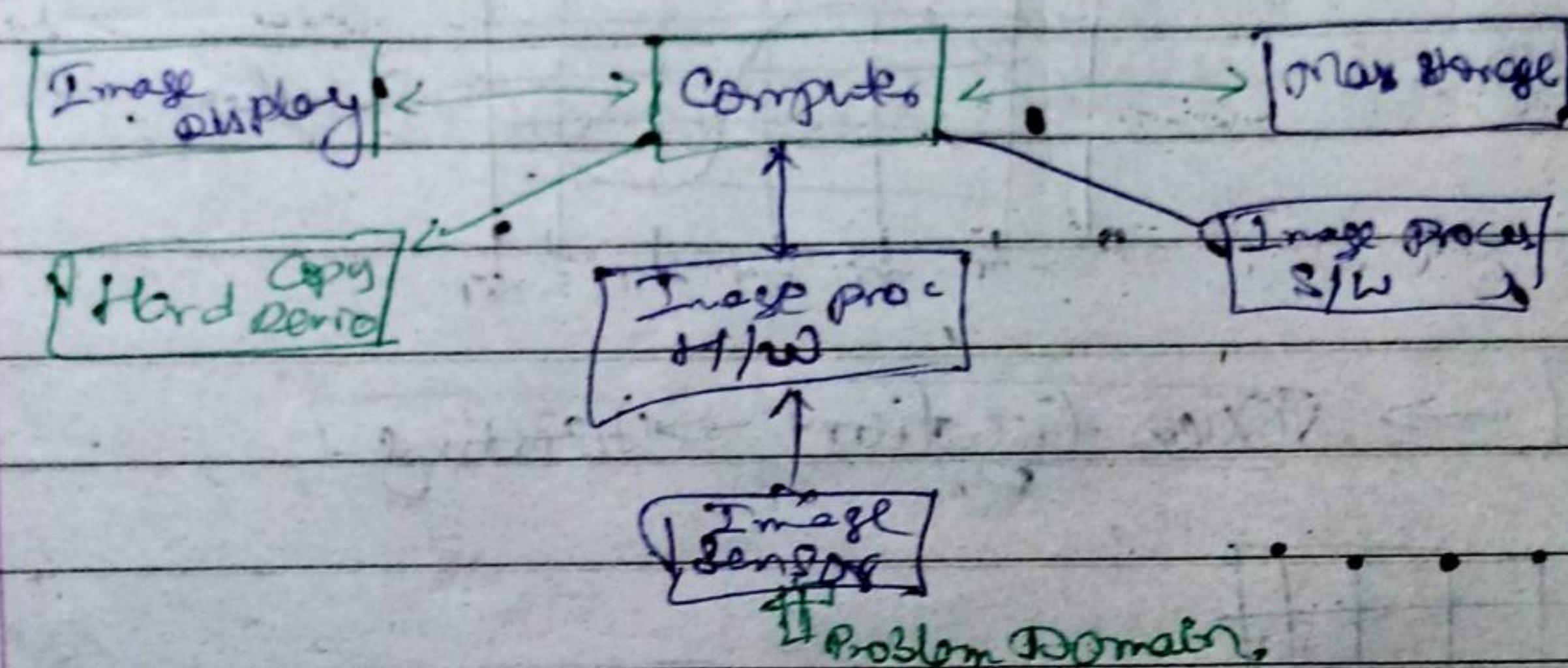


read diagram Component of general purpose image p



(a) Concept of brightness adaptation and discrimination in Image processing.

Explain the smoothing of Images in freq domain using ideal, Butterworth & Gaussians Pass filter.

(b) Explain the process of brightness adaptation & discrimination in Image proc.

In contouring. ② checker board effect
④ distance measure.

Brightness Adaptation

2021

Image Quality

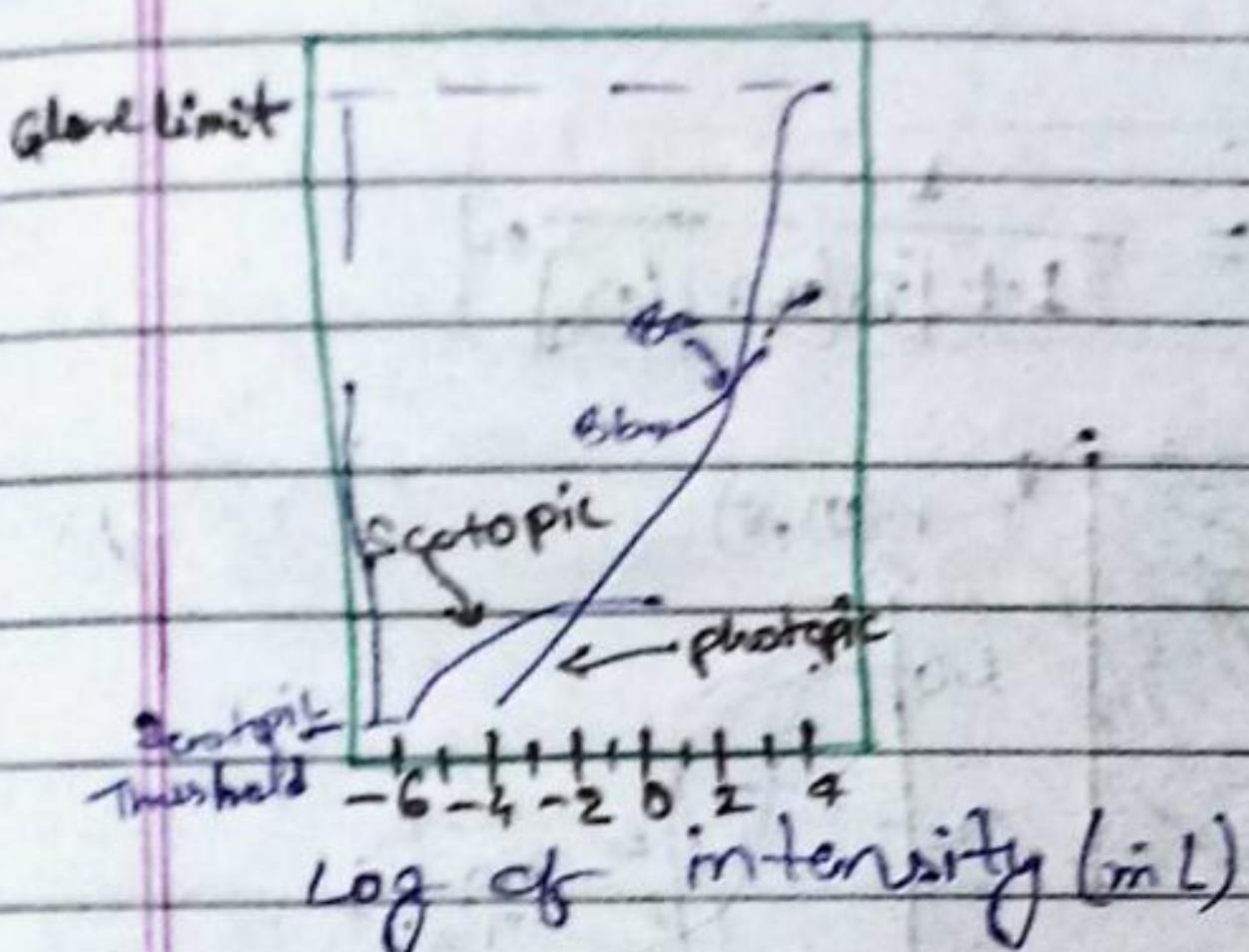
2021

PAGE NO.

DATE: / / 2021

Ans The human eye has a wide dynamic range by changing the eye's overall sensitivity and this is called Brightness adaptation.

② The eye's ability to discriminate black & white at different intensity levels



③ * Explain the smoothing of images in the frequency domain: - ideal, Butterworth and Gaussian low pass filters.

Ques ⇒ Smoothing (blurring) is achieved in the frequency domain by high - frequency attenuation or low - pass filtering.

► Three types of low pass filters:-

① Ideal ② Butterworth ③ Gaussian.

► All filters $H(u,v)$ are understood to be discrete function of size $(P \times Q)$, i.e.
 $u=0, 1, 2, \dots, P-1$ and $v=0, 1, 2, \dots, Q-1$.

(Note) Butterworth filter has "got a control parameter called filter order. * For higher order it behave like ideal filter and it approaches Gaussian filter for lower order.

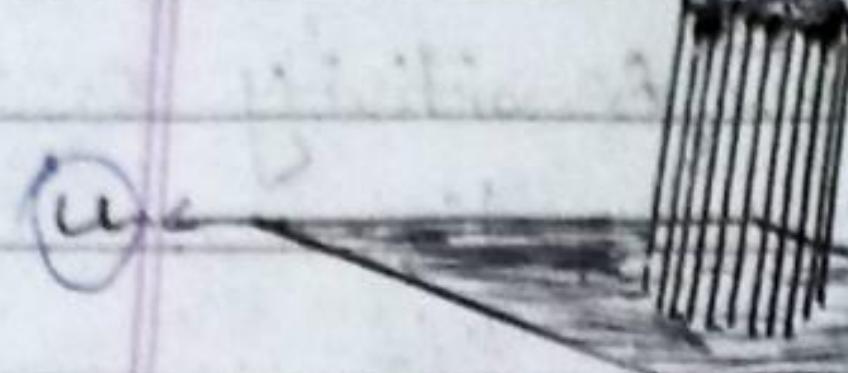
$$D(u, v) = [(u - P/2)^2 + (v - Q/2)^2]^{1/2}$$

PAGE NO.

