

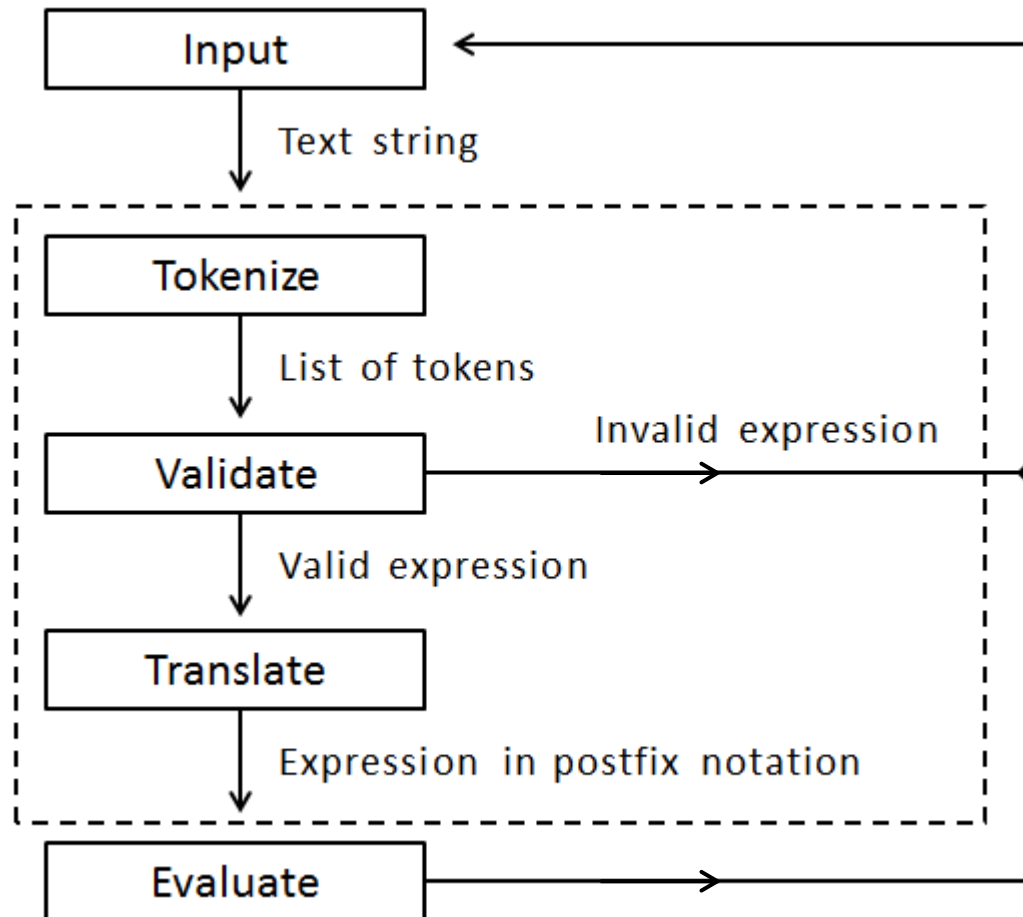
Abacus

by

Micael Loberg

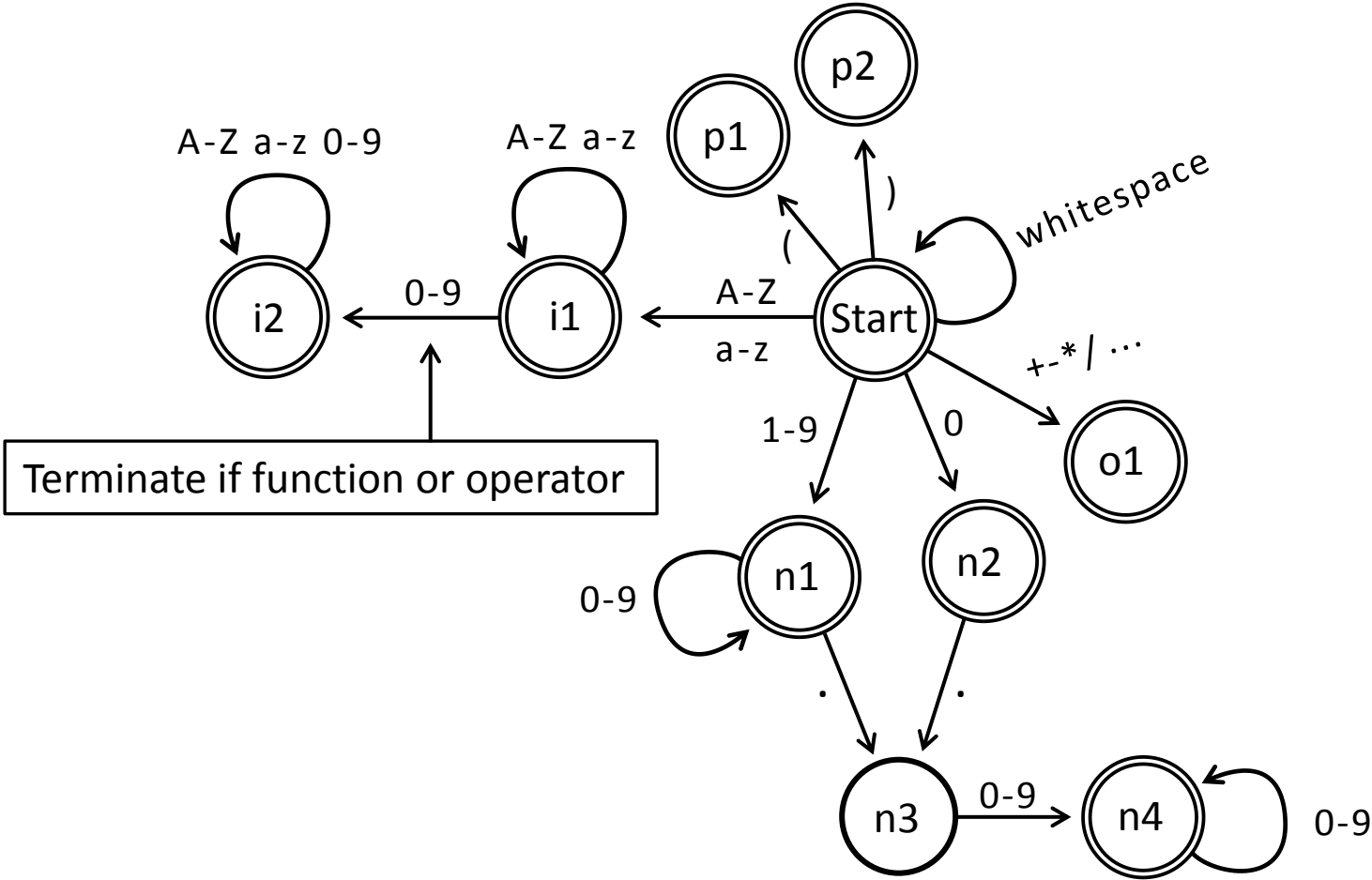
Wenting Jin

Tommy Vågratt

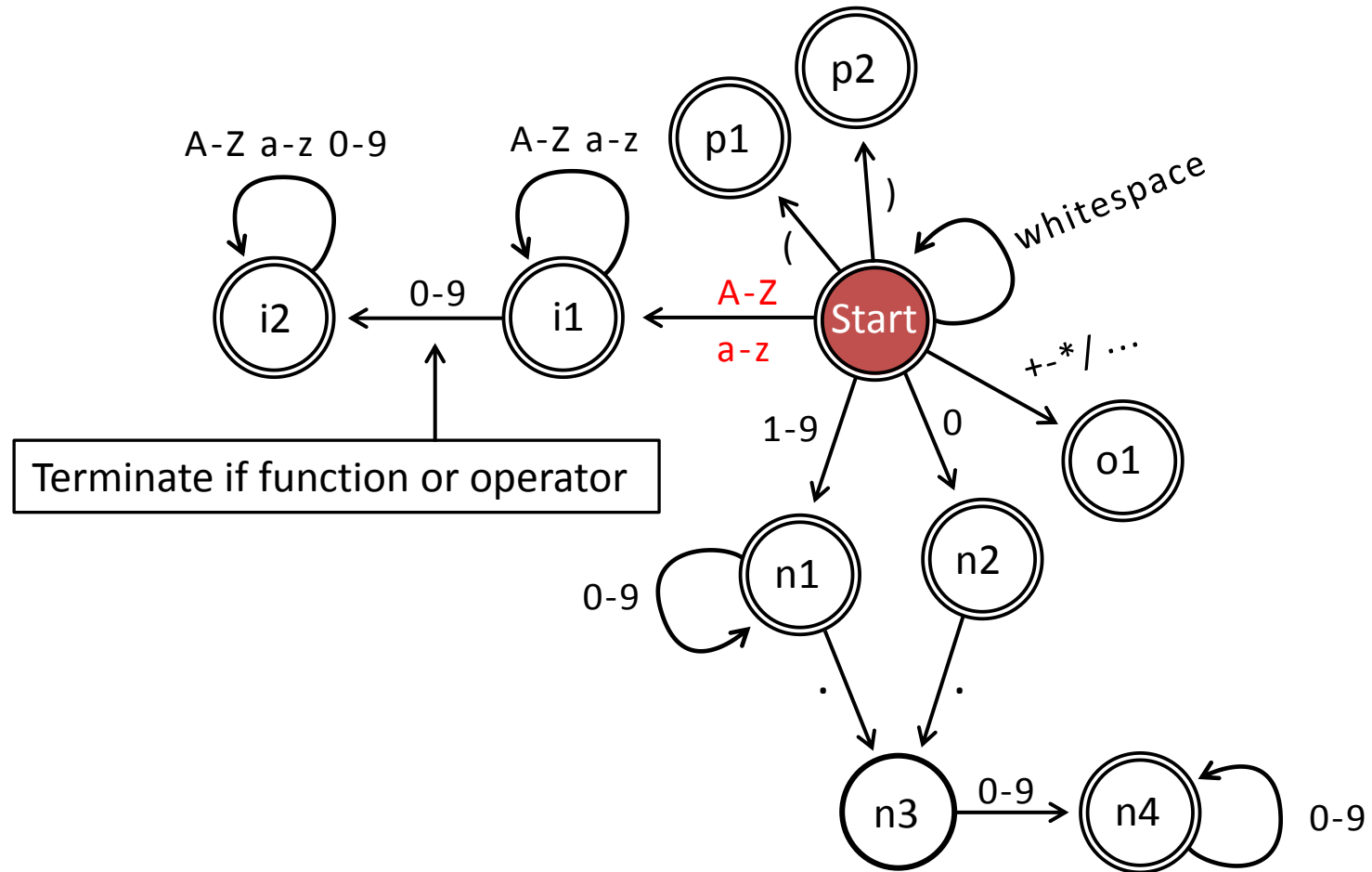


Tokenize

$x1 = -1.6 * \cos(\text{Pi})$

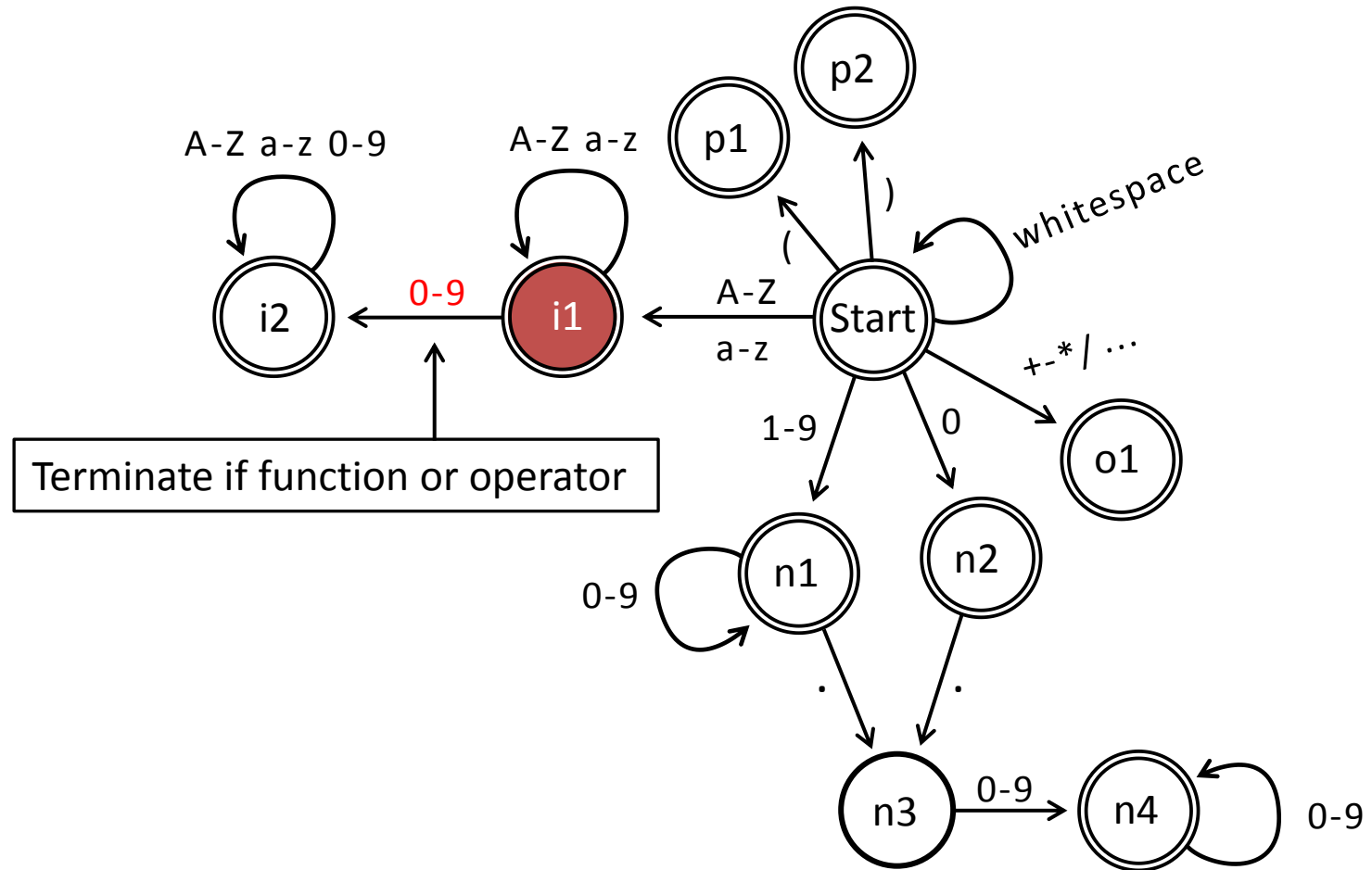


$x1 = -1.6 * \cos(\text{Pi})$
↑



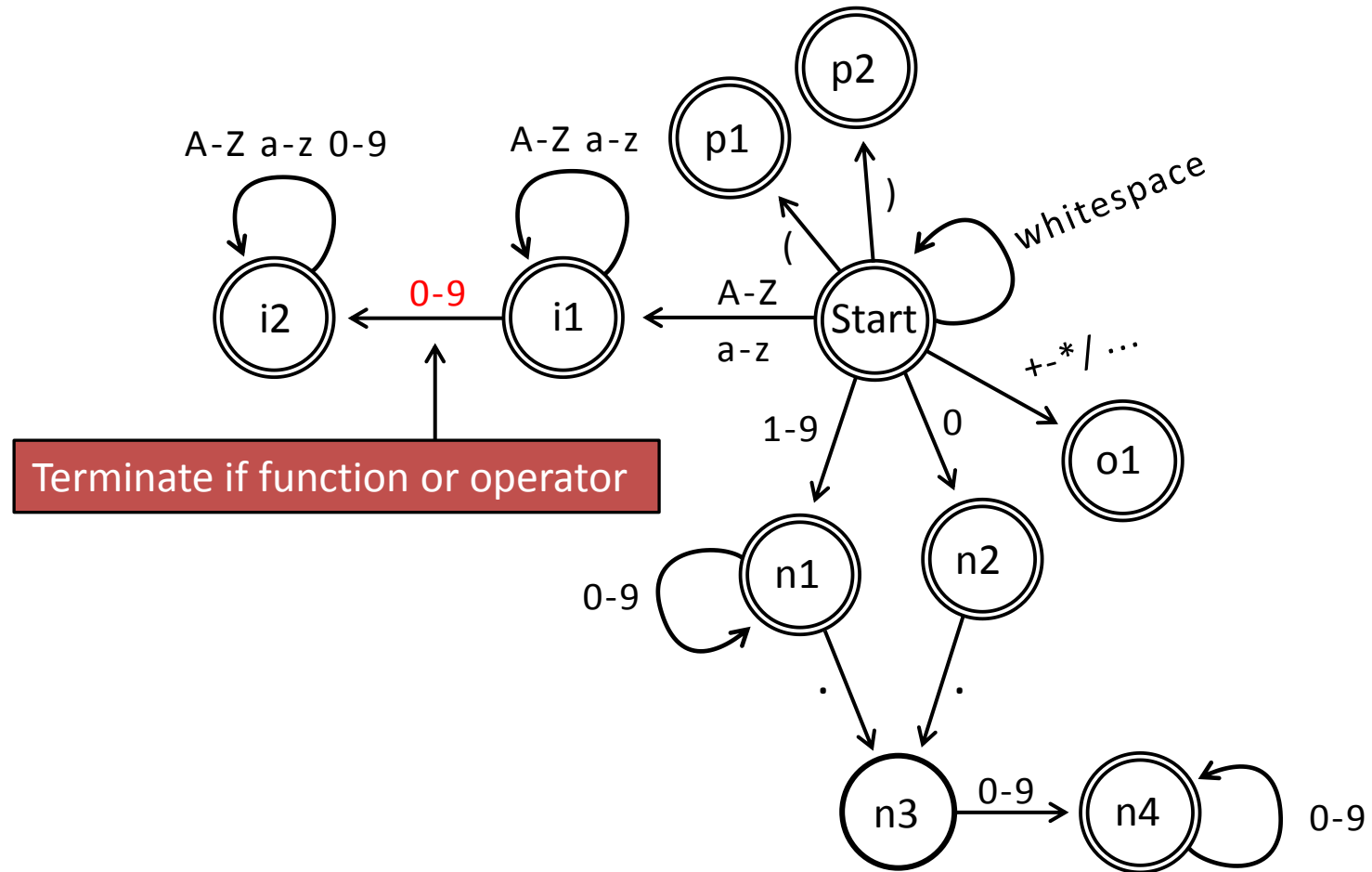
$$x\textcolor{red}{1} = -1.6 * \cos(\text{Pi})$$

