

Assignment 3

Subject Name : Theory of Automata & Formal Languages

Subject Code : ACSE0404

Unit – 1 and 2

Convert the NDA to DFA given $M = (\{q_0, q_1, q_2\}, \{a, b\}, \delta, q_0, \{q_1\})$ with state table as given below

Q1.

	<i>a</i>	<i>b</i>
<i>q</i> ₀	{ <i>q</i> ₁ , <i>q</i> ₂ }	∅
<i>q</i> ₁	∅	{ <i>q</i> ₂ }
<i>q</i> ₂	∅	{ <i>q</i> ₂ }

Q.2.

Construct the state diagram for the finite-state machine with the state table shown below.

State	<i>g</i>		<i>h</i>	
	Input		Input	
	0	1	0	1
<i>s</i> ₀	<i>s</i> ₁	<i>s</i> ₀	1	0
<i>s</i> ₁	<i>s</i> ₃	<i>s</i> ₀	1	1
<i>s</i> ₂	<i>s</i> ₁	<i>s</i> ₂	0	1
<i>s</i> ₃	<i>s</i> ₂	<i>s</i> ₁	0	0

Q.3. Design a DFA, the language recognized by the Automaton being $L = \{a^n b : n \geq 0\}$

Q.4 . Obtain the DFA that accepts/recognizes the language $L(M) = \{w \mid w \in \{a,b,c\}^* \text{ and } w \text{ contains the pattern } abac\}$.

Q.5 . Construct an FA accepting all strings in $\{0,1\}^*$ having even number of 0's.

Q.6. Construct a finite automaton accepting all strings over $\{0, 1\}$

(a) having odd number of 0's

(b) having even number of 0's and even number of 1's

Q.7. Determine an FA, M accepting L, where $L = \{ w \in \{0,1\}^* : \text{Every 0 in } w \text{ has a 1 immediately to its right} \}$.

Q.8. Determine an NFA that accepts the language $L = (aa^*(a+b))$.

Q.9. Determine a deterministic Finite State Automaton from the given Nondeterministic FSA.

$$M = (\{q_0, q_1\}, \{a, b\}, \delta, q_0, \{q_1\})$$

with the state table diagram for δ given below.

δ	a	b
q_0	$\{q_0, q_1\}$	$\{q_1\}$
q_1	\emptyset	$\{q_0, q_1\}$

Q.10. Determine a NFA accepting $\{ab, ba\}$ and use it to find a DFA accepting it.

Q.11. Obtain the regular expressions for the following sets:

- (a) The set of all strings over $\{a, b\}$ beginning and ending with 'a'.
- (b) $\{b^2, b^5, b^8, \dots\}$
- (c) $\{a^{2n+1} \mid n > 0\}$

Q.12. Obtain the regular expressions for the languages given by

- (a) $L_1 = \{a^{2n}b^{2m+1} \mid n \geq 0, m \geq 0\}$
- (b) $L_2 = \{a, bb, aa, abb, ba, bbb, \dots\}$
- (c) $L_3 = \{w \in \{0,1\}^* \mid w \text{ has no pair of consecutive zeros}\}$
- (d) $L_4 = \{\text{strings of 0's and 1's ending in } 00\}$

Q.13 Give Regular expressions for the following on $\Sigma = \{a, b, c\}$

- (a) all strings containing exactly one a
- (b) all strings containing no more than three a 's

Q.14 . Find regular expressions over $\Sigma = \{a, b\}$ for the language defined as follows:

