

Chapter 2.2

- 1) If this loop does not contain a stop or a go to, then it will repeat exactly N times.

5)

| p | q | $\sim p$ | $\sim q$ | $\sim p \vee q$ | $\sim p \vee q \rightarrow q$ |
|-----|-----|----------|----------|-----------------|-------------------------------|
| T | T | F | F | T | F |
| T | F | F | T | F | T |
| F | T | T | F | T | F |
| F | F | T | T | T | T |

7)

| p | q | r | $\sim q$ | $p \wedge \sim q$ | $p \wedge \sim q \rightarrow r$ |
|-----|-----|-----|----------|-------------------|---------------------------------|
| T | T | T | F | F | T |
| T | T | F | F | F | T |
| T | F | T | T | T | T |
| T | F | F | T | T | F |
| F | T | T | F | F | T |
| F | T | F | F | F | T |
| F | F | T | T | F | T |
| F | F | F | T | F | T |

(2)

a)

| p | q | r | $\sim r$ | $p \wedge \sim r$ | $q \vee r$ | $p \wedge \sim r \leftrightarrow q \vee r$ |
|-----|-----|-----|----------|-------------------|------------|--|
| T | T | T | F | F | T | F |
| T | T | F | T | T | T | T |
| T | F | T | F | F | T | F |
| T | F | F | T | T | F | F |
| F | T | T | F | F | T | F |
| F | T | F | T | F | T | F |
| F | F | T | F | F | T | F |
| F | F | F | T | F | F | T |

13)(a)

| p | q | $\sim p$ | $p \rightarrow q$ | $\sim p \vee q$ |
|-----|-----|----------|-------------------|-----------------|
| T | T | F | T | T |
| T | F | F | F | F |
| F | T | T | T | T |
| F | F | T | T | T |

\therefore From the TT, $p \rightarrow q$ and $\sim p \vee q$ are logically equivalent.

(3)

(b)

| p | q | $\sim q$ | $p \rightarrow q$ | $\sim(p \rightarrow q)$ | $p \wedge \sim q$ |
|-----|-----|----------|-------------------|-------------------------|-------------------|
| T | T | F | T | F | F |
| T | F | T | F | T | T |
| F | T | F | T | F | F |
| F | F | T | T | F | F |

\therefore From the TT $\sim(p \rightarrow q)$ and $(p \wedge \sim q)$ are logically equivalent

16) A : You paid full price
 B : You didn't buy it at Crown Books
 $A \rightarrow B$
 $B \vee A$

| A | B | $A \rightarrow B$ | $B \vee A$ |
|---|---|-------------------|------------|
| T | T | T | T |
| T | F | F | T |
| F | T | T | T |
| F | F | T | F |

\therefore The given statements are not logically equivalent.

(4)

17) A: "If 2 is a factor of n and 3 is a factor of n , then 6 is a factor of n ."

B: "2 is not a factor of n or 3 is not a factor of n or 6 is a factor of n ."

P: 2 is a factor of n

Q: 3 is a factor of n .

R: 6 is a factor of n .

$\sim P$: 2 is not a factor of n .

$\sim Q$: 3 is not a factor of n .

A: $(P \wedge Q) \rightarrow R$

B: $(\sim P \vee \sim Q) \vee R$

A $\Rightarrow (P \wedge Q) \rightarrow R \Rightarrow \sim [P \wedge Q] \vee R$

$= (\sim P \vee \sim Q) \vee R$

$= B$

Therefore, both statements are equivalent.

(5)

| P | Q | R | $P \wedge Q$ | $\sim P \vee \sim Q$ | $(P \wedge Q) \rightarrow R$ | $(\sim P \vee \sim Q) \vee R$ |
|---|---|---|--------------|----------------------|------------------------------|-------------------------------|
| T | T | T | T | F | T | T |
| T | T | F | T | F | F | F |
| T | F | T | F | T | T | T |
| T | F | F | F | T | T | T |
| F | T | T | F | T | T | T |
| F | T | F | F | T | T | T |
| F | F | T | F | T | T | T |
| F | F | F | F | T | T | T |

Thus $(P \wedge Q) \rightarrow R \equiv (\sim P \vee \sim Q) \vee R$

20) (a) $p \rightarrow q \Rightarrow (\sim p \vee q)$

$$\neg(\neg p \vee q) = \neg(\neg p) \wedge \neg q \\ = p \wedge \neg q$$

p is a square and p is not a rectangle.

(b) Today is New Year's Eve and tomorrow is not January.

(c) The decimal expansion of r is terminating and r is not rational.

(6)

(d) $q: n$ is odd or n is 2

$\neg q: n$ is not odd and n is not 2.
 n is prime and n is not odd and
 n is not 2.

(e) $q: x$ is positive or x is 0

$\neg q: x$ is not positive and x is not 0.
 x is non-negative and x is not positive
and x is not 0.

(f) $q: \text{Jim and Sue are her uncle and aunt}$

$\neg q: \text{Jim is not her uncle or Sue is not her aunt.}$

Tom is Ann's father and ~~for~~ Jim is not her uncle or Sue is not her aunt.

(g) $q: n$ is divisible by 2 and n is divisible by 3

$\neg q: n$ is not divisible by 2 or n is not divisible by 3.

(7)

n is divisible by 6 and n is not divisible by 2 or n is not divisible by 3.

22) (a) Contrapositive of $p \rightarrow q$ is $\neg q \rightarrow \neg p$

If p is not a rectangle, then p is not a square.

(b) If tomorrow is not January, then today is not New Year's Eve.

(c) If r is not rational, then the decimal expansion of r is not ~~de~~ terminating

(d) If either n is odd or n is not 2, then n is not prime.

(e) If either x is not positive or x is not 0, then x is not non-negative

(f) If either Jim is not Ann's uncle or Sue is not her aunt, then Tom is not her father

(g) If either n is not divisible by 2 or n is not divisible by 3, then n

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is not divisible by 6.

23) a) Converse: If p is rectangle, then p is a square.

Inverse: If p is not a square, then p is not a rectangle.

b) Converse: If tomorrow is January, then today is New Year's Eve.

Inverse: If today is not New Year's Eve, then tomorrow is not January.

c) Converse: If r is rational, then the decimal expansion of r is terminating.

Inverse: If the decimal expansion of r is not terminating, then r is not rational.

d) Converse: If n is odd or n is 2, then n is prime.

Inverse: If n is not prime, then n is not odd and n is not 2.

⑨

e) Converse: If x is positive or x is 0 then x is non-negative

Inverse: If x is non-negative, then x is not positive and x is not 0.

f) Converse: If Tim is Ann's uncle and Sue is her aunt, then Tom is her father.

Inverse: If Tom is not Ann's father, then Tim is not her uncle or Sue is not her aunt.

g) Converse: If n is divisible by 2 and n is divisible by 3, then n is divisible by 6.

Inverse: If n is not divisible by 6, then n is not divisible by 2 or n is not divisible by 3.