## **Homework #1** (100 points)

207.547 Seminar in Experimental Psychology: Computational Modeling Spring 2018

Due: Thursday, March 29, at 11:59 pm

Each of the eight retention models below predicts the probability of correct recall as a function of time interval *t* given model parameters as

*POW1*: 
$$p(\theta = (b)) = (t+1)^{-b}$$
 (0 < b < 3)

*POW2*: 
$$p(\theta = (a, b)) = a(t + 1)^{-b}$$
 (0 < a < 1, 0 < b < 3)

EXP1: 
$$p(\theta = (b)) = e^{-bt} (0 < b < 3)$$

EXP2: 
$$p(\theta = (a, b)) = ae^{-bt} (0 < a < 1, 0 < b < 3)$$

EXPOW: 
$$p(\theta = (a, b, c)) = ae^{-bt}(t+1)^{-c}$$
 (0 < a < 1, 0 < b, c < 3)

HYP1: 
$$p(\theta = (b)) = \frac{1}{1 + ht}$$
 (0 < b < 1)

HYP2: 
$$p(\theta = (a,b)) = \frac{a}{1+bt}$$
 (0 < a < 1, 0 < b < 1)

SINE: 
$$p(\theta = (a)) = (\sin(at) + 1)/2 \ (0 < a < 100)$$

with a binomial likelihood function of the following form,

$$f(y=(y_1,y_2,...,y_m)|\theta)=\prod_{i=1}^m \tfrac{n!}{(n-y_i)!y_i!} \; p(\theta)^{y_i} (1-p(\theta))^{n-y_i}$$

Download the R programs, *Parm\_Estm.R* and *MLE\_LSE.R*, from the link provided in the ClassPrep, and modify them so the maximum likelihood estimates (MLEs) of all models are obtained.

Attach a single ZIP file that includes copies of your modified R programs and a single PDF file of the figure created. The figure must show all best-fit curves. In addition, attach a table summarizing MLE parameter estimates and values of the percent variance accounted for (i.e., r²). Also include one paragraph discussion of the results.

**Bonus (challenge) question (extra 20 points)**: Program your own code that estimate parameters with least squares estimates (LSEs) of the six models.