↑

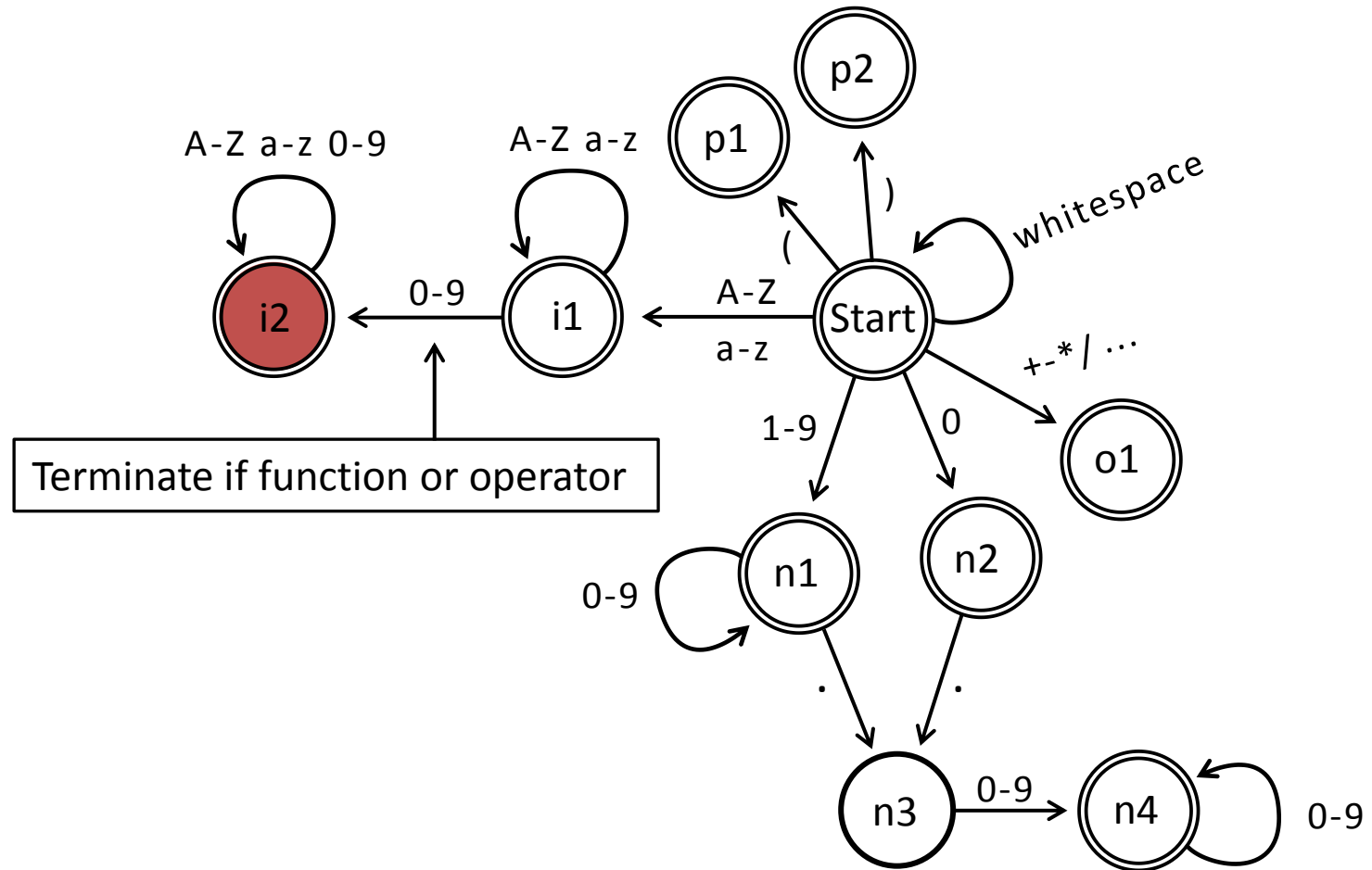


$$x\textcolor{red}{1} = -1.6 * \cos(\text{Pi})$$

↑

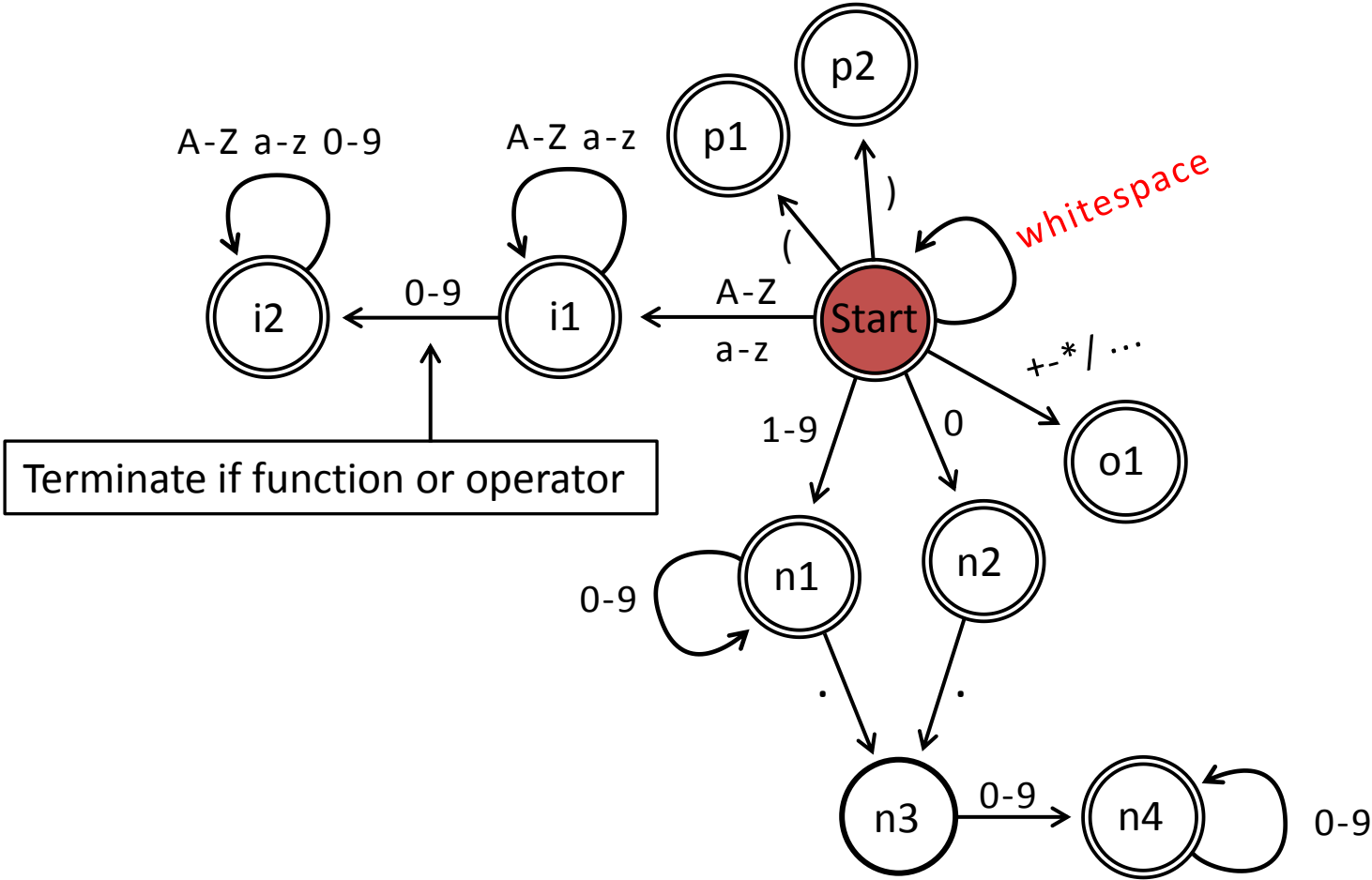


$x1_{\underline{r}} = -1.6 * \cos(\text{Pi})$
↑



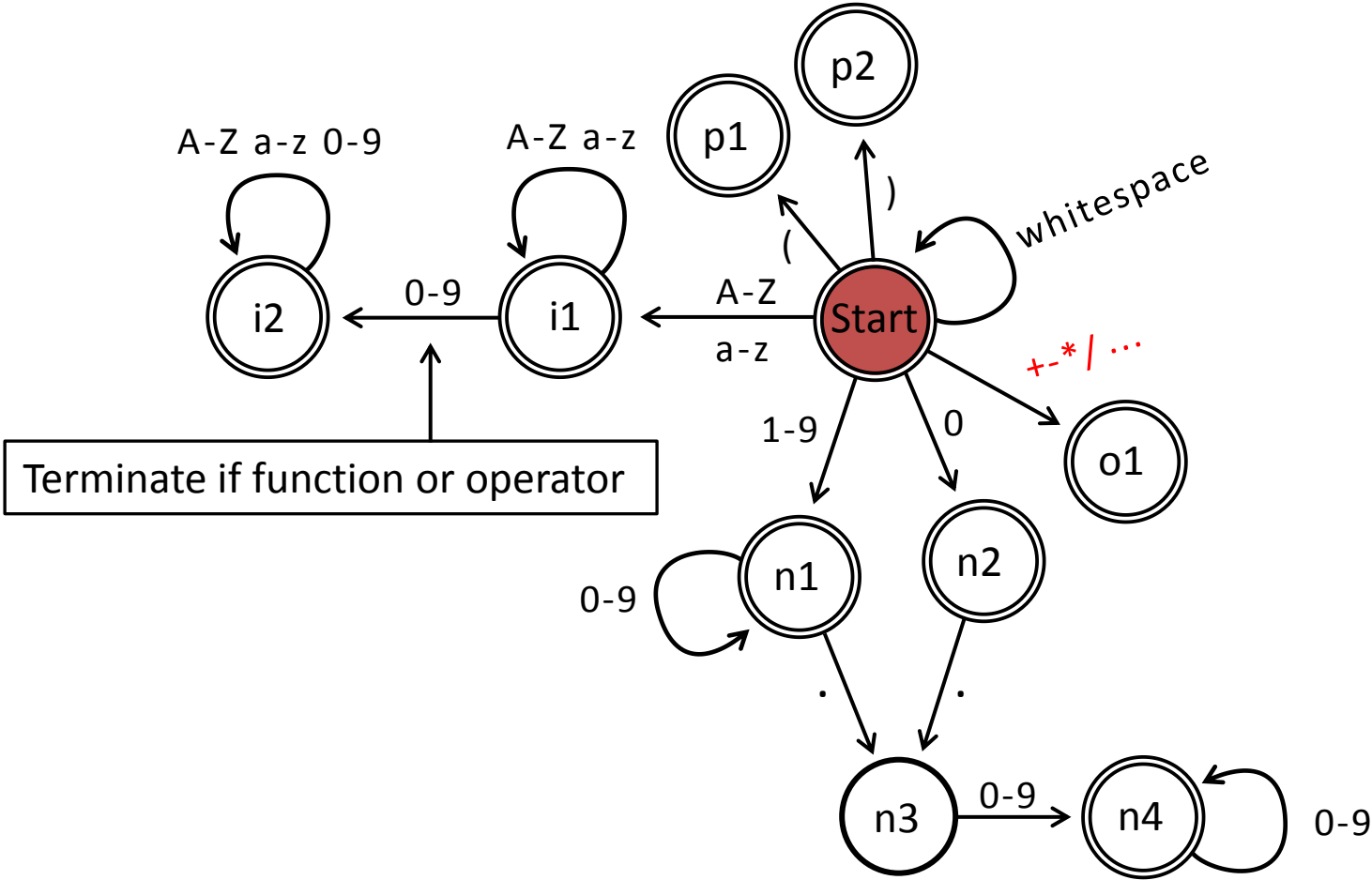
x1

$x1_{\underline{}} = -1.6 * \cos(\text{Pi})$



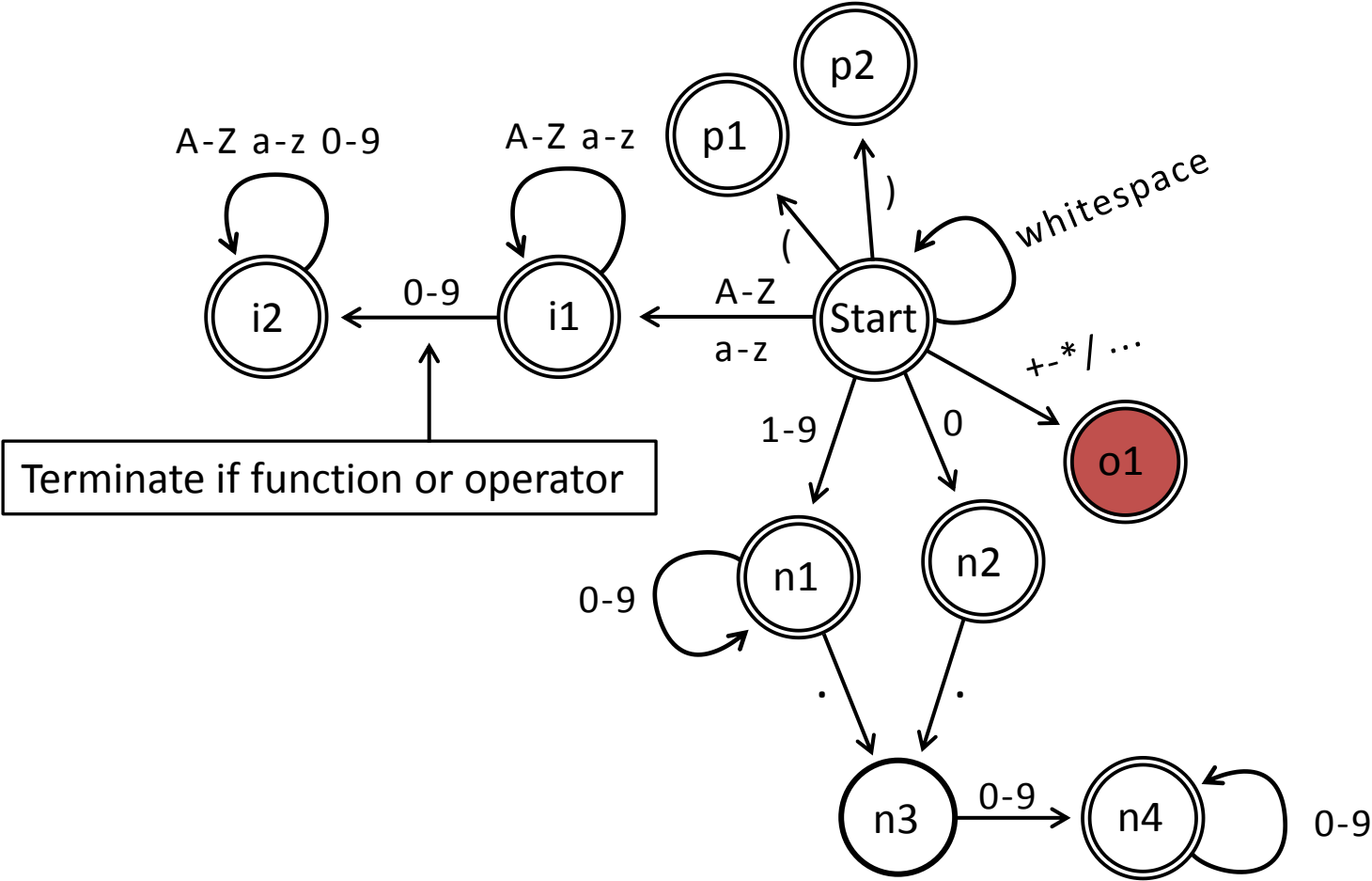
x1

$x1 = -1.6 * \cos(\text{Pi})$