- (a) $L_1 = \{a^m b^m : m > 0\}$
- (b) $L_2 = \{b^m a b^n : m > 0, n > 0\}$

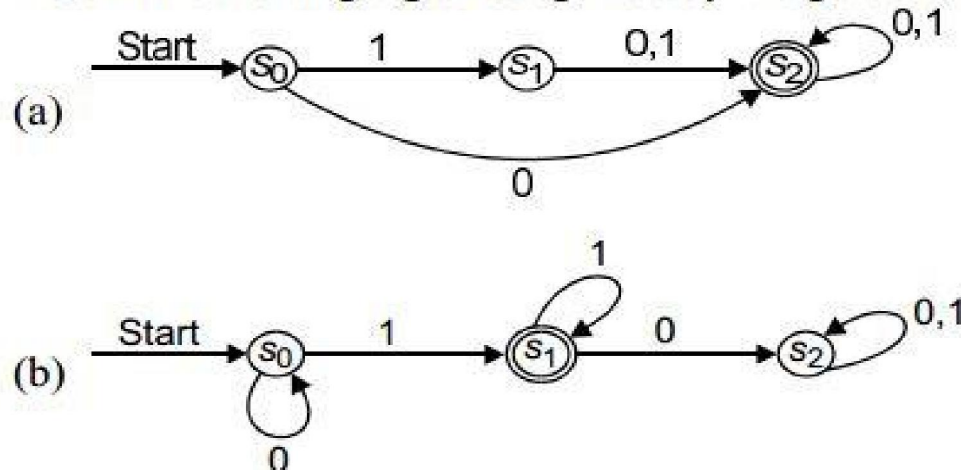
Q.15. Determine all strings in $L((a+b)^*b(a+ab)^*)$ of length less than four.

Q.16. Find the regular expressions for the languages defined by

- (i) $L_1 = \{a^n b^m : n \geq 1, m \geq 1, nm \geq 3\}$
- (ii) $L_2 = \{ab^n w : n \geq 3, w \in \{a, b\}^+\}$
- (iii) $L_3 = \{vwv : v, w \in \{a, b\}^*, |v| = 2\}$

Q.17

Determine the languages recognized by the given DFA.



Q.18.

What are the strings in the regular sets specified by the regular expressions given below.

- (a) 10^*
- (b) $(10)^*$
- (c) $0 \cup 01$
- (d) $0(0 \cup 1)^*$
- (e) $(0^* 1)^*$.

Q.19. Construct a NDA that recognizes the regular set $1^* \cup 01$.

Q.20 Find an NDA which recognizes the set $0^* 1^*$.

Q.21

Convert the regular expression $(ab \cup a)^*$ to an NFA.

Convert the regular expression $(a \cup b)^* aba$ to an NFA.

Q.22 Give regular expressions for each of the following subsets of $\{a, b\}^*$,

- (a) $\{x \mid x \text{ contains an even number of } a\text{'s}\}$
- (b) $\{x \mid x \text{ contains an odd number of } b\text{'s}\}$

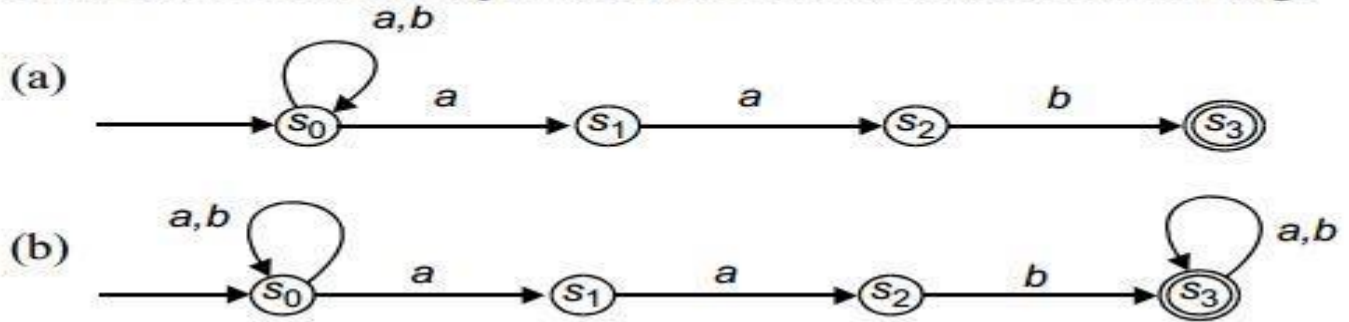
(c) $\{x \mid x \text{ contains an even number of a's or an odd number of b's}\}$

Q.23 Give the DFA accepting the sets of strings matching the following regular expressions:

