

## Lecture 4: Nonideal Transistor Theory

### Outline

- ❑ Nonideal Transistor Behavior
  - High Field Effects
    - Mobility Degradation
    - Velocity Saturation
  - Channel Length Modulation
  - Threshold Voltage Effects
    - Body Effect
    - Drain-Induced Barrier Lowering
    - Short Channel Effect
  - Leakage
    - Subthreshold Leakage
    - Gate Leakage
    - Junction Leakage
- ❑ Process and Environmental Variations

# Ideal Transistor I-V

□ Shockley long-channel transistor models

$$I_{ds} = \begin{cases} 0 & V_{gs} < V_t & \text{cutoff} \\ \beta \left( V_{gs} - V_t - \frac{V_{ds}}{2} \right) V_{ds} & V_{ds} < V_{dsat} & \text{linear} \\ \frac{\beta}{2} (V_{gs} - V_t)^2 & V_{ds} > V_{dsat} & \text{saturation} \end{cases}$$

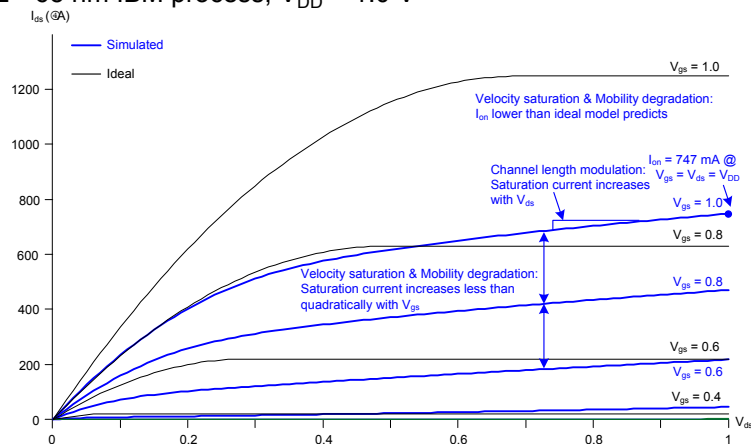
4: Nonideal Transistor Theory

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## Ideal vs. Simulated nMOS I-V Plot

□ 65 nm IBM process,  $V_{DD} = 1.0$  V



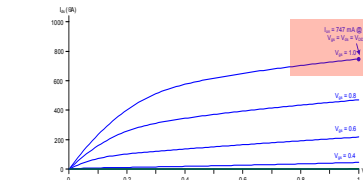
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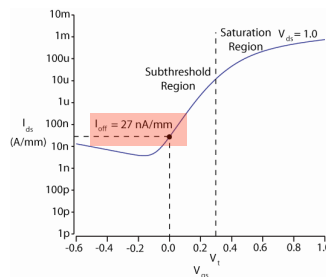
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## ON and OFF Current

- $I_{on} = I_{ds} @ V_{gs} = V_{ds} = V_{DD}$ 
  - Saturation



- $I_{off} = I_{ds} @ V_{gs} = 0, V_{ds} = V_{DD}$ 
  - Cutoff



## Electric Fields Effects

- Vertical electric field:  $E_{vert} =$  \_\_\_\_\_
  - Attracts carriers into channel
  - Long channel:  $Q_{channel} \propto E_{vert}$
- Lateral electric field:  $E_{lat} =$  \_\_\_\_\_
  - Accelerates carriers from drain to source
  - Long channel:  $v = \mu E_{lat}$

## Coffee Cart Analogy

- ❑ Tired student runs from VLSI lab to coffee cart
- ❑ Freshmen are pouring out of the physics lecture hall
- ❑  $V_{ds}$  is how long you have been up
  - Your velocity = fatigue  $\times$  mobility
- ❑  $V_{gs}$  is a wind blowing you against the glass ( $\text{SiO}_2$ ) wall
- ❑ At high  $V_{gs}$ , you are buffeted against the wall
  - *Mobility degradation*
- ❑ At high  $V_{ds}$ , you scatter off freshmen, fall down, get up
  - *Velocity saturation*
    - Don't confuse this with the saturation region

## Mobility Degradation

- ❑ High  $E_{\text{vert}}$  effectively reduces mobility
  - Collisions with oxide interface

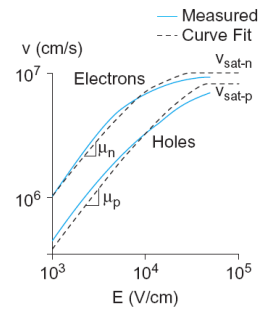
$$\mu_{\text{eff}-n} = \frac{540 \frac{\text{cm}^2}{\text{V} \cdot \text{s}}}{1 + \left( \frac{V_{gs} + V_t}{0.54 \frac{\text{V}}{\text{nm}} t_{\text{ox}}} \right)^{1.85}} \quad \mu_{\text{eff}-p} = \frac{185 \frac{\text{cm}^2}{\text{V} \cdot \text{s}}}{1 + \frac{|V_{gs} + 1.5V_t|}{0.338 \frac{\text{V}}{\text{nm}} t_{\text{ox}}}}$$

