



CS 412 Intro. to Data Mining

การขุดค้น Mining คือ การ pattern ที่ซ่อนอยู่

Chapter 6. Mining Frequent Patterns, Association and Correlations: Basic Concepts and Methods

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What Is Pattern Discovery?

- What are patterns?
items
- **Patterns**: A set of items, subsequences, or substructures that occur frequently together (or strongly correlated) in a data set
- Patterns represent **intrinsic** and **important properties** of datasets
patterns are the interesting information in the data
- **Pattern discovery**: Uncovering patterns from massive data sets
- Motivation examples:
 - What products were often purchased together? สินค้าอะไรที่คนมักซื้อด้วยกันเสมอ?
 - What are the subsequent purchases after buying an iPad?
หลังจากที่ซื้อ iPad แล้วมักจะซื้ออะไรต่อ?
 - What code segments likely contain copy-and-paste bugs?
Ex. ลืมเปลี่ยนชื่อตัวแปรในฟังก์ชันกับ Code ใหม
 - What word sequences likely form phrases in this corpus?

Pattern Discovery: Why Is It Important?

- Finding **inherent regularities** in a data set
- **Foundation** for many essential data mining tasks
 - Association, correlation, and causality analysis
 - Mining sequential, structural (e.g., sub-graph) patterns
 - Pattern analysis in spatiotemporal, multimedia, time-series, and stream data
 - Classification: Discriminative pattern-based analysis
 - Cluster analysis: Pattern-based subspace clustering
- Broad applications
 - Market basket analysis, cross-marketing, catalog design, sale campaign analysis, Web log analysis, biological sequence analysis

↓ สัตว์เฉพาะที่ Date Mining ค้นหาลักษณะ
คล้ายกัน

support = จำนวน transaction ที่มีส่วนประกอบของ item < absolute relative

Basic Concepts: k-Itemsets and Their Supports

- **Itemset**: A set of one or more items

- **k-itemset**: $X = \{x_1, \dots, x_k\}$

- Ex. {Beer, Nuts, Diaper} is a 3-itemset

- **(absolute) support (count)** of X, $\text{sup}\{X\}$: Frequency or the number of occurrences of an itemset X

- Ex. $\text{sup}\{\text{Beer}\} = 3$

- Ex. $\text{sup}\{\text{Diaper}\} = 4$

- Ex. $\text{sup}\{\text{Beer, Diaper}\} = 3$

- Ex. $\text{sup}\{\text{Beer, Eggs}\} = 1$

Transaction ID

Tid	Items bought
10	Beer, Nuts, Diaper
20	Beer, Coffee, Diaper
30	Beer, Diaper, Eggs
40	Nuts, Eggs, Milk
50	Nuts, Coffee, Diaper, Eggs, Milk

- **(relative) support**, $s\{X\}$: The fraction of transactions that contains X (i.e., the probability that a transaction contains X)

- Ex. $s\{\text{Beer}\} = 3/5 = 60\%$ → เลขที่ส่วนคือ transaction ทั้งหมด

- Ex. $s\{\text{Diaper}\} = 4/5 = 80\%$

- Ex. $s\{\text{Beer, Eggs}\} = 1/5 = 20\%$

relation support คือ transaction ที่ support item set นั้น?

Basic Concepts: Frequent Itemsets (Patterns)

- An itemset (or a pattern) X is *frequent* if the support of X is no less than a *minsup* threshold σ
- Let $\sigma = 50\%$ (σ : *minsup* threshold)

คำอธิบาย < 95 / 100
คำอธิบาย < 95 / 100

For the given 5-transaction dataset



Tid	Items bought
10	Beer, Nuts, Diaper
20	Beer, Coffee, Diaper
30	Beer, Diaper, Eggs
40	Nuts, Eggs, Milk
50	Nuts, Coffee, Diaper, Eggs, Milk

- All the frequent 1-itemsets:
 - Beer: 3/5 (60%); Nuts: 3/5 (60%)
 - Diaper: 4/5 (80%); Eggs: 3/5 (60%)
- All the frequent 2-itemsets:
 - {Beer, Diaper}: 3/5 (60%)
- All the frequent 3-itemsets?
 - None