↑



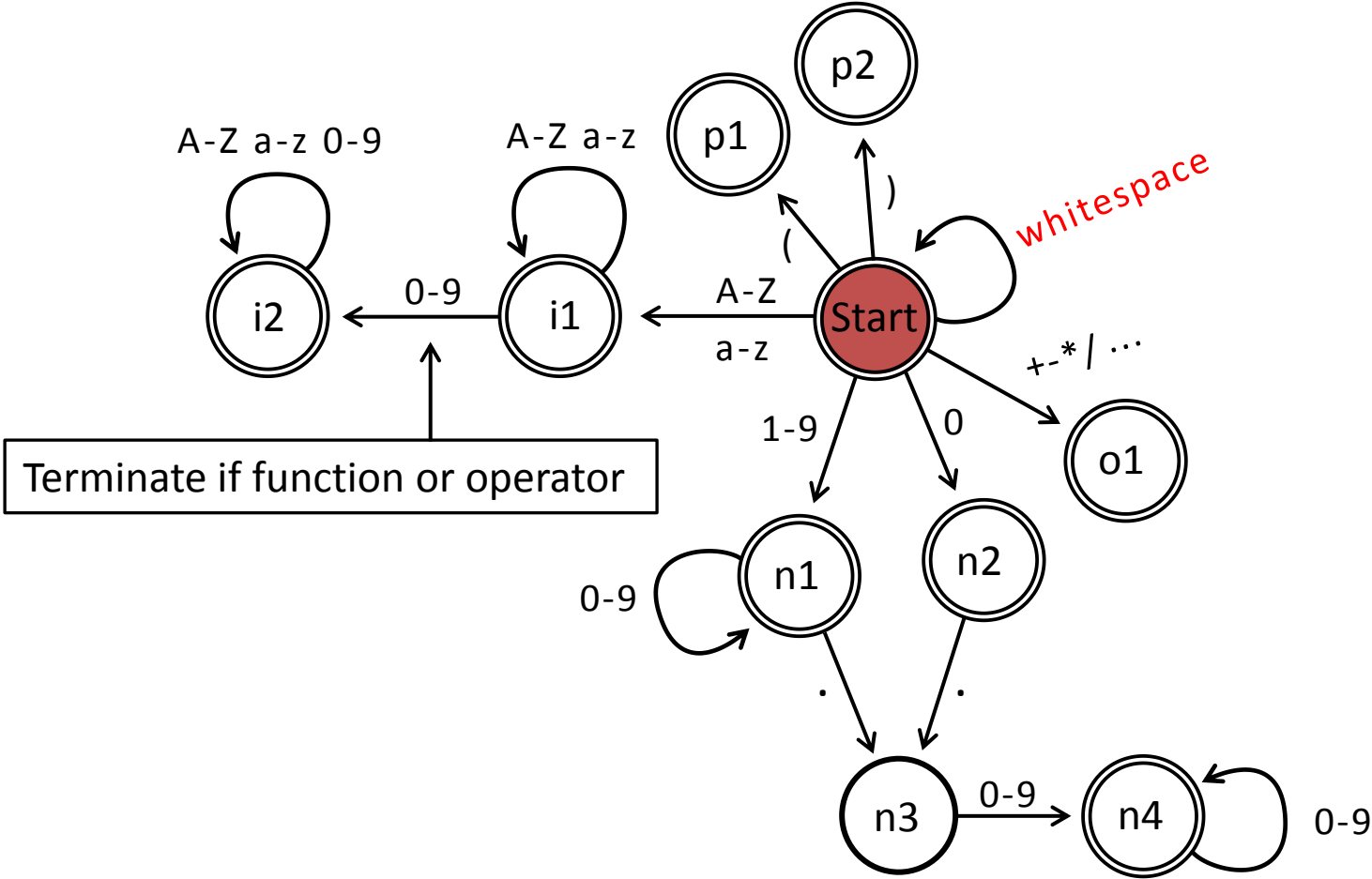
x1

$x1 = \underline{-}1.6 * \cos(\text{Pi})$



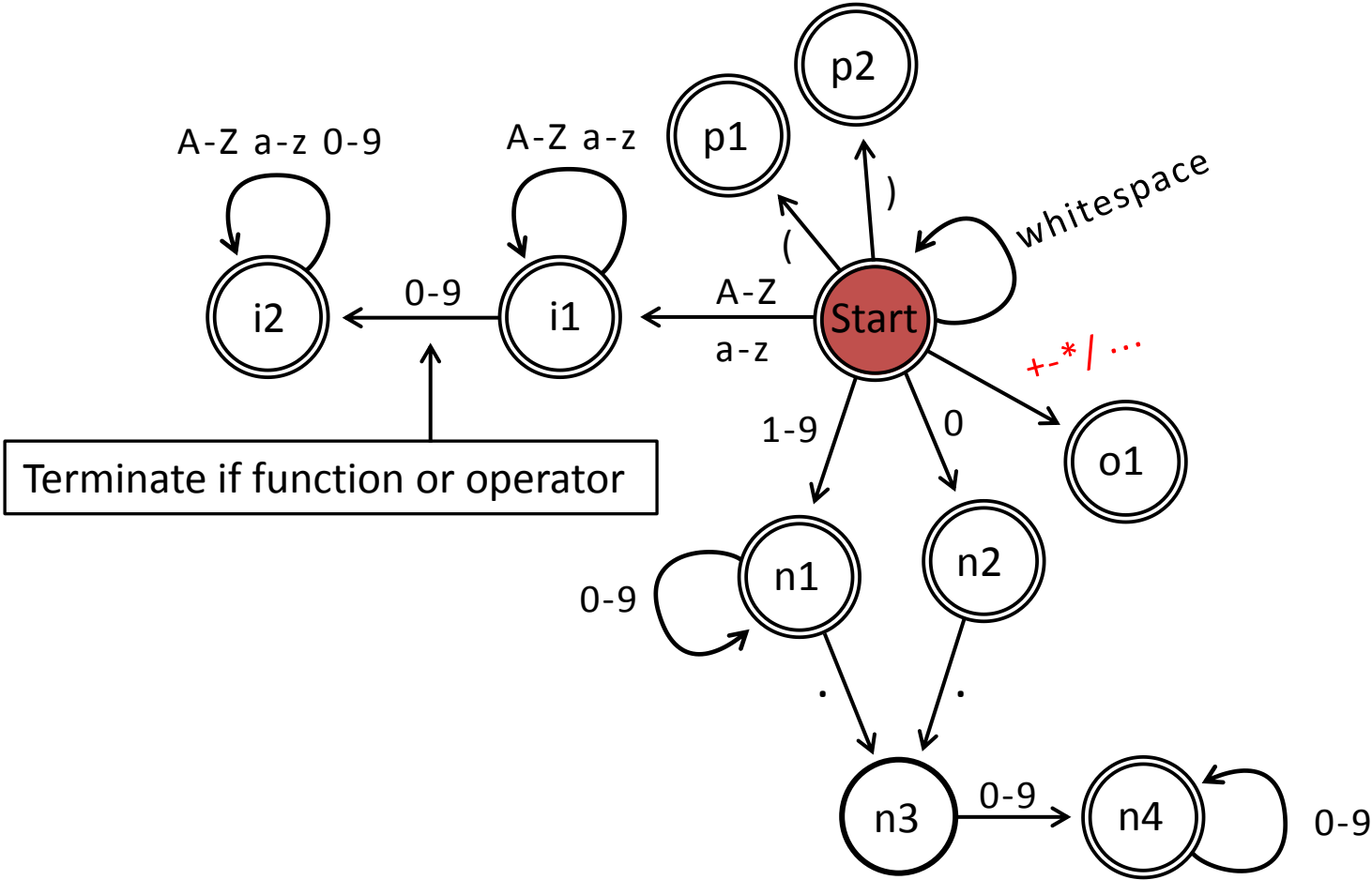
x1 =

$x1 = \underline{-} 1.6 * \cos(\text{Pi})$



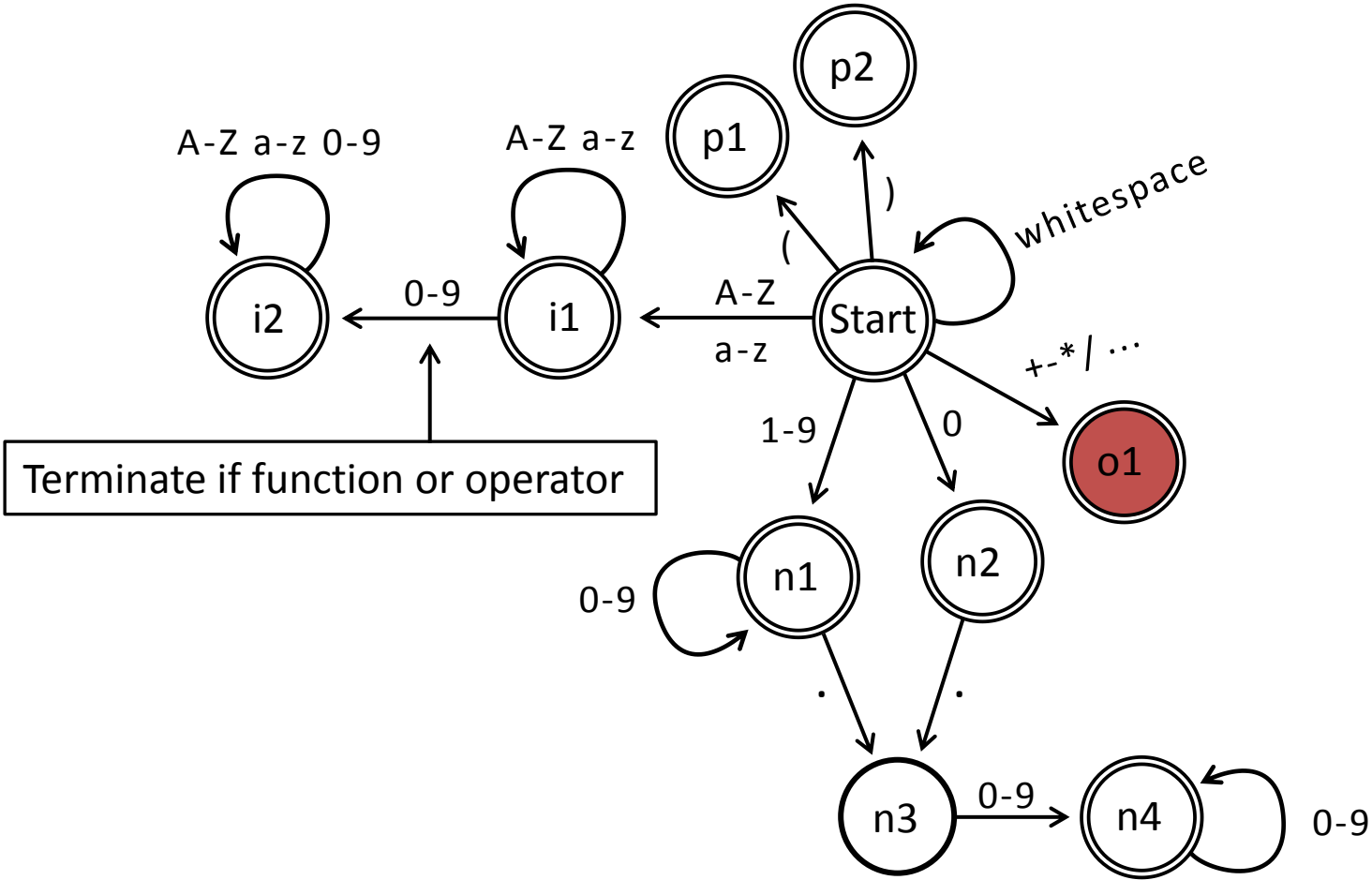
x1 =

$x1 = -1.6 * \cos(\text{Pi})$



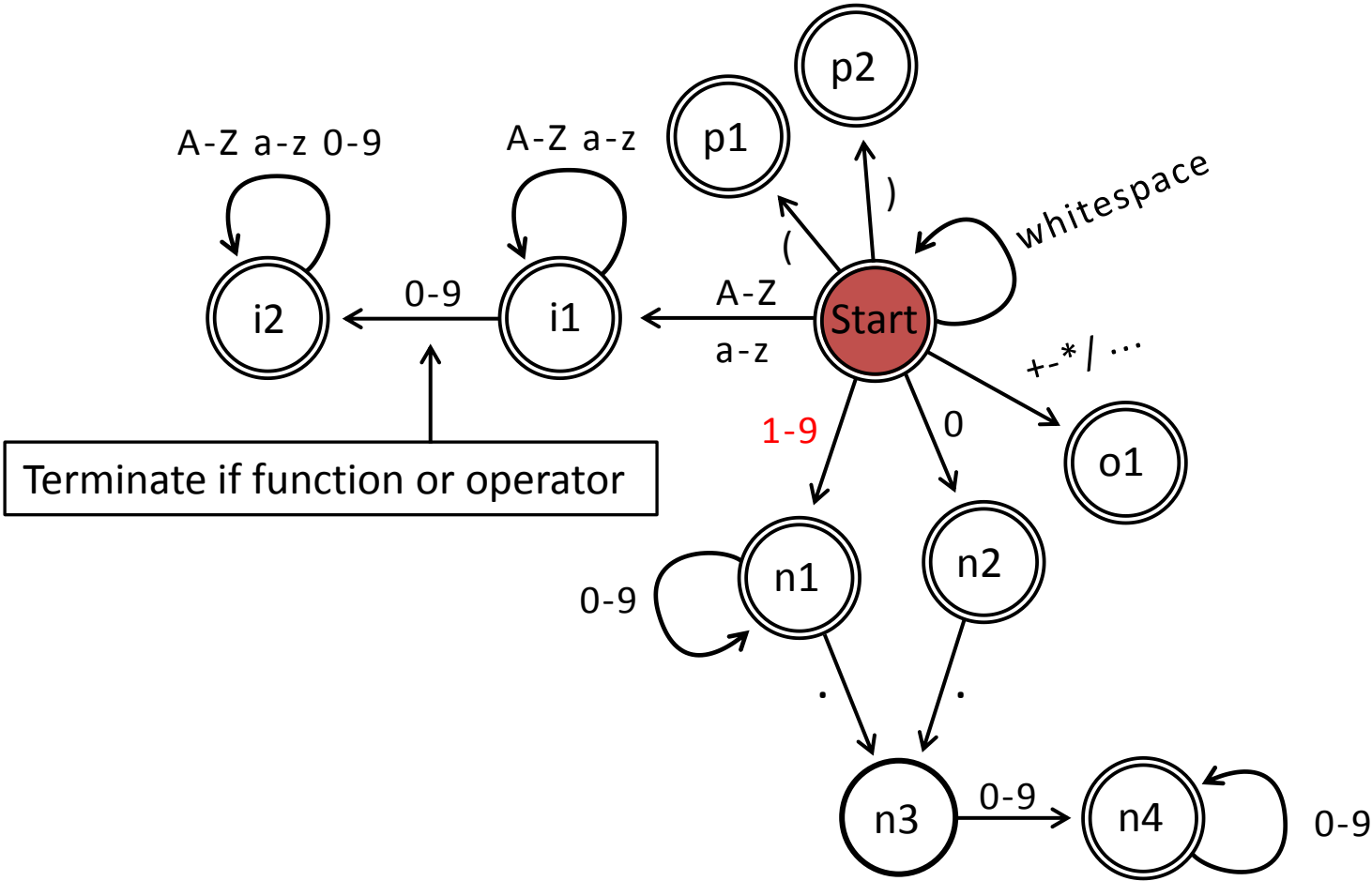
x1 =

```
x1 = -1.6 * cos(Pi)
```



```
x1 = -
```