# Velocity Saturation

- At high  $E_{lat}$ , carrier velocity rolls off

- Carriers scatter off atoms in silicon lattice
- Velocity reaches  $v_{sat}$ 
  - Electrons:  $10^7$  cm/s
  - Holes:  $8 \times 10^6$  cm/s
- Better model

$$v = \begin{cases} \frac{\mu_{eff} E}{1 + \frac{E}{E_c}} & E < E_c \\ v_{sat} & E \geq E_c \end{cases} \quad E_c = \frac{2v_{sat}}{\mu_{eff}}$$



# Vel Sat I-V Effects

- Ideal transistor ON current increases with  $V_{DD}^2$

$$I_{ds} = \mu C_{ox} \frac{W}{L} \frac{(V_{gs} - V_t)^2}{2} = \frac{\beta}{2} (V_{gs} - V_t)^2$$

- Velocity-saturated ON current increases with  $V_{DD}$

$$I_{ds} = C_{ox} W (V_{gs} - V_t) v_{max}$$

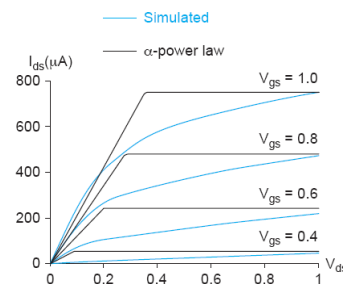
- Real transistors are partially velocity saturated
  - Approximate with  $\alpha$ -power law model
  - $I_{ds} \propto V_{DD}^\alpha$
  - $1 < \alpha < 2$  determined empirically ( $\approx 1.3$  for 65 nm)

## $\alpha$ -Power Model

$$I_{ds} = \begin{cases} 0 & V_{gs} < V_t & \text{cutoff} \\ I_{dsat} \frac{V_{ds}}{V_{dsat}} & V_{ds} < V_{dsat} & \text{linear} \\ I_{dsat} & V_{ds} > V_{dsat} & \text{saturation} \end{cases}$$

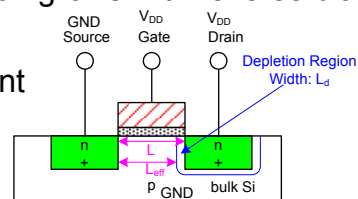
$$I_{dsat} = P_c \frac{\beta}{2} (V_{gs} - V_t)^\alpha$$

$$V_{dsat} = P_v (V_{gs} - V_t)^{\alpha/2}$$



## Channel Length Modulation

- ❑ Reverse-biased p-n junctions form a *depletion region*
  - Region between n and p with no carriers
  - Width of depletion  $L_d$  region grows with reverse bias
  - $L_{eff} = L - L_d$
- ❑ Shorter  $L_{eff}$  gives \_\_\_\_\_ current
  - $I_{ds}$  \_\_\_\_\_ with  $V_{ds}$
  - Even in saturation



## Channel Length Mod I-V

$$I_{ds} = \frac{\beta}{2} (V_{gs} - V_t)^2 (1 + \lambda V_{ds})$$

- $\lambda$  = *channel length modulation coefficient*
  - not feature size
  - Empirically fit to I-V characteristics

## Threshold Voltage Effects

- $V_t$  is  $V_{gs}$  for which the channel starts to invert
- Ideal models assumed  $V_t$  is constant
- Really depends (weakly) on almost everything else:
  - Body voltage: *Body Effect*
  - Drain voltage: *Drain-Induced Barrier Lowering*
  - Channel length: *Short Channel Effect*

## Body Effect

- ❑ Body is a fourth transistor terminal
- ❑  $V_{sb}$  affects the charge required to invert the channel
  - Increasing  $V_s$  or decreasing  $V_b$  increases  $V_t$

$$V_t = V_{t0} + \gamma (\sqrt{\phi_s + V_{sb}} - \sqrt{\phi_s})$$

- ❑  $\phi_s$  = *surface potential* at threshold

$$\phi_s = 2V_T \ln \frac{N_A}{n_i}$$

- Depends on doping level  $N_A$
- And intrinsic carrier concentration  $n_i$

- ❑  $\gamma$  = *body effect coefficient*

$$\gamma = \frac{t_{ox}}{\epsilon_{ox}} \sqrt{2q\epsilon_{si}N_A} = \frac{\sqrt{2q\epsilon_{si}N_A}}{C_{ox}}$$

