

1. Discuss the importance of visualizing the solutions of the N-Queens Problem to understand the placement of queens better. Use a graphical representation to show how queens are placed on the board for different values of N. Explain how visual tools can help in debugging the algorithm and gaining insights into the problem's complexity. Provide examples of visual representations for N = 4, N = 5, and N = 8, showing different valid solutions.
 - a. Visualization for 4-Queens:
 Input: N = 4
 Output:
 Explanation: Each 'Q' represents a queen, and '.' represents an empty space.
 - b. Visualization for 5-Queens:
 Input: N = 5
 Output:
 - c. Visualization for 8-Queens:
 Input: N = 8
 Output:

```

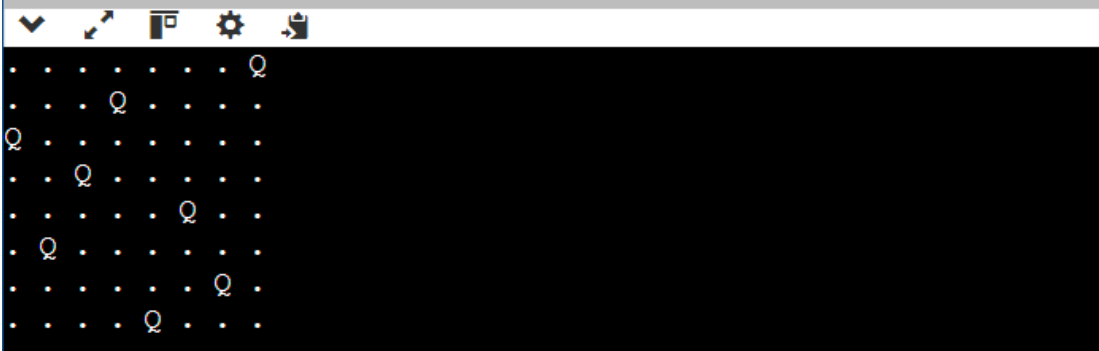
1 def print_board(board):
2     for row in board:
3         print(" ".join(row))
4     print()
5 def solve_n_queens(n):
6     def is_safe(board, row, col):
7         for i in range(row):
8             if board[i][col] == 'Q':
9                 return False
10            if col - (row - i) >= 0 and board[i][col - (row - i)] == 'Q':
11                return False
12            if col + (row - i) < n and board[i][col + (row - i)] == 'Q':
13                return False
14        return True
15    def solve(board, row):
16        if row == n:
17            print_board(board)
18            return
19        for col in range(n):
20            if is_safe(board, row, col):
21                board[row][col] = 'Q'
22                solve(board, row + 1)
23                board[row][col] = '.'
24    board = [['.' for _ in range(n)] for _ in range(n)]
25    solve(board, 0)
26    print("N = 4:")
27    solve_n_queens(4)
28    print("N = 5:")
29    solve_n_queens(5)
30    print("N = 8:")
31    solve_n_queens(8)

```

```

18         return
19     for col in range(n):
20         if is_safe(board, row, col):
21             board[row][col] = 'Q'
22             solve(board, row + 1)
23             board[row][col] = '.'
24     board = [['.' for _ in range(n)] for _ in range(n)]
25     solve(board, 0)
26     print("N = 4:")
27     solve_n_queens(4)
28     print("N = 5:")
29     solve_n_queens(5)
30     print("N = 8:")
31     solve_n_queens(8)
32