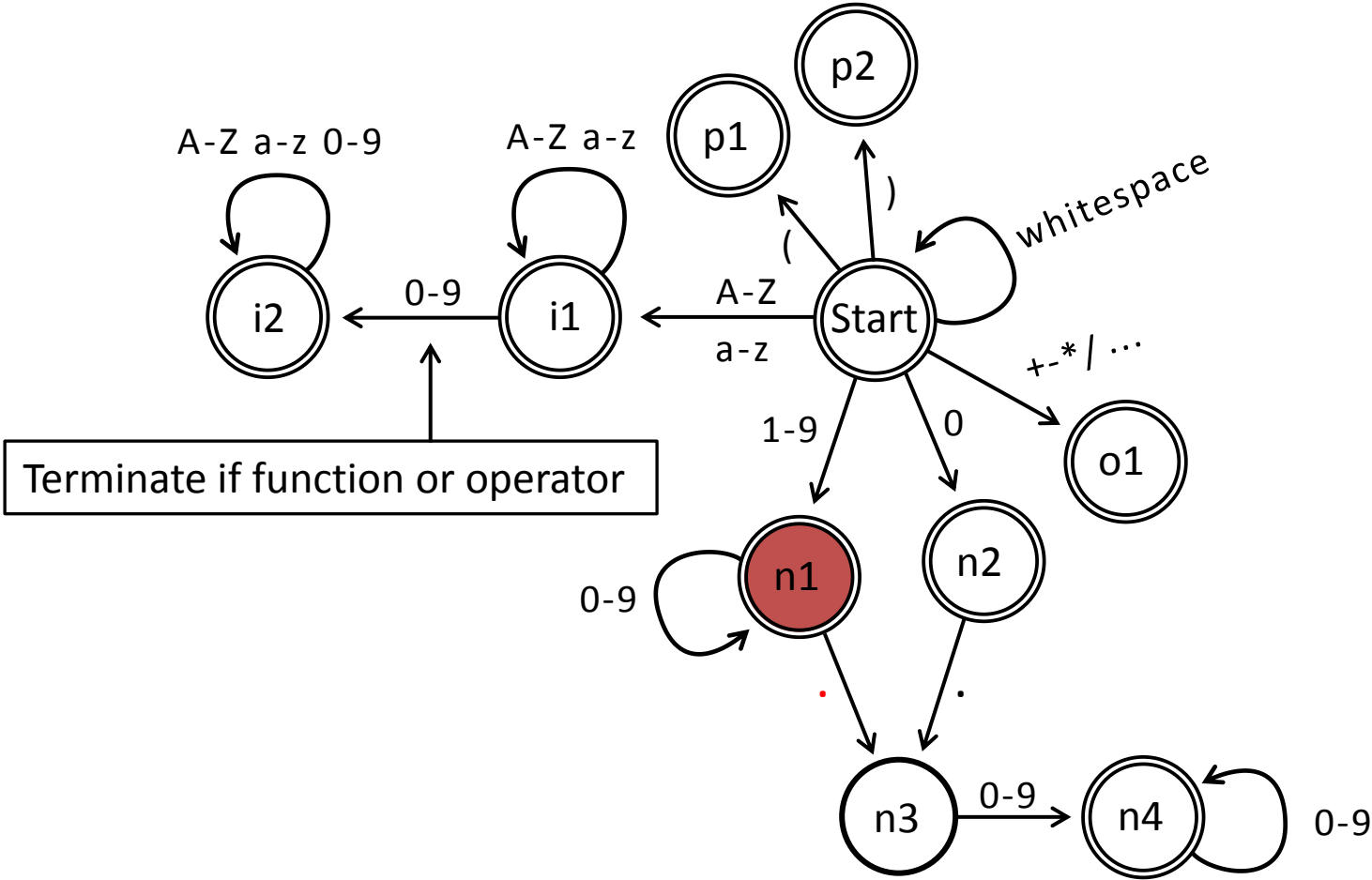
$x1 = -1.6 * \cos(\text{Pi})$



x1 = -

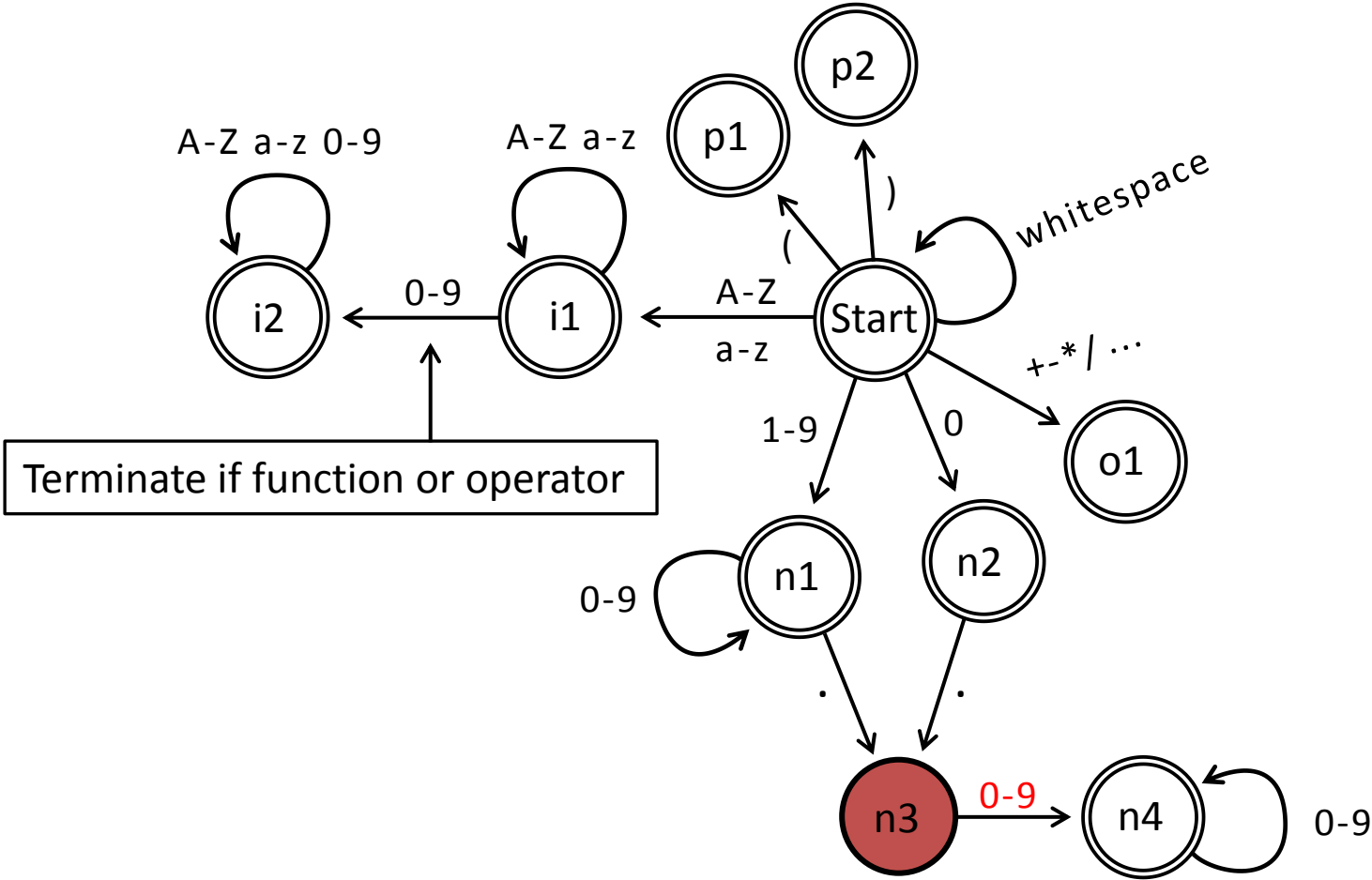
$x1 = -1.6 * \cos(\text{Pi})$

↑



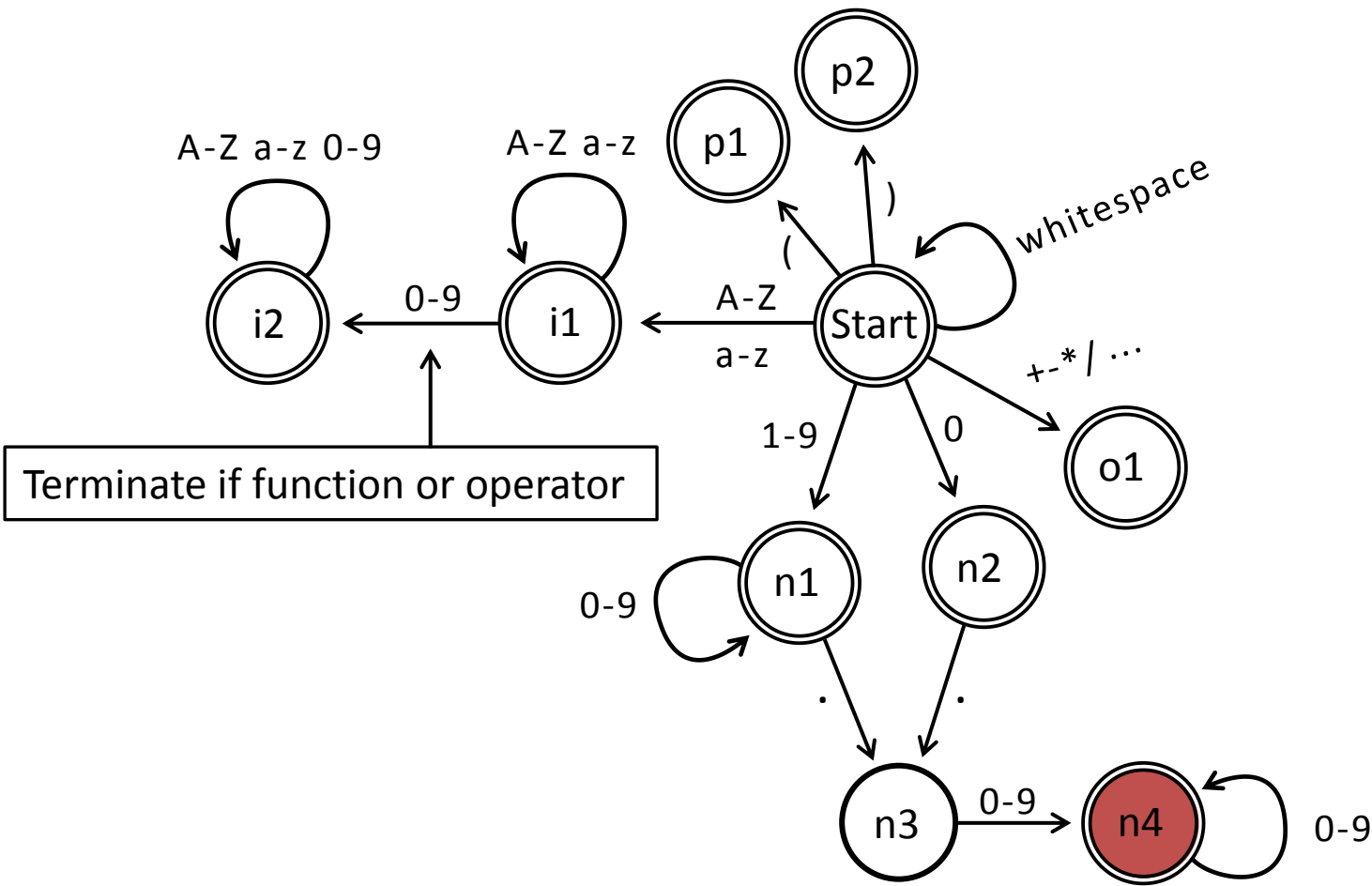
x1 = - 1


```
x1 = -1.6 * cos(Pi)
```



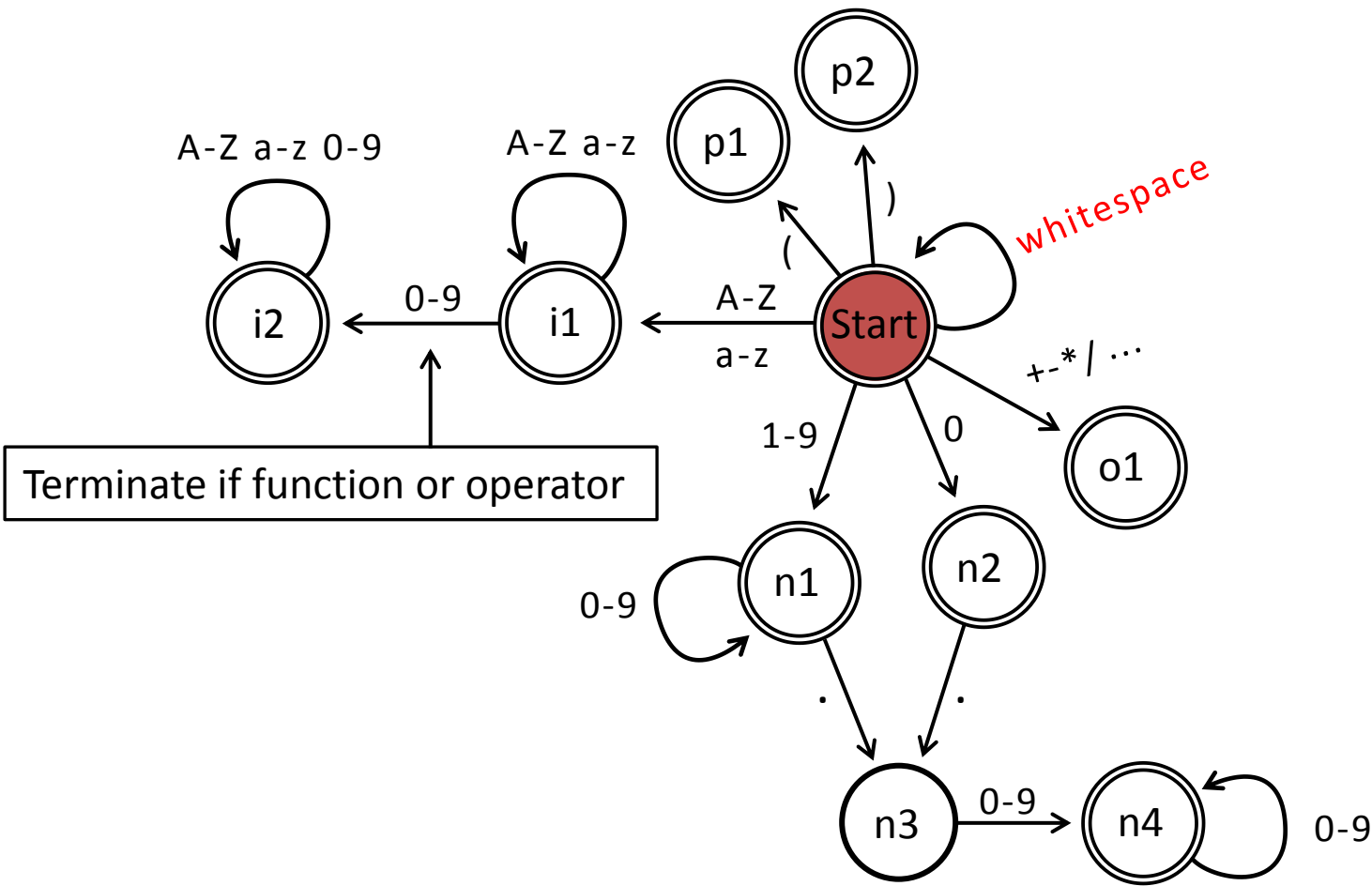
```
x1 = -1.
```

$x1 = -1.6 * \cos(\text{Pi})$



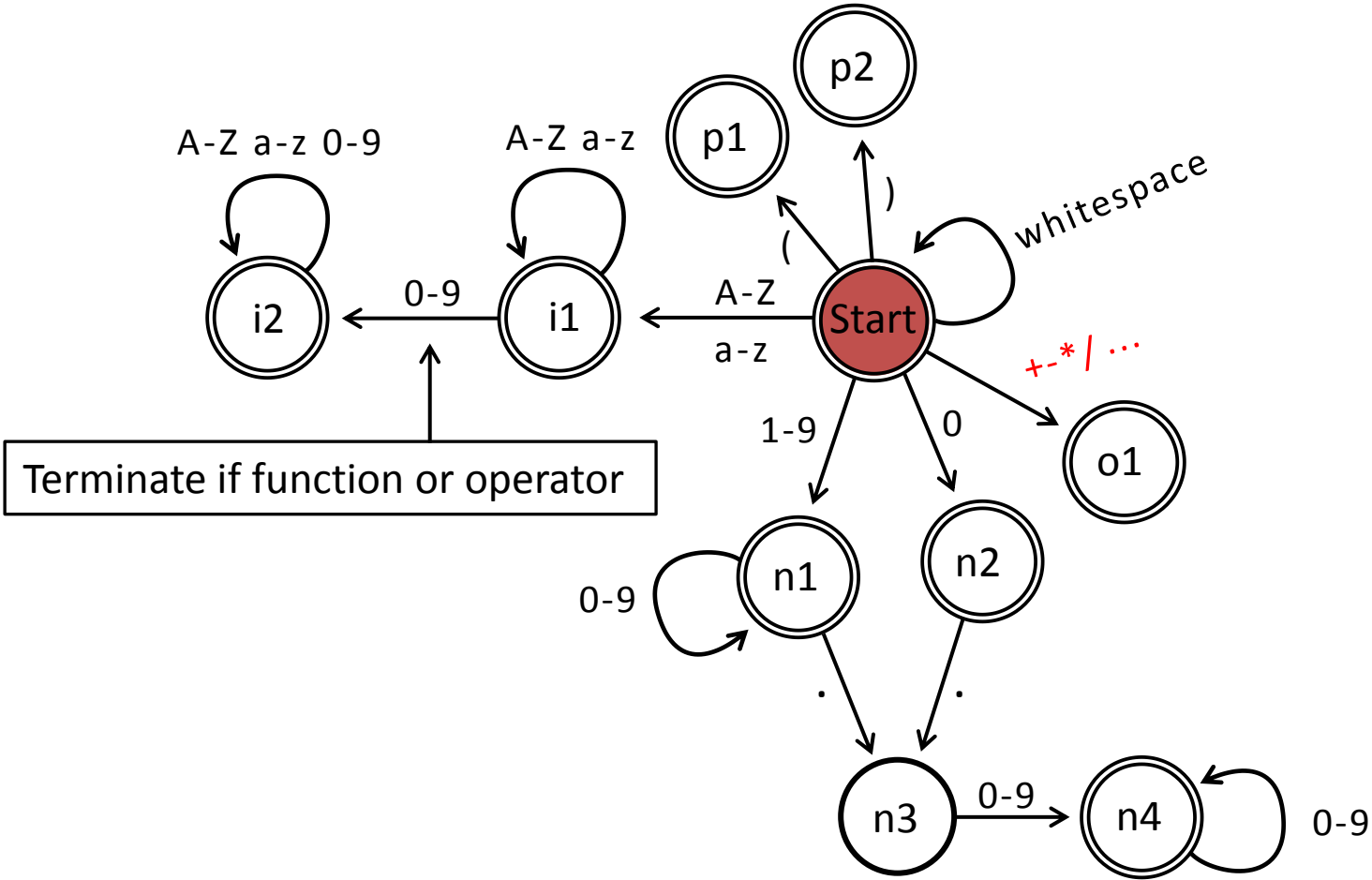
x1 = - 1.6

$x1 = -1.6 * \cos(\text{Pi})$



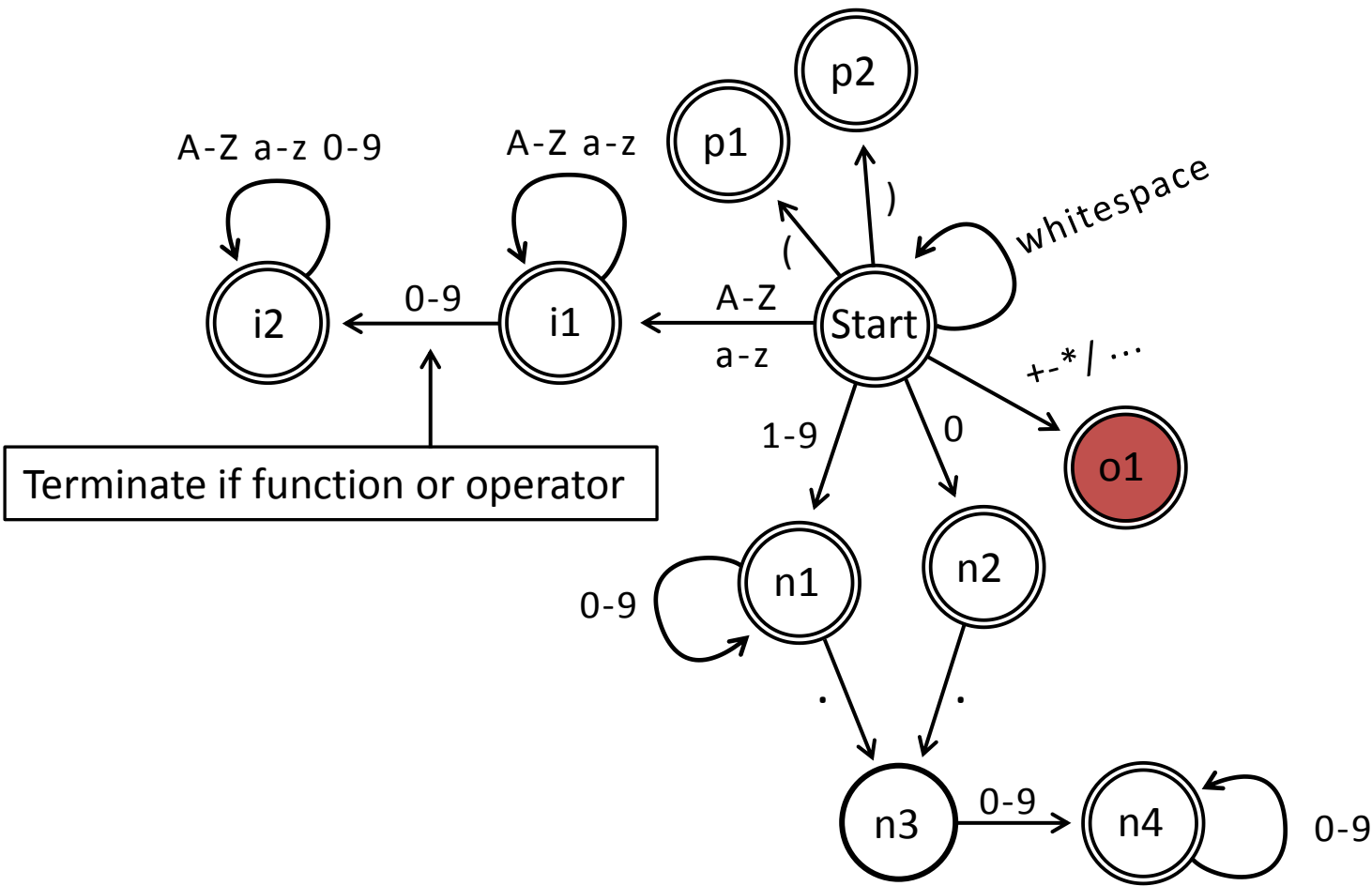
x1 = - 1.6

```
x1 = -1.6 * cos(Pi)
```



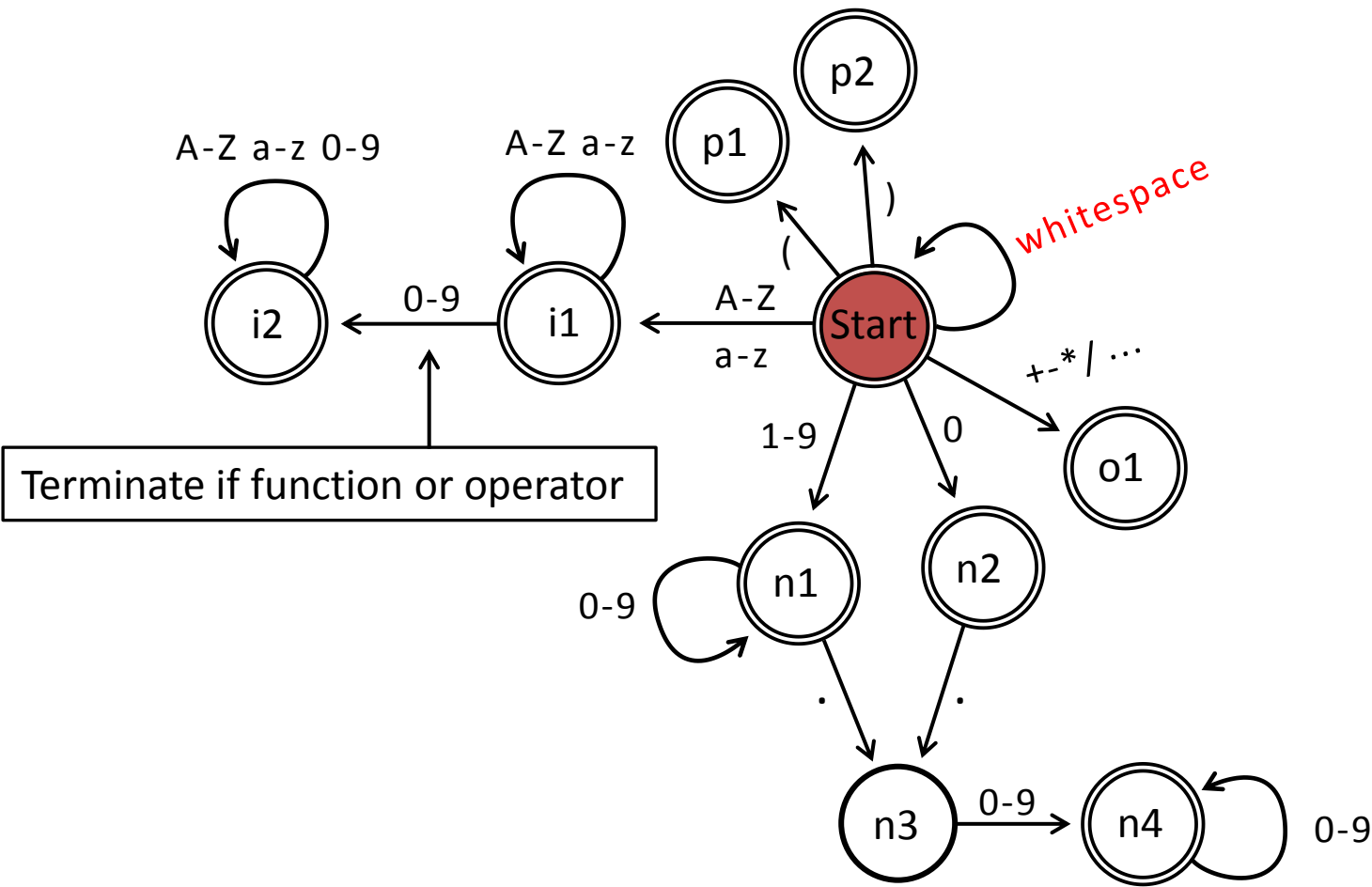
