

Safe interleaving
of accesses by T_1 and T_2
to A, B, \dots .



When we swap
read/write/commit
operations in schedules

- we will never permit
swaps that change the
order of operations
within an individual
transaction in the schedule



Main idea:

- try to swap R/W of transactions in schedule
- = so as to arrive at a sequential execution
(= no overlaps)
- ⇒ we cannot do swaps that change the effects of the R/W on any individual data item



Conflicting pairs:

$t \downarrow$

$R_1(A)$
 $w_2(A)$

$w_1(A)$
 $R_2(A)$

$w_2(A)$
 $w_1(A)$



Schedule S of slide 18:

$$S = \frac{W_3(A) \ W_2(C) \ R_1(A) \ W_1(B) \ R_1(C)}{W_2(A) \ \underline{R_4(A)} \ \underline{W_4(D)}}$$

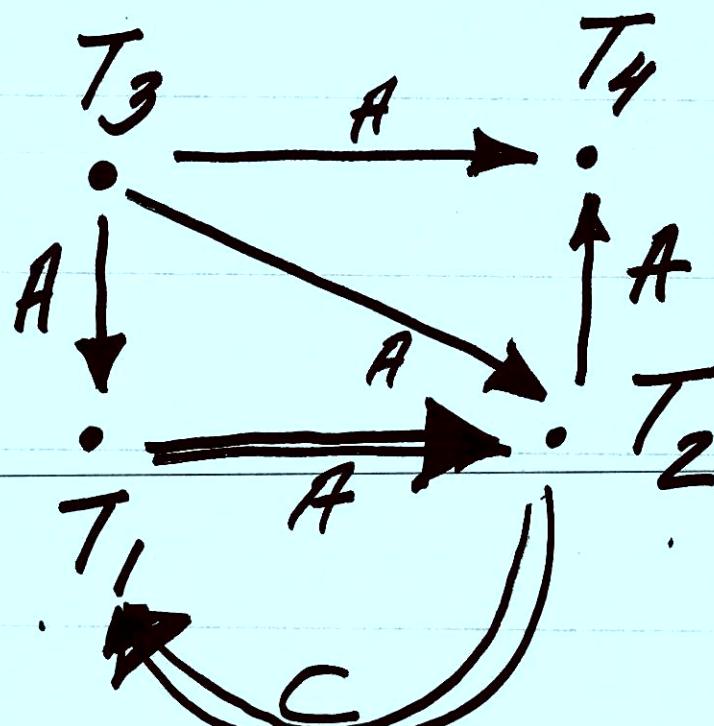
✓ A: $W_3(A)$ $R_1(A)$

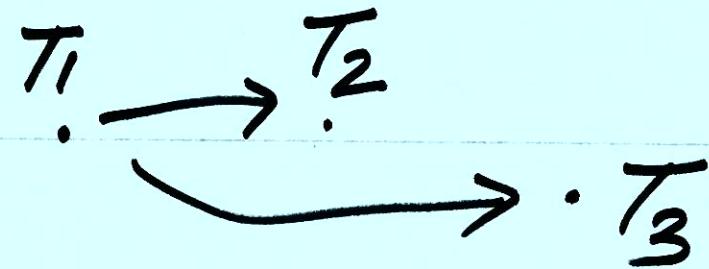
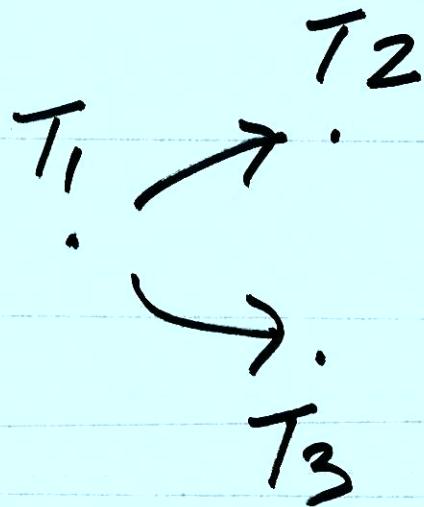
$W_2(A)$ $R_4(A)$

