

# Algorithm and Data Structures

"Problem Solving is a skill that can be developed via practice"

→ Define the Problem.

- what exactly is the problem we are trying to solve?

→ Identify the problem

- How and why did this problem happen?

→ what are the possible solutions?

- The ideal solution could be one of the many possible solutions.

→ A decision is to be made.

- Any decision is usually is better than no decision.

- 80% of problems should be solved at the moment they come up.  
Only 20% will need time & research.

→ Assign responsibilities to carry out the decision.

- If a team, who will do what and when.
- If alone, still decide what & when.

→ Set a schedule.

- without a schedule & deadline, it's just a discussion.

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## Core Components of Computational Thinking.

→ Decomposition

- Break down complex problems

into smaller, simpler problems.

→ Pattern recognition.

- Make connections between similar problems & experience

→ Abstraction

- Identify important information and ignore irrelevant details.

→ Algorithm

→ Sequential rules to follow in order to solve a problem.

# Algorithm

- A "finite sequence" of  
"well defined" computational  
steps that transform  
"input" into "output"

## Basic constructs of algorithm

- Linear Sequence: - statements  
that follow one after the  
other.
- Conditional - "if then else"
- Loop - sequence of statements  
that are repeated  
number of times.

# Data Structure

A data structure is a way to store and organise data in order to facilitate access and modification.

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Array  $\Rightarrow$  Sequential data structure.  
Linear data structure.

$\Downarrow$   
Stores data in a sequential manner.

1	2	3	4	5
---	---	---	---	---

1 2 3 4 5 Index/  
0 1 2 3 4 Subscript

All elements are stored in a single memory block.

Every element of an array is of

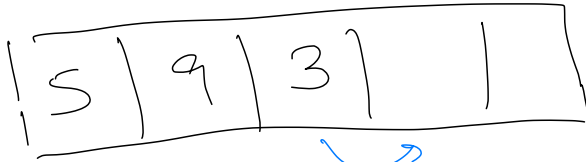
same type.

Fast

Benefit :- Random access.

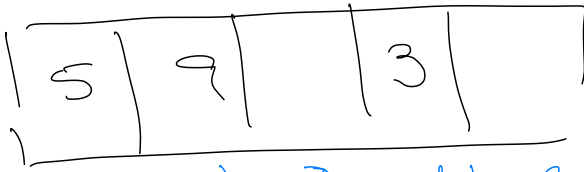
start location +  $i \times$  size of array element type.

Insert / Delete is inefficient in array.

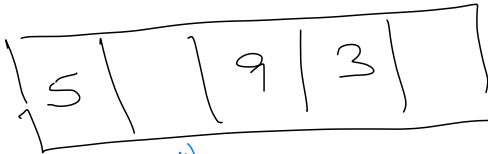


Insert  
between 5  
and 9, 1.

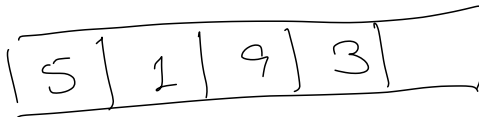
Shift 3 to right



Shift 9 to right



Insert 1



# Stack



LIFO

Last In

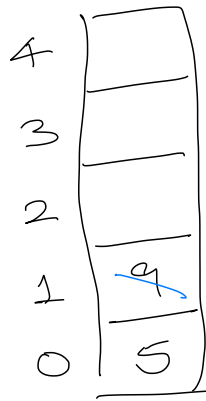
First Out

top ← add

& delete

done with

respect to top.



top → ~~2~~ 0

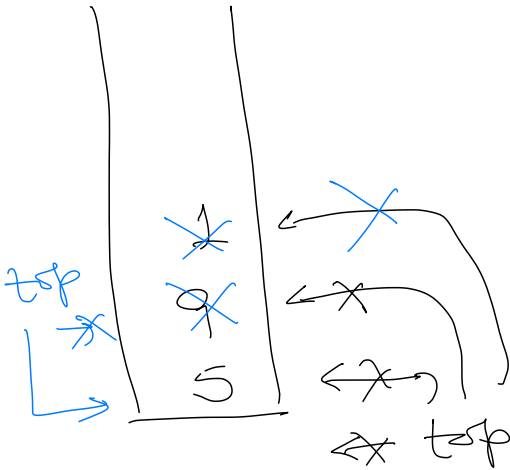
Push(5)

Push(9)

Pop() → 9

Push(elem) → add element to stack.