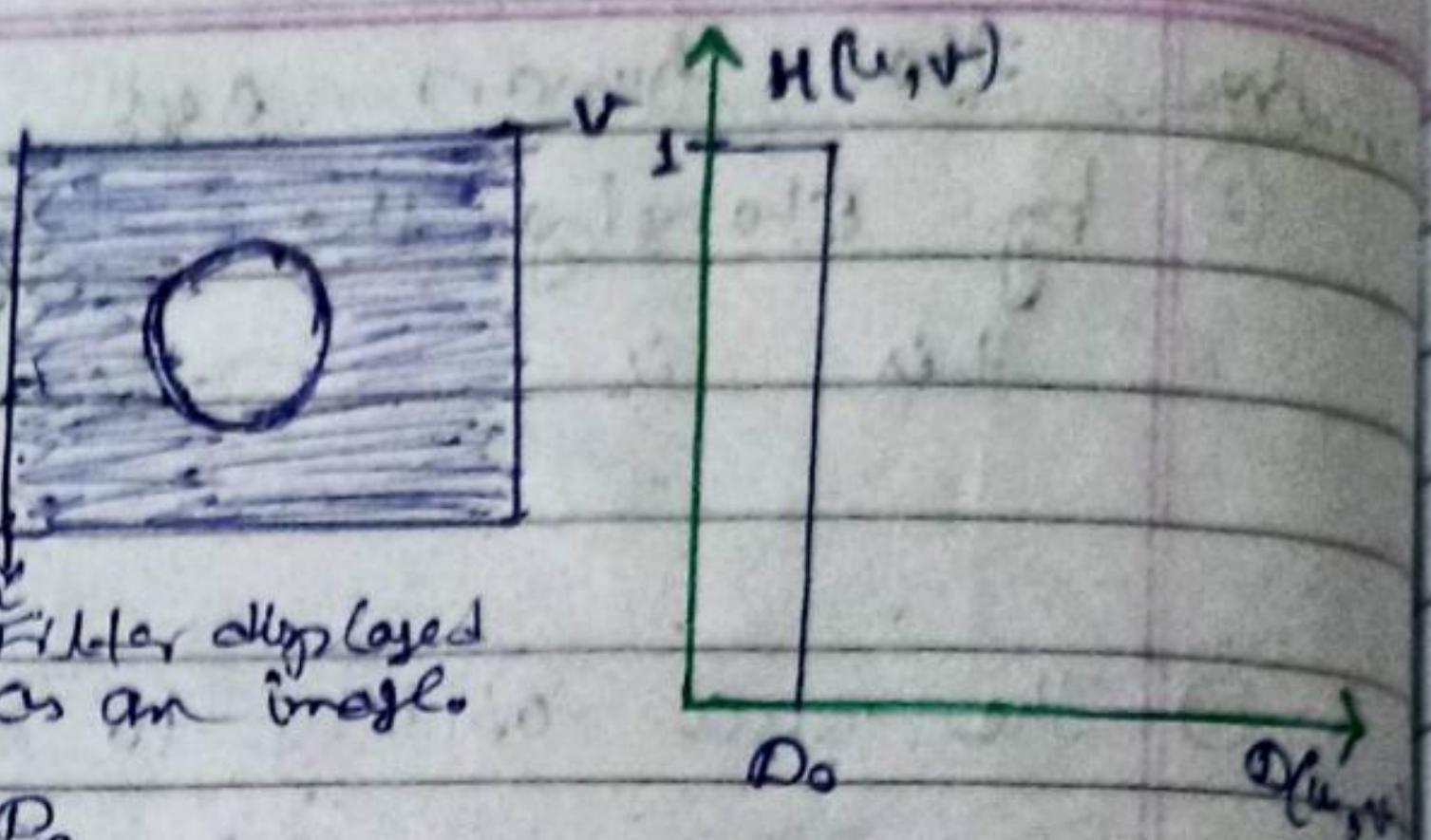
DATE: / / 20

① Ideal low pass filter:-

$$H(u, v)$$

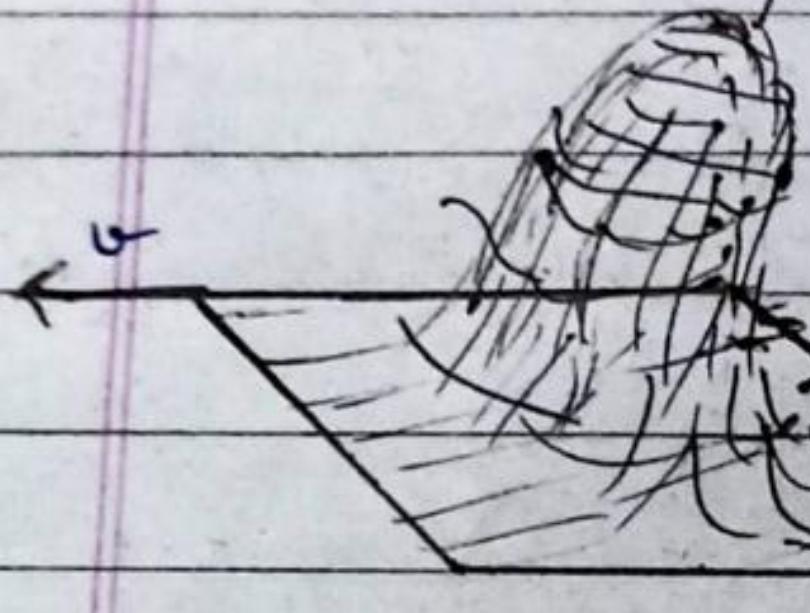


* plot of an ideal filter



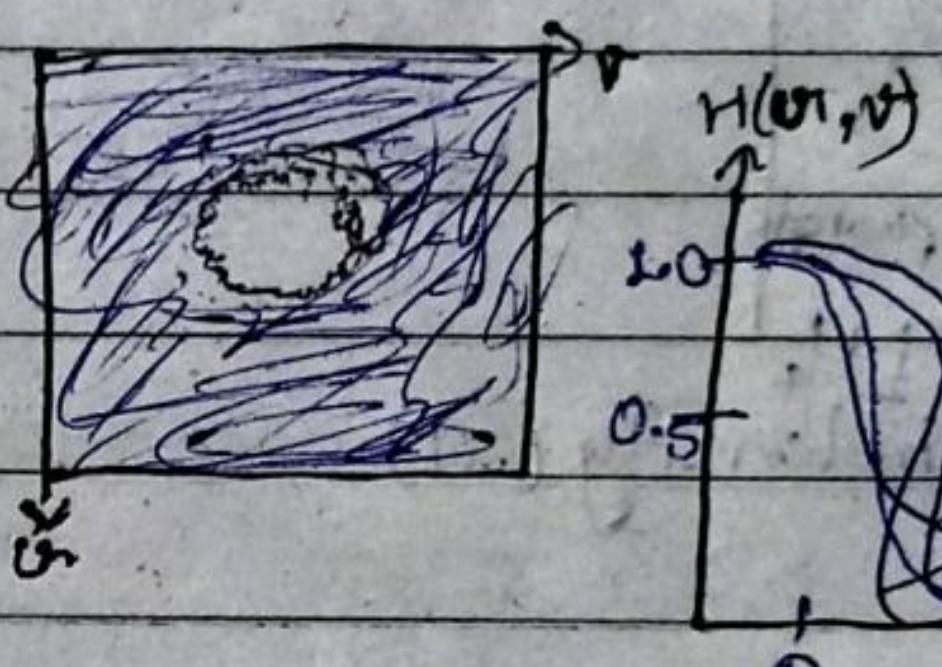
② Butterworth filter:-

$$H(u, v)$$



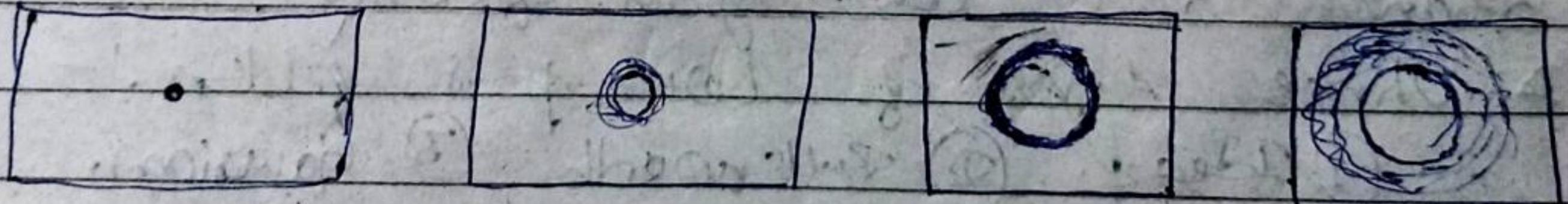
* same as above

$$H(u, v) = \frac{1}{1 + [D(u, v)/D_0]^{2n}}$$



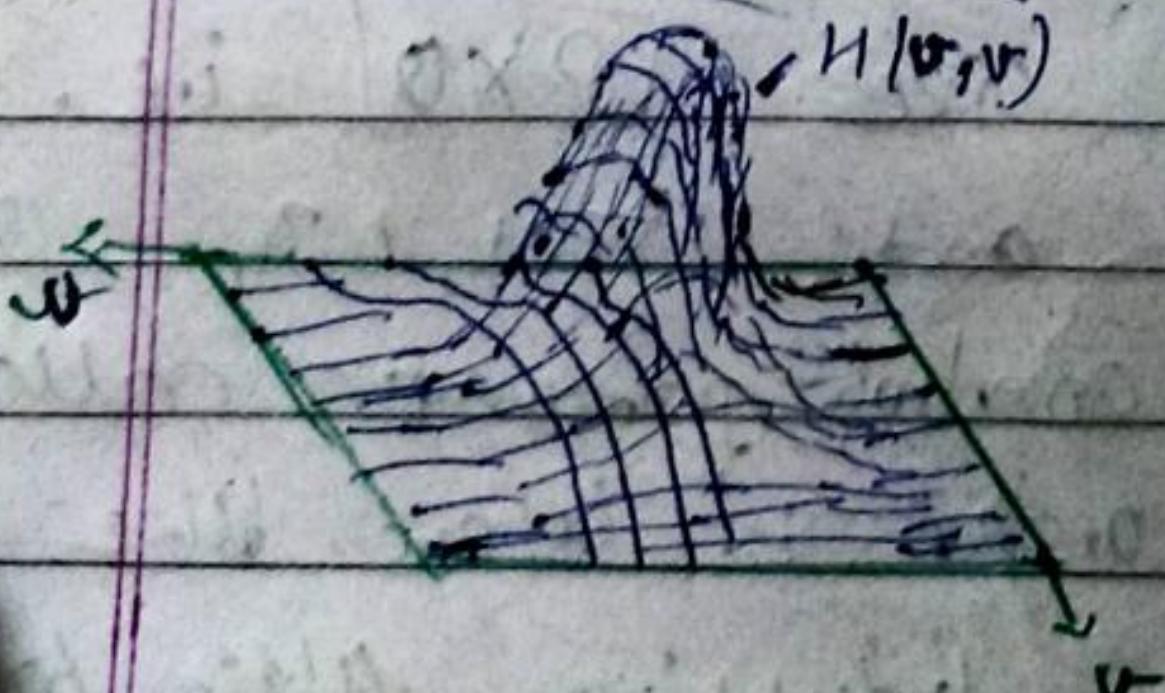
③ Spatial Representation :-

$H(u, v)$

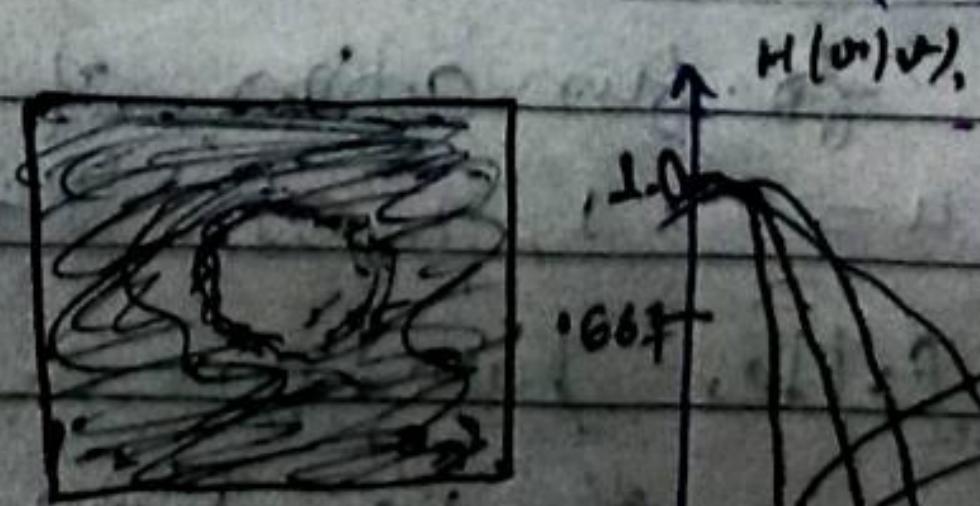


④ Gaussian Filter:-

$H(u, v)$

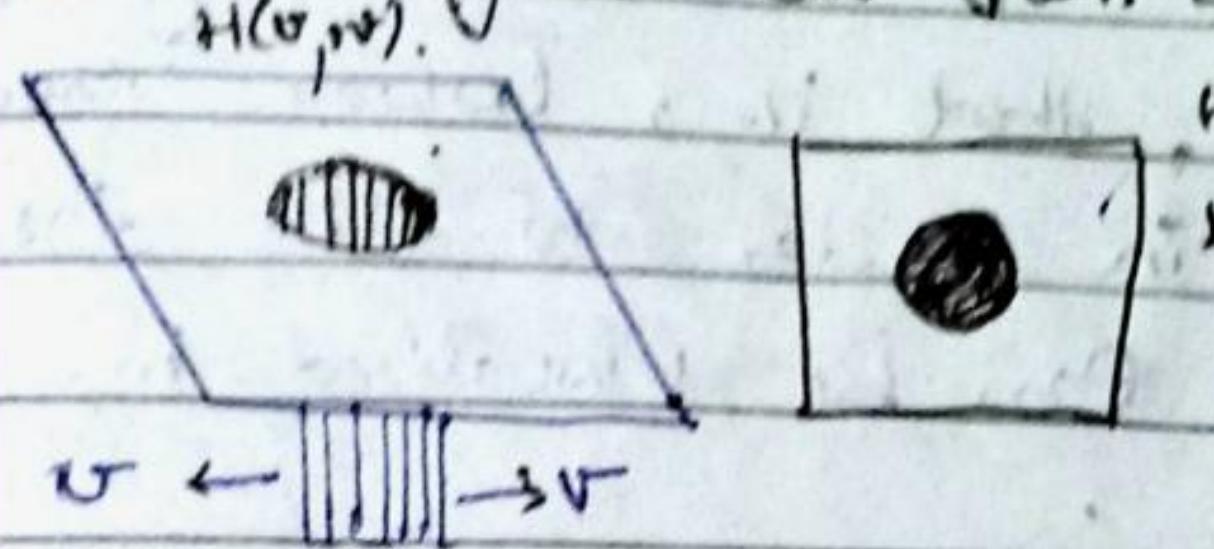


$$H(u, v) = e^{-\pi^2(D_{u,v})^2/2D_0^2}$$

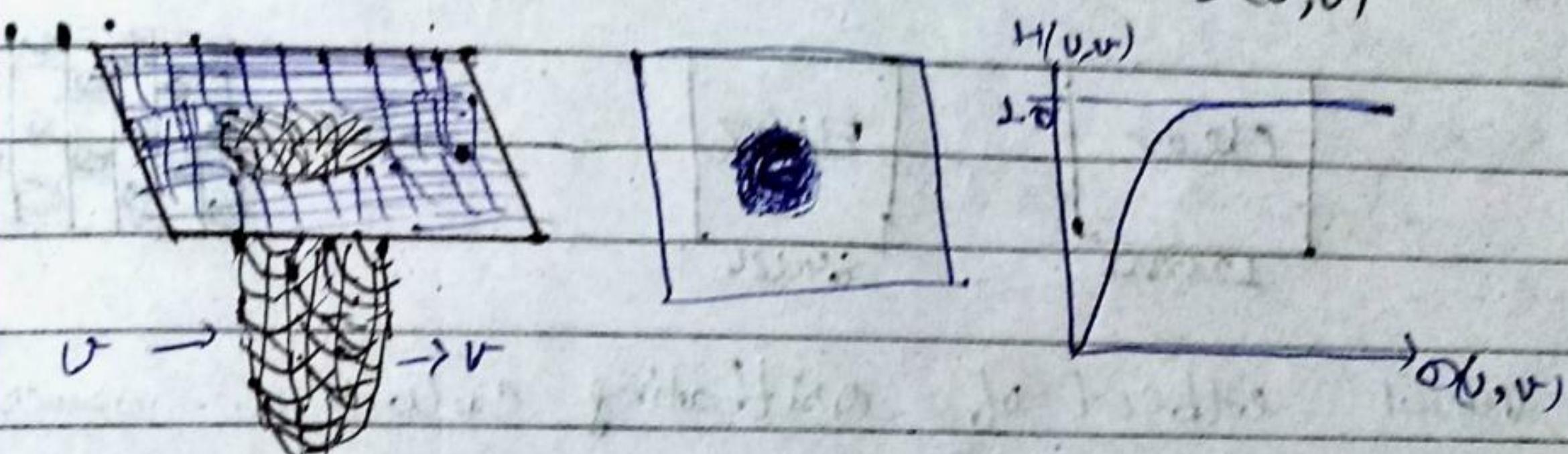


$D_0 = 10$
 $D_0 = 20$
 $D_0 = 40$
 $D_0 = 80$

(1) Ideal High-Low pass filters.