```



2. Discuss the generalization of the N-Queens Problem to other board sizes and shapes, such as rectangular boards or boards with obstacles. Explain how the algorithm can be adapted to handle these variations and the additional constraints they introduce. Provide examples of solving generalized N-Queens Problems for different board configurations, such as an 8×10 board, a 5×5 board with obstacles, and a 6×6 board with restricted positions.
 - a. 8×10 Board:
 - 8 rows and 10 columns
 - Output: Possible solution [1, 3, 5, 7, 9, 2, 4, 6]
 - Explanation: Adapt the algorithm to place 8 queens on an 8×10 board, ensuring no two queens threaten each other.
 - b. 5×5 Board with Obstacles:
 - Input: $N = 5$, Obstacles at positions [(2, 2), (4, 4)]
 - Output: Possible solution [1, 3, 5, 2, 4]
 - Explanation: Modify the algorithm to avoid placing queens on obstacle positions, ensuring a valid solution that respects the constraints.
 - c. 6×6 Board with Restricted Positions:
 - Input: $N = 6$, Restricted positions at columns 2 and 4 for the first queen
 - Output: Possible solution [1, 3, 5, 2, 4, 6]
 - Explanation: Adjust the algorithm to handle restricted positions, ensuring the queens are placed without conflicts and within allowed columns.

```

1 def is_safe(board, row, col):
2     for i in range(row):
3         if board[i] == col or \
4             board[i] - i == col - row or \
5             board[i] + i == col + row:
6             return False
7     return True
8 def solve_n_queens(n, board=None, row=0):
9     if board is None:
10        board = [-1] * n
11    if row == n:
12        return [board.copy()]
13    solutions = []
14    for col in range(n):
15        if is_safe(board, row, col):
16            board[row] = col
17            solutions += solve_n_queens(n, board, row + 1)
18            board[row] = -1
19    return solutions
20 def solve_8x10():
21     n = 8
22     board = [0] * n
23     solutions = []
24     for col in range(10):
25         if is_safe(board, 0, col):
26             board[0] = col
27             solutions += solve_n_queens(n, board, 1)
28             board[0] = -1
29     return solutions
30 def solve_5x5_with_obstacles(obstacles):
31     n = 5
32     board = [-1] * n
33     solutions = []
34     def is_safe_with_obstacles(board, row, col):
35         if (row, col) in obstacles:
36             return False
37         return is_safe(board, row, col)

```

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```

38 def solve_with_obstacles(n, board=None, row=0):
39     if board is None:
40         board = [-1] * n
41     if row == n:
42         return [board.copy()]
43     solutions = []
44     for col in range(n):
45         if is_safe_with_obstacles(board, row, col):
46             board[row] = col
47             solutions += solve_with_obstacles(n, board, row + 1)
48             board[row] = -1
49     return solutions
50 return solve_with_obstacles(n, board)
51 def solve_6x6_with_restricted_positions(restricted):
52     n = 6
53     board = [-1] * n
54     solutions = []
55     def is_safe_with_restrictions(board, row, col):
56         if col in restricted:
57             return False
58         return is_safe(board, row, col)
59     def solve_with_restrictions(n, board=None, row=0):
60         if board is None:
61             board = [-1] * n
62         if row == n:
63             return [board.copy()]
64         solutions = []
65         for col in range(n):
66             if is_safe_with_restrictions(board, row, col):
67                 board[row] = col
68                 solutions += solve_with_restrictions(n, board, row + 1)
69                 board[row] = -1
70         return solutions
71     return solve_with_restrictions(n, board)
72 print("8x10 Board Solutions:", solve_8x10())
73 print("5x5 Board with Obstacles Solutions:", solve_5x5_with_obstacles([(2, 2), (4, 4)]))
74 print("6x6 Board with Restricted Positions Solutions:", solve_6x6_with_restricted_positions([2, 4]))

```

```

52 n = 6
53 board = [-1] * n
54 solutions = []
55 def is_safe_with_restrictions(board, row, col):
56     if col in restricted:
57         return False
58     return is_safe(board, row, col)
59 def solve_with_restrictions(n, board=None, row=0):
60     if board is None:

```

input