- Make space at top.
- Store element at top.



Push(5)

Push(9)

Push(1)

Pop() → removes element from stack.

Psp()  $\rightarrow$  1

Psp()  $\rightarrow$  9

→ Fetch element at top  
→ Set top to previous element  
→ Return the fetched element.

IsEmpty()

→ if top stores a element then stack is not empty

else stack is empty.

IsFull()

→ if stack has space for atleast one more element

then stack is not full

else stack is full.

ADT  $\rightarrow$  Abstract Data Type } Defines WHAT & NOT HOW.

Define ADT in JAVA

$\rightarrow$  Use Regwood interface.



```

interface StackIntf {
    void Push (int);
    int Pop ();
    boolean IsFull ();
    boolean IsEmpty ();
}

```

Queue

↓

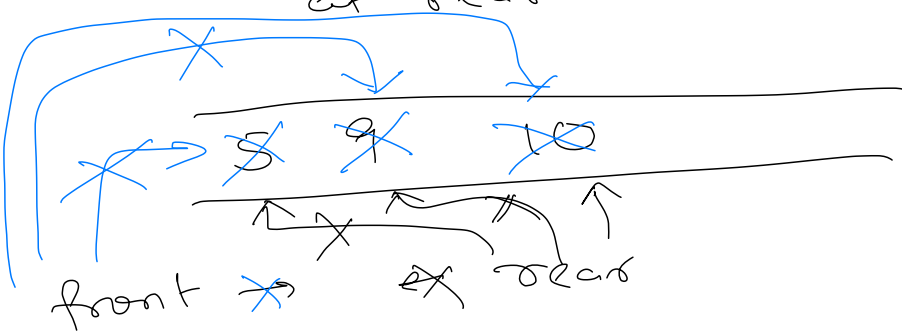
FIFO

First In

First Out

Add (elem)  
 {  
   Make space at  
   rear  
   Store element  
   at rear.  
 }

front → Remove element from front  
           of queue  
 rear → Adding of element is done  
           at rear of queue.



Add (5)  
~~Add (9)~~

Delete  $O(1)$

Add  $O(10)$

- Move front to next element
- Remove element from front.

Delete  $O(1) \rightarrow 5$

Delete  $O(1) \rightarrow 9$

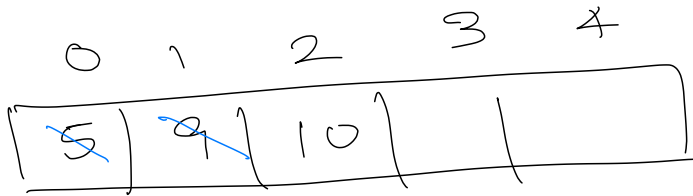
Delete  $O(1) \rightarrow 10$

Is Empty()

- if front equals rear then queue is empty
- else queue is not empty.

Is Full()

- If no space after rear then queue is full
- else queue is not full.



front  $\rightarrow$  ~~-1~~ ~~0~~ 1

rear  $\rightarrow$  ~~-1~~ ~~0~~ 1 2

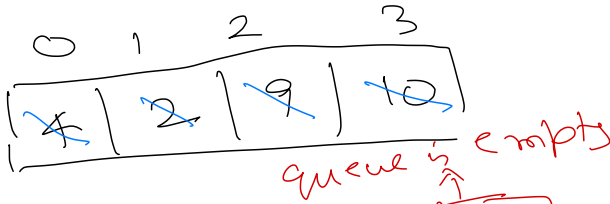
Add  $O(5)$

Add  $O(9)$

Add  $O(10)$

Delete  $O(1) \rightarrow 5$       Delete  $O(1) \rightarrow 9$

Linear Queue  $\rightarrow$  Has problem that Queue can be empty & Full at the same time.