```
x1 = - 1.6
```

$x1 = -1.6 * \text{cos}(\text{Pi})$



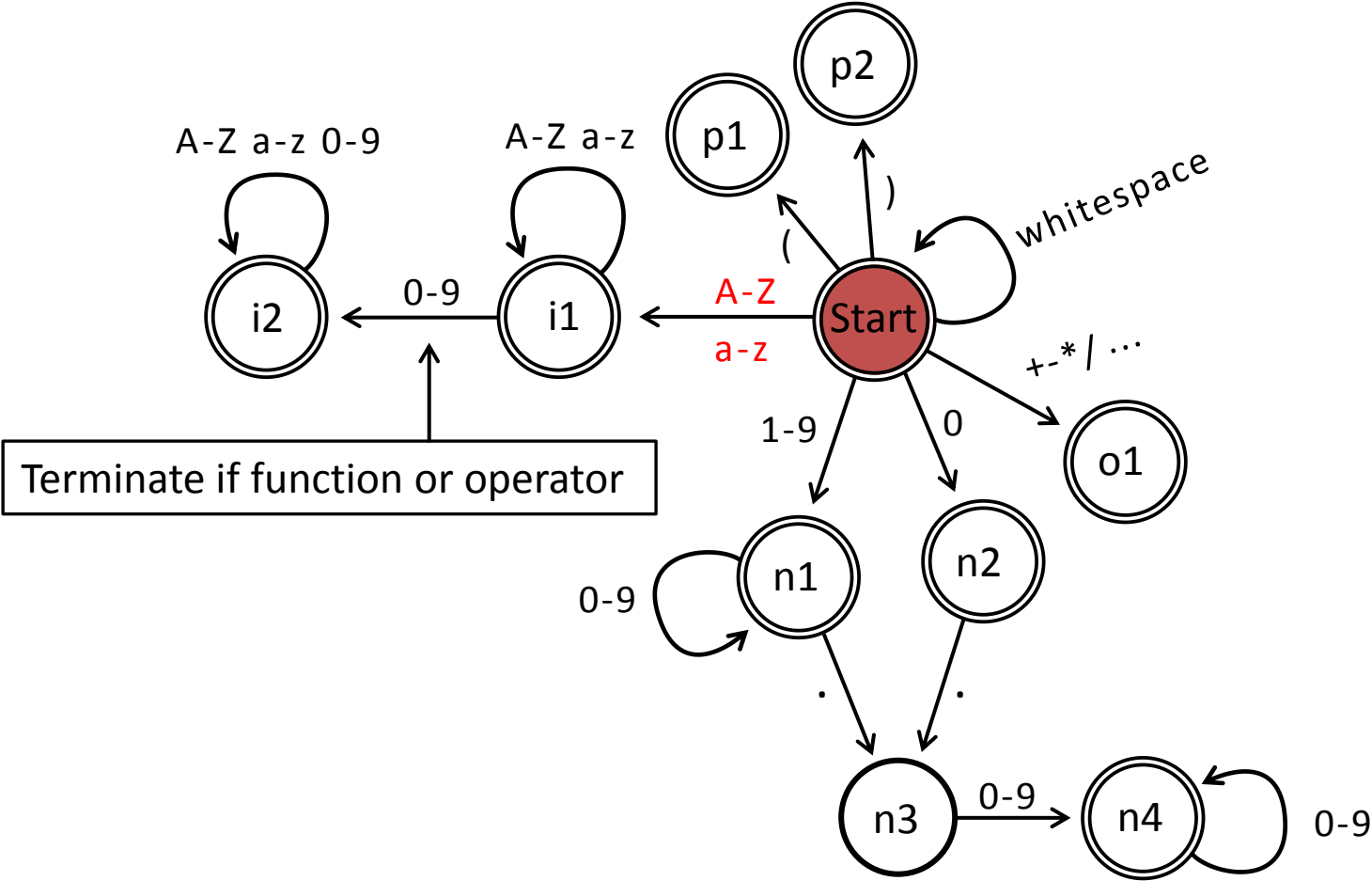
x1 = - 1.6 *

$x1 = -1.6 * \text{cos}(\text{Pi})$



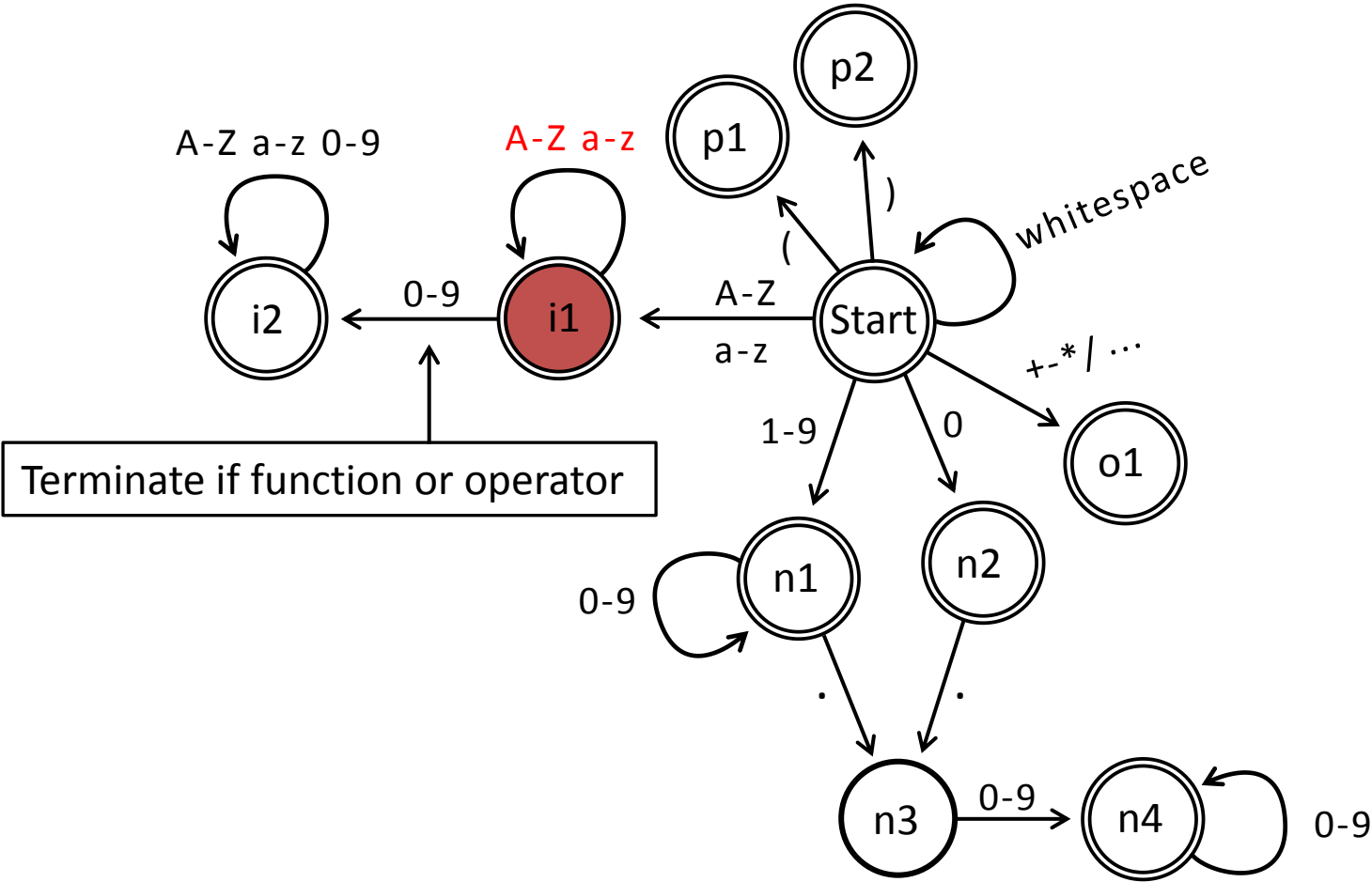
x1 = - 1.6 *

$x1 = -1.6 * \text{cos}(\text{Pi})$



x1 = - 1.6 *

```
x1 = -1.6 * cos(Pi)
```



x1

=

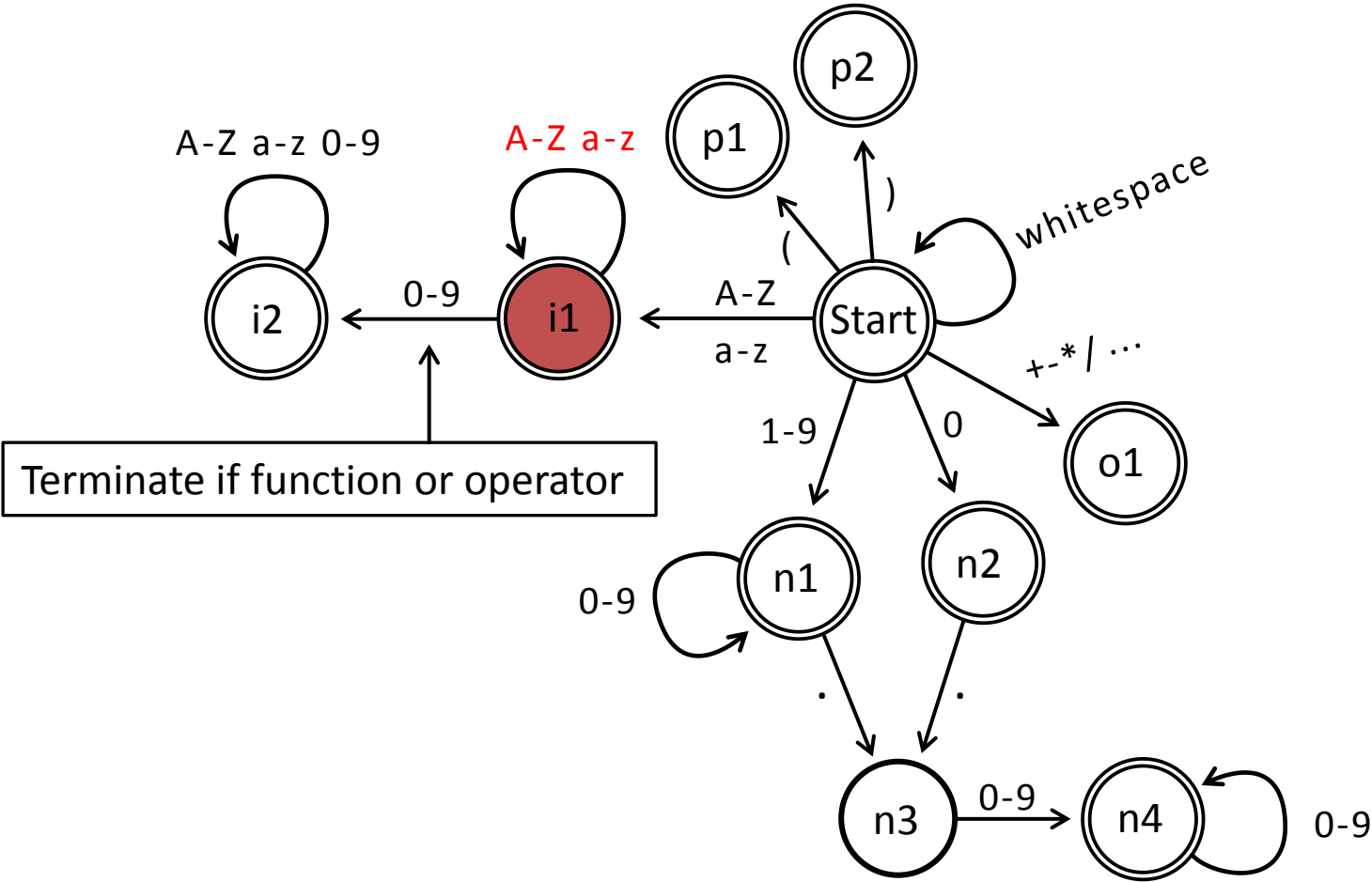
-

1.6

*

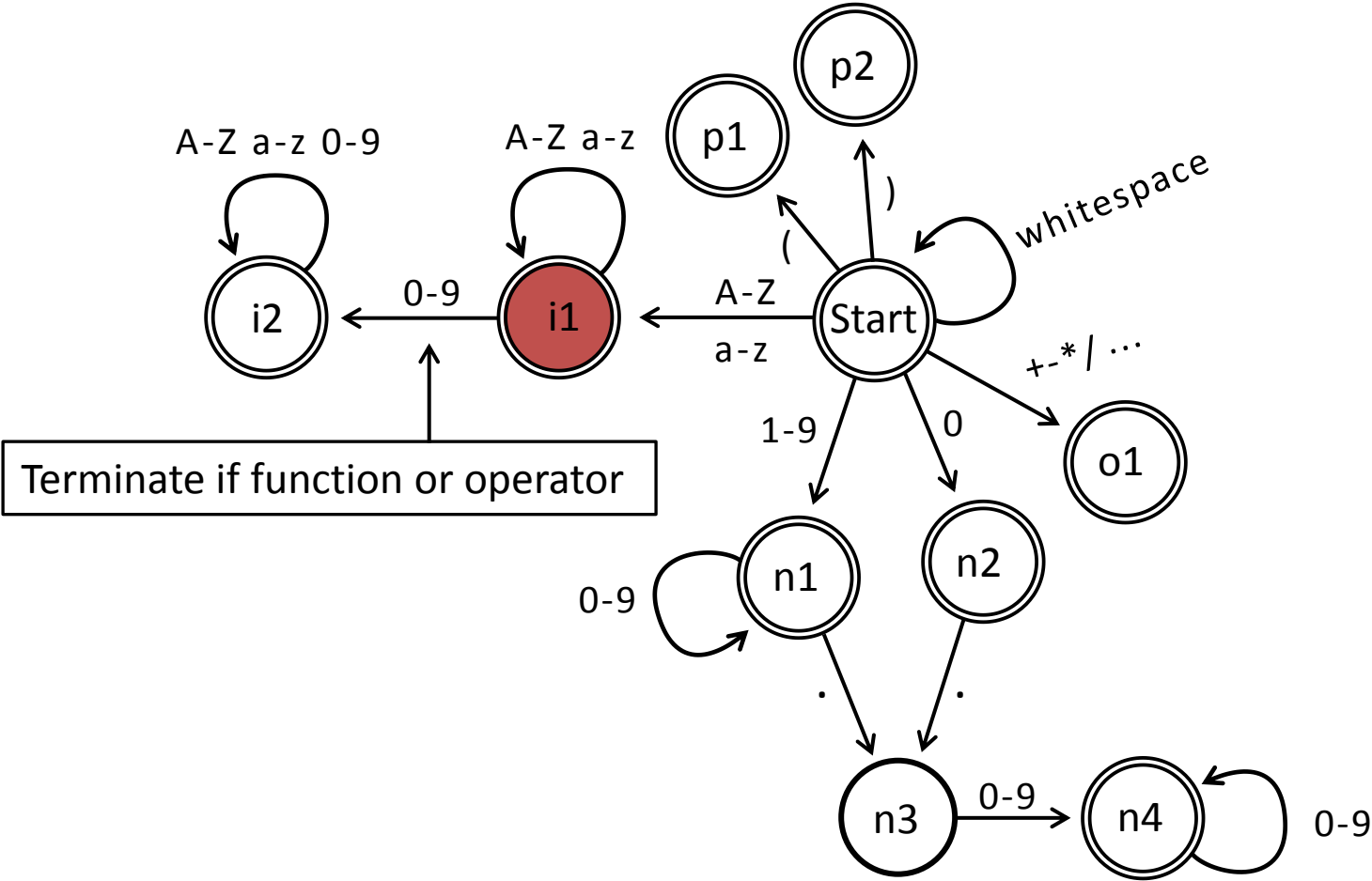
c


```
x1 = -1.6 * coS(Pi)
```



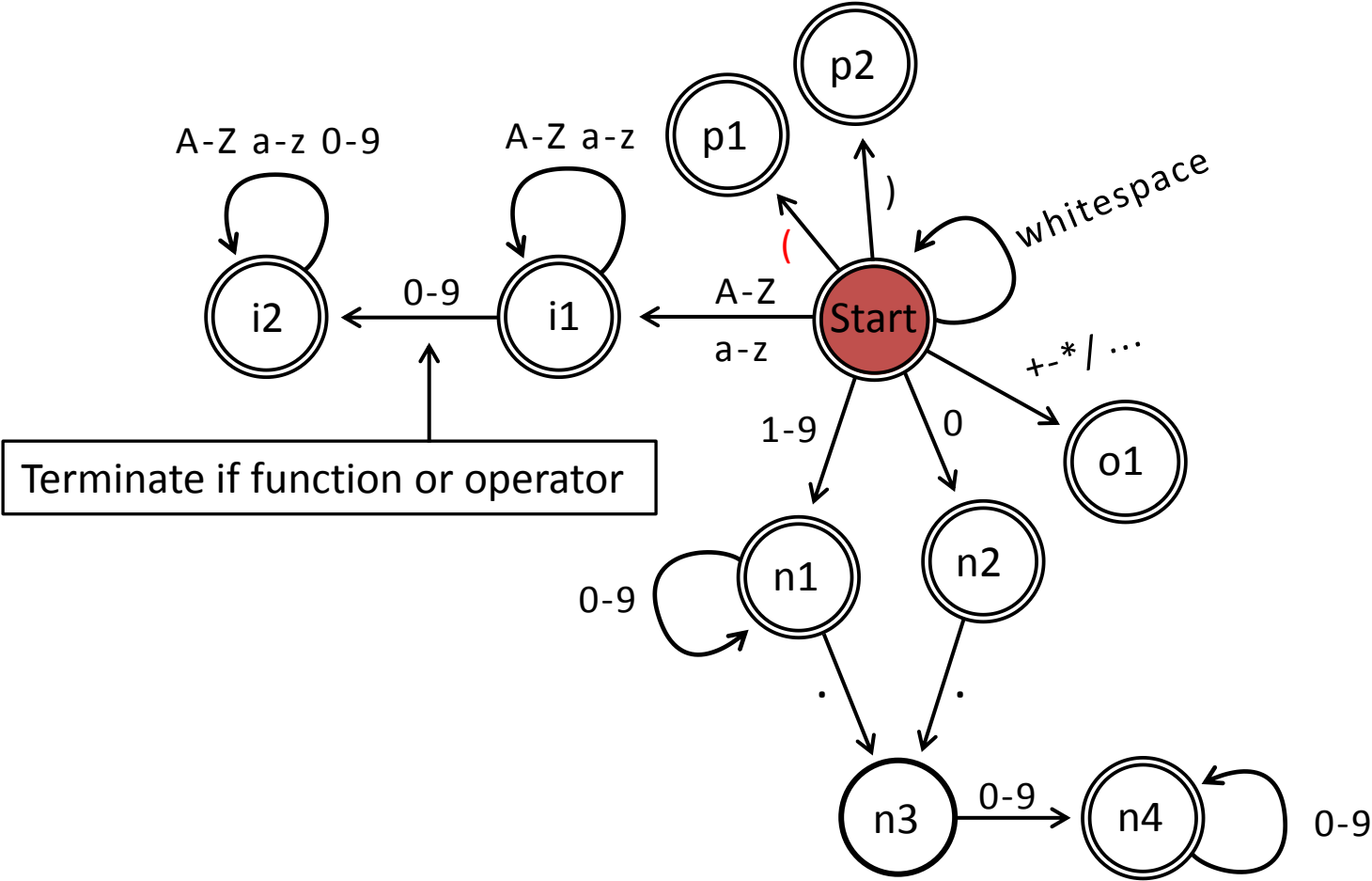
```
x1 = -1.6 * co
```

```
x1 = -1.6 * cos(Pi)
```