```

4, 7, 0, 2, 5], [9, 3, 1, 7, 2, 0, 6, 4], [9, 3, 1, 7, 4, 2, 0, 5], [9, 3, 1, 7, 4, 6, 0, 5], [9, 3, 5, 7, 2, 0, 6, 1], [9, 3, 5, 7, 2,
0, 6, 4], [9, 3, 6, 2, 7, 1, 4, 0], [9, 3, 6, 4, 2, 0, 5, 7], [9, 4, 0, 3, 6, 2, 5, 1], [9, 4, 0, 3, 6, 2, 7, 1], [9, 4, 1, 3, 0, 2, 7, 5
], [9, 4, 1, 3, 6, 2, 7, 5], [9, 4, 2, 0, 3, 1, 7, 5], [9, 4, 2, 0, 6, 1, 7, 5], [9, 4, 2, 7, 3, 6, 0, 5], [9, 4, 6, 0, 2, 7, 1, 3], [9,
4, 6, 0, 2, 7, 5, 3], [9, 4, 6, 0, 3, 1, 7, 5], [9, 4, 6, 3, 0, 2, 7, 5], [9, 5, 0, 2, 4, 6, 1, 3], [9, 5, 0, 2, 4, 7, 1, 3], [9, 5, 0, 4
, 1, 7, 2, 6], [9, 5, 1, 4, 6, 0, 2, 7], [9, 5, 1, 4, 7, 0, 6, 3], [9, 5, 2, 0, 3, 6, 4, 1], [9, 5, 2, 0, 3, 7, 4, 1], [9, 5, 2, 0, 7, 3,
1, 6], [9, 5, 3, 0, 4, 7, 1, 6], [9, 6, 1, 3, 7, 0, 2, 5], [9, 6, 1, 5, 2, 0, 7, 3], [9, 6, 1, 5, 2, 0, 7, 4], [9, 6, 3, 0, 2, 7, 5, 1],
[9, 6, 4, 2, 0, 5, 7, 1], [9, 7, 1, 4, 2, 0, 6, 3], [9, 7, 3, 0, 2, 5, 1, 6], [9, 7, 4, 2, 0, 6, 1, 5]]
5x5 Board with Obstacles Solutions: [[0, 2, 4, 1, 3], [0, 3, 1, 4, 2], [2, 4, 1, 3, 0], [3, 1, 4, 2, 0], [4, 1, 3, 0, 2], [4, 2, 0, 3, 1]
]
6x6 Board with Restricted Positions Solutions: []

```

3. Write a program to solve a Sudoku puzzle by filling the empty cells. A sudoku solution must satisfy all of the following rules: Each of the digits 1-9 must occur exactly once in each row. Each of the digits 1-9 must occur exactly once in each column. Each of the digits 1-9 must occur exactly once in each of the 9 3x3 sub-boxes of the grid. The '.' character indicates empty cells.

Example 1:

Input: board =

```
[["5","3",".", ".", ".", "7", ".", ".", ".", "."],
["6",".", ".", ".", "1","9","5",".", ".", "."],
```

```
[["9","8",".", ".", ".", ".", ".", "6","."],
["8",".", ".", ".", "6",".", ".", ".", "3"],
["4",".", ".", "8",".", "3",".", ".", "1"],
["7",".", ".", "2",".", ".", ".", "6"],
[["6",".", ".", ".", "2","8","."],
[["4","1","9",".", "5"],
[["8",".", "7","9"]]
```

Output:

```
[["5","3","4","6","7","8","9","1","2"],
["6","7","2","1","9","5","3","4","8"],
["1","9","8","3","4","2","5","6","7"],
["8","5","9","7","6","1","4","2","3"],
["4","2","6","8","5","3","7","9","1"],
["7","1","3","9","2","4","8","5","6"],
["9","6","1","5","3","7","2","8","4"],
["2","8","7","4","1","9","6","3","5"],
["3","4","5","2","8","6","1","7","9"]]
```

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```

1 def solve_sudoku(board):
2     def is_valid(board, row, col, num):
3         for i in range(9):
4             if board[row][i] == num or board[i][col] == num:
5                 return False
6             if board[3 * (row // 3) + i // 3][3 * (col // 3) + i % 3] == num:
7                 return False
8         return True
9     def solve(board):
10        for row in range(9):
11            for col in range(9):
12                if board[row][col] == '.':
13                    for num in map(str, range(1, 10)):
14                        if is_valid(board, row, col, num):
15                            board[row][col] = num
16                            if solve(board):
17                                return True
18                            board[row][col] = '.'
19                    return False
20        return True
21    solve(board)
22    board = [
23        ["5", "3", ".", ".", "7", ".", ".", ".", "."],
24        ["6", ".", ".", "1", "9", "5", ".", ".", "."],
25        [".", "9", "8", ".", ".", ".", ".", "6", "."],
26        ["8", ".", ".", "6", ".", ".", ".", "3", "."],
27        ["4", ".", ".", "8", ".", "3", ".", ".", "1"],
28        ["7", ".", ".", "2", ".", ".", ".", "6", "."],
29        [".", "6", ".", ".", "2", "8", ".", ".", "."],
30        [".", ".", "4", "1", "9", ".", ".", "5"],
31        [".", ".", ".", "8", ".", ".", "7", "9"]
32    solve_sudoku(board)
33    print(board)