- (a) $(000^* + 111^*)^*$
- (b) $(01 + 10)(01 + 10)(01 + 10)$
- (c) $(0 + 1(01^*0)^*1)^*$

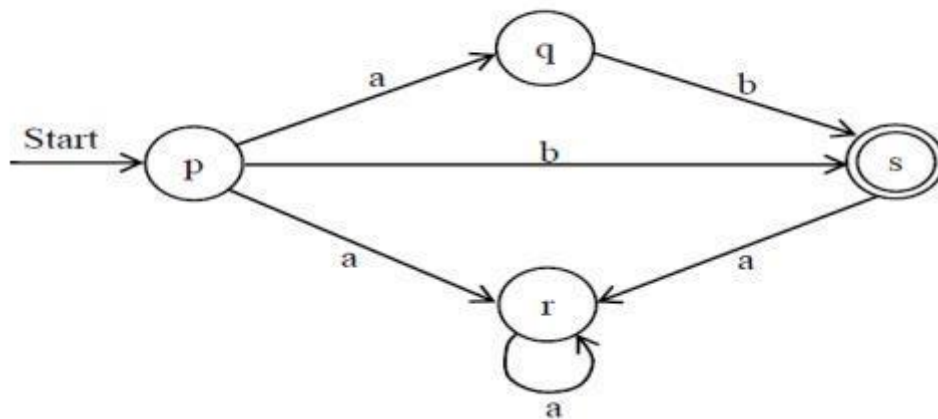
Q.24.

Convert the NDA to equivalent DFA for each of the following:



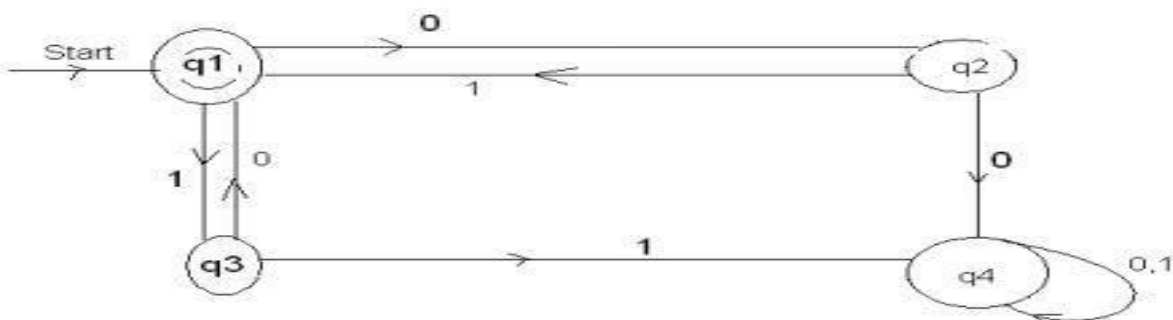
Q.25.

Convert the following NFA to DFA



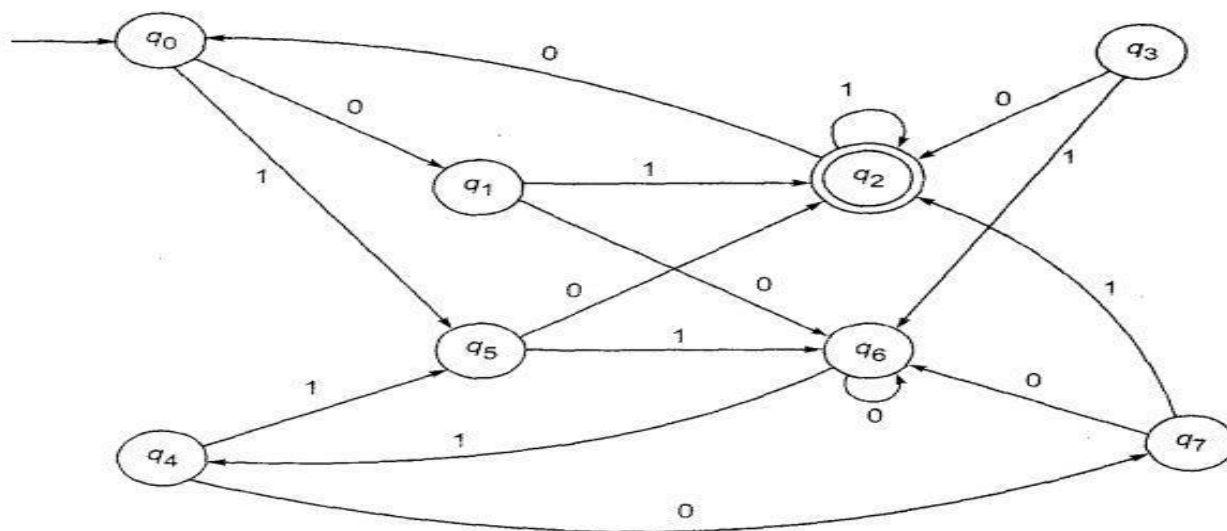
Q.26.