$$H(u, v) = \begin{cases} 0 & \text{if } D(u, v) \leq D_0 \\ 1 & \text{if } D(u, v) > D_0. \end{cases}$$



(2) Butterworth 'High' filter:-

$$H(u, v) = \frac{1}{1 + D^2 [D_0 / D(u, v)]^{2n}}$$

(3) Gaussian High filter:-

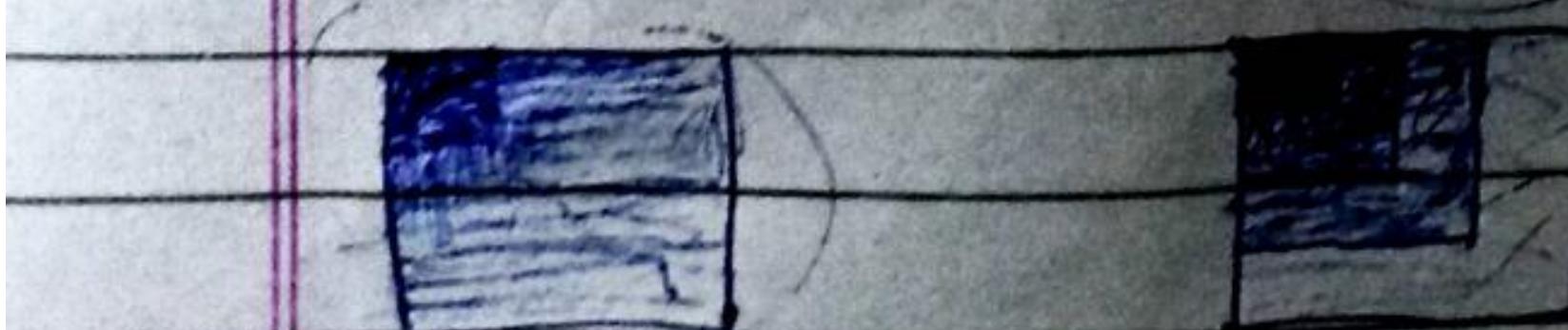
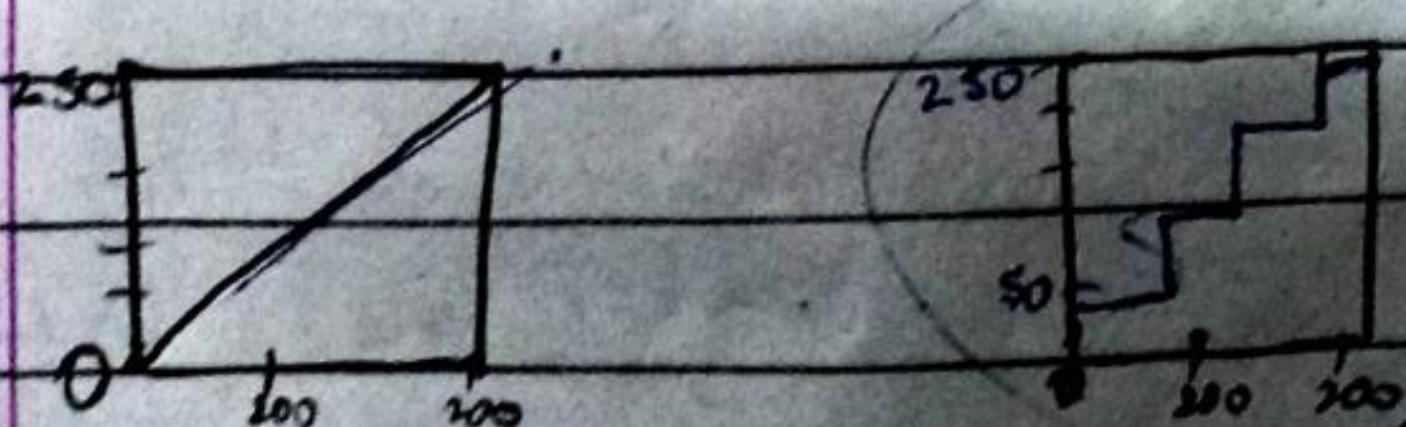
$$H(u, v) = f_{u,v} \cdot 1 - e^{-\sigma^2(u, v) / 2\sigma_0^2}$$

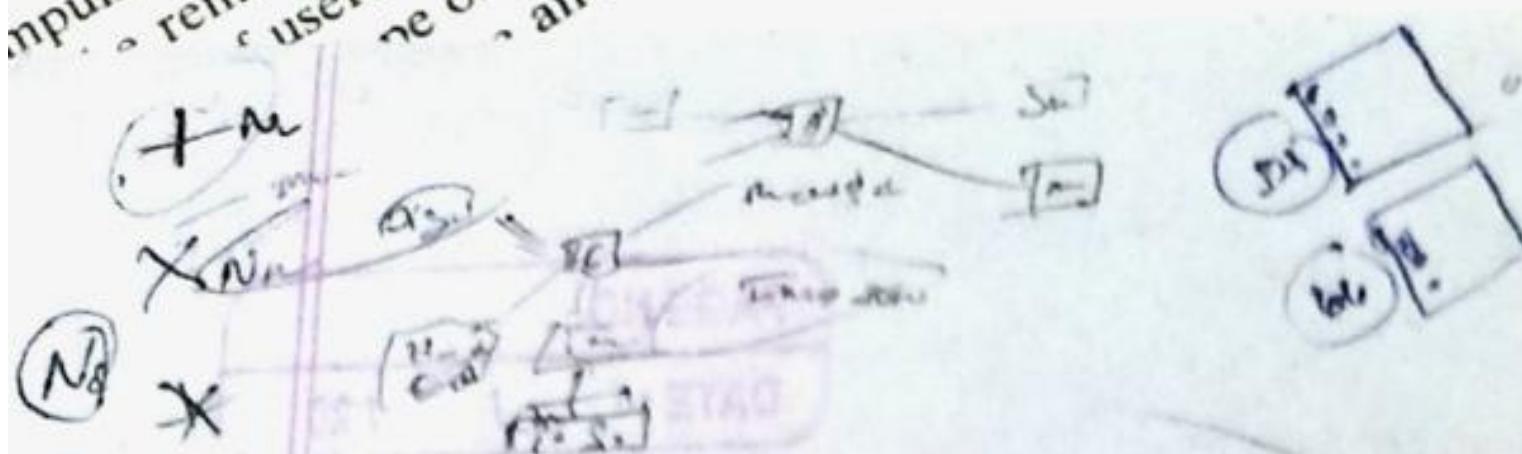
(a) 3

* False contouring:— Decreasing the gray-level resolution of a digital image may

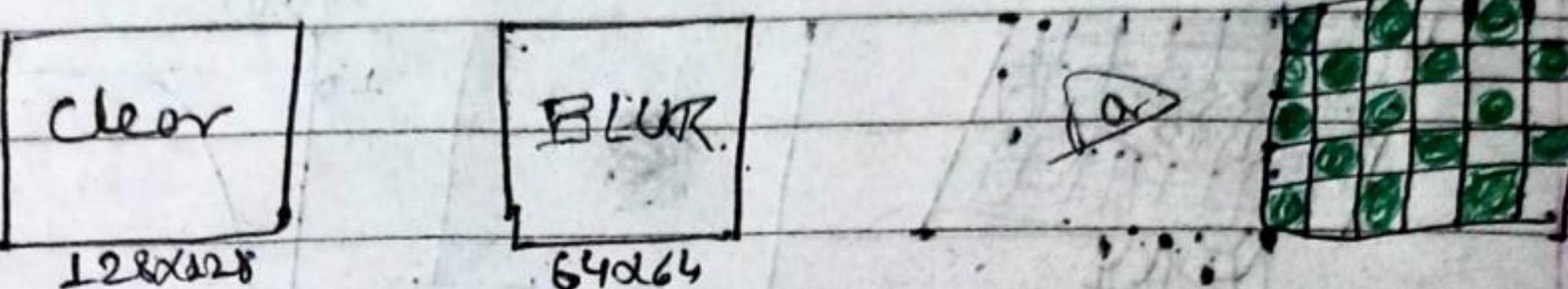
result in what is known as 'false contouring'

▷ This effect is caused by the use of the insufficient number of gray levels in smooth areas of a digital image.





