

EE23BTECH11054 - Sai Krishna Shanigarapu*

EXERCISE 9.2

13 If the sum of n terms of an A.P. is $3n^2 + 5n$ and its m^{th} term is 164, find the value of m .

Solution:

$$y(n) = 3(n+1)^2 + 5(n+1) \quad (1)$$

$$Y(z) = \frac{2z^2(4z-1)}{(z-1)^3} \quad (2)$$

$$U(z) = \frac{1}{1-z^{-1}} \quad (3)$$

$$y(n) = x(n) * u(n) \quad (4)$$

$$X(z) = \frac{Y(z)}{U(z)} \quad (5)$$

$$= \frac{8-2z^{-1}}{(1-z^{-1})^2} \quad (6)$$

$$x(n) = Z_z^{-1}[X(z)] \quad (7)$$

$$= (6n+8)(u(n)) \quad (8)$$

| Symbol | Parameters |
|--------|-----------------------|
| $y(n)$ | Sum of n terms |
| $x(n)$ | general term |
| $u(n)$ | unit step function |
| $Y(z)$ | Z-transform of $y(n)$ |
| $X(z)$ | Z-transform of $x(n)$ |
| $U(z)$ | Z-transform of $u(n)$ |

TABLE I
PARAMETERS

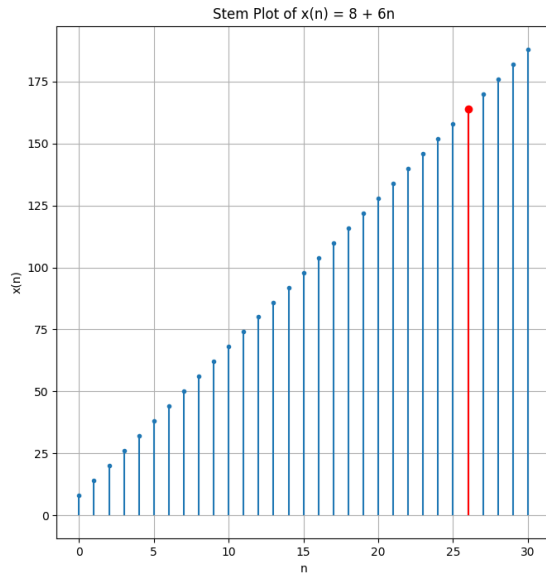


Fig. 1. Plot of $x(n)$ vs n

$$\therefore m = 26$$