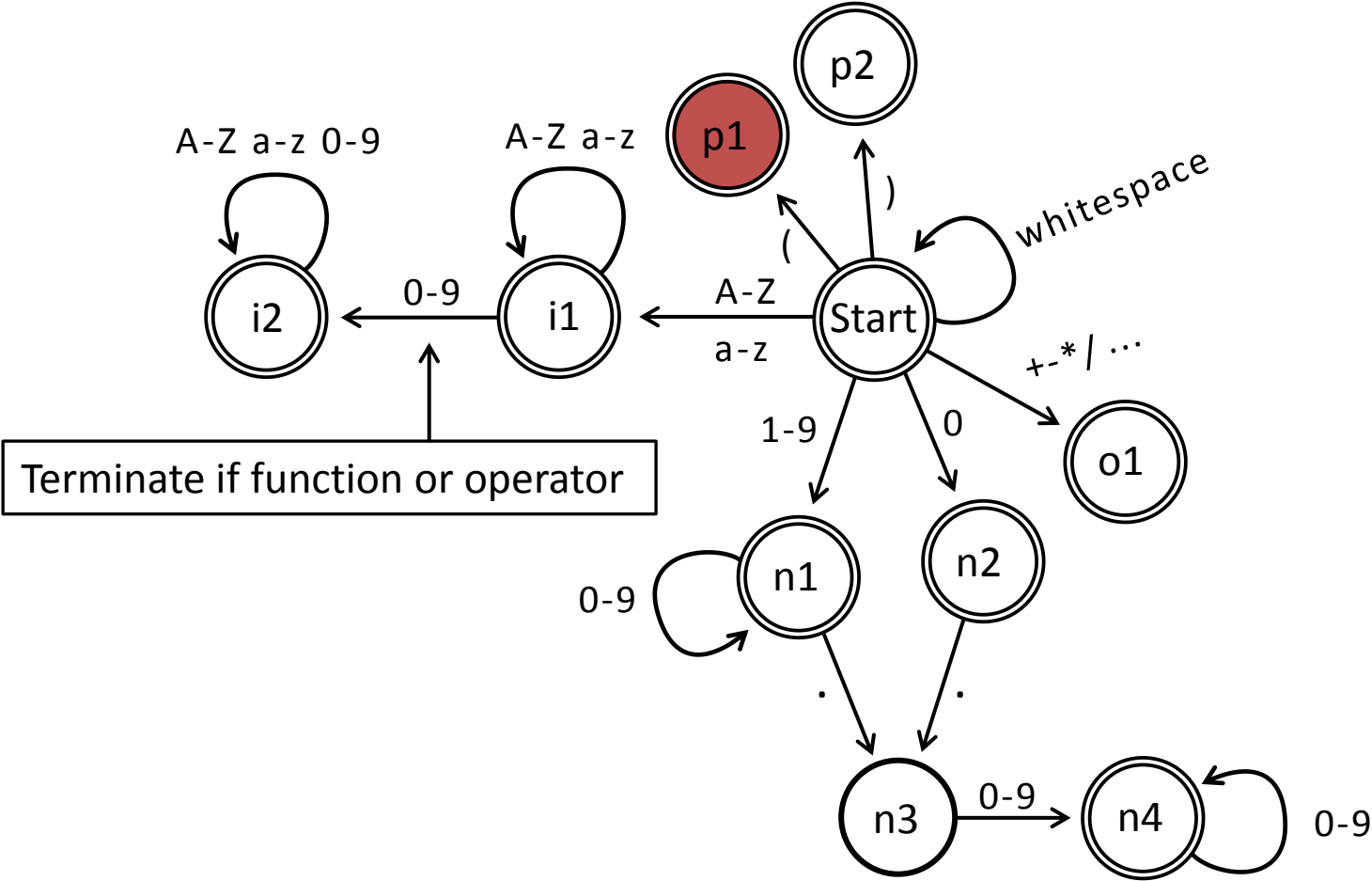
x1 = -1.6 * cos

```
x1 = -1.6 * cos(Pi)
```



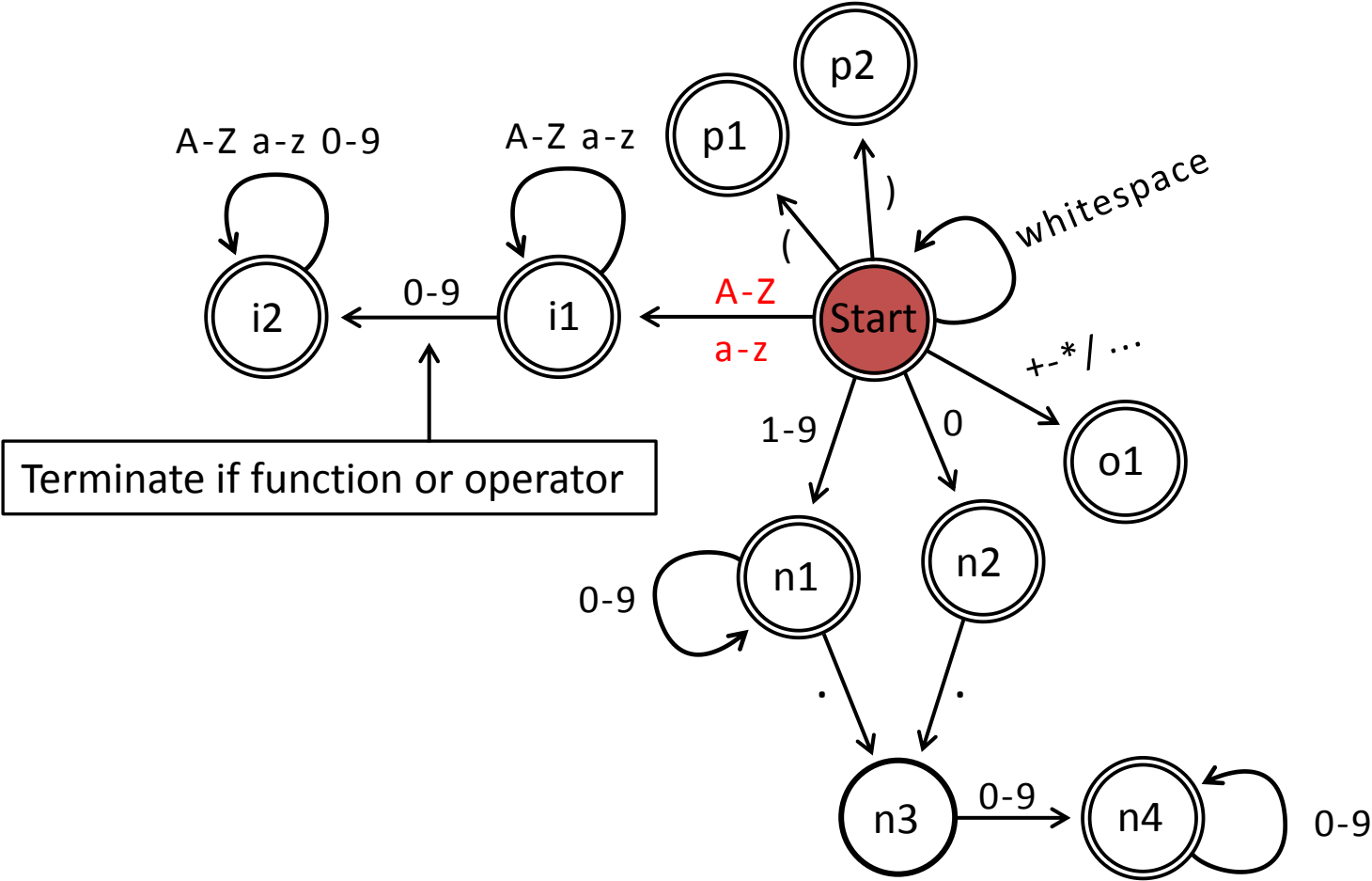
x1 = -1.6 * cos

```
x1 = -1.6 * cos(Pi)
```



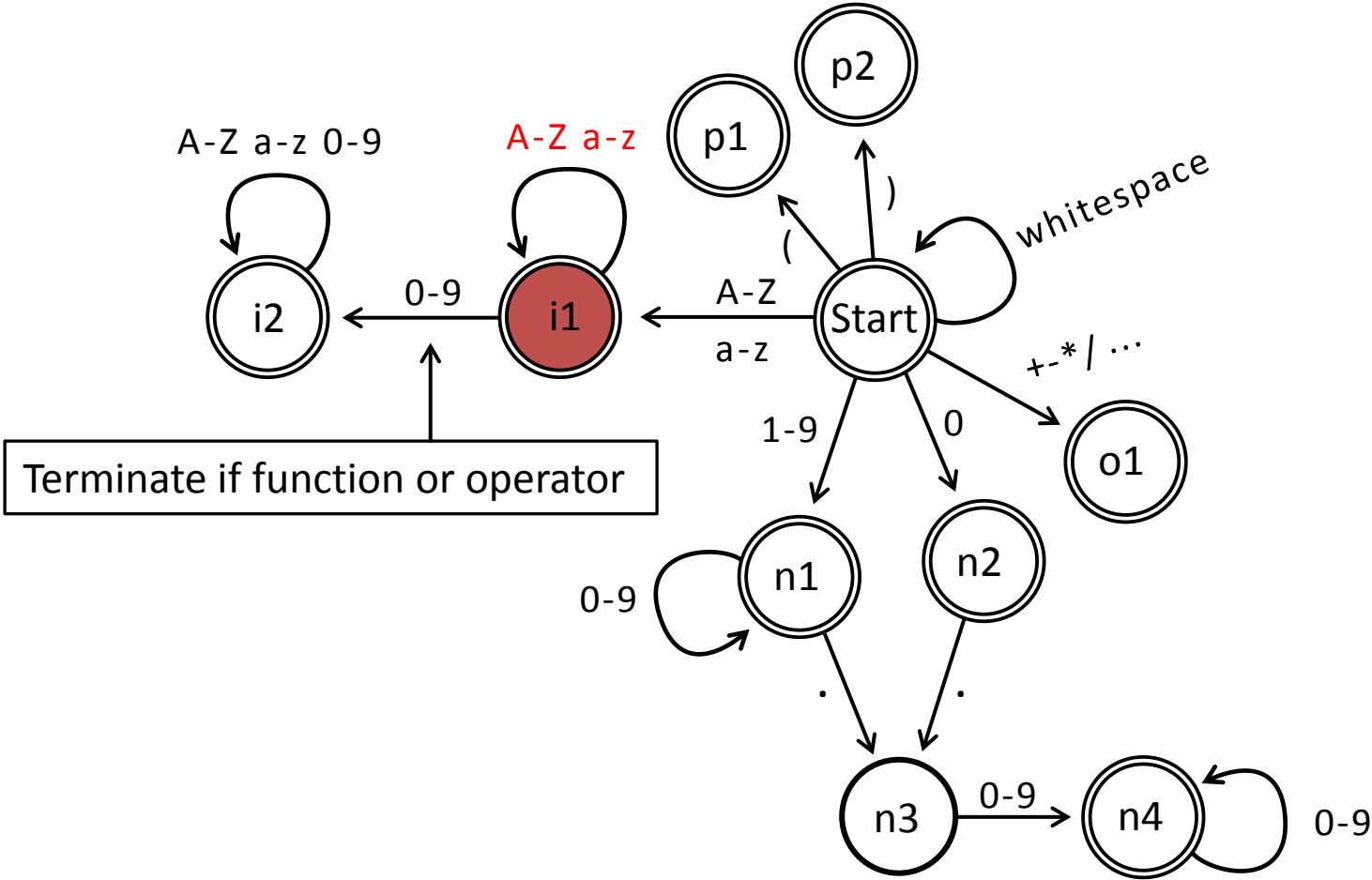
```
x1 = -1.6 * cos (
```

```
x1 = -1.6 * cos(Pi)
```



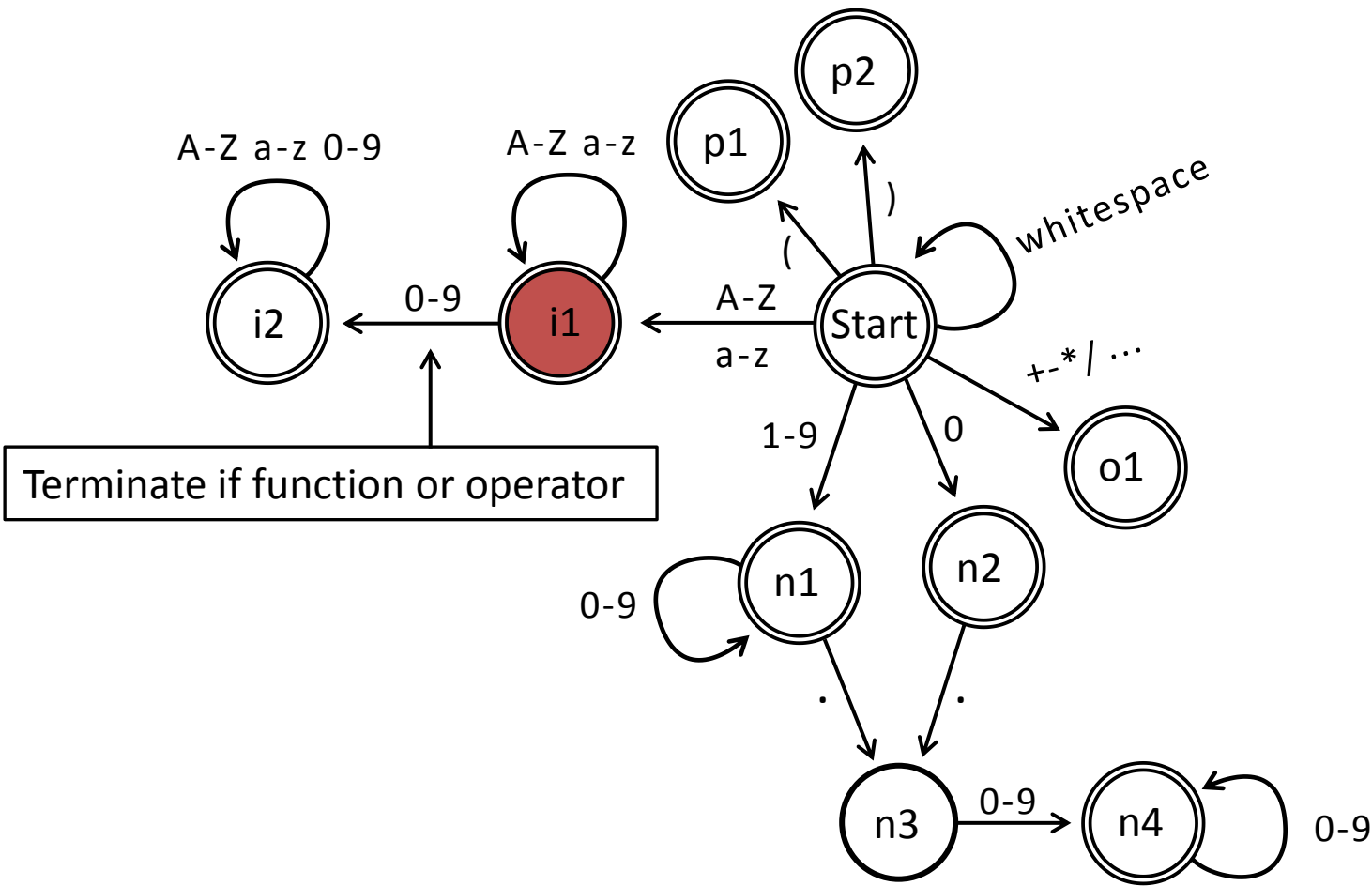
x1	=	-	1.6	*	cos	(
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```
x1 = -1.6 * cos(Pi)
```



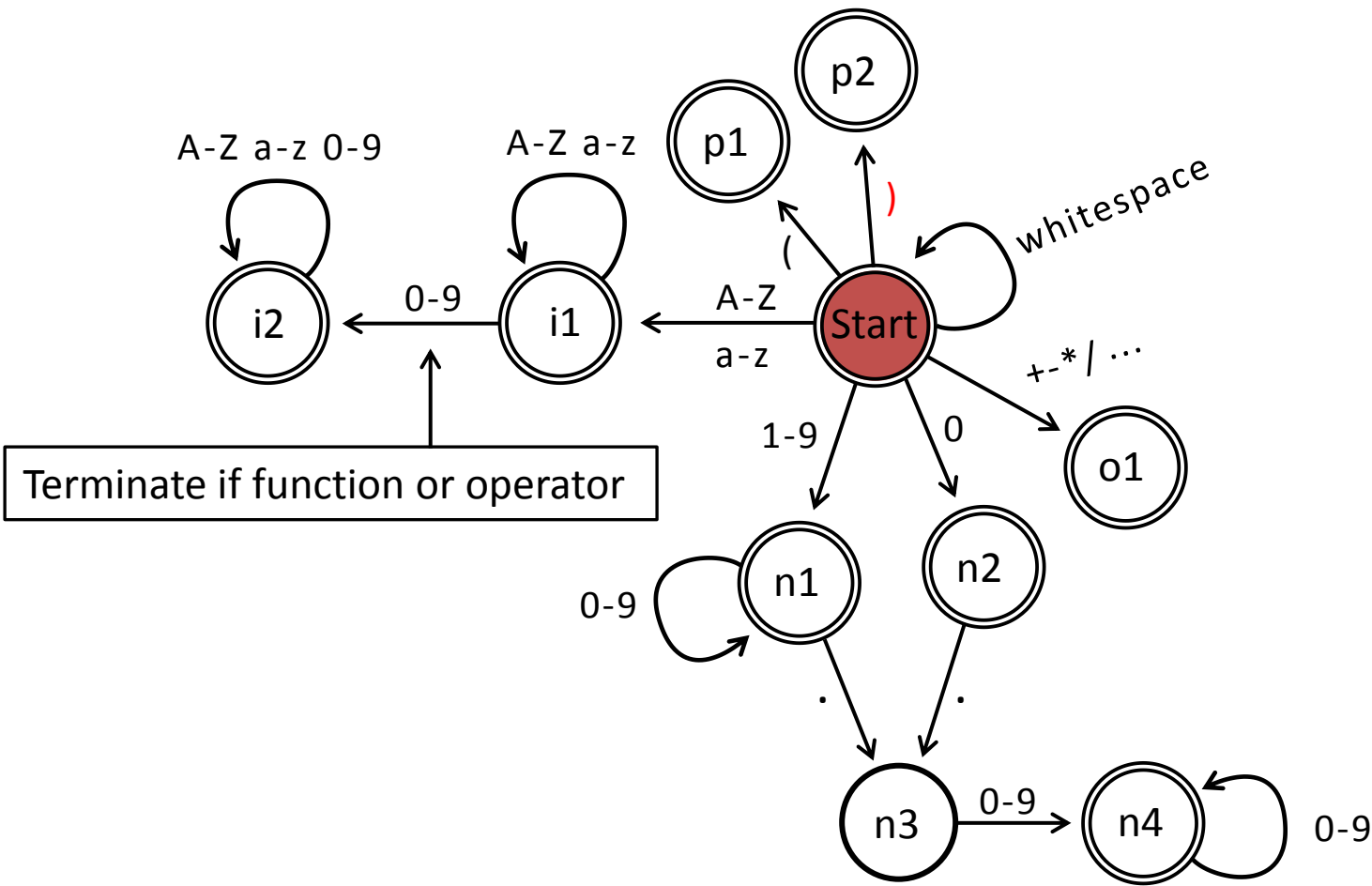
```
x1 = -1.6 * cos ( P
```

```
x1 = -1.6 * cos(Pi)
```



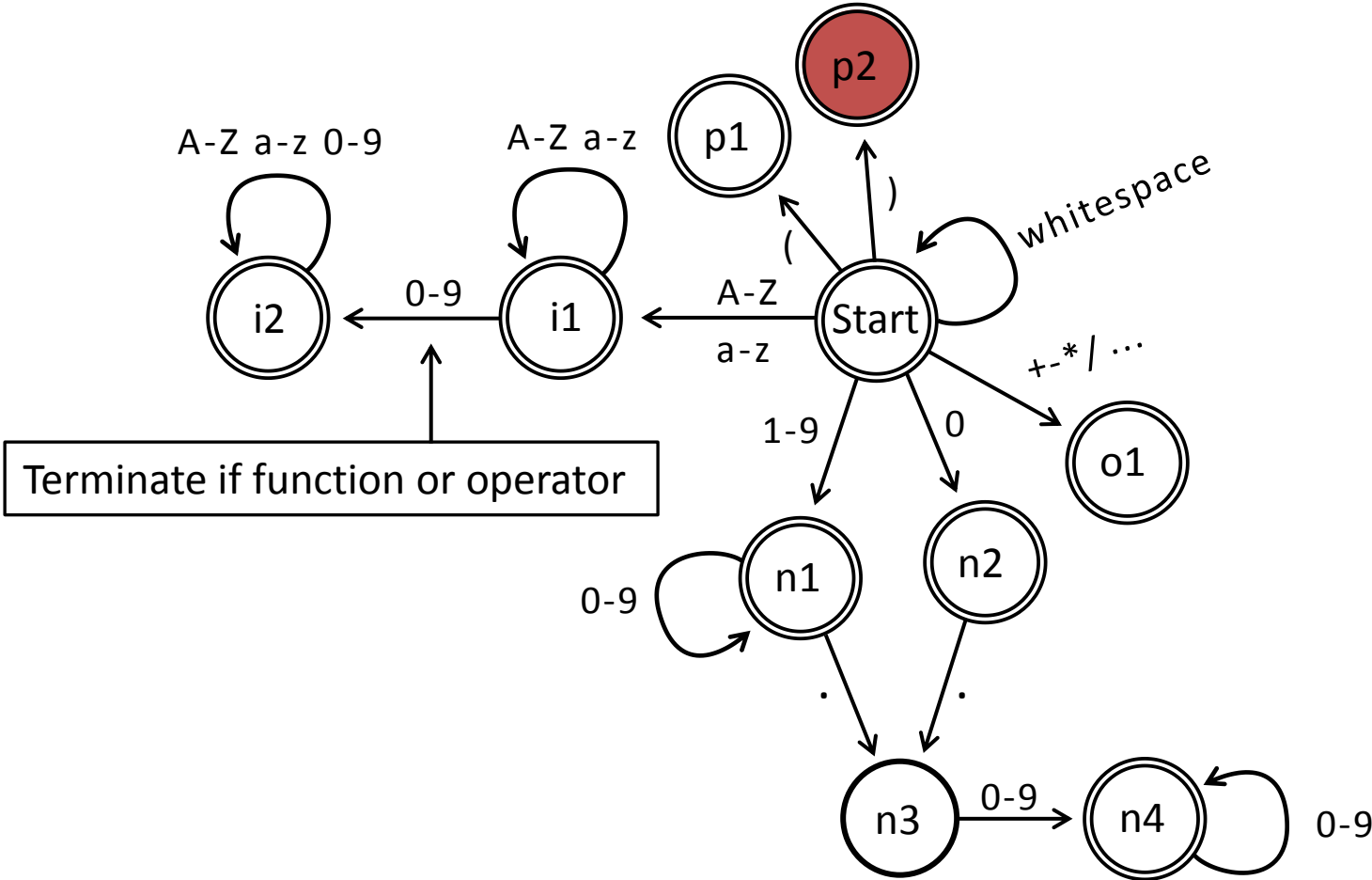
```
x1 = -1.6 * cos ( Pi
```