- Why do these itemsets (shown on the left) form the complete set of frequent k -itemsets (patterns) for any k ?
- Observation:** We may need an efficient method to mine a complete set of frequent patterns

From Frequent Itemsets to Association Rules

- Comparing with itemsets, rules can be more telling

- Ex. $Diaper \Rightarrow Beer$ *การซื้อ Diaper ก็มักจะซื้อ Beer ด้วย*

- Buying diapers may likely lead to buying beers*

- How strong is this rule? (support, confidence)

- Measuring association rules: $X \Rightarrow Y$ (s, c)

- Both X and Y are itemsets

- Support**, s : The probability that a transaction contains $X \cup Y$

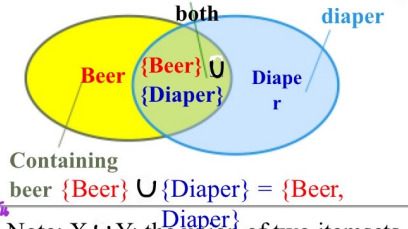
- Ex. $s\{Diaper, Beer\} = 3/5 = 0.6$ (i.e., 60%)

- Confidence**, c : The *conditional probability* that a transaction containing X also contains Y

- Calculation: $c = \sup(X \cup Y) / \sup(X)$

- Ex. $c = \sup\{Diaper, Beer\} / \sup\{Diaper\} = 3/4 = 0.75$

Tid	Items bought
10	Beer, Nuts, Diaper
20	Beer, Coffee, Diaper
30	Beer, Diaper, Eggs
40	Nuts, Eggs, Milk
50	Nuts, Coffee, Diaper, Eggs, Milk



Note: $X \cup Y$: the union of two itemsets

The set contains both X and Y

Mining Frequent Itemsets and Association Rules

- **Association rule mining**

- Given two thresholds: $minsup$, $minconf$
 - Find **all** of the rules, $X \rightarrow Y (s, c)$
 - such that, $s \geq minsup$ and $c \geq minconf$
 - Let $minsup = 50\%$ *minsup mining itemset is 50% only*
 - Freq. 1-itemsets: Beer: 3, Nuts: 3, Diaper: 4, Eggs: 3
 - Freq. 2-itemsets: {Beer, Diaper}: 3
 - Let $minconf = 50\%$
 - $Beer \rightarrow Diaper$ (60%, 100%)
 - $Diaper \rightarrow Beer$ (60%, 75%)
- (Q: Are these all rules?)

Tid	Items bought
10	Beer, Nuts, Diaper
20	Beer, Coffee, Diaper
30	Beer, Diaper, Eggs
40	Nuts, Eggs, Milk
50	Nuts, Coffee, Diaper, Eggs, Milk

- **Observations:**

- Mining association rules and mining frequent patterns are very close problems
- Scalable methods are needed for mining large datasets

Efficient Pattern Mining Methods

- The Downward Closure Property of Frequent Patterns
- The Apriori Algorithm
- Extensions or Improvements of Apriori
- Mining Frequent Patterns by Exploring Vertical Data Format
- FPGrowth: A Frequent Pattern-Growth Approach
- Mining Closed Patterns

The Apriori Algorithm—An Example

Database TDB

Tid	Items
10	A, C, D
20	B, C, E
30	A, B, C, E
40	B, E

minsup = 2

C1

1st scan

Itemset	sup
{A}	2
{B}	3
{C}	3
{D}	1
{E}	3

F1

Itemset	sup
{A}	2
{B}	3
{C}	3
{E}	3

C2

2nd scan

Itemset	sup
{A, B}	1
{A, C}	2
{A, E}	1
{B, C}	2
{B, E}	3
{C, E}	2

F2

Itemset	sup
{A, C}	2
{B, C}	2
{B, E}	3
{C, E}	2

C3

Itemset
{B, C, E}

3rd scan

F3

Itemset	sup
{B, C, E}	2

2 Itemset