② checkerboard effect. It caused by pixel replication, that is, lower resolution images were duplicated in order to fill the display area. This phenomenon can be visualized in the images shown below.



► The visual effect of oscillating colors or waves to produce a grid in the appearance of a chess or checkerboard.

③ Distance measure:

① Euclidean Distance

② city Block distance

③ chess - Board distance

By let $P = (x, y)$ $Q = (s, t)$ $\text{① } D_e = \sqrt{(x-s)^2 + (y-t)^2}$

AS

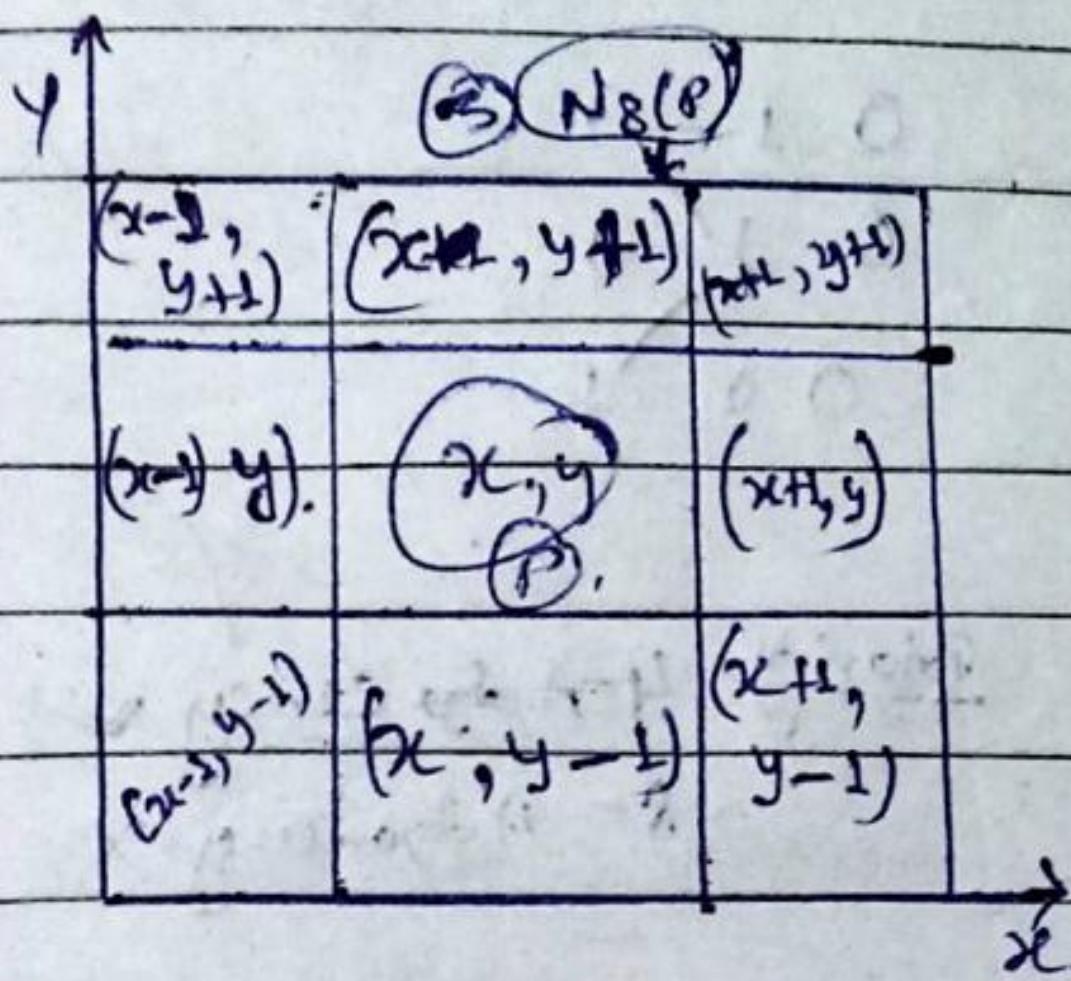
② city Block: $D_c = |x - s| + |y - t|$

③ chess - Board distance: - also known as $D_b(P, Q)$.

$D_b(P, Q) = \max(|x - s|, |y - t|)$



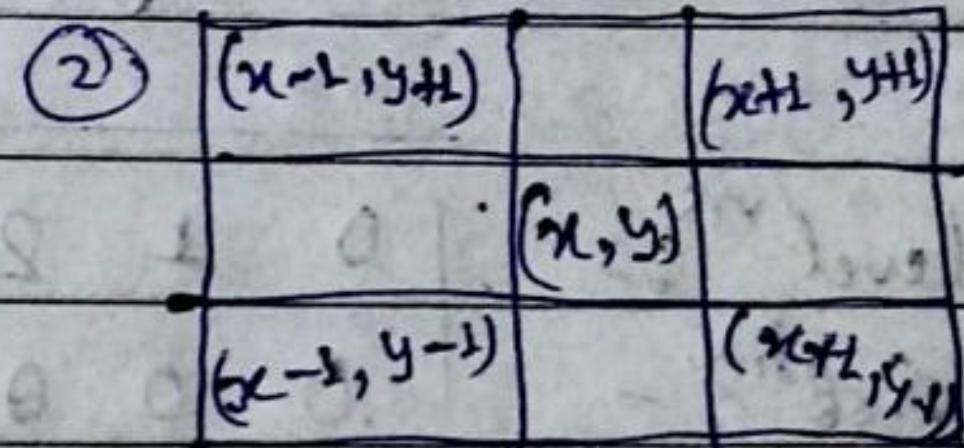
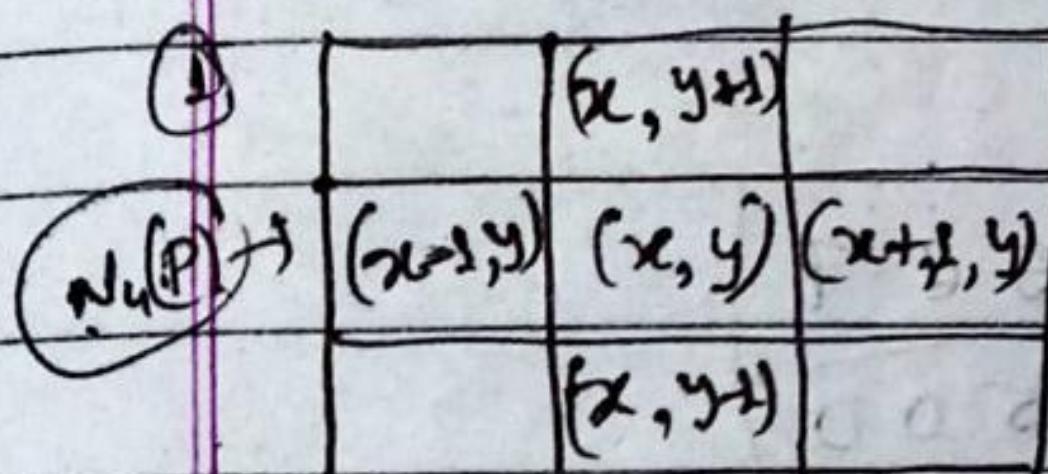
* Neighbourhood of Pixel :- Any Image can be represented as follow:-



① $N_4(p)$ 4-Neighbour :- Is set horizontal & vertical.

② $N_0(p)$:- The set of 4-diagonal neighbours.

③ $N_8(p)$ 8-neighbour :- Union of 4-Neig. & diag..



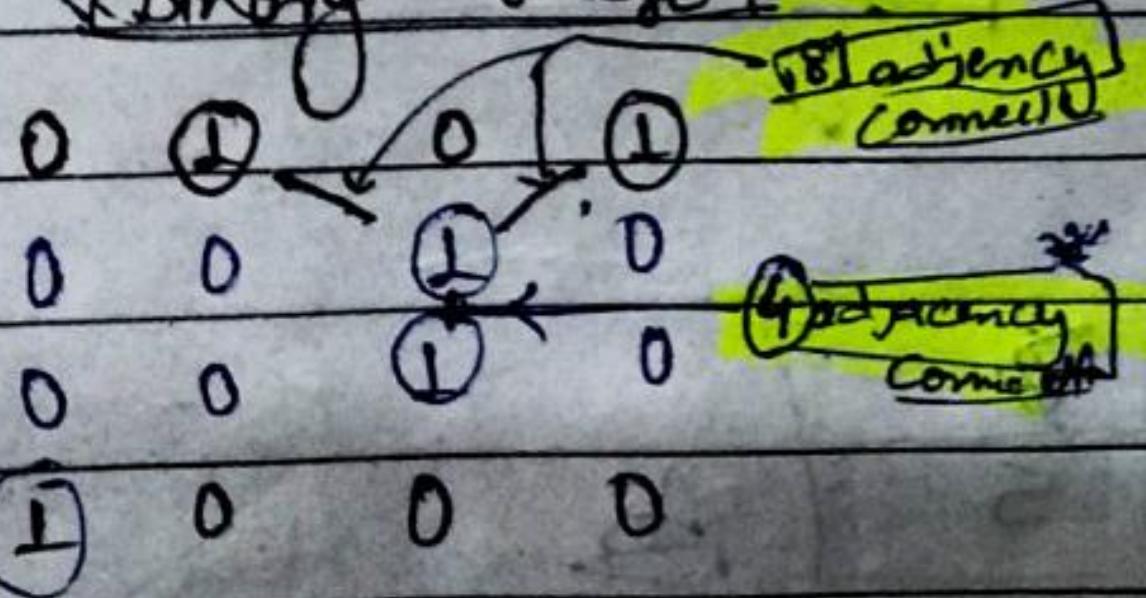
③ $N_8(p) = N_4(p) + N_0(p)$

$N_8(p)$

② Connectivity :- or Adjacency (Two pixels that are neighbours and have the same gray level are adjacent).

