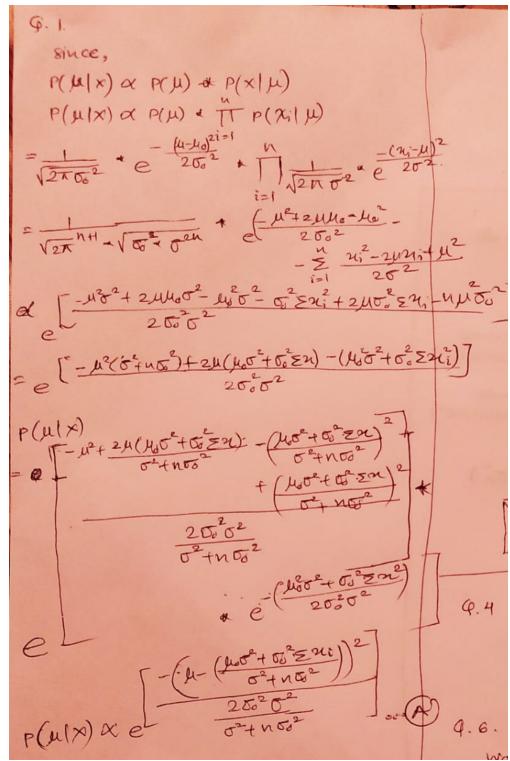
Name: Suraj Sunil Pawar

Student ID: 200315997 Unity ID: spawar2

## Q 1)



#### Q 2)

From the equation, A) the derived posterior distribution is the quadratic and a Gaussian distribution as it is proportional to the Normal form.

$$\hat{\varphi}$$
. 2.  $\frac{(u-un)^2}{e^2 + u^2} \sim N(un, 6n^2)$ 

where,  $\sigma_n^2 = \frac{\sigma_0^2 \sigma_0^2}{\sigma_0^2 + u^2 \sigma_0^2}$  and

 $un = \frac{u_0 \sigma_0^2 + \sigma_0^2}{\sigma_0^2 + u^2 \sigma_0^2}$ 

### Q 3)

$$\frac{Q.3}{\sigma^{2}} = \frac{\sigma_{0}^{2}\sigma^{2}}{\sigma^{2}+n\sigma_{0}^{2}} = \frac{1}{\left(\sigma_{0}^{2}+n\sigma_{0}^{2}\right)}$$

$$= \frac{1}{\left(\sigma_{0}^{2}+\frac{n}{\sigma^{2}}\right)^{2}}$$

$$= \frac{1}{\left(\sigma_{0}^{2}+\frac{n$$

## **Q 4)** From equation C) weights can be derived as below

$$\begin{array}{ccc}
\varphi.4 & w_e = \frac{\sigma^2}{\sigma^2 + n\sigma^2} & \text{and} \\
w_1 = \frac{n\sigma^2}{\sigma^2 + n\sigma^2}
\end{array}$$

## Q 5)

Above equations, w0 and w1 indicate the weights are inversely proportional to their vars.

# Q 6) The sum of weights w0 and w1 is equal to the

$$4.6.$$

$$w_0 + w_1 = \frac{\sigma^2}{\sigma^2 + m\sigma_0^2} + \frac{n\sigma_0^2}{\sigma^2 + m\sigma_0^2}$$

$$= \frac{\sigma^2 + n\sigma_0^2}{\sigma^2 + m\sigma_0^2}$$

$$= 1$$

$$w_0 + w_1 = 1$$

## Q 7)

As the weight w0's numerator is 1 and denominator is one plus somethings so anyhow it is going to be between 0 and 1.

Similarly, for w1, its values lie between 1 and 0.

Hence, both weight values lie between 1 and 0.

## Q 8)

From previous answers, it can be inferred weight values lies between 1 and 0. The maximum values of  $\mu_n=\mu_0+\overline{x}$ . But since both weights are inversely dependent on n, the edge case of 0 and 1 are not possible. Hence,  $\mu_n$  will always lie between  $\mu_0$  and  $\overline{x}$ .

```
import numpy as np
import scipy.stats as st
from matplotlib import pyplot as pt
sample_size = 20
li = np.linspace(0, 10, sample_size)
M0, sd0 = 4, 0.8
d_prior = st.norm(m0, sd0).pdf(li)
Mx, sdx = 6, 1.5
sample_size = st.norm(mx, sdx).pdf(li)
x_t = st.norm(mx,sdx).rvs(sample_size)
var = 1 / ((1 / sd0 ** 2) + (sample_size / sdx ** 2))
mean = var * ((m0 / sd0**2) + (np.mean(x_t) * sample_size / sdx **2))
print("Posterior distibution:\n Mean =", round(mean, 3))
print("var =", round(var,3))
post = st.norm(mean, np.sqrt(var)).pdf(li)
pt.plot(li, d_prior, "r-", label = 'Prior Distribution')
pt.figure(figsize=(20,20))
pt.plot(li, post, "b", label = 'Posterior Distribution')
pt.plot(li, sample_size, "g-", label = 'sample_size Distribution')
pt.legend(loc = 'upper right')
pt.ylabel('Probability Density')
pt.title('Probability Density Plot')
pt.xlabel('X')
pt.show()
 Posterior distibution:
 Mean = 5.727
 Variance = 0.096
                      Probability Density Plot
                                         Prior Distribution
   1.2
                                         Sample Distribution
                                         Posterior Distribution
   1.0
 Probability Density
9.0
8.0
   0.2
```