Add Q(4)  
Add Q(2)  
Add Q(9)  
Add Q(10)

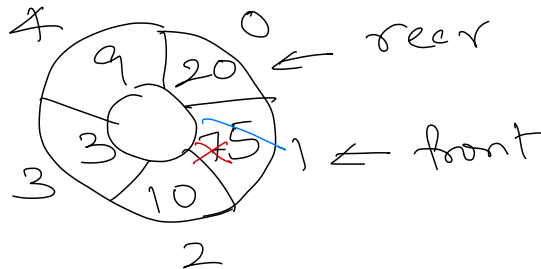
front  $\rightarrow$  ~~1~~ 0 ~~1~~ 2 3  
rear  $\rightarrow$  ~~1~~ 0 ~~1~~ 2 3

queue is full.

Delete Q()  $\rightarrow$  4  
Delete Q()  $\rightarrow$  2  
Delete Q()  $\rightarrow$  9  
Delete Q()  $\rightarrow$  10

Circular Queue

N = Array Size = 5



front  $\rightarrow$  0  
rear  $\rightarrow$  0

front  $\rightarrow$  -2  
rear  $\rightarrow$  ~~1~~ 0 ~~1~~ 2 3 4 0

rear  $\rightarrow$  4

Increment rear by 1 MOD N

rear  $\rightarrow$  5    MOD 5  $\Rightarrow$  0

↓  
value remains  
in range of  
0 to N-1

Add Q(5) rear  $\rightarrow$  0

rear = (rear + 1) MOD N

rear  $\rightarrow$  1

Add Q(10) rear  $\rightarrow$  2

Delete Q()  $\rightarrow$  front  $\rightarrow$  0

$\Rightarrow$  5

front = (front + 1) MOD N

front  $\rightarrow$  1

Add Q(3) rear  $\rightarrow$  3

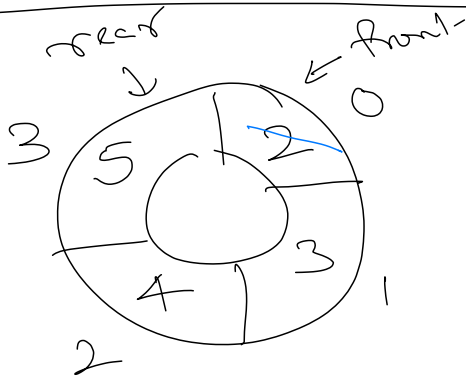
Add Q(9) rear  $\rightarrow$  4

Add Q(20) rear  $\rightarrow$  5 (5 MOD 5)  
0

~~Add Q(7) rear  $\rightarrow$  6~~

$(\text{rear} + 1) \text{ MOD } N$  equals front  
↑↑  
queue full in circular Q.

→ In circular queue, we end up storing max  $(N-1)$  elements.



$N = 4$

front = ~~0~~

rear = ~~0 1 2 3~~

Add Q(2)

Add Q(3)

Add Q(4)

Add Q(5)

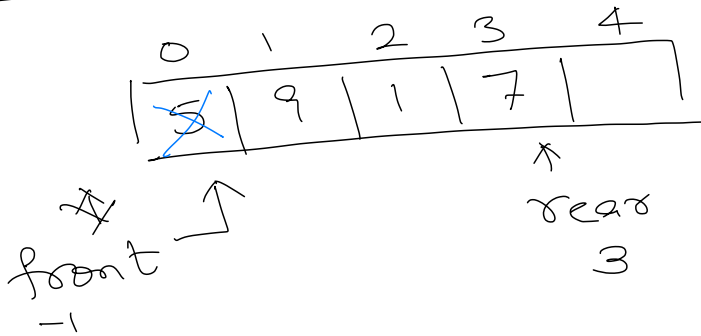
if front equals -1 AND  
rear equals last element then  
queue full

Delete Q() → 2

Add Q(10) → ~~Queue is full.~~



# Linear Queue



## Delete Q()

- Move front to next element.
- Remove element from front.
- Shift all elements of queue to left by 1 place.  
↓  
This is done to avoid condition that queue is empty as well as full.  
In efficient way.

OR

- if queue is empty AND queue is full then
  - Reset front and rear  
 $\text{front} = -2, \text{rear} = -1.$

<del>5</del>	<del>7</del>	<del>3</del>
0	1	2

Add Q(5)  
Add Q(7)  
Add Q(3)

front  $\rightarrow$  ~~1~~ ~~0~~ ~~2~~ 2  
rear  $\rightarrow$  ~~1~~ ~~0~~ ~~2~~ 2  $\Leftarrow$  Queue is full.