a) 4-adjacency

Binary image (**)

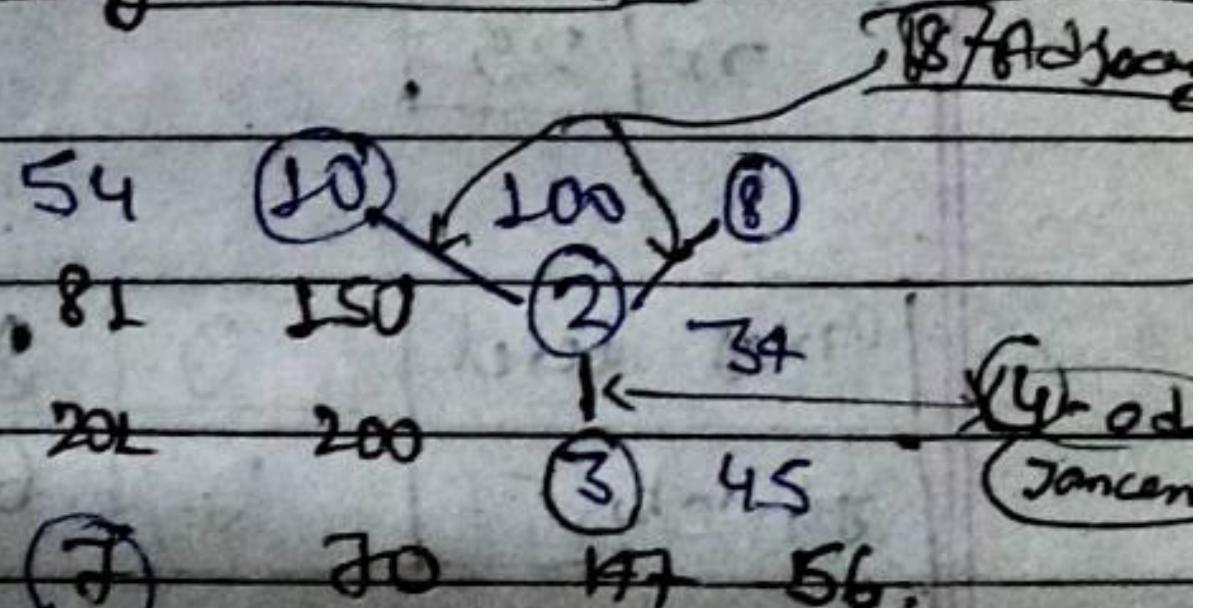


Not connected
Because
neighbours are zero.

$$V = \{1\}$$

b) 8-adjacency

Gray-scale image



Neighbour
not matching

$V = \{1, 2, 3, \dots, 10\}$
Only these can make connection.

② (C) Mixed (m) - Adjacency:-

$$V = \{1, 2\}$$

$$\begin{matrix} 0 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{matrix}$$

$$\begin{matrix} 0 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{matrix}$$

$$\begin{matrix} 0 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{matrix}$$

$$\begin{matrix} 0 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{matrix}$$

$$\begin{matrix} 0 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{matrix}$$

$$\begin{matrix} 0 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{matrix}$$

Priority 4-Adjacency ✓
8-Adjacency ✗

m - adjacency.

9.	Array level :-	0 1 2 3 4 5 6 7
9.	No. of pixels :-	0 0 0 6 14 5 0 0

SOL

η_L η_K	$N \cdot \eta$ n_K	$\frac{P_{DK}}{n_K}$	CDF η_K (%)	η_{K7}	Max error
0	0	0	0.0	0	0
1	0	0	0.0	0	0
2	0	0	0.0	0	0
3	6	0.24	0.24	1.68	2
4	14	0.56	0.80	4.5	
5	5	0.20	0.91	5.67	6.7
6	0	0	0.1	0.7	0.7
7	0	0	0.1	0.7	0.7

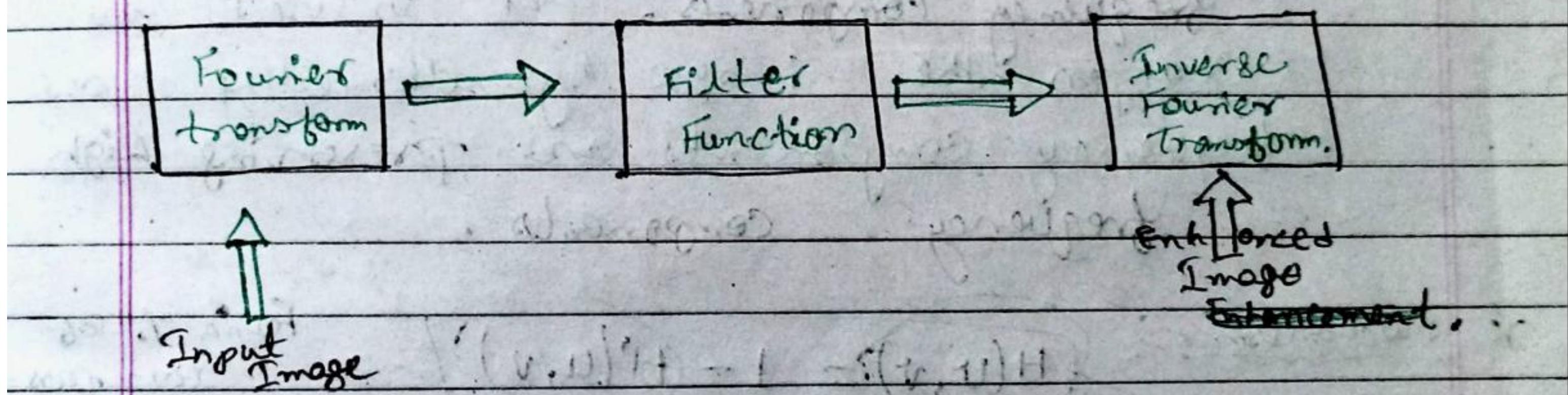
$n = 25$

Array level	0	2	6	7	/
Pixels	0	6	14	5	A.

Q(B) Explain with the Block diagram, the basic steps for image processing filtering in frequency domain.

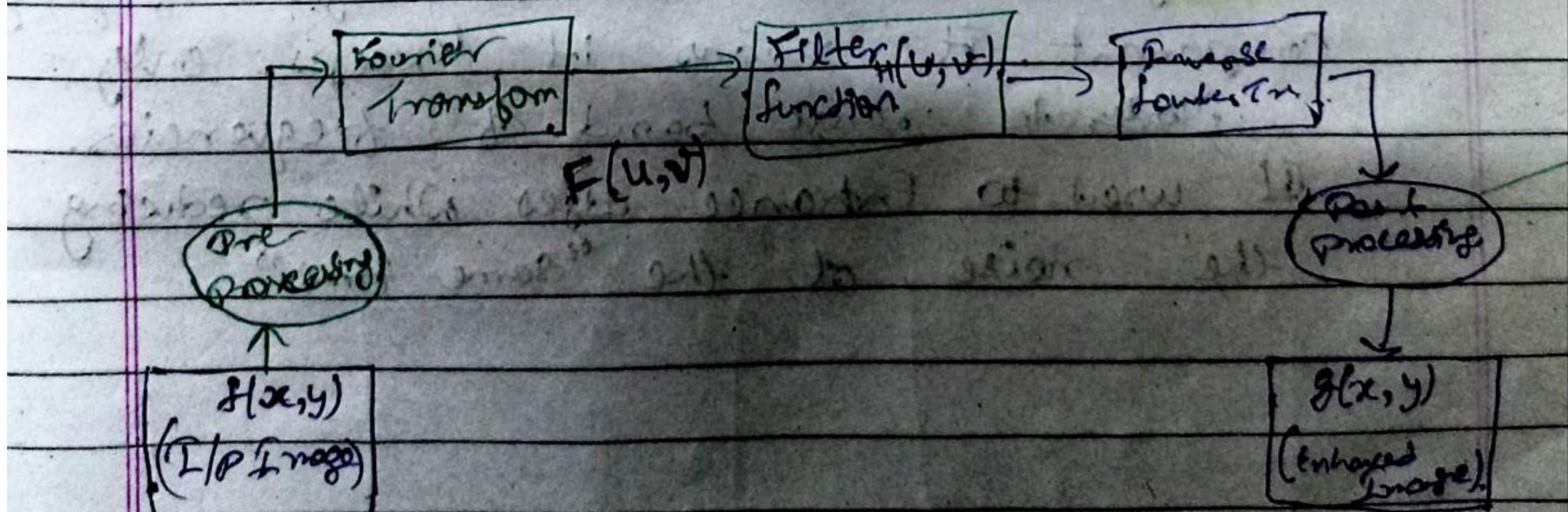
Qn Basic steps of frequency domain filtering.

The filtering in the spatial domain demands a filter mask (it also referred as kernel or convolution file). The filter mask is a matrix of odd usually size which is applied directly on the original data of the image.



* Frequency domain methods:-

- ① Filtering ② Homomorphic Filtering



Filters

PAGE NO.

DATE:

/ / 20

① Low pass filter :- It removes the high frequency component that means it keeps low frequency components. It is used to smoothing the image.

Mechanism:

$$G(u, v) = H(u, v) \cdot F(u, v)$$

F_{Tot}
Filtering mask

Fourier transform of
original image

② High pass filter :- It removes "low frequency" components that means it keeps high frequency components. "It is used to sharpen the image by attenuating low frequency components and preserving high frequency components."