## Body Effect Cont.

- ❑ For small source-to-body voltage, treat as linear

$$V_t = V_{t0} + k_\gamma V_{sb}$$

$$k_\gamma = \frac{\gamma}{2\sqrt{\phi_s}} = \frac{\sqrt{\frac{q\epsilon_{si}N_A}{\psi_T \ln \frac{N_A}{n_i}}}}{2C_{ox}}$$

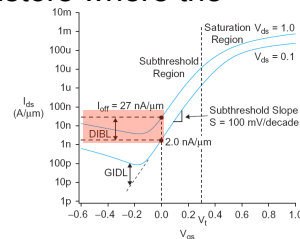


# DIBL

- ❑ Electric field from drain affects channel
- ❑ More pronounced in small transistors where the drain is closer to the channel
- ❑ Drain-Induced Barrier Lowering
  - Drain voltage also affect  $V_t$

$$V_t' = V_t - \eta V_{ds}$$

- ❑ High drain voltage causes current to \_\_\_\_\_



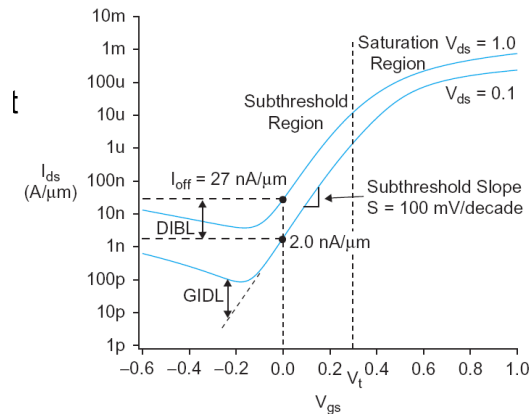
# Short Channel Effect

- ❑ In small transistors, source/drain depletion regions extend into the channel
  - Impacts the amount of charge required to invert the channel
  - And thus makes  $V_t$  a function of channel length
- ❑ Short channel effect:  $V_t$  increases with  $L$ 
  - Some processes exhibit a reverse short channel effect in which  $V_t$  decreases with  $L$

# Leakage

- ❑ What about current in cutoff?
- ❑ Simulated results
- ❑ What differs?

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# Leakage Sources

- ❑ Subthreshold conduction
  - Transistors can't abruptly turn ON or OFF
  - Dominant source in contemporary transistors
- ❑ Gate leakage
  - Tunneling through ultrathin gate dielectric
- ❑ Junction leakage
  - Reverse-biased PN junction diode current

# Subthreshold Leakage

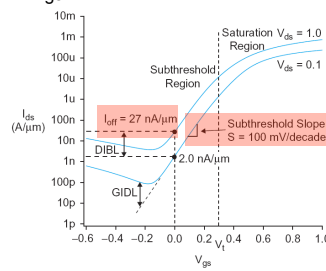
- Subthreshold leakage exponential with  $V_{gs}$

$$I_{ds} = I_{ds0} e^{\frac{V_{gs} - V_{t0} + \eta V_{ds} - k_f V_{sb}}{nV_T}} \left( 1 - e^{-\frac{V_{ds}}{V_T}} \right)$$

- $n$  is process dependent
  - typically 1.3-1.7
- Rewrite relative to  $I_{off}$  on log scale

$$I_{ds} = I_{off} 10^{\frac{V_{gs} + \eta(V_{ds} - V_{dd}) - k_f V_{sb}}{S}} \left( 1 - e^{-\frac{V_{ds}}{v_t}} \right) \quad S = \left[ \frac{d(\log_{10} I_{ds})}{dV_{gs}} \right]^{-1} = n v_t \ln 10$$

- $S \approx 100$  mV/decade @ room temperature



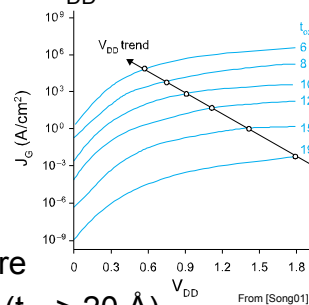
# Gate Leakage

- Carriers tunnel through very thin gate oxides
- Exponentially sensitive to  $t_{ox}$  and  $V_{DD}$

$$I_{gate} = WA \left( \frac{V_{DD}}{t_{ox}} \right)^2 e^{-B \frac{t_{ox}}{V_{DD}}}$$

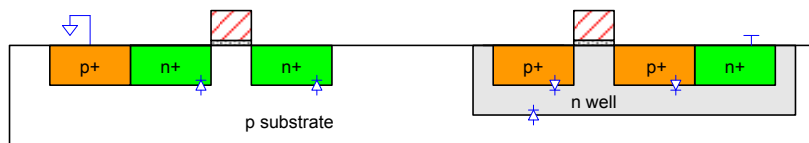
- $A$  and  $B$  are tech constants
- Greater for electrons
  - So nMOS gates leak more