$\Rightarrow$  Queue is empty.

Delete Q()  $\Rightarrow$  5  
Delete Q()  $\Rightarrow$  7  
Delete Q()  $\Rightarrow$  3

```

class C1 {
data member
member functions    F1();
}

```

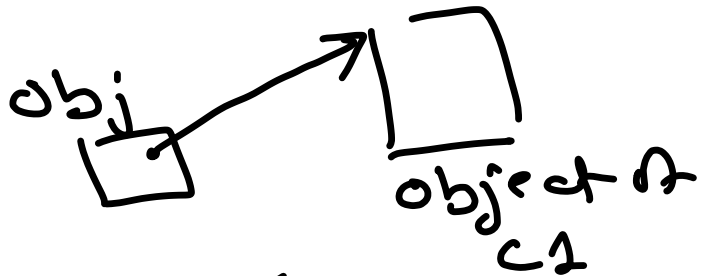
C1 obj;

$\rightarrow$  variable that stores reference to object of class.



obj.F1(); ← Null Pointer Exception.

obj = new C1();



obj.F1(); ✓

---

```
class Stack {  
    public void Push(int)  
    public int Pop() { ... }  
};
```

3

Defining Stack  
as ADT



```
interface Stack Intf {  
    public void Push(int);  
    public int Pop();  
};
```

7

class Stack Using Array  
implements StackIntf

{  
:  
}

3  
Reverse (int [] elements,  
StackIntf stack)  
{  
stack.Push(..);  
:  
stack.Pop();  
}

}

stack  
[ ] →

obj = new Stack Using Array();  
Reverse (arr, obj);

---

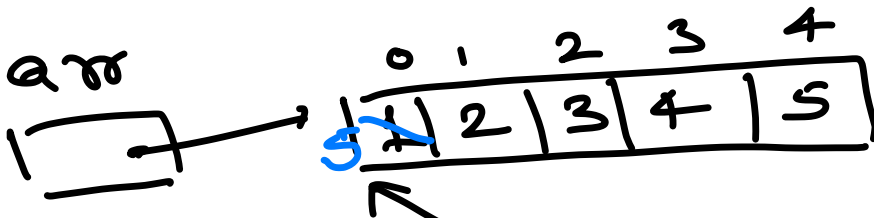
main()

int [] arr = { 1, 2, ..., 5 };

Reverse (arr, ... );

⋮

}

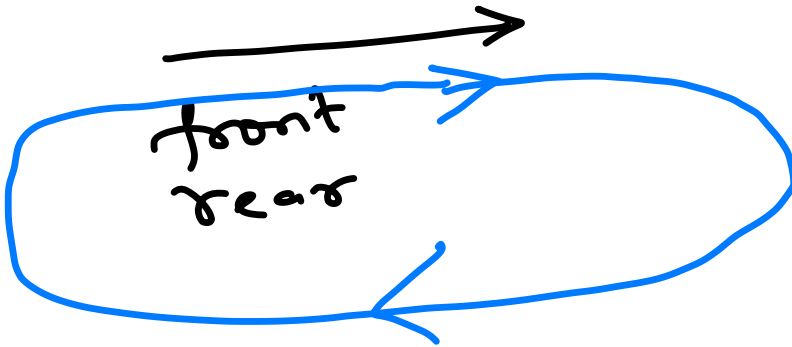
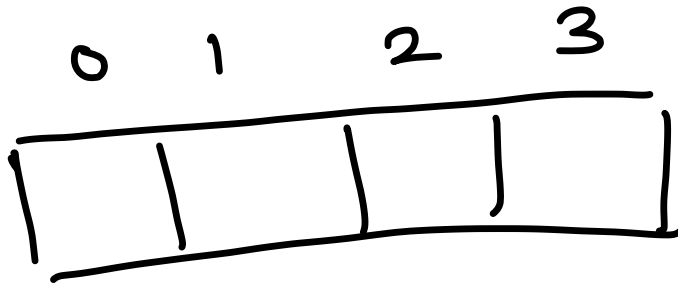


OR

Reverse (int [] elements, ... ) {  
elements [0] = 5;