Mechanism:-

$$H(u, v) = 1 - H'(u, v)$$

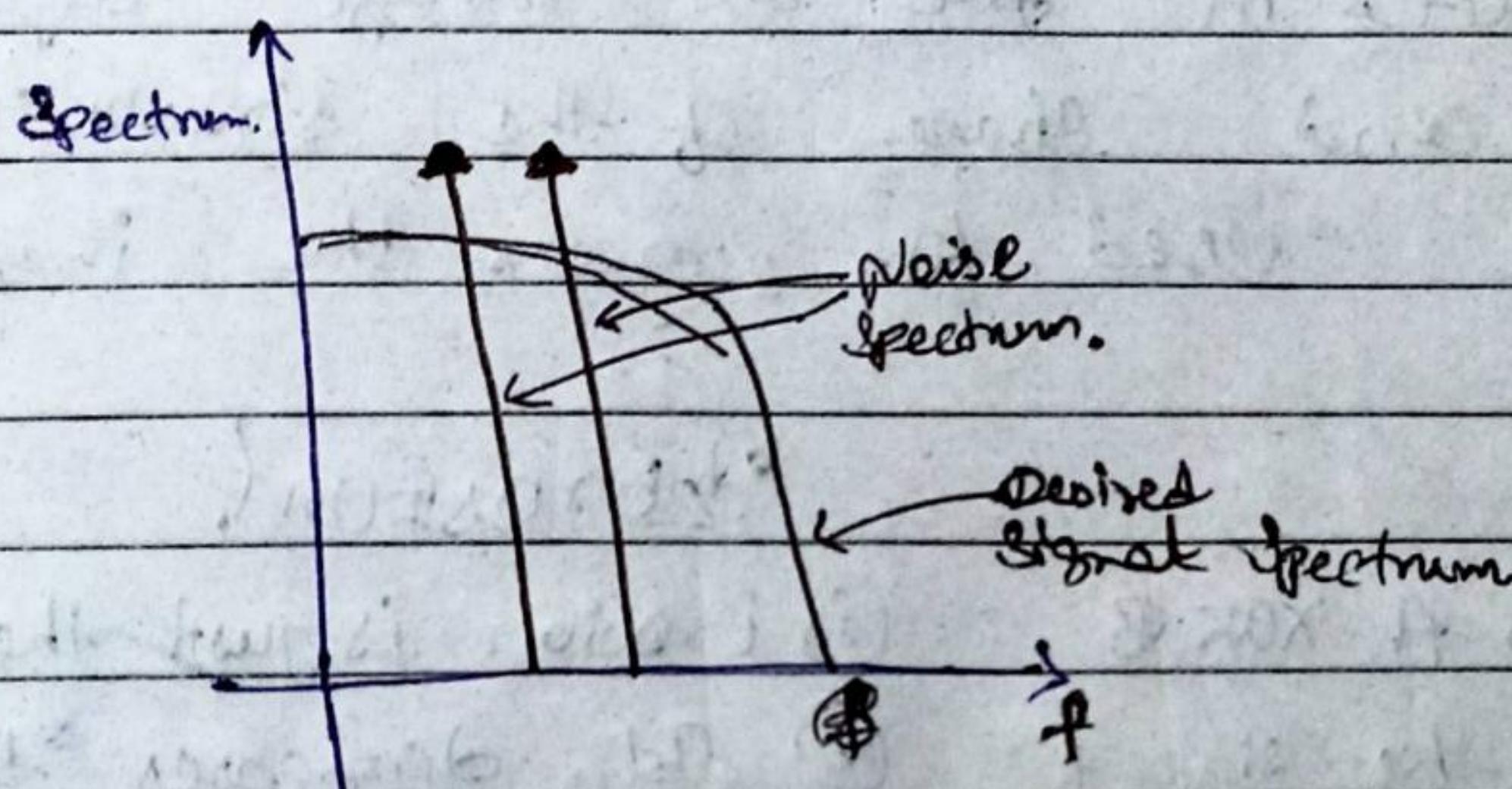
Fourier T. of
low pass fil.

Fourier T.
of High pass
filter.

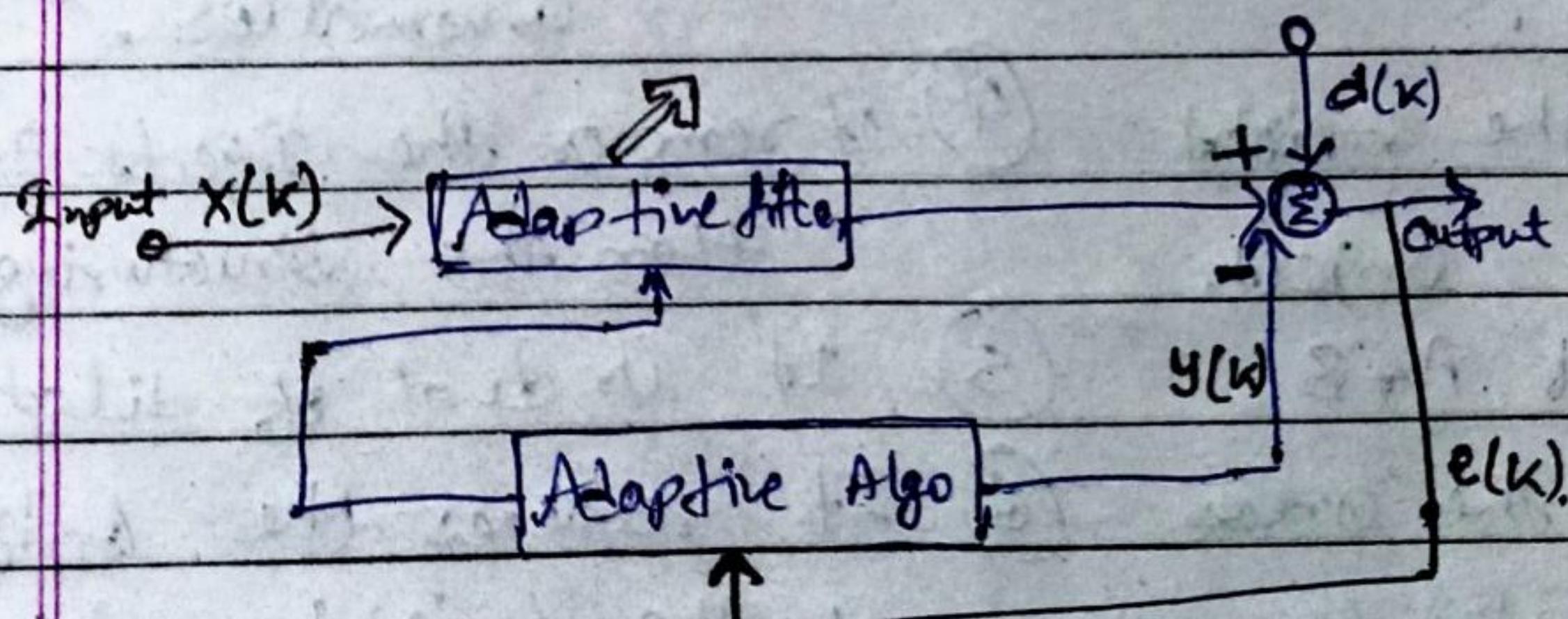
③ Band pass filter :- This removes the "very low" frequency component as well as "very high" frequency component. It means it keeps only moderate range band of frequencies. It uses to Enhance edges while reducing the noise at the "same time".

Explain adaptive filtering method of restoring images. List its Advantages

Adaptive filters are commonly used in image processing to enhance or restore data by removing noise without significantly blurring the structures in the image.



* Configuration of an Adaptive filter *



Both produced by structuring element (SE). Erosion & dilation.

PAGE NO.

DATE: / / 20

Q.6 Explain erosion and dilation operations used for morphological processing.

Ans. ① Dilation adds pixels to the boundaries of objects in an image, while; ② Erosion removes pixels from object boundaries. The no. of pixels added or removed from the objects in the image depends on the size and shape of the structuring element used for process the image.

Dilation

① Dilation is A $\oplus B$.

② It increases the size of the object.

③ It fills the holes of broken areas.

④ It increases the brightness of the object.

⑤ It is XOR of A $\oplus B$

⑥ It connects the areas that are separated by space smaller than SE.

⑦ It used prior in closing operation.

Erosion

① Erosion is just the dual of dilation.

② It decreases the size of the objects.

③ It removes the small anomalies.

④ It removes the objects smaller than the structuring elements.

⑤ It is dual of dilation.

⑥ It reduces the brightness of the bright object.

⑦ It used later in closing operation.

Dilation
(of Binary)

1	0	1	0	0
0	1	0	0	0
0	0	1	0	0
0	0	0	1	0
0	0	0	0	1

It takes only from D4 neighbours.

I/O Image

1	1
1	0
0	0
0	0
0	0

O/p Image

Morphological
Erosion (of a Gray Scale
Image)

PAGE NO. _____
DATE: / / 20

15	17	19	17
53	57	61	62
126	128	129	128
132	130		
140	138		

H/Img.

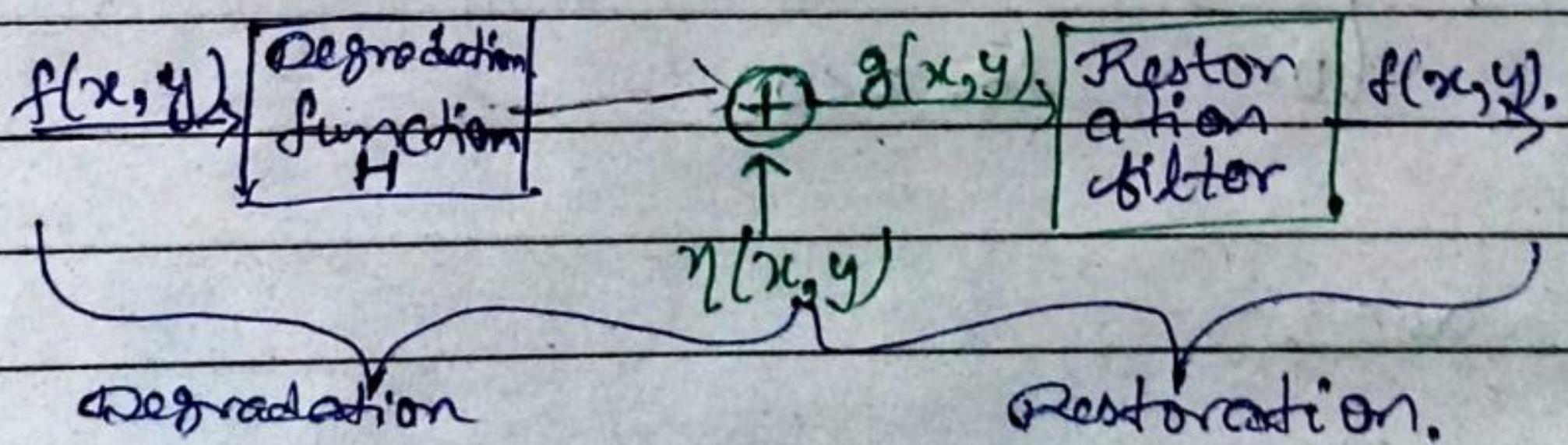
16	16
57	
128	
132	
140	

O/Img.

Q.6 Explain Basic model of Image restoration process

Ans Explain any four important noise probability density function

Sol Image restoration is the process of recovering an image that has been degraded by some knowledge of degradation function H & the additive noise term $\eta(x,y)$. In restoration Degradation is modelled and its inverse process is applied to recover the original image.



① Degraded image is given in spatial domain by:-

$$g(x,y) = h(x,y) * f(x,y) + \eta(x,y)$$

② Degraded image is given in frequency domain:-

$$G(u,v) = H(u,v)F(u,v) + N(u,v)$$

Some Important Noise Probability

PAGE NO. _____ DATE: / / 120

(1) Gaussian noise:-

$$P(z) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(z-\mu)^2/2\sigma^2}$$

(2) Ray-length noise:-

$$P(z) = \begin{cases} \frac{2}{b} (z-a) e^{-(z-a)^2/b} & \text{for } z \geq a \\ 0 & \text{for } z < a \end{cases}$$

$$\sigma^2 = \frac{b(4-\pi)}{9}$$

(3) Erlang (gamma) noise:-

$$P(z) = \begin{cases} \frac{\alpha^b z^{b-1}}{(b-1)!} e^{-\alpha z} & \text{for } z \geq 0 \\ 0 & \text{for } z < 0 \end{cases}$$

(4) Exponential noise:-

$$P(z) = \begin{cases} \alpha e^{-\alpha z} & \text{for } z \geq 0 \\ 0 & \text{for } z < 0 \end{cases}$$

(5) Uniform noise:-

$$P(z) = \begin{cases} \frac{1}{b-a} & \text{if } a \leq z \leq b \\ 0 & \text{otherwise} \end{cases}$$

(6) Impulse (salt-and-pepper) noise:-

$$P(z) = \begin{cases} P_a & \text{for } z=a \\ P_b & \text{for } z=b \\ 0 & \text{otherwise} \end{cases}$$

Types of restoration filters

- ① Inverse filter
- ② Pseudo Inverse filter
- ③ Wiener filter.

