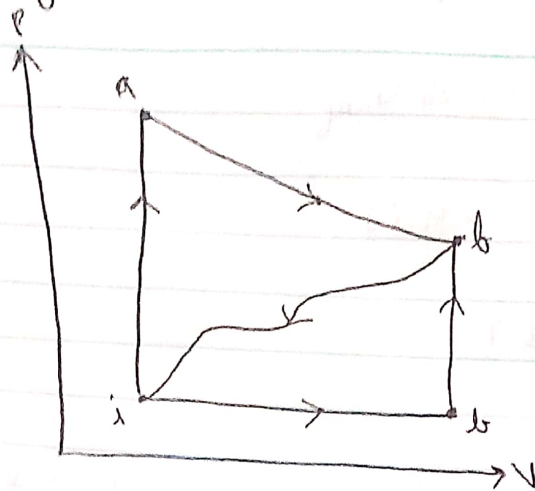


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PHYS-230  
LAB QUIZ #14

Consider the following thermodynamic processes (i) and (ii) shown on a  $P-V$  diagram:-



We know that  $W_{i \rightarrow b} = 10.2 \text{ J}$ ,  $Q_{i \rightarrow b} = 19.8 \text{ J}$  &  $W_{i \rightarrow f} = 25.1 \text{ J}$

(a) Determine  $Q_{i \rightarrow f}$ .

(b) What is the change in internal energy in the process  $f \rightarrow i$ ,  $\Delta U_{fi}$ ?

(c) If  $Q_{fi} = -34.7 \text{ J}$ , determine  $W_{fi}$ .

(d) If  $U_f = 32.3 \text{ J}$ , determine  $U_i$ .

(e) If  $U_b = 28.5 \text{ J}$ , determine  $Q_{ia}$  and  $Q_{af}$ .

(f) If  $U_a = 47.2 \text{ J}$ , determine  $Q_{ia}$  &  $Q_{af}$ .

Ans. (a) Finding  $\Delta U$  for  $i \rightarrow f$  from 1st law:-

$$Q_{i \rightarrow f} - W_{i \rightarrow f} = \Delta U_{i \rightarrow f} \quad (1)$$

$$\Rightarrow 19.8 \text{ J} - 10.2 \text{ J} = \Delta U_{if}$$

$$\Rightarrow \Delta U_{if} = 9.6 \text{ J} = \Delta U_{if}$$

Using 1st law, we have :-

$$Q_{if} - W_{if} = \Delta U_{if}$$

$$Q_{if} - 23.1 \text{ J} = 9.6 \text{ J}$$

$$\therefore Q_{if} = 32.7 \text{ J}$$

(2)

Change in internal energy  $\Delta U$  is a state function, so it depends on the end points,  $f$  and  $i$ .

The internal energy is calculated from point  $i$  to  $f$ , which gives  $9.6 \text{ J}$ .

$$\begin{aligned} \Delta U &= U_f - U_i \\ &= 9.6 \text{ J} \end{aligned}$$

In this case, it is from  $f$  to  $i$ ,

$$\begin{aligned} \therefore \Delta U &= U_i - U_f \\ &= -(U_f - U_i) \\ &= -9.6 \text{ J} \end{aligned}$$

(3)

$$\cancel{Q_{if}} \quad Q_{fi} = -32.7 \text{ J}$$

from 1st law,

(2)

$$Q_{bi} - W_{bi} = \Delta U_{bi}$$

$$\Rightarrow -34.7 \text{ J} - W_{bi} = -9.6 \text{ J}$$

$$\therefore W_{bi} = -25.1 \text{ J}$$

(d) From (b), we have  $\Delta U = U_i - U_f = -9.6 \text{ J}$

$$\Rightarrow U_i = -9.6 + 32.3 \text{ J} \\ = 22.7 \text{ J}$$

(e)  $P_{int} = 19.8 \text{ J}$

$$\therefore Q_{ib} + Q_{bf} = 19.8 \text{ J} \rightarrow \textcircled{1}$$

$$Q_{bf} - W_{bf} = \Delta U_{bf} = U_f - U_i, \text{ volume remains constant.}$$

$$\therefore W_{bf} = 0 \text{ (As, } W = \int P dV)$$

$$\Rightarrow Q_{bf} = U_f - U_i$$

$$\Rightarrow Q_{bf} = 32.3 - U_i$$

$$\Rightarrow Q_{bf} = 32.3 - 28.5$$

$$\therefore Q_{bf} = 3.8 \text{ J}$$

From  $\textcircled{1}$ ,

$$Q_{ib} + 3.8 = 19.8 \text{ J}$$

$$Q_{ib} = 16 \text{ J}$$



(B)  $Q_{\text{inf}} = Q_{\text{in}} + Q_{\text{out}} = 32.7 \text{ J} \rightarrow (2)$

For process ia,

$$Q_{\text{in}} - W_{\text{ia}} = \Delta U_{\text{ia}} = U_a - U_i,$$

In this process,  $V$  is constant we have  $W_{\text{ia}} = 0$ .

$$\therefore Q_{\text{in}} = U_a - U_i \\ = 47.2 \text{ J} - 22.7 \text{ J}$$

$$\therefore Q_{\text{in}} = 24.5 \text{ J}$$

From (2),

$$Q_{\text{inf}} = 24.5 + Q_{\text{out}} = 32.7 \text{ J}$$

$$\therefore Q_{\text{out}} = 8.2 \text{ J}$$