}

int [] arr;  
arr = new int [5];  
arr [0] = 1; arr [2] = 3;  
arr [1] = 2; arr [3] = 4;  
arr [4] = 5;



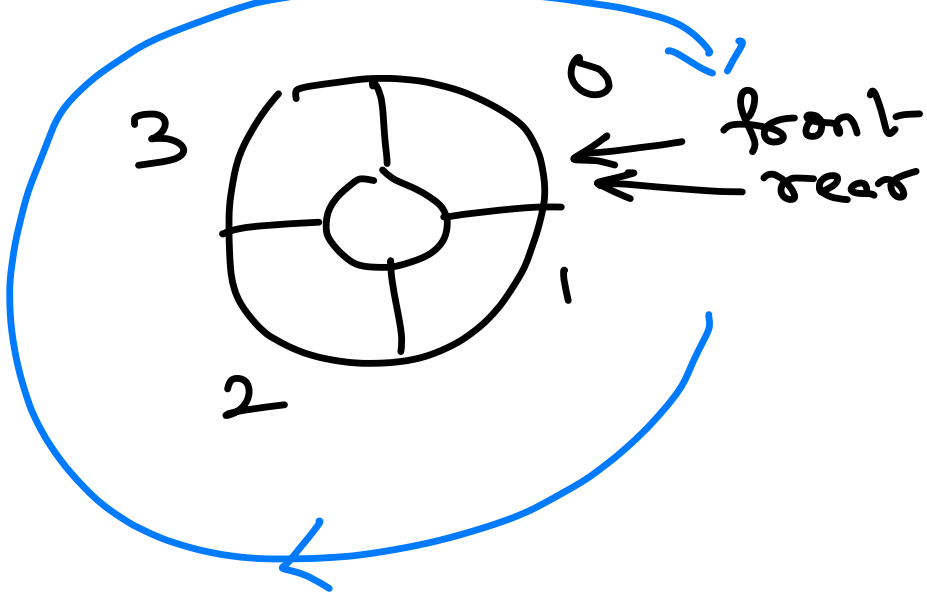
```

++ rear;
if (rear == n)
    rear = 0;

```

OR

$$rear = \frac{(rear + 1) \% n}{0..(n-1)}$$



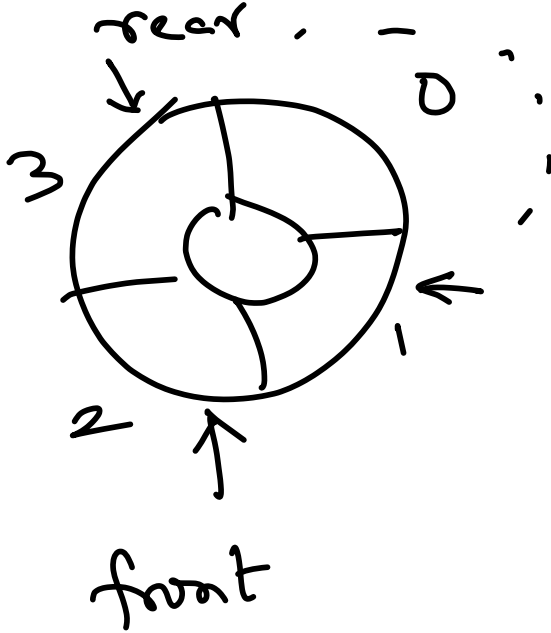
front equals rear  $\leftarrow$  Empty

rear just before front  $\leftarrow$  Full

$\Downarrow$   
 $(\text{rear} + 1) \% n$  equals front

new with [4].

0	1	2	3	...
1	1	1	1	...



① Check for balanced parenthesis.

$$\begin{array}{c} ( ) ( ) \\ \hline ( [ ) ] \end{array} \checkmark$$

$$\begin{array}{c} ) ( \\ \hline ( [ ] ) \end{array} \checkmark$$

Hint: use stack.

boolean IsBalanced (String str)