PAGE NO.

DATE: / / 20

(Q1)

Explain in brief, 2-D Fourier transform properties.

Soln

- Linearity → • Scaling → • Differentiation →
- Convolution → • Frequency shift → • Time shift.

(Q2)

Explain Wiener filtering in Image processing

Soln

Wiener filter (minimum mean square error filter). It executes and optimal trade off b/w filtering and noise smoothing. It removes the additional noise and inputs in the blurring simultaneously. Wiener filter is real and even. It minimizes the overall mean square error by -

$$\boxed{e^2 = F \{(f-f')^2\}} ; \quad \begin{cases} f = \text{original Img.} \\ f' = \text{restored Img.} \end{cases} \quad E\{.\} \rightarrow \text{mean value of quantity.}$$

$$\boxed{H(u,v) = H^*(u,v) / (|H(u,v)|^2 + (S_n(u,v) / S_f(u,v)))}$$

* No blur only additive noise:-

$$\Rightarrow \boxed{W(u,v) = 1 / (1 + S_n(u,v) / S_f(u,v))} ; \quad \boxed{W(u,v) = SNR / (1 + SNR)}$$

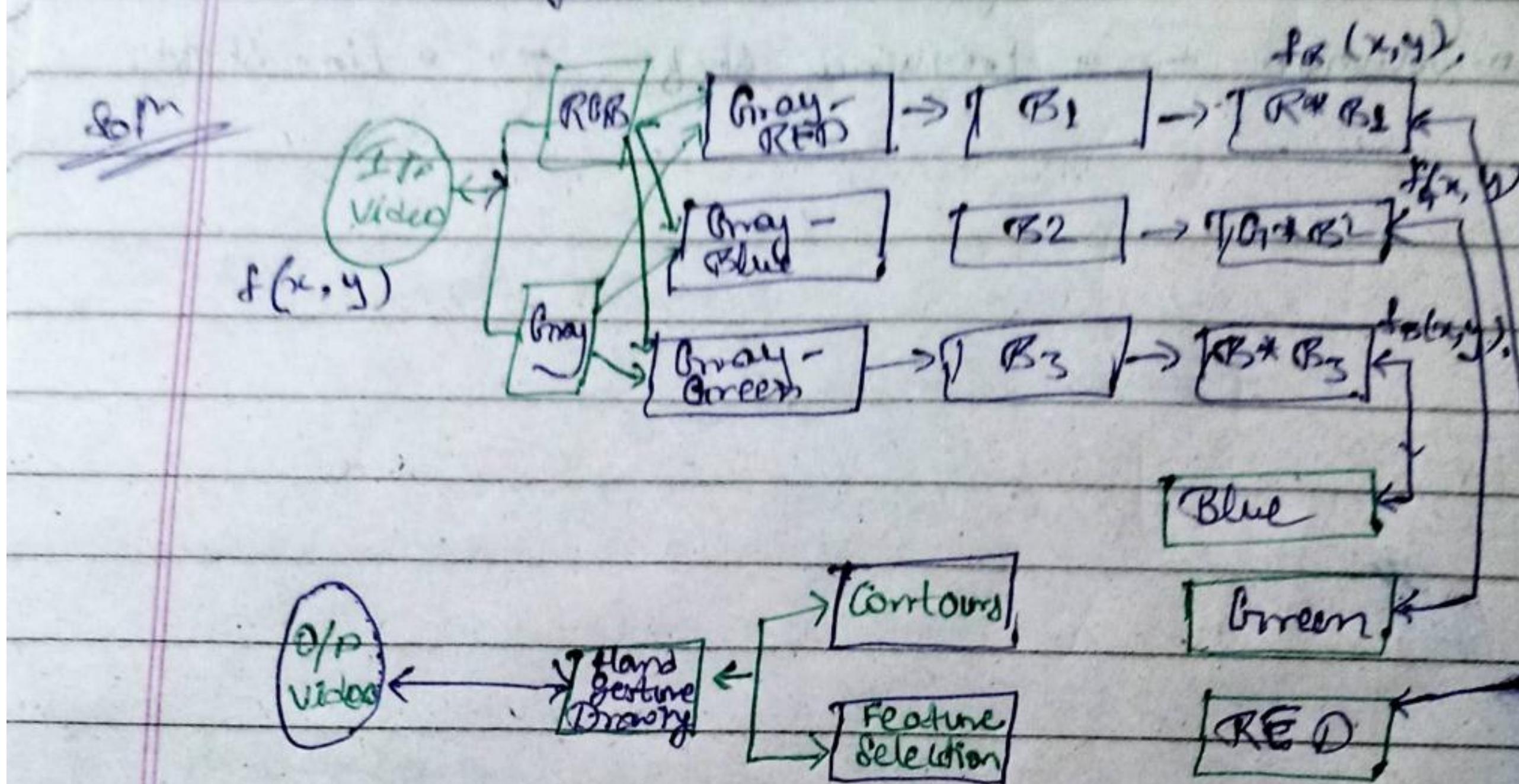
$$\boxed{SNR = S_f(u,v) / S_n(u,v)}$$

* No noise only blur:-

$$\boxed{S_n(u,v) = 0}$$

$$\boxed{W(u,v) = 1 / H(u,v)}$$

(Q) Draw Block diag. for converting gray level intensity to color transform and explain it.



Expln:-

Expln:-

Expln:-

Question:- Write short notes:-

(8)

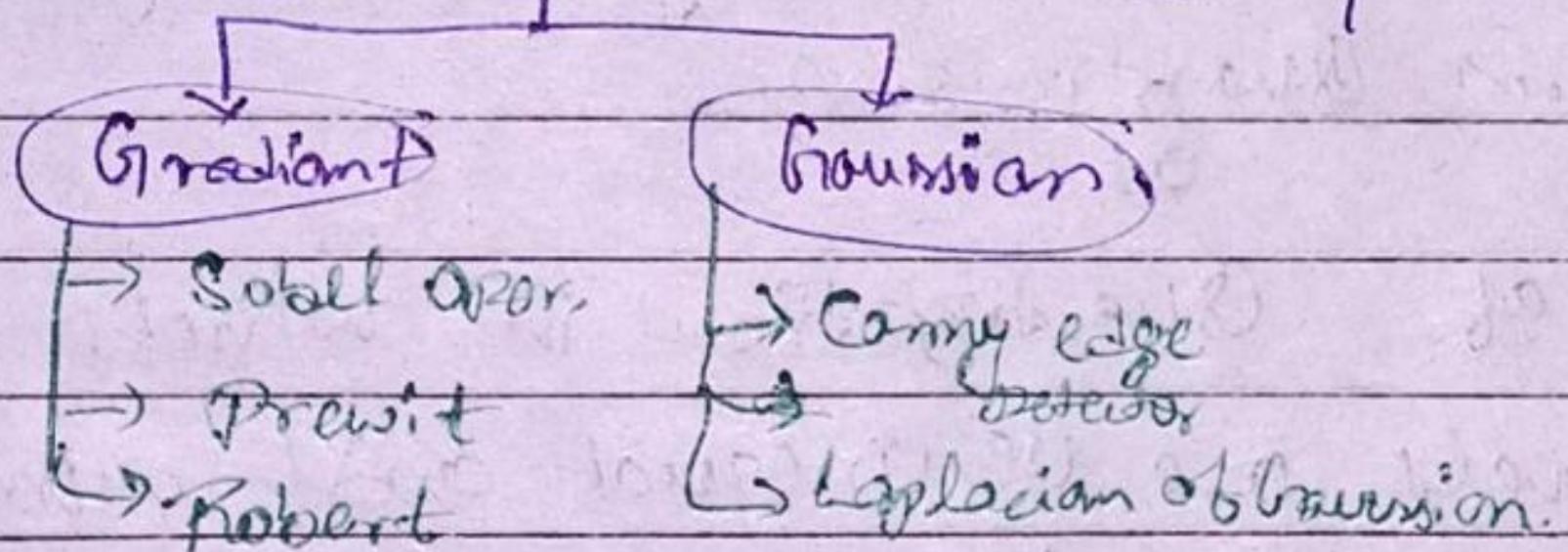
- (1) Uniform and non-uniform Quantization.
- (2) Perspective projection.
- (3) Band pass filter.
- (4) Edge linking (5) Boundary detection.

(6) Edge linking :- It process takes an Unordered set of edge pixels produced by an edge detector as an input to form an ordered list of edges.

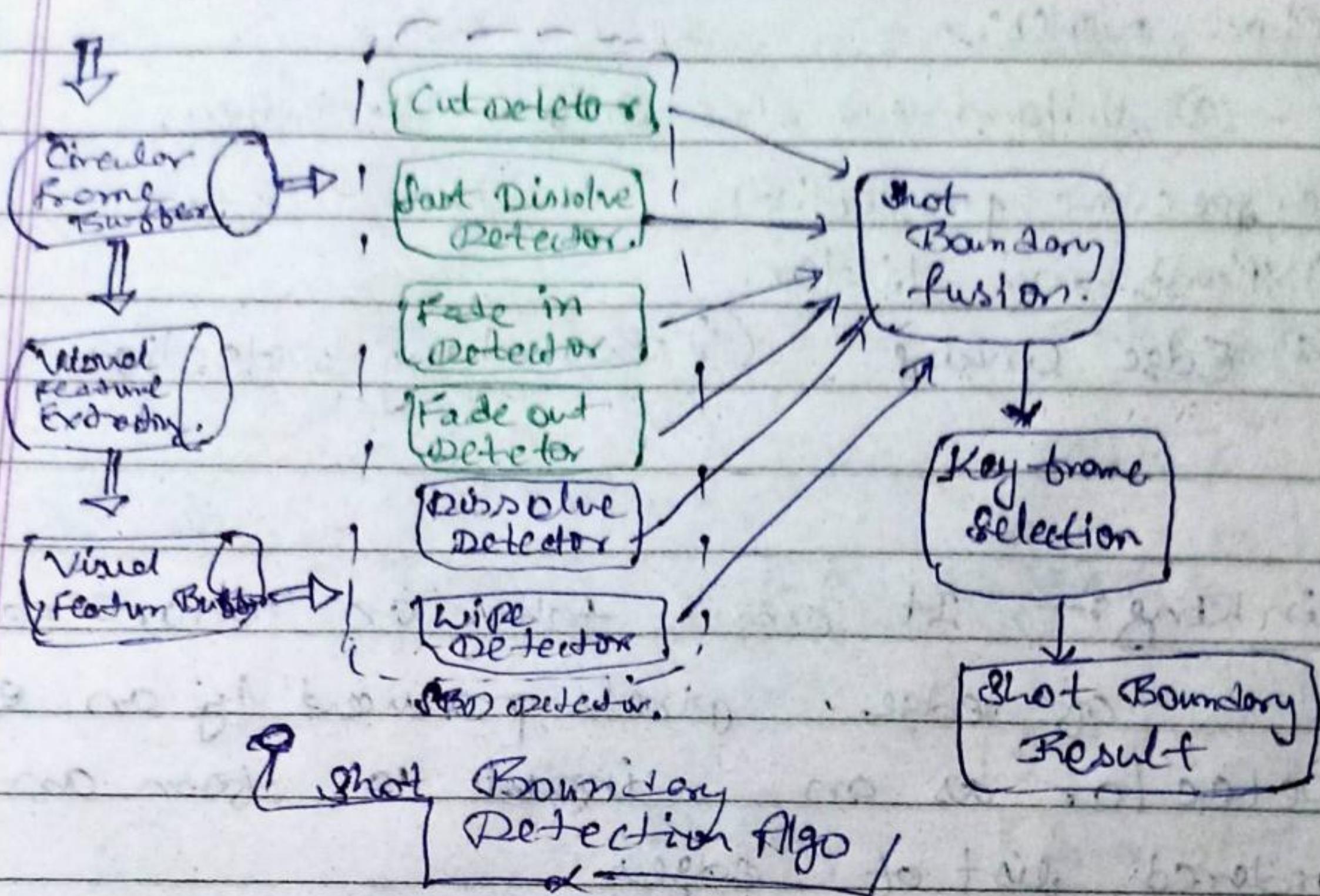
* Three types of edge :- • Horizontal • vertical • Diagonal

* Edge detection :- • pattern • Image • Feature extraction.