```

```

11        for col in range(9):
12            if board[row][col] == '.':
13                for num in map(str, range(1, 10)):
14                    if is_valid(board, row, col, num):
15                        board[row][col] = num
16                        if solve(board):

```

input

```

[[('5', '3', '4', '6', '7', '8', '9', '1', '2'), ('6', '7', '2', '1', '9', '5', '3', '4', '8'), ('1', '9', '8', '3', '4', '2', '5', '6', '7'), ('8', '5', '9', '7', '6', '1', '4', '2', '3'), ('4', '2', '6', '8', '5', '3', '7', '9', '1'), ('7', '1', '3', '9', '2', '4', '8', '5', '6'), ('9', '6', '1', '5', '3', '7', '2', '8', '4'), ('2', '8', '7', '4', '1', '9', '6', '3', '5'), ('3', '4', '5', '2', '8', '6', '1', '7', '9')]]

```

4. Write a program to solve a Sudoku puzzle by filling the empty cells. A sudoku solution must satisfy all of the following rules: Each of the digits 1-9 must occur exactly once in each row. Each of the digits 1-9 must occur exactly once in each column. Each of the digits 1-9 must occur exactly once in each of the 9 3x3 sub-boxes of the grid. The '.' character indicates empty cells.

Example 1:

Input: board =

```
[["5","3",".", ".", "7", ".", ".", ".", "."],
 ["6",".", ".", "1","9","5",".", ".", "."],
 [".","9","8",".", ".", ".", ".", "6","."],
 ["8",".", ".", ".", "6",".", ".", ".", "3"],
 ["4",".", ".", "8",".", "3",".", ".", "1"],
 ["7",".", ".", "2",".", ".", ".", "6","."],
 [".","6",".", ".", ".", "2","8",".", "."],
 [".",".", "4","1","9",".", ".", "5"],
 [".",".", "8",".", ".", "7","9"]]
```

Output:

```
[["5","3","4","6","7","8","9","1","2"],
 ["6","7","2","1","9","5","3","4","8"],
 ["1","9","8","3","4","2","5","6","7"],
 ["8","5","9","7","6","1","4","2","3"],
 ["4","2","6","8","5","3","7","9","1"],
 ["7","1","3","9","2","4","8","5","6"],
 ["9","6","1","5","3","7","2","8","4"],
 ["2","8","7","4","1","9","6","3","5"],
 ["3","4","5","2","8","6","1","7","9"]]
```

```
1 def solve_sudoku(board):
2     def is_valid(board, row, col, num):
3         for i in range(9):
4             if board[row][i] == num or board[i][col] == num:
5                 return False
6             if board[3 * (row // 3) + i // 3][3 * (col // 3) + i % 3] == num:
7                 return False
8         return True
9
10    def solve(board):
11        for row in range(9):
12            for col in range(9):
13                if board[row][col] == '.':
14                    for num in map(str, range(1, 10)):
15                        if is_valid(board, row, col, num):
16                            board[row][col] = num
17                            if solve(board):
18                                return True
19                            board[row][col] = '.'
20        return False
21    return True
22
23 solve(board)
24 board = [
25     ["5","3",".", ".", "7", ".", ".", ".", "."],
26     ["6",".", ".", "1","9","5",".", ".", "."],
27     [".","9","8",".", ".", ".", ".", "6","."],
28     ["8",".", ".", ".", "6",".", ".", ".", "3"],
29     ["4",".", ".", "8",".", "3",".", ".", "1"],
30     ["7",".", ".", "2",".", ".", ".", "6","."],
31     [".","6",".", ".", ".", "2","8",".", "."],
32     [".",".", "4","1","9",".", ".", "5"],
33     [".",".", "8",".", ".", "7","9"]
34 ]
35 solve_sudoku(board)
36 print(board)
```

input

```
[['5', '3', '4', '6', '7', '8', '9', '1', '2'], ['6', '7', '2', '1', '9', '5', '3', '4', '8'], ['1', '9', '8', '3', '4', '2', '5', '6', '7'],
 ['8', '5', '9', '7', '6', '1', '4', '2', '3'], ['4', '2', '6', '8', '5', '3', '7', '9', '1'], ['7', '1', '3', '9', '2', '4', '8', '5', '6'],
 ['9', '6', '1', '5', '3', '7', '2', '8', '4'], ['2', '8', '7', '4', '1', '9', '6', '3', '5'], ['3', '4', '5', '2', '8', '6', '1', '7', '9']]
```

5. You are given an integer array `nums` and an integer `target`. You want to build an expression out of `nums` by adding one of the symbols '+' and '-' before each integer in `nums` and then

concatenate all the integers. For example, if `nums = [2, 1]`, you can add a '+' before 2 and a '-' before 1 and concatenate them to build the expression "+2-1". Return the number of different expressions that you can build, which evaluates to `target`.

