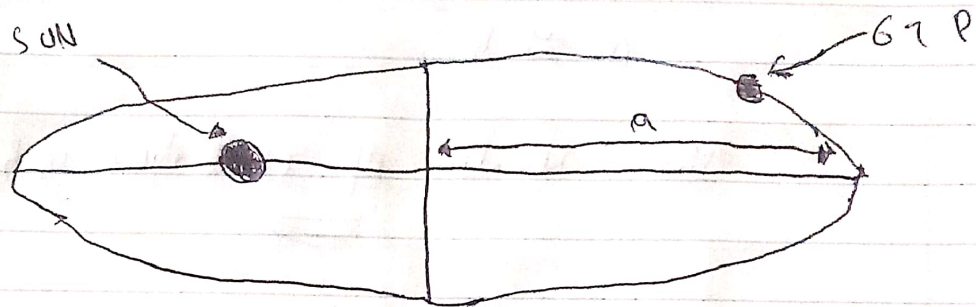


05/18/2021

PHYS-230LAB QUIZ #13

The Rosetta mission was the first one to launch a spacecraft on a comet, specifically comet 67P / Churyumov-Gerasimenko. 67P has a semi major axis $a = 3.4830$ AU with an eccentricity $e = 0.64162$.



- What is the velocity of 67P at the aphelion (point of maximum distance to the Sun)?
- What is the total mechanical energy of this comet?
- What is its velocity at the perihelion (point of minimum distance to the Sun)?
- What is the velocity of 67P at a distance $r = 4.1283$ AU from the Sun?
- What is the orbital period of 67P? (For this question you may assume a circular orbit with radius equal to a).

DATA:

$$G = 6.6728 \times 10^{-11} \frac{\text{N m}^2}{\text{kg}^2}$$

$$M_{67P} = 9.982 \times 10^{12} \text{ kg}$$

$$M_{\text{sun}} = 1.989 \times 10^{30} \text{ kg}$$

$$1 \text{ AU} = 1.495978707 \times 10^{11} \text{ m}$$

Ans: (a) $V_{\text{aphelion}} = \sqrt{\frac{GM_{\text{sun}}}{a} \left(\frac{1-e}{1+e} \right)}$

$$= \sqrt{\frac{6.6725 \times 10^{-11} \times 1.989 \times 10^{30}}{10^{11} \times 3.4630 \times 1.495978707} \left(\frac{1-e}{1+e} \right)}$$

$$= \sqrt{\frac{2.56180142 \times 10^8 \times 0.35898}{1.64102}}$$

$$= \sqrt{0.560404792 \times 10^4}$$

$$= \underline{\underline{7486.0 \text{ m/s}}}$$

\therefore The velocity of 67P at the aphelion is 7486 m/s

(b) $E = - \frac{GM_s M_c}{2a}$

$$E = - \frac{6.6725 \times 10^{-11} \times 9.982 \times 1.989 \times 10^{42}}{2 \times 3.4630 \times 1.495978707 \times 10^{11}}$$

$$E = \underline{\underline{-12.7859504 \times 10^{20} \text{ J}}}$$

The total mechanical energy of this comet
 $= -12.7859504 \times 10^{20} \text{ J}$

(3)

$$\begin{aligned}
 (c) \quad v_{\text{perihelion}} &= \sqrt{\frac{GM_{\text{sun}}}{a} \left(\frac{1+e}{1-e} \right)} \\
 &= \sqrt{\frac{6.6725 \times 10^{-11} \times 1.989 \times 10^{30} \times 1.64102}{10^4 \times 3.4630 \times 1.495978707 \times 0.35848}} \\
 &= 10^4 \sqrt{11.7108679} \\
 &= \underline{\underline{34221.1 \text{ m/s}}}
 \end{aligned}$$

Velocity at the perihelion = 34221.1 m/s

$$\begin{aligned}
 (d) \quad v &= \sqrt{GM_s \left(\frac{2}{r} - \frac{1}{a} \right)} \\
 v &= \sqrt{\frac{6.6725 \times 10^{-11} \times 1.989 \times 10^{30}}{1.495978707 \times 10^4} \left[\frac{2}{4.1283} - \frac{1}{3.4630} \right]} \\
 v &= \underline{\underline{13176.1 \text{ m/s}}}
 \end{aligned}$$

Velocity of 67P at a distance $r = 4.1283 \text{ AU}$
 = 13176.1 m/s

$$\begin{aligned}
 (e) \quad T &= 2\pi \sqrt{\frac{a^3}{GM_{\text{sun}}}} \\
 T &= 2\pi \sqrt{\frac{(3.4630)^3 \times (1.495978707)^3 \times 10^{33}}{6.6725 \times 10^{-11} \times 1.989 \times 10^{30}}} \\
 &= 2\pi \sqrt{10.4163589 \times 10^{14}} \\
 T &= \underline{\underline{20.3369134 \times 10^7 \text{ s}}}
 \end{aligned}$$