```
x1 = -1.6 * cos(Pi)
```



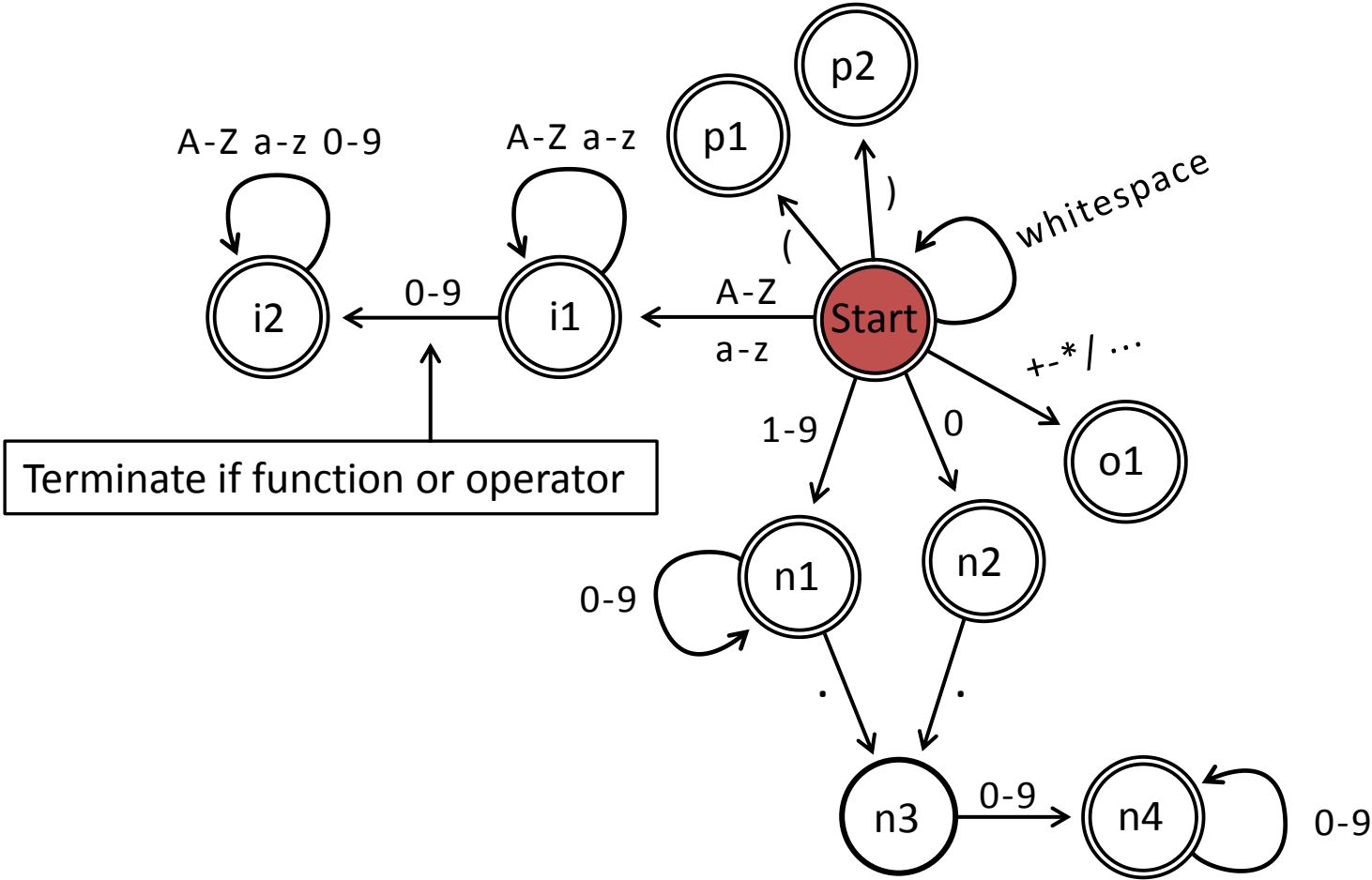
x1	=	-	1.6	*	cos	(Pi
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$x1 = -1.6 * \cos(\text{Pi})$



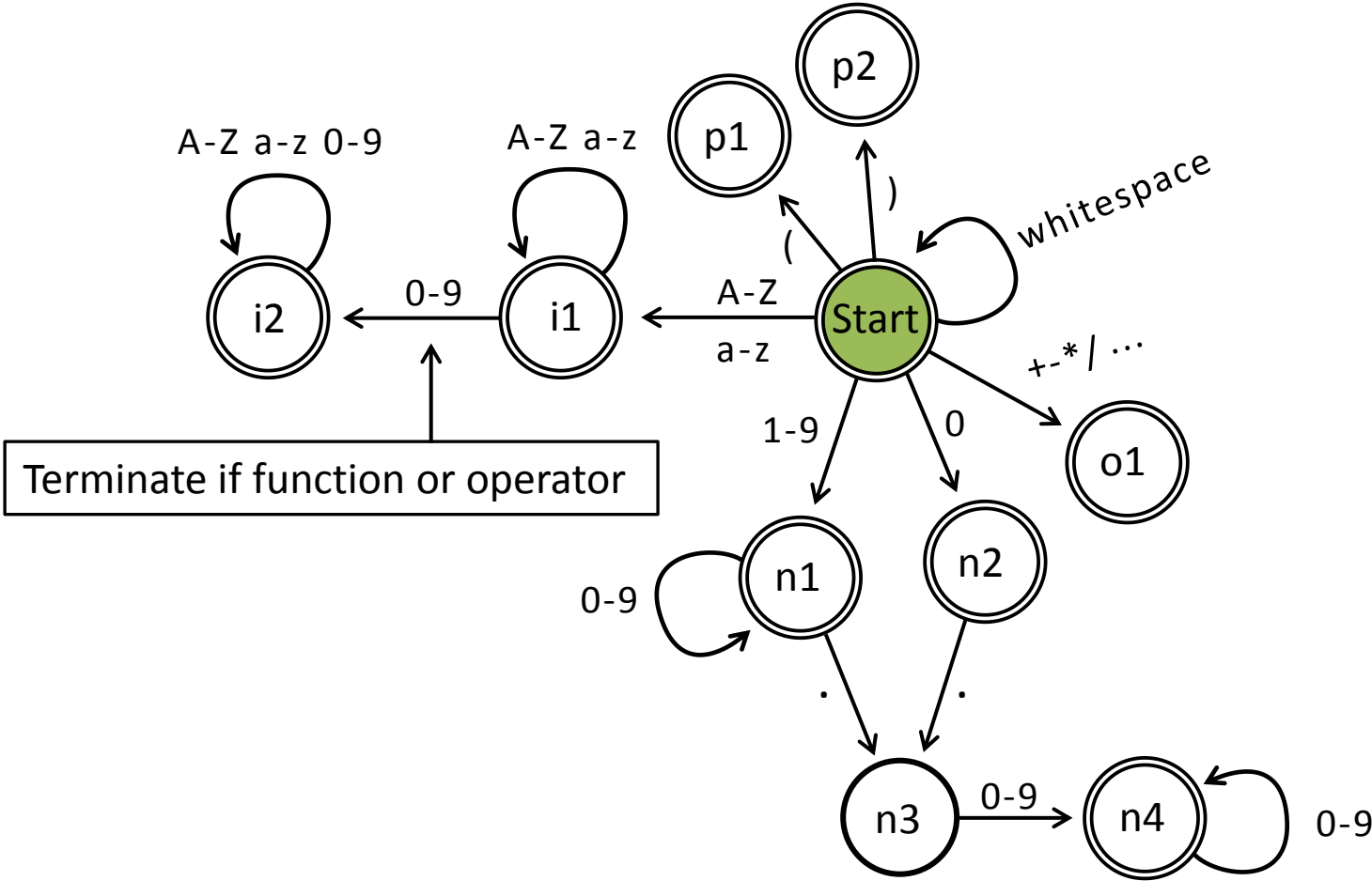
x1 = - 1.6 * cos (Pi)

$x1 = -1.6 * \cos(\text{Pi})$
↑



x1 = - 1.6 * cos (Pi)