Example 1:

Input: `nums = [1,1,1,1,1]`, `target = 3`

Output: 5

Explanation: There are 5 ways to assign symbols to make the sum of `nums` be `target` 3.

-1 + 1 + 1 + 1 + 1 = 3

+1 - 1 + 1 + 1 + 1 = 3

+1 + 1 - 1 + 1 + 1 = 3

+1 + 1 + 1 - 1 + 1 = 3

+1 + 1 + 1 + 1 - 1 = 3

Example 2:

Input: `nums = [1]`, `target = 1`

Output: 1

```
1 def findTargetSumWays(nums, target):
2     from collections import defaultdict
3     def dfs(index, current_sum):
4         if index == len(nums):
5             return 1 if current_sum == target else 0
6             return dfs(index + 1, current_sum + nums[index]) + dfs(index + 1, current_sum - nums[index])
7         return dfs(0, 0)
8     print(findTargetSumWays([1, 1, 1, 1, 1], 3))
9     print(findTargetSumWays([1], 1))
10
11
12
```

5
1

6. Given an array of integers `arr`, find the sum of `min(b)`, where `b` ranges over every (contiguous) subarray of `arr`. Since the answer may be large, return the answer modulo `109 + 7`.

Example 1:

Input: `arr = [3,1,2,4]`

Output: 17

Explanation:

Subarrays are [3], [1], [2], [4], [3,1], [1,2], [2,4], [3,1,2], [1,2,4], [3,1,2,4].

Minimums are 3, 1, 2, 4, 1, 1, 2, 1, 1, 1.

Sum is 17.

Example 2:

Input: `arr = [11,81,94,43,3]`

Output: 444


```

1 def sum_of_min_subarrays(arr):
2     MOD = 10**9 + 7
3     n = len(arr)
4     total_sum = 0
5     stack = []
6
7     for i in range(n):
8         while stack and arr[stack[-1]] > arr[i]:
9             j = stack.pop()
10            k = stack[-1] if stack else -1
11            total_sum += arr[j] * (i - j) * (j - k) % MOD
12            total_sum %= MOD
13            stack.append(i)
14
15     while stack:
16         j = stack.pop()
17         k = stack[-1] if stack else -1
18         total_sum += arr[j] * (n - j) * (j - k) % MOD
19         total_sum %= MOD
20
21     return total_sum
22
23 print(sum_of_min_subarrays([3, 1, 2, 4]))
24 print(sum_of_min_subarrays([11, 81, 94, 43, 3]))
25

```

input

17
444

7. Given an array of distinct integers candidates and a target integer target, return a list of all unique combinations of candidates where the chosen numbers sum to target. You may return the combinations in any order. The same number may be chosen from candidates an unlimited number of times. Two combinations are unique if the frequency of at least one of the chosen numbers is different. The test cases are generated such that the number of unique combinations that sum up to target is less than 150 combinations for the given input.

Example 1:

Input: candidates = [2,3,6,7], target = 7

Output: [[2,2,3],[7]]

Explanation:

2 and 3 are candidates, and $2 + 2 + 3 = 7$. Note that 2 can be used multiple times.

7 is a candidate, and $7 = 7$.

These are the only two combinations.

