $t_1 > 0$ . The minimum value of  $t_1$  in milliseconds such that there is no transient in the voltage across the 100  $\mu F$  capacitor, is \_\_\_\_\_ (Round off to 2 decimal places). (GATE EE 2023)

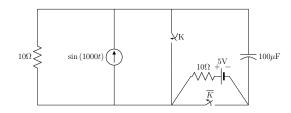


Fig. 1. Circuit 1

## **Solution:**

1) Switch K is open and  $\overline{K}$  is closed.

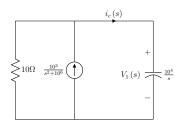


Fig. 2. Circuit 2

Using Current divider rule,

$$i_c(s) = \left(\frac{10^3}{s^2 + 10^6}\right) \left(\frac{10}{10 + \frac{10^4}{s}}\right) \qquad (1)$$
$$= \frac{10^3 s}{(3^2 + 10^6)(1 + 10^3)} \qquad (2)$$

$$= \frac{10^{3}s}{(s^{2} + 10^{6})(s + 10^{3})}$$
(2)  
$$V_{1}(s) = \frac{10^{7}}{(s^{2} + 10^{6})(s + 10^{3})}$$
(3)

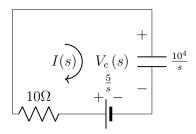


Fig. 3. Circuit 3

$$I(s) = \frac{\frac{5}{s} - V_1(s)}{10 + \frac{10^4}{s}} \tag{4}$$

$$V_c(s) = \frac{5}{s} - 10\left(\frac{5 - V_1(s)}{1 + 10^{-3}s}\right)$$
 (5)

For transient analysis,

$$\frac{5 - V_1(s)}{1 + 10^{-3}s} = 0 \tag{6}$$

$$\implies V_1(s) = 5 \tag{7}$$

$$\frac{10^7}{(s^2+10^6)(s+10^3)} = \frac{5}{s}$$
 (8)

$$\frac{5}{s+10^3} + \frac{10^3 - s}{s^2 + 10^6} = \frac{5}{s} \tag{9}$$

$$\frac{-s}{s^2 + 10^6} + \frac{10^3}{s^2 + 10^6} + \frac{1}{s + 10^3} = \frac{1}{s}$$
 (10)

From Table I

$$-\cos(1000t_1) + \sin(1000t_1) + e^{-10^3t_1} = 1 \quad (11)$$

$$\implies t_1 \approx 1.57 \text{msec}$$
 (12)

S Domain	Time Domain
$\frac{1}{s}$	$u\left( t\right)$
$\frac{-s}{a^2+s^2}$	$-\cos\left(at\right)$
$\frac{a}{a^2+s^2}$	$\sin{(at)}$
$\frac{1}{s+a}$	$e^{-at}$

TABLE I LAPLACE TRANSFORMS

2) Switch K is closed and  $\overline{K}$  is open.

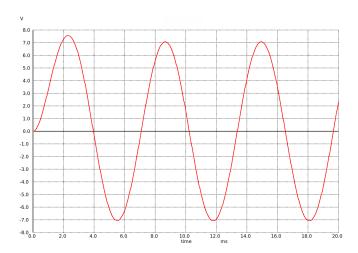


Fig. 4. plot of  $V_1$ 

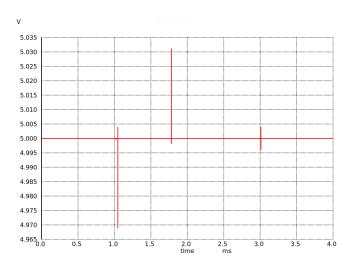


Fig. 5. plot of  $V_c$