- Negligible for older processes ( $t_{ox} > 20$  Å)
- Critically important at 65 nm and below ( $t_{ox} \approx 10.5$  Å)



## Junction Leakage

- ❑ Reverse-biased p-n junctions have some leakage
  - Ordinary diode leakage
  - Band-to-band tunneling (BTBT)
  - Gate-induced drain leakage (GIDL)



## Diode Leakage

- ❑ Reverse-biased p-n junctions have some leakage

$$I_D = I_s \left( e^{\frac{V_D}{V_T}} - 1 \right)$$

- ❑ At any significant negative diode voltage,  $I_D = -I_s$
- ❑  $I_s$  depends on doping levels
  - And area and perimeter of diffusion regions
  - Typically  $< 1 \text{ fA}/\mu\text{m}^2$  (negligible)

## Band-to-Band Tunneling

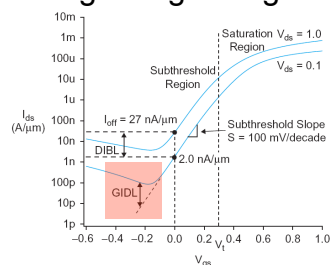
- ❑ Tunneling across heavily doped p-n junctions
  - Especially sidewall between drain & channel when *halo doping* is used to increase  $V_t$
- ❑ Increases junction leakage to significant levels

$$I_{BTBT} = W X_j A \frac{E_j}{E_g^{0.5}} V_{dd} e^{-B \frac{E_g^{1.5}}{E_j}} \quad E_j = \sqrt{\frac{2q N_{halo} N_{sd}}{\epsilon (N_{halo} + N_{sd})}} \left( V_{DD} + v_T \ln \frac{N_{halo} N_{sd}}{n_i^2} \right)$$

- $X_j$ : sidewall junction depth
- $E_g$ : bandgap voltage
- A, B: tech constants

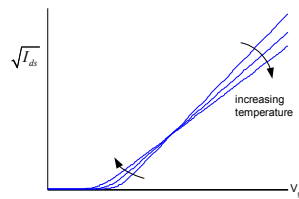
## Gate-Induced Drain Leakage

- ❑ Occurs at overlap between gate and drain
  - Most pronounced when drain is at  $V_{DD}$ , gate is at a negative voltage
  - Thwarts efforts to reduce subthreshold leakage using a negative gate voltage



## Temperature Sensitivity

- ☐ Increasing temperature
  - Reduces mobility
  - Reduces  $V_t$
- ☐  $I_{ON}$  \_\_\_\_\_ with temperature
- ☐  $I_{OFF}$  \_\_\_\_\_ with temperature



## So What?

- ☐ So what if transistors are not ideal?
  - They still behave like switches.
- ☐ But these effects matter for...
  - Supply voltage choice
  - Logical effort
  - Quiescent power consumption
  - Pass transistors
  - Temperature of operation

## Parameter Variation

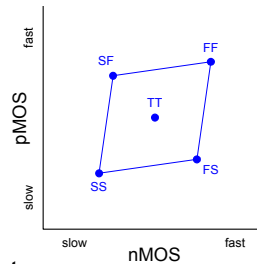
- ❑ Transistors have uncertainty in parameters
  - Process:  $L_{\text{eff}}$ ,  $V_t$ ,  $t_{\text{ox}}$  of nMOS and pMOS
  - Vary around typical (T) values

- ❑ Fast (F)

- $L_{\text{eff}}$ : \_\_\_\_\_
- $V_t$ : \_\_\_\_\_
- $t_{\text{ox}}$ : \_\_\_\_\_

- ❑ Slow (S): opposite

- ❑ Not all parameters are independent for nMOS and pMOS



## Environmental Variation

- ❑  $V_{\text{DD}}$  and  $T$  also vary in time and space

- ❑ Fast:

- $V_{\text{DD}}$ : \_\_\_\_\_
- $T$ : \_\_\_\_\_

Corner	Voltage	Temperature
F	1.98	0 C
T		
S	1.62	125 C

## Process Corners

- ❑ Process corners describe worst case variations
  - If a design works in all corners, it will probably work for any variation.
- ❑ Describe corner with four letters (T, F, S)
  - nMOS speed
  - pMOS speed
  - Voltage
  - Temperature

## Important Corners

- ❑ Some critical simulation corners include

Purpose	nMOS	pMOS	$V_{DD}$	Temp
Cycle time	⌋	⌋	⌋	⌋
Power	⌋	⌋	⌋	⌋
Subthreshold leakage	F	F	F	S