

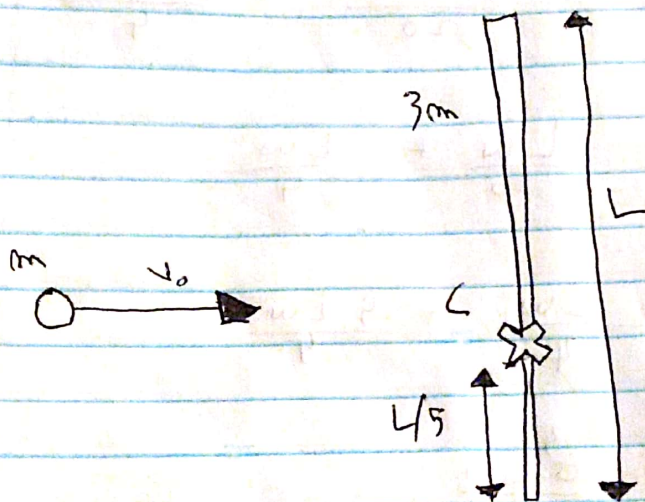
NAME :- SHREYAS SRINIVASA
PALOMAR ID :- 012551187

05/04/2021

PHYS - 230

LAB QUIZ #11

A point mass of mass m and initial velocity v_0 is moving towards a thin, vertical rod of length L and mass $3m$ as shown in the diagram below (values shown below). They experience a perfectly inelastic collision at the point labeled as C (so that the point mass gets stuck to the rod at that point). Determine the final linear and angular velocities of the system.



$$m = 1.23 \text{ kg}$$

$$L = 2.54 \text{ m}$$

$$v_0 = 5.68 \text{ m/s}$$

Ans.:

Using conservation of linear momentum,
$$m v_0 = 3m v$$

Using conservation of linear momentum again, we get

$$m v_0 = (3m + m) v$$
$$\text{or, } v = \frac{m v_0}{4m} = \frac{v_0}{4}$$

where v is the speed after collision.

Using conservation of linear momentum,

$$\frac{m v_0 L}{5} = \frac{m v L}{5} + \frac{1}{2} \cdot 3 m L^2 \cdot \omega$$

$$\Rightarrow \frac{m v_0 L}{5} = \frac{m v L}{5} + \frac{m L^2 \omega}{4}$$

$$\Rightarrow \frac{m v_0 L}{5} = \frac{m v_0 L}{20} + \frac{m L^2 \omega}{4}$$

$$\Rightarrow \frac{m v_0 L}{5} = \frac{m L^2 \omega}{20} + \frac{m L^2 \omega}{4}$$

$$\Rightarrow \frac{v_0}{5} = \frac{L \omega}{20} + \frac{L \omega}{4}$$

$$\Rightarrow v_0 = \frac{L \omega}{4} + 5 \frac{L \omega}{4}$$

$$\Rightarrow v_0 = \frac{6 L \omega}{4}$$

$$\Rightarrow \omega = \frac{2 v_0}{3 L}$$

Angular velocity, $\omega = \frac{2 \times 5.68}{3 \times 2.54}$

$$= \frac{11.36}{7.62}$$

$$= 1.49 \text{ rad/s}$$

Linear speed, $v = \frac{v_0}{4} = \frac{5.68}{4} = 1.42 \text{ m/s}$