Edge Detection operators :- (1) Gradient (2) Gaussian.



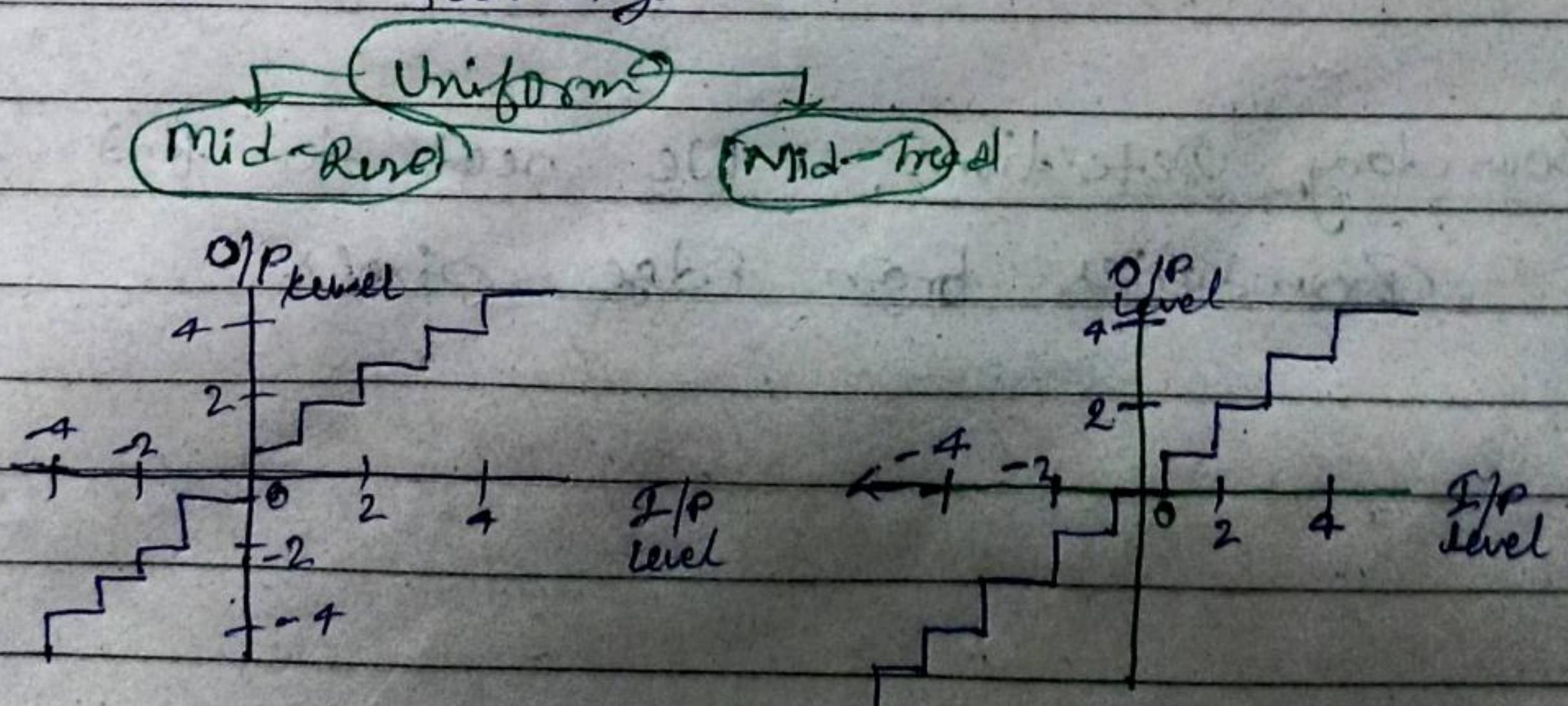
(5) Boundary Detection :- We need to find object boundaries from Edge pixels.



① Uniform & Non-Uniform Quantization:

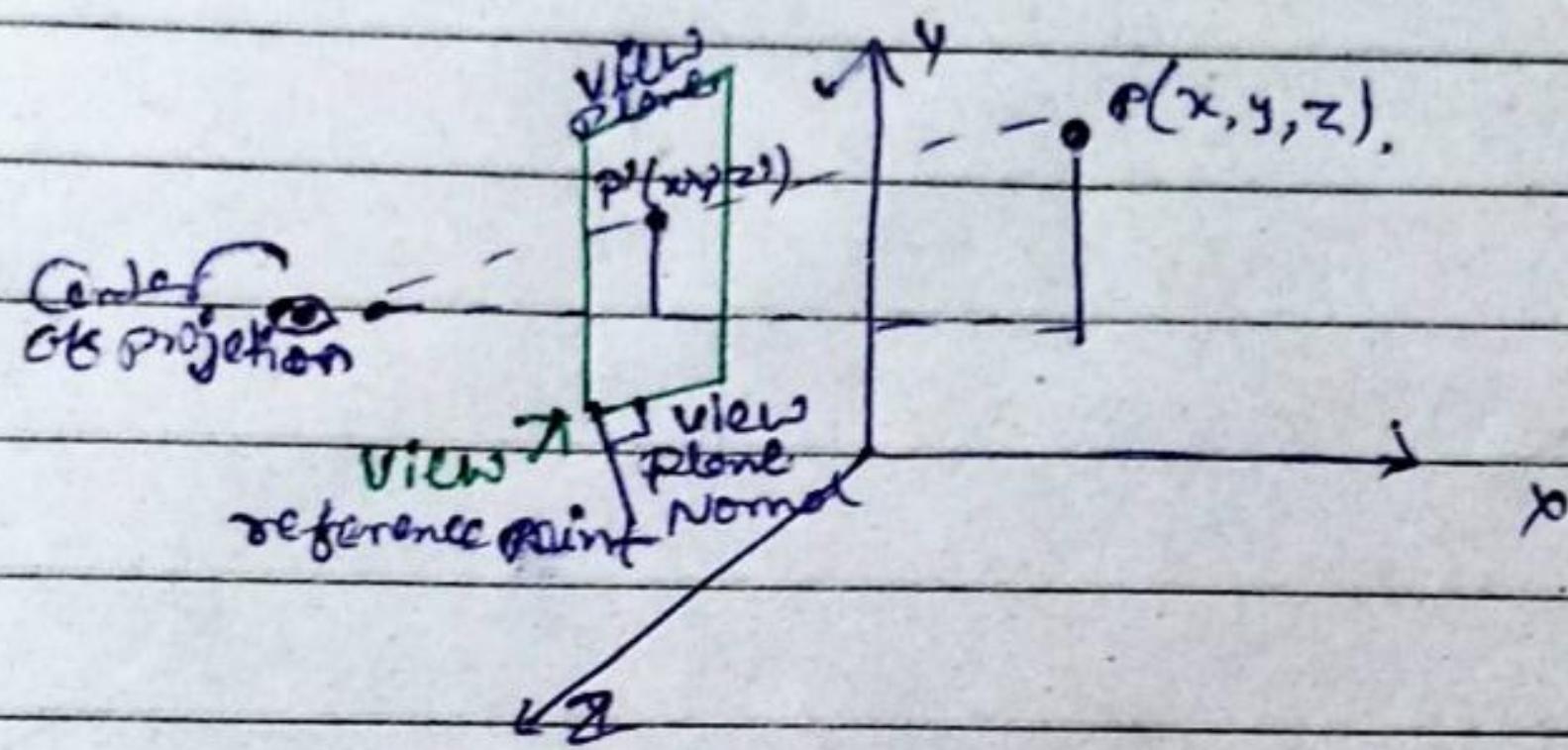
Sol The type of quantization in which the quantization levels are uniformly spaced is termed as a Uniform Quantization.

The type of quantization in which the quantization levels are unequal and mostly the relation b/w them is logarithmic, is termed as a Non-Uniform Quantization.



(3)

Perspective Projection:- the center of projection is at infinite distance from projection plane. The projection produces realistic views but doesn't preserve relative proportions of an object dimension.

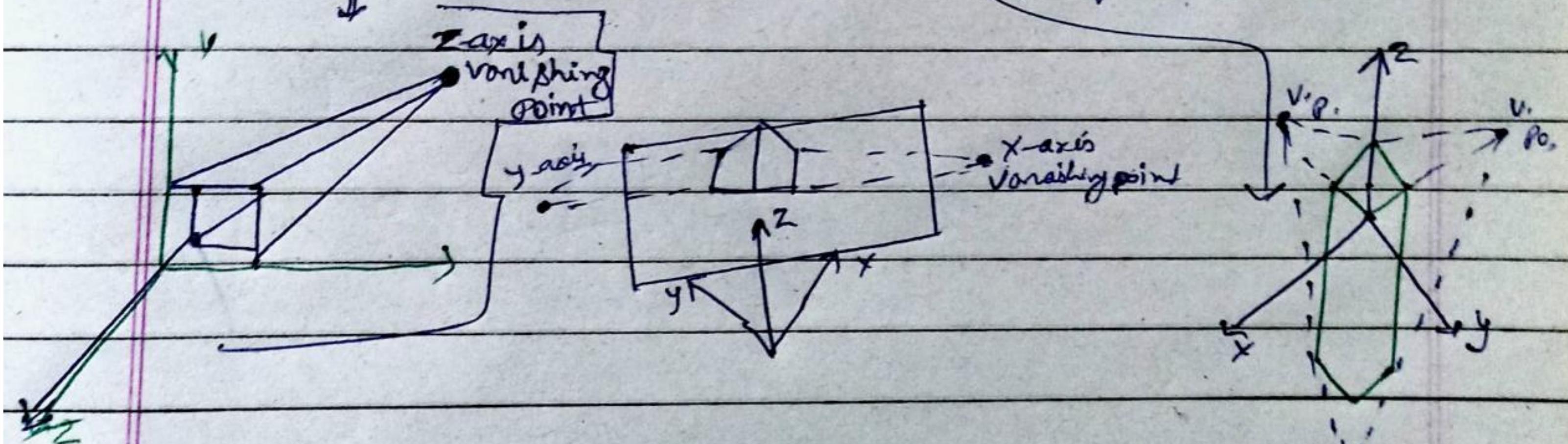


* Types of Perspective projection *

One-point perspective

Two-point perspective

Three-point perspective



* Application:- The technique is used by artist in preparing drawing of three (3-D) Dim. objects & scene.