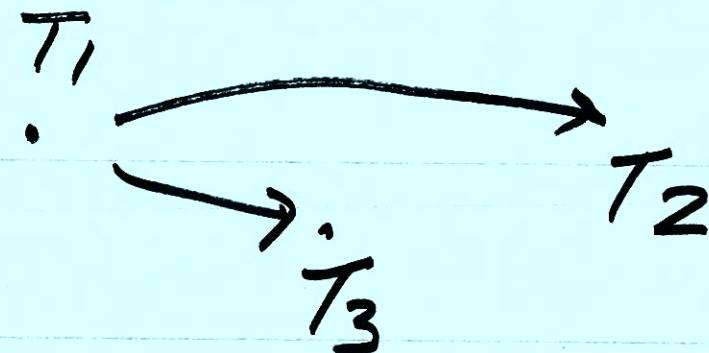
✓ B: $W_1(B)$

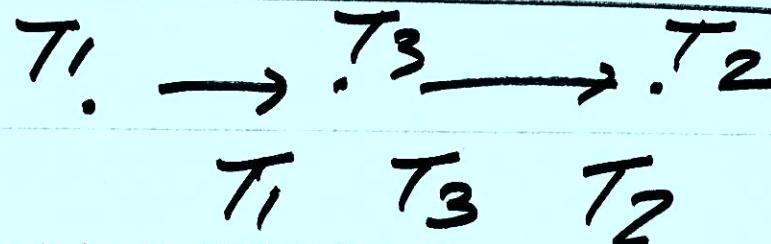
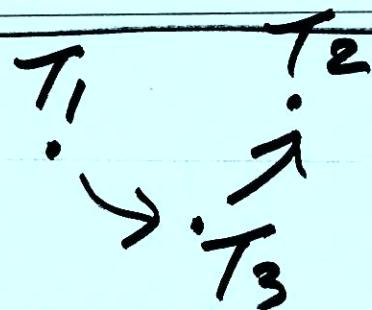
✓ C: $W_2(C)$ $R_1(C)$

✓ D: $W_4(D)$





$$T_1 \quad T_2 \quad T_3$$


$$T_1 \quad T_3 \quad T_2$$


$S: w_1(A), R_2(A), c_2, c_1$

commit for T_2

↓

commit for T_1

T_2 reads from T_1

- if T_1 does not commit
 $\rightarrow S$ is not recoverable



T_1 reads from T_2 in sched S
 (intuition: $S: \dots \underline{W_2(A)} \underline{R_1(A)}$)

if, for some data item A:

$R_1(A)$ is the first read
 operation on A after the
latest write operation

on A by T_2

$S: \dots W_3(B) R_1(C) W_2(B)$



S: $R_3(C)$ $w_4(C)$ $w_5(C)$ $w_3(C)$,

— $R_5(C)$ $w_5(C)$ $R_4(C)$ —

— $R_5(C)$ —

T_5 reads from T_3 (on C);

T_4 reads from T_5



* Recoverable schedule:

- each T commits only after each xaction from which it had read has committed

yes ✓ $S_1: W_1(A), C_1, R_2(A), C_2 \quad (\text{ACR})$

yes ✓ $S_2: W_1(A), R_2(A), C_1, C_2 \quad (\text{no ACR})$

yes ✓ $S_3: W_1(A), R_3(A), C_1, R_2(A), C_3, C_2$

 no - $S_4: W_1(A), R_3(A), C_3, C_1, R_2(A), C_2$
 (T_1-T_3)

- Schedules that avoid cascading rollbacks (ACR):
 - each T reads from a committed transaction



$\Sigma : \underline{R_1(A)}, \underline{R_2(A)}, \underline{R_3(B)}, \underline{W_1(A)},$
 $\underline{R_2(C)}, \underline{R_2(B)}, \underline{W_2(B)}, \underline{W_1(C)}$

1. Maximize concurrency:

Assume each transaction

- takes a lock on each data item immediately before it first uses it, and
- releases the lock immediately after the last time it accesses the data item



$S(T_1) : R_1(A), W_1(A), W_1(C)$

$S(T_2) : R_2(A), R_2(C), R_2(B), W_2(B)$

$S(T_3) : R_3(B)$



$\underline{S^{lu}(T_3) : \underline{L_3(B)}, \underline{R_3(B)}, \underline{u_3(B)}}$

$\underline{S^{lu}(T_1) : \underline{L_1(A)}, \underline{R_1(A)}, \underline{W_1(A)}, \underline{u_1(A)},}$
 $\underline{\underline{L_1(C)}, \underline{W_1(C)}, \underline{u_1(C)}}$

$\underline{S^{lu}(T_2) : \underline{L_2(A)}, \underline{R_2(A)}, \underline{u_2(A)}, \underline{L_2(C)},}$
 $\underline{R_2(C)}, \underline{u_2(C)}, \underline{L_2(B)}, \underline{R_2(B)}, \underline{W_2(B)},$
 $\underline{\underline{u_2(B)}}$

