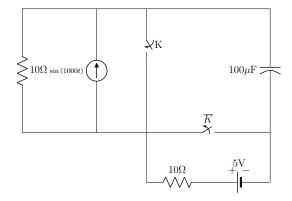
EE23BTECH11054 - Sai Krishna Shanigarapu*

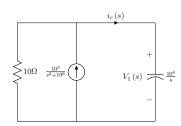
GATE EE 2023

54. The circuit shown in the figure is initially in the steady state with the switch K in open condition and K in closed condition. The switch K is closed and K is opened simultaneously at the instant $t = t_1$, where $t_1 > 0$. The minimum value of t_1 in milliseconds such that there is no transient in the voltage across the 100 μF capacitor, is ____ (Round off to 2 decimal places). (GATE EE 2023)



Solution:

Case(i) Switch K is open and \overline{K} is closed.



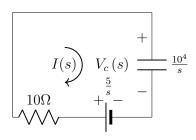
Using Current divider rule,

$$i_c(s) = \left(\frac{10^3}{s^2 + 10^6}\right) \left(\frac{10}{10 + \frac{10^4}{s}}\right)$$
 (1)

$$=\frac{10^3s}{(s^2+10^6)(s+10^3)}\tag{2}$$

$$= \frac{10^{3}s}{(s^{2} + 10^{6})(s + 10^{3})}$$
(2)
$$V_{1}(s) = \frac{10^{7}}{(s^{2} + 10^{6})(s + 10^{3})}$$
(3)

Case(ii) Switch K is closed and \overline{K} is open.



$$I(s) = \frac{\frac{5}{s} - V_1(s)}{10 + \frac{10^4}{s}} \tag{4}$$

$$V_c(s) = \frac{5}{s} - 10\left(\frac{5 - V_1(s)}{1 + 10^{-3}s}\right)$$
 (5)

For transient analysis,

$$\frac{5 - V_1(s)}{1 + 10^{-3}s} = 0 \qquad (6)$$

$$\implies V_1(s) = 5 \quad (7)$$

$$\Rightarrow V_1(s) = 5 \qquad (7)$$

$$\frac{10^7}{(s^2 + 10^6)(s + 10^3)} = \frac{5}{s} \qquad (8)$$

$$\frac{5}{s+10^3} + \frac{10^3 - s}{s^2 + 10^6} = \frac{5}{s} \quad (9)$$

$$\frac{-s}{s^2 + 10^6} + \frac{10^3}{s^2 + 10^6} + \frac{1}{s + 10^3} = \frac{1}{s} \quad (10)$$

$$-\cos(1000t_1) + \sin(1000t_1) + e^{-10^3 t_1} = 1 \quad (11)$$

$$\implies t_1 \approx 1.57 \text{msec}$$
 (12)

S Domain	Time Domain
$\frac{1}{s}$	$u\left(t\right)$
$\frac{-s}{a^2+s^2}$	$-\cos\left(at\right)$
$\frac{a}{a^2+s^2}$	$\sin{(at)}$
$\frac{1}{s+a}$	e^{-at}

TABLE I Laplace transforms

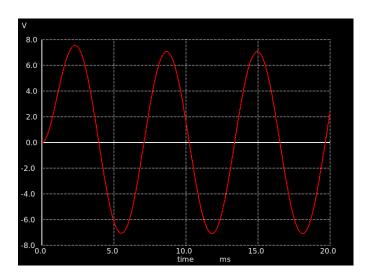


Fig. 1. plot of V_1 in case(i)

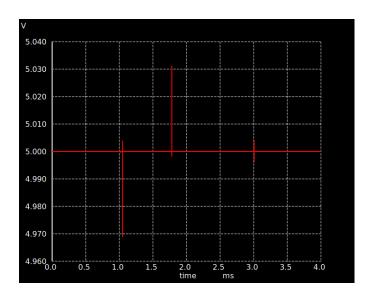


Fig. 2. plot of V_c in case(ii)