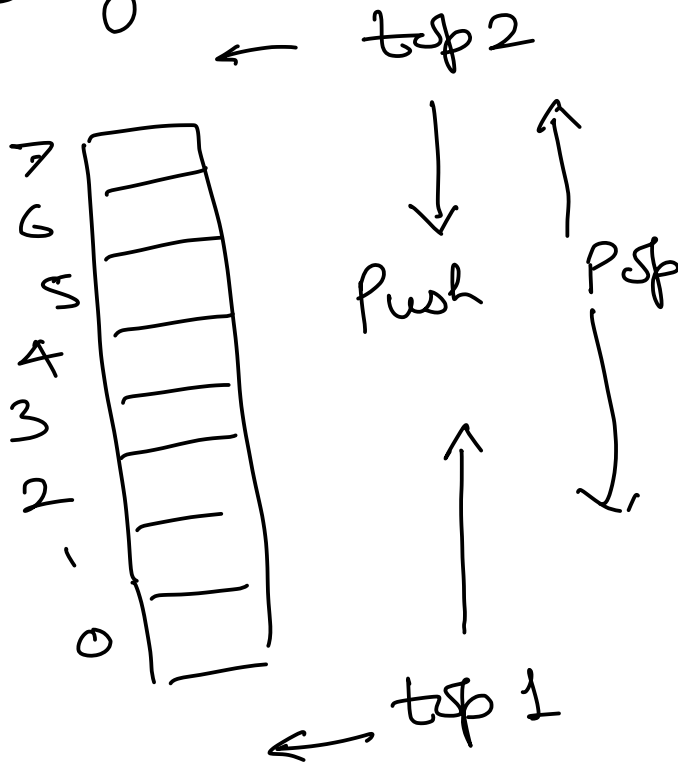
\* ② Implement Stack using Queue.

\* ③ Implement Queue using Stack.

Hint: ② will need two queues.

③ will need two stacks.

④ Implement 2 Stacks in a single array.



# Linked list

## Array : Need?

When we need to store multiple elements.

And do same processing on those elements.

Properties of array:

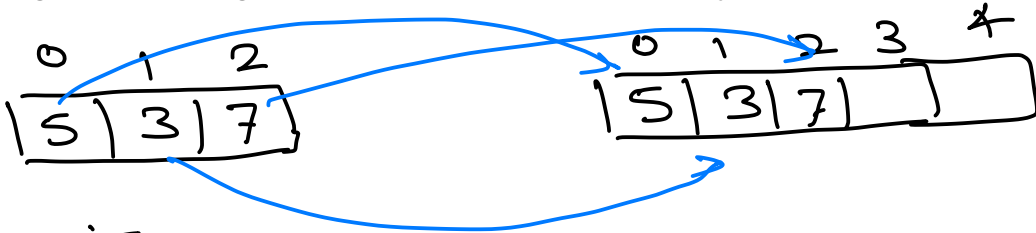
- Data structure that stores multiple elements, all of the **same type**.
- All elements of an array are **stored sequentially** in memory, one after another.

Advantages of array:

- Efficient lookup OR **Random access**.
- Efficient in adding or removing elements **at the end of array**.

Disadvantages of array

- **Fixed size**. Resizing of array is inefficient.
- **Inserting and deleting** of elements, in middle of array is inefficient.



Resize

→ Create a larger array

|| → Copy values from existing array to new one.

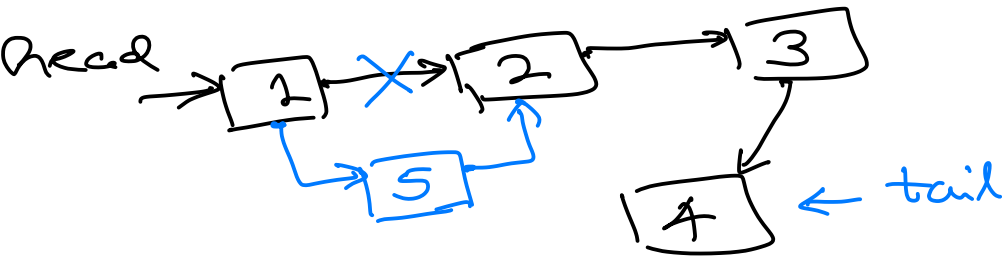
→ Release old memory.



Initial array Size = 1000 copy 1000 elem.  
Resized array Size = 2000  
Resized array Size = 4000 copy 2000 elements

Linked list → Do not store elements next to each other.

0	1	2	3	4
1	2	3	4	



Properties of linked list

- Stores data as a chain of **nodes**.
- Each node contains **data** and a **pointer** to next node in chain.
- We need to know where first node is of list - **head**.