Convert the following DFA into regular expression.



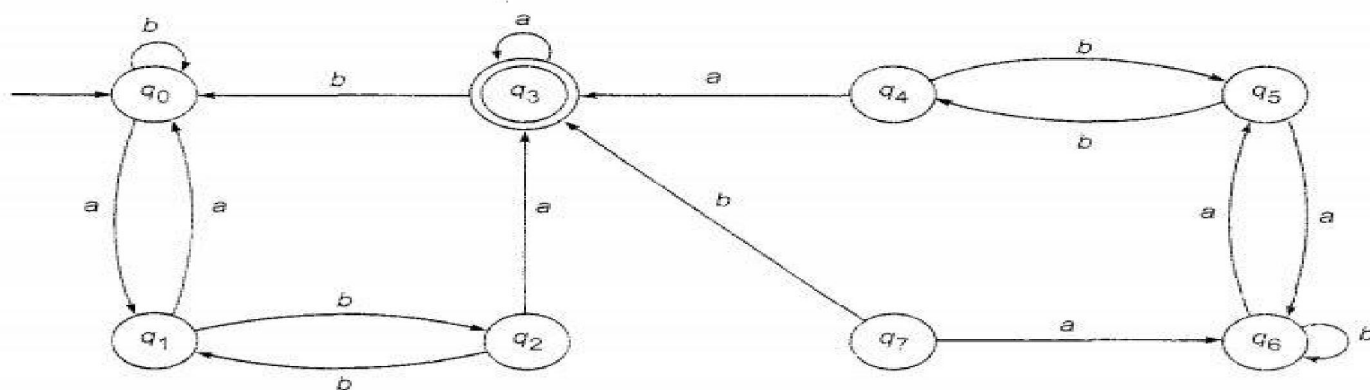
Q.27

Construct a minimum state automaton equivalent to the finite automaton described by



Q.28

Construct the minimum state automaton equivalent to the transition diagram given by Fig. 3.14.



Q.29

Construct a minimum state automaton equivalent to a DFA whose transition table is defined by Table

TABLE		DFA	
State		a	b
→q ₀		q ₁	q ₂
q ₁		q ₄	q ₃
q ₂		q ₄	q ₃
⊙q ₃		q ₅	q ₆
⊙q ₄		q ₇	q ₆
q ₅		q ₃	q ₆
q ₆		q ₆	q ₆
q ₇		q ₄	q ₆

Q.30.

Construct a Mealy machine which is equivalent to the Moore machine defined by Table

TABLE Moore Machine

Present state	Next state		Output
	$a = 0$	$a = 1$	
$\rightarrow q_0$	q_1	q_2	1
q_1	q_3	q_2	0
q_2	q_2	q_1	1
q_3	q_0	q_3	1

Q.31.

Construct a Moore machine equivalent to the Mealy machine M defined by Table

TABLE Mealy Machine

Present state	Next state			
	$a = 0$		$a = 1$	
	state	output	state	output
$\rightarrow q_1$	q_1	1	q_2	0
q_2	q_4	1	q_4	1
q_3	q_2	1	q_3	1
q_4	q_3	0	q_1	1

Q.32

Construct a minimum state automaton equivalent to the DFA described by