Example 2:

Input: candidates = [2,3,5], target = 8

Output: [[2,2,2,2],[2,3,3],[3,5]]

```

1 def combinationSum(candidates, target):
2     result = []
3
4     def backtrack(remaining, combo, start):
5         if remaining == 0:
6             result.append(list(combo))
7             return
8         elif remaining < 0:
9             return
10
11        for i in range(start, len(candidates)):
12            combo.append(candidates[i])
13            backtrack(remaining - candidates[i], combo, i)
14            combo.pop()
15
16        backtrack(target, [], 0)
17        return result
18
19
20 candidates1 = [2, 3, 6, 7]
21 target1 = 7
22 print(combinationSum(candidates1, target1)) # Output: [[2, 2, 3], [7]]
23 candidates2 = [2, 3, 5]
24 target2 = 8
25 print(combinationSum(candidates2, target2)) # Output: [[2, 2, 2, 2], [2, 3, 3], [3, 5]]
26
27
28

```

input

```

[[2, 2, 3], [7]]
[[2, 2, 2, 2], [2, 3, 3], [3, 5]]

```

8. Given a collection of candidate numbers (candidates) and a target number (target), find all unique combinations in candidates where the candidate numbers sum to target. Each number in candidates may only be used once in the combination. The solution set must not contain duplicate combinations.

Example 1:

Input: candidates = [10,1,2,7,6,1,5], target = 8

Output:

```

[
  [1,1,6],
  [1,2,5],
  [1,7],
  [2,6]
]

```

Example 2:

Input: candidates = [2,5,2,1,2], target = 5

Output:

```

[
  [1,2,2],
  [5]
]

```

```

1 def combination_sum2(candidates, target):
2     def backtrack(start, path, target):
3         if target == 0:
4             result.append(path)
5             return
6         for i in range(start, len(candidates)):
7             if i > start and candidates[i] == candidates[i - 1]:
8                 continue
9             if candidates[i] > target:
10                break
11            backtrack(i + 1, path + [candidates[i]], target - candidates[i])
12
13    candidates.sort()
14    result = []
15    backtrack(0, [], target)
16    return result
17
18 # Example 1
19 candidates1 = [10, 1, 2, 7, 6, 1, 5]
20 target1 = 8
21 print(combination_sum2(candidates1, target1))
22
23 # Example 2
24 candidates2 = [2, 5, 2, 1, 2]
25 target2 = 5
26 print(combination_sum2(candidates2, target2))
27
28

```

input

```

[[1, 1, 6], [1, 2, 5], [1, 7], [2, 6]]
[[1, 2, 2], [5]]

```

9. Given an array `nums` of distinct integers, return all the possible permutations. You can return the answer in any order.

Example 1:

Input: `nums = [1,2,3]`

Output: `[[1,2,3],[1,3,2],[2,1,3],[2,3,1],[3,1,2],[3,2,1]]`

Example 2:

Input: `nums = [0,1]`

Output: `[[0,1],[1,0]]`

Example 3:

Input: `nums = [1]`

Output: `[[1]]`

```

1 from itertools import permutations
2
3 def permute(nums):
4     return [list(p) for p in permutations(nums)]
5
6 print(permute([1, 2, 3]))
7 print(permute([0, 1]))
8 print(permute([1]))
9
10

```

input

```

[[1, 2, 3], [1, 3, 2], [2, 1, 3], [2, 3, 1], [3, 1, 2], [3, 2, 1]]
[[0, 1], [1, 0]]
[[1]]

```

10. Given a collection of numbers, `nums`, that might contain duplicates, return all possible unique permutations in any order.

Example 1:

Input: `nums = [1,1,2]`

Output:

`[[1,1,2],`

`[1,2,1],`

`[2,1,1]]`

Example 2:

Input: `nums = [1,2,3]`

Output: `[[1,2,3],[1,3,2],[2,1,3],[2,3,1],[3,1,2],[3,2,1]]`

```

1 from typing import List
2
3 def permuteUnique(nums: List[int]) -> List[List[int]]:
4     def backtrack(start):
5         if start == len(nums):
6             result.append(nums[:])
7             return
8         seen = set()
9         for i in range(start, len(nums)):
10            if nums[i] in seen:
11                continue
12            seen.add(nums[i])
13            nums[start], nums[i] = nums[i], nums[start]
14            backtrack(start + 1)
15            nums[start], nums[i] = nums[i], nums[start]
16
17     result = []
18     nums.sort()
19     backtrack(0)
20     return result
21 print(permuteUnique([1, 1, 2]))
22 print(permuteUnique([1, 2, 3]))
23

```

inp

```

[[1, 1, 2], [1, 2, 1], [2, 1, 1]]
[[1, 2, 3], [1, 3, 2], [2, 1, 3], [2, 3, 1], [3, 2, 1], [3, 1, 2]]

```