→ where data is stored.

Advantages of linked list

- Can easily grow / shrink in size.
- Efficient in insertion and deletion of elements.

## Disadvantages of linked list

- Random access is inefficient.

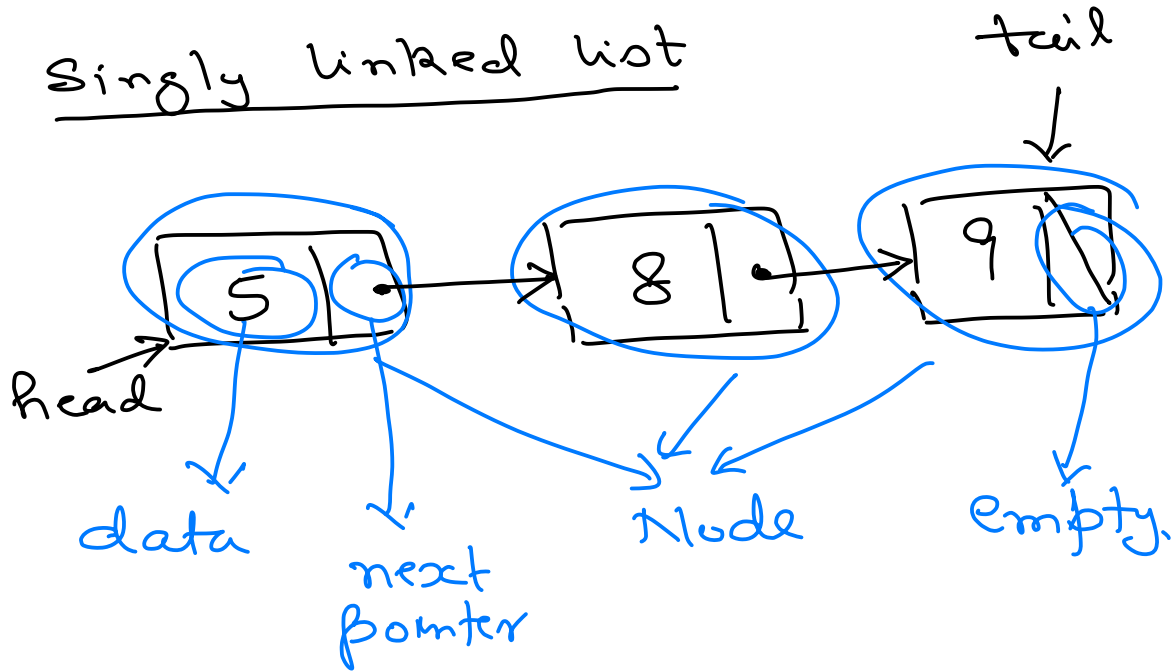
## Types of linked list

- Singly linked list (Uni-directional)
- Doubly linked list (Bi-directional)
- Circular list.

One node keeps track of one neighbour only.

Each node keeps track of both of its neighbours

## Singly linked list



## Traversal

Starting from first element, access each element one at a time, till the last element.

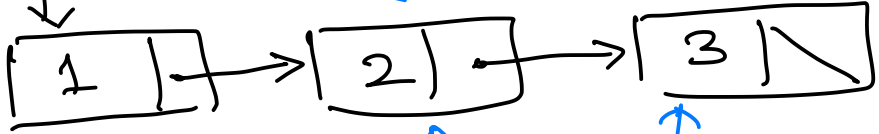
Traversal.

```
for ( i = 0; i < elements.length; ++i )  
    stack.Push (elements[i]);
```

- ① what if list is empty?
- ② what if list is not empty?

head  $\rightarrow$  empty  $\Leftarrow$  list is empty.

head  $\rightarrow$    $\Leftarrow$  list is not empty



$\swarrow$   $\nwarrow$   $\nearrow$   
 \* current  
 \* empty

o/p: 1 2 3

Traversal of singly list

- if list is empty then Stop.
- Set current to first node of list.
- while (current is not empty) do
  - Process current node.
  - Move current to current node's next.
- Stop.

Traversal of singly list (Optimised)

- Set current to first node of list.
- while (current is not empty) do
  - Process current node.
  - Move current to current node's next.
- Stop.