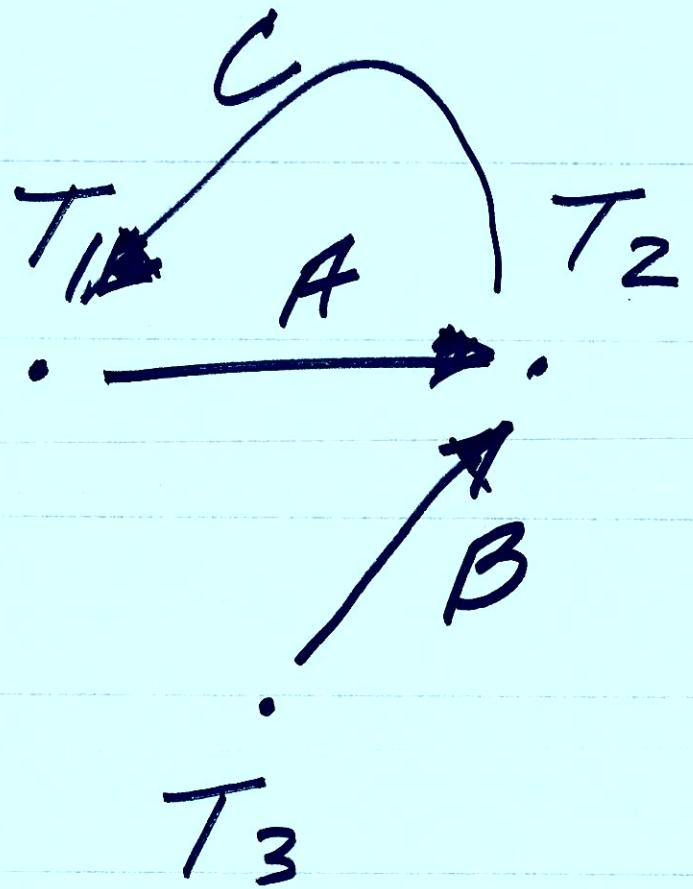


Resulting schedule :

S' : $t_1(A), \underline{R_1(A)}, \underline{W_1(A)}, u_1(A),$
 $t_2(A), \underline{R_2(A)}, \underline{t_3(B)}, \underline{R_3(B)}, u_3(B),$
 $\underline{u_2(A)},$
 $t_2(C), \underline{R_2(C)}, u_2(C), t_2(B),$
 $\underline{R_2(B)}, \underline{W_2(B)}, u_2(B), \underline{t_1(C)},$
 $\underline{W_1(C)}, \underline{u_1(C)}$

A: R_1, W_1, R_2
B: R_3, R_2, W_2
C: R_2, W_1





2. 2PL - two-phase locking on $\sqrt{ }$

$S(T_1)$: $R_1(A)$, ~~$R_1(B)$~~ , $w_1(A)$, $w_1(C)$

$\sqrt{ }(T_2)$: $\underline{R_2(A)}$, $R_2(C)$, $\underline{R_2(B)}$, $w_2(B)$

$\sqrt{ }(T_3)$: $R_3(B)$

$\nabla^{2PL}(T_1)$: $\ell_1(A)$, $R_1(A)$, $w_1(A)$, $\ell_1(C)$,
 $u_1(A)$, $w_1(C)$, $u_1(C)$

$\nabla^{2PL}(T_2)$: $\ell_2(A)$, $R_2(A)$, $\ell_2(C)$, $R_2(C)$,
 $\ell_2(B)$, ~~$R_2(B)$~~ , ~~$\ell_2(C)$~~ , $u_2(C)$,
 $u_2(A)$, ~~$R_2(B)$~~ , ~~$W_2(B)$~~ , $u_2(B)$



$S^{2PL}(T_3)$: $\ell_3(B), R_3(B), u_3(B)$



$S^{2PL} : l_1(A), \underline{R_1(A)}, l_3(B), \underline{R_3(B)},$
 $u_3(B), \underline{W_1(A)}, l_1(C), u_1(A),$
 $l_2(A), \underline{R_2(A)}, \underline{W_1(C)}, u_1(C),$
 $l_2(C), \underline{R_2(C)}, l_2(B), u_2(C),$
 $u_2(A), \underline{R_2(B)}, \underline{W_2(B)}, u_2(B)$

A: R_1 W_1 R_2

$T_1 \xrightarrow{G, R} T_2$

B: R_3 R_2 W_2

$\nearrow T_B$

C: W_1 R_2

$\cdot T_3$