```
x1 = -1.6 * cos(Pi)
```



x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

Validate

$A \rightarrow \text{Variable} = A \mid E$

$E \rightarrow N \text{ operator } E \mid N$

$N \rightarrow T \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$

$A \rightarrow \text{Variable} = A \mid E$

$E \rightarrow N \text{ operator } E \mid N$

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$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$

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$N \rightarrow T \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$

A

x1 = - 1.6 * cos (Pi)



$A \rightarrow \text{Variable} = A \mid E$

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$N \rightarrow T \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$

$$\begin{array}{c} A \\ / \quad | \quad \backslash \\ \text{Variable} = A \end{array}$$

x1 = - 1.6 * cos (Pi)

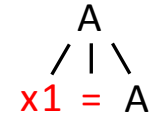


$A \rightarrow \text{Variable} = A \mid E$

$E \rightarrow N \text{ operator } E \mid N$

$N \rightarrow T \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$



x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

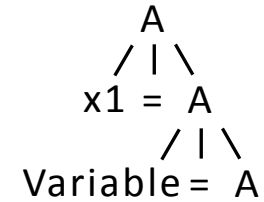
↑

$A \rightarrow \text{Variable} = A \mid E$

$E \rightarrow N \text{ operator } E \mid N$

$N \rightarrow T \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$



x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

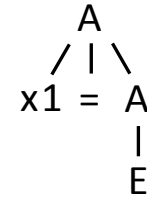
↑

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$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$



x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

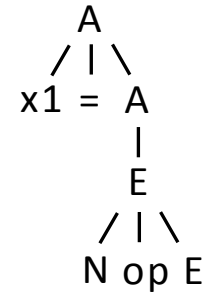
↑

$A \rightarrow \text{Variable} = A \mid E$

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$N \rightarrow T \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$



x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

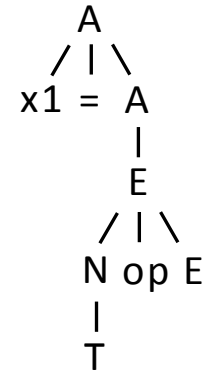
↑

$A \rightarrow \text{Variable} = A \mid E$

$E \rightarrow N \text{ operator } E \mid N$

$N \rightarrow \textcolor{red}{T} \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$



x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

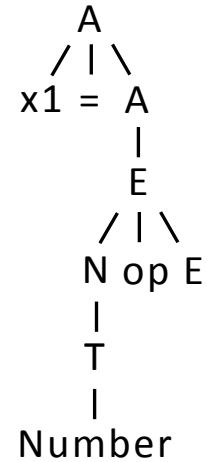
↑

$A \rightarrow \text{Variable} = A \mid E$

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$N \rightarrow T \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$



x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

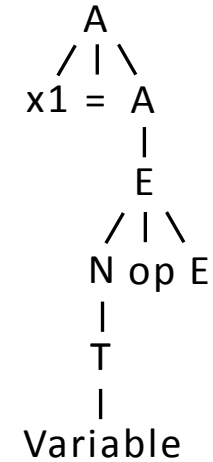
↑

$A \rightarrow \text{Variable} = A \mid E$

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$N \rightarrow T \mid - T$

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x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

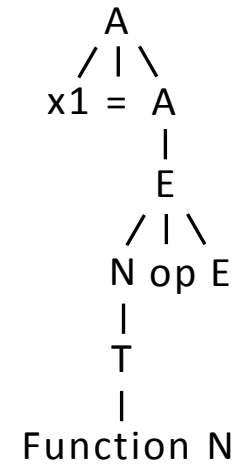
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x1	=	-	1.6	*	cos	(Pi)
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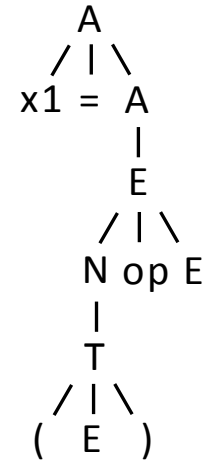
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x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

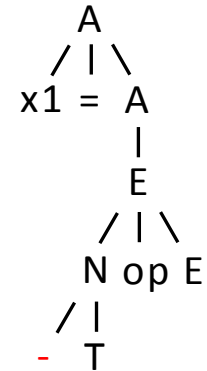
↑

$A \rightarrow \text{Variable} = A \mid E$

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x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

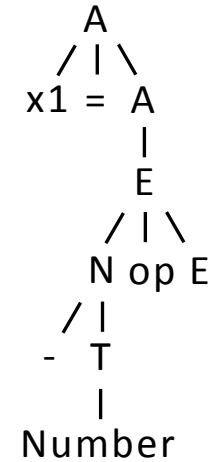
↑

$A \rightarrow \text{Variable} = A \mid E$

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x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

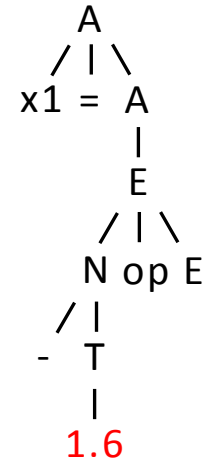
↑

$A \rightarrow \text{Variable} = A \mid E$

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x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

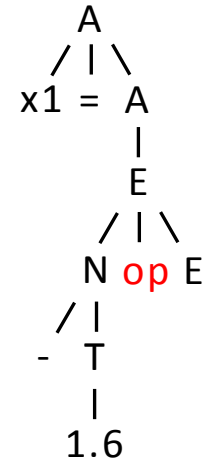
↑

$A \rightarrow \text{Variable} = A \mid E$

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$N \rightarrow T \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function N} \mid (E)$



x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

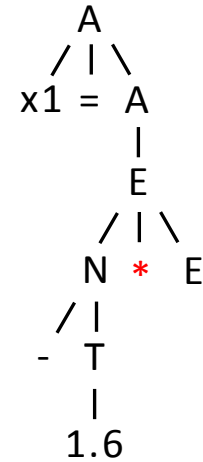
↑

$A \rightarrow \text{Variable} = A \mid E$

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x1	=	-	1.6	*	cos	(Pi)
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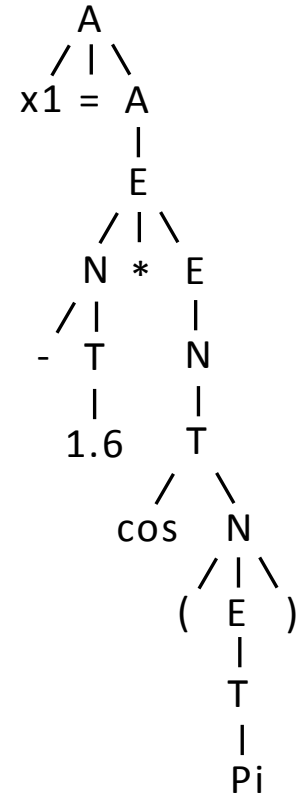
↑

$A \rightarrow \text{Variable} = A \mid E$

$E \rightarrow N \text{ operator } E \mid N$

$N \rightarrow T \mid - T$

$T \rightarrow \text{Number} \mid \text{Variable} \mid \text{Function } N \mid (E)$



x1	=	-	1.6	*	cos	(Pi)
----	---	---	-----	---	-----	---	----	---

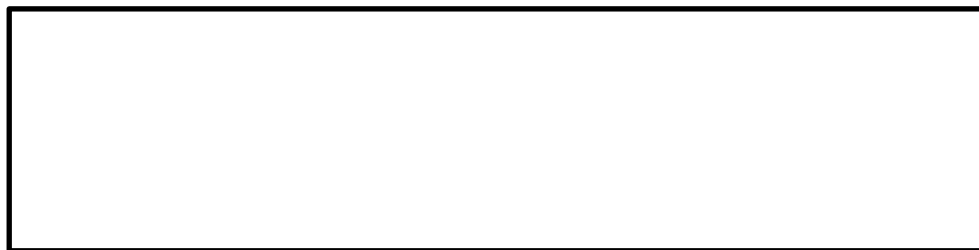


Translate

x1 = - 1.6 * cos (Pi)



Stack



Output

x1 = - 1.6 * cos (Pi)

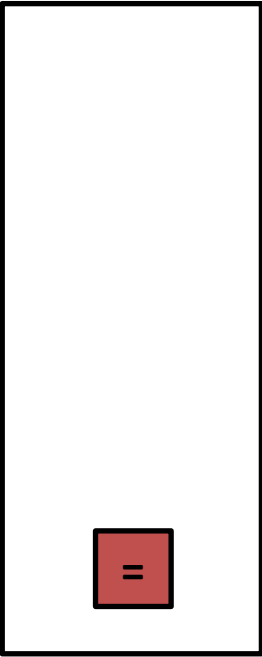


Stack



Output

x1 = - 1.6 * cos (Pi)

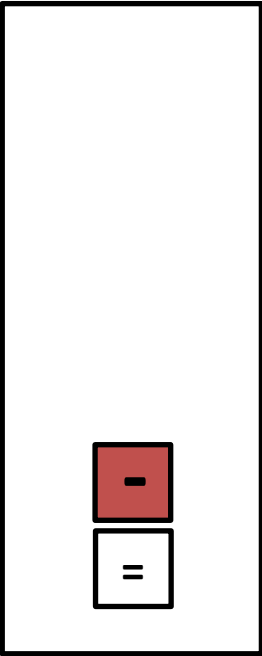


Stack



Output

x1 = - 1.6 * cos (Pi)

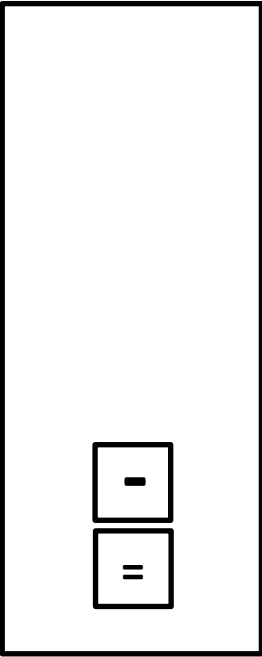


Stack



Output

x1 = - 1.6 * COS (Pi)

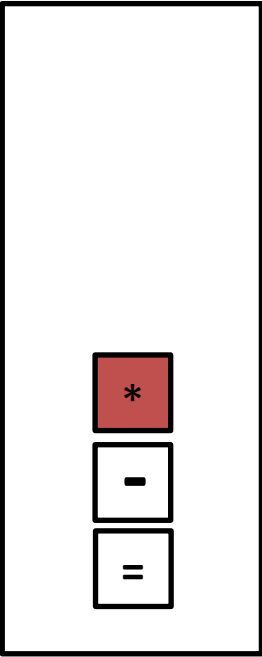


Stack



Output

x1 = - 1.6 * COS (Pi)

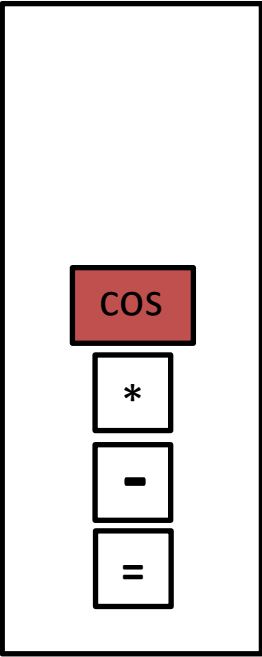


Stack



Output

x1 = - 1.6 * COS (Pi)

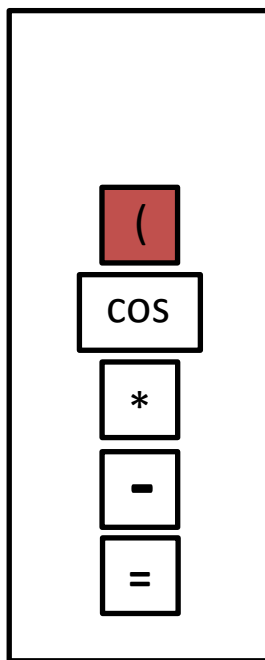


Stack



Output

x1 = - 1.6 * COS (Pi)

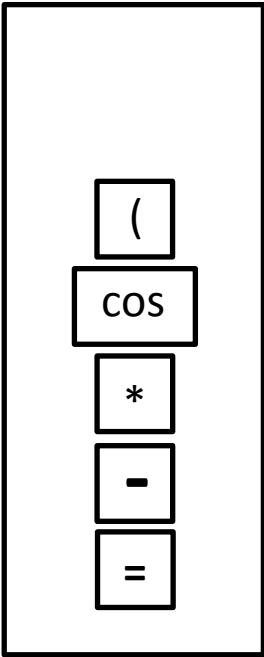


Stack



Output

x1 = - 1.6 * COS (Pi)

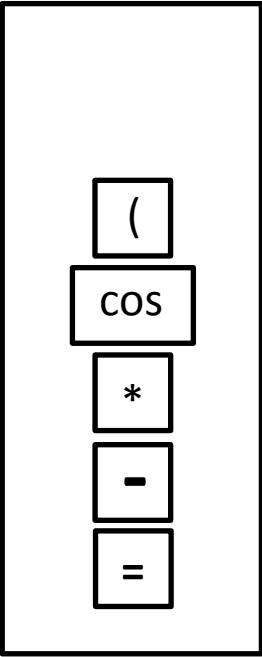


Stack



Output

x1 = - 1.6 * COS (Pi)



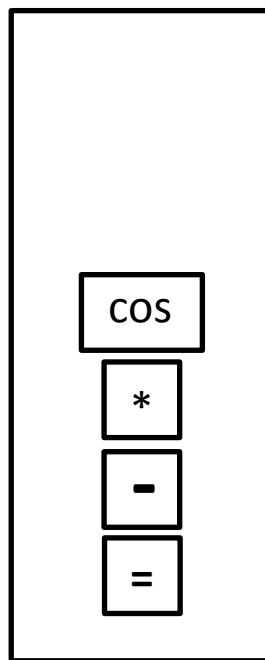
Stack



Output

x1 = - 1.6 * COS (Pi)

End of input



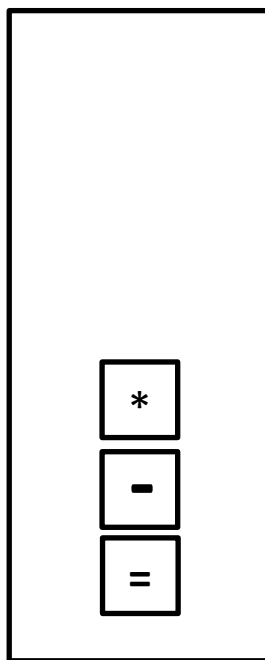
Stack



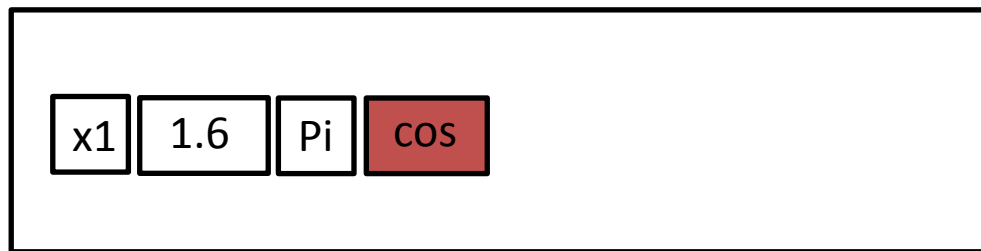
Output

x1 = - 1.6 * cos (Pi)

End of input



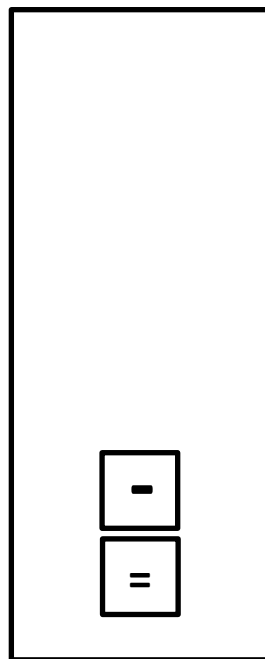
Stack



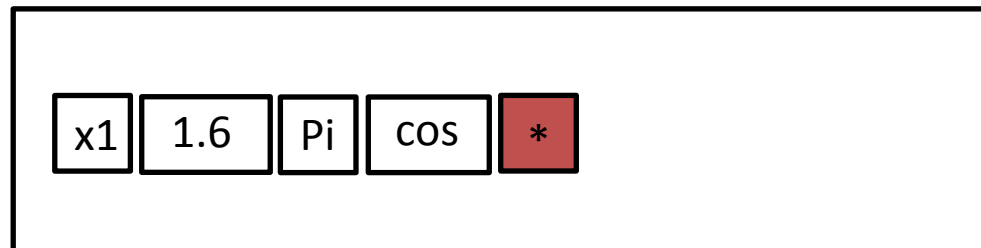
Output

x1 = - 1.6 * cos (Pi)

End of input



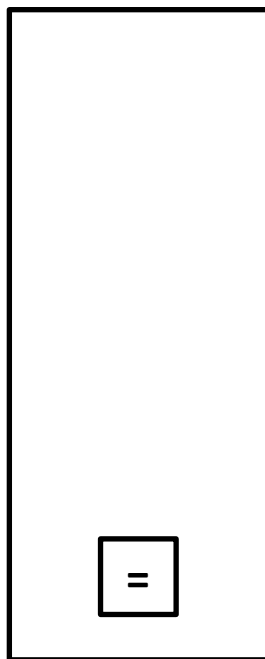
Stack



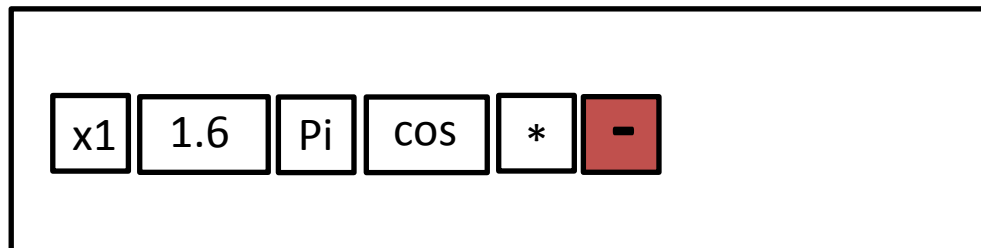
Output

x1 = - 1.6 * cos (Pi)

End of input



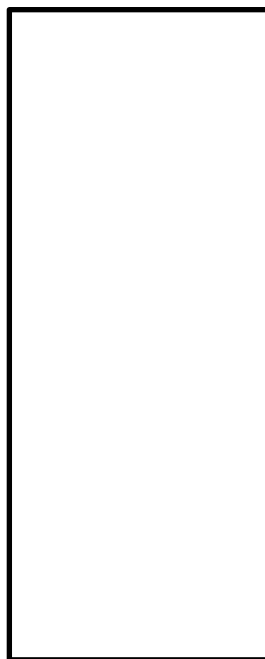
Stack



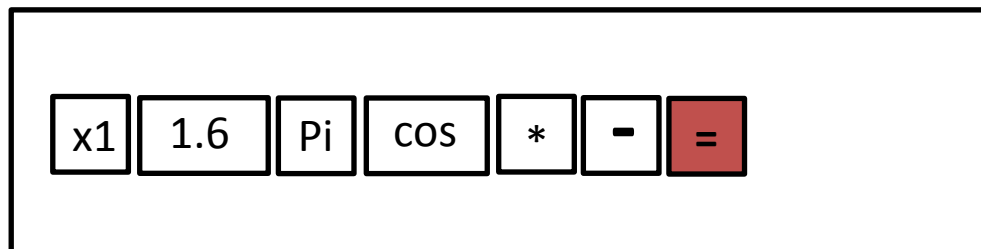
Output

x1 = - 1.6 * cos (Pi)

End of input



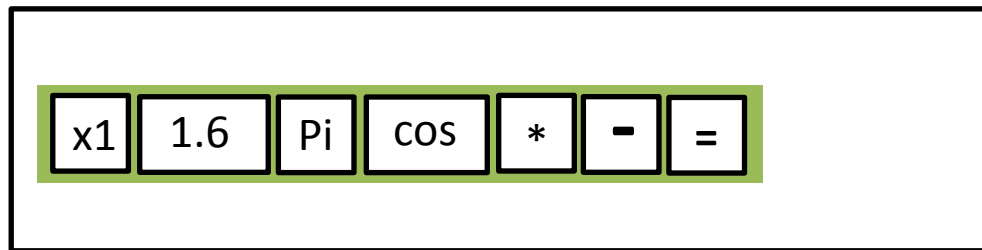
Stack



Output

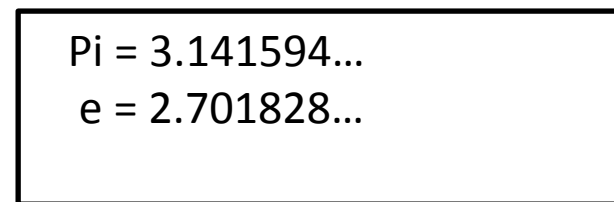


Stack



Output

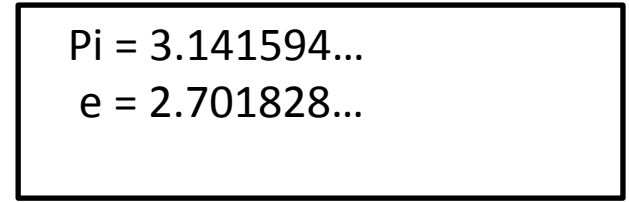
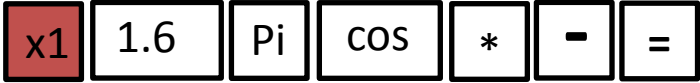
Evaluate



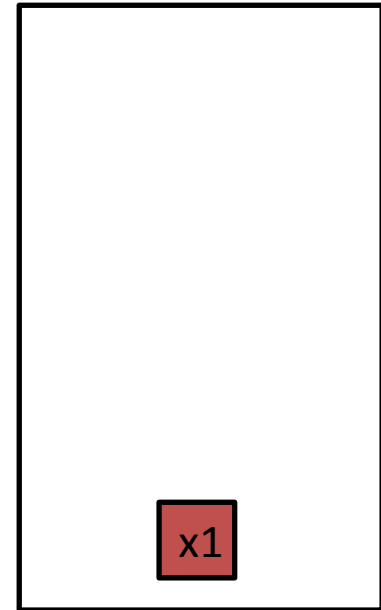
Enviroment



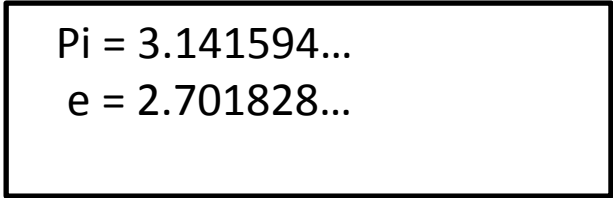
Stack



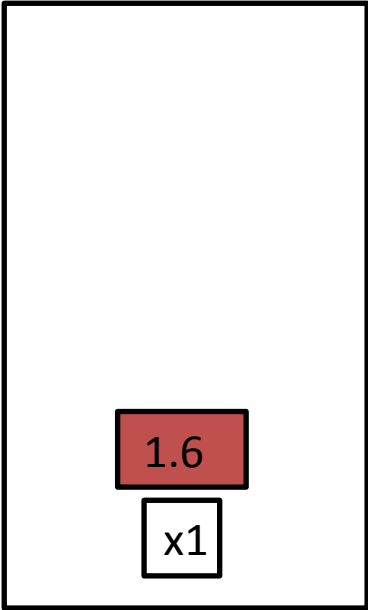
Enviroment



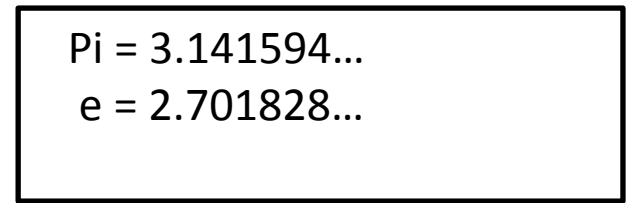
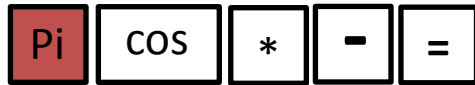
Stack



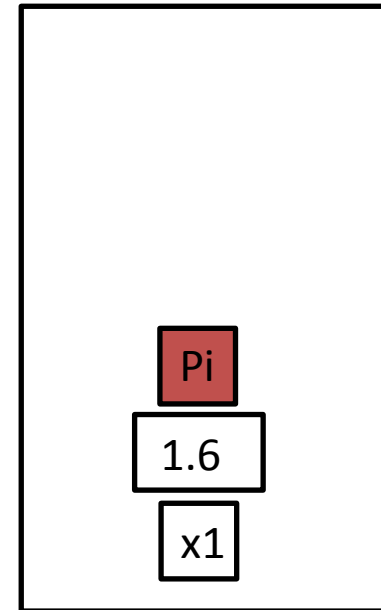
Enviroment



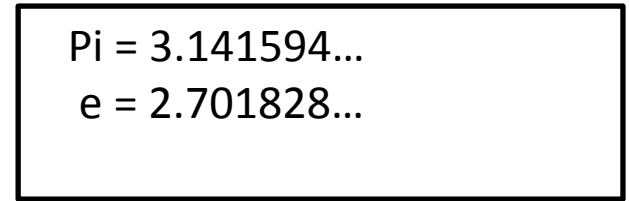
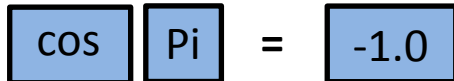
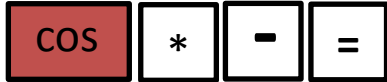
Stack



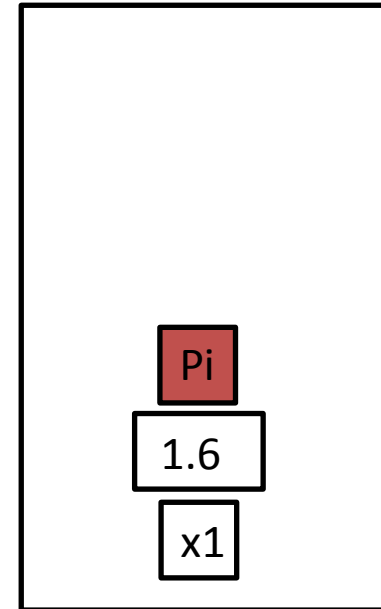
Enviroment



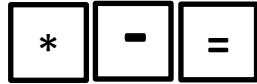
Stack



Enviroment

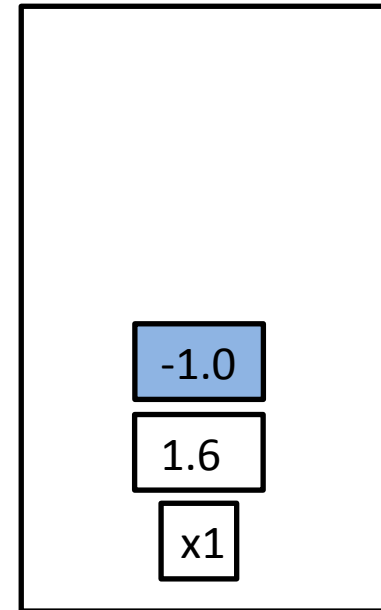


Stack



Pi = 3.141594...
e = 2.701828...

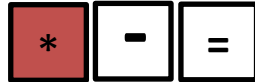
Enviroment



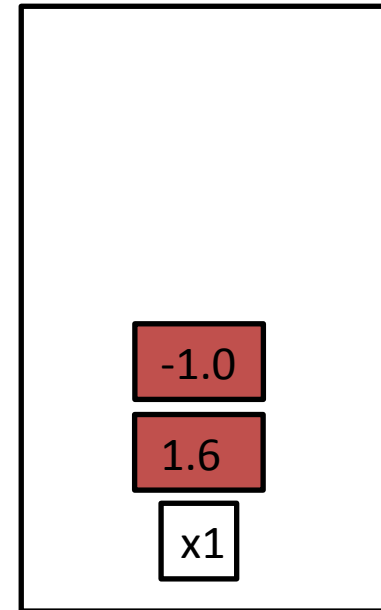
Stack

Pi = 3.141594...
e = 2.701828...

Enviroment



$$-1.0 \times 1.6 = -1.6$$

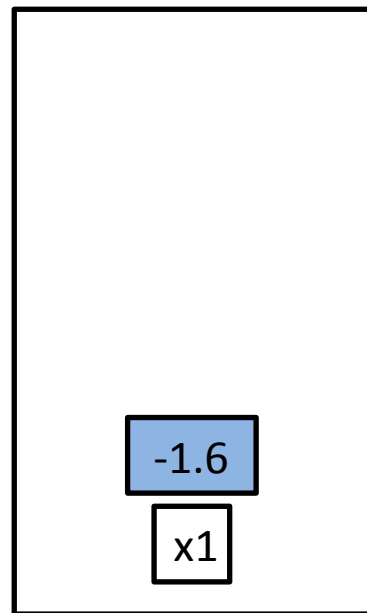


Stack



Pi = 3.141594...
e = 2.701828...

Enviroment



Stack

Pi = 3.141594...
e = 2.701828...

Enviroment



$$[-] \quad [-1.6] = [1.6]$$

-1.6

x1

Stack

Pi = 3.141594...
e = 2.701828...

Enviroment

=



1.6

x1

Stack

Pi = 3.141594...
e = 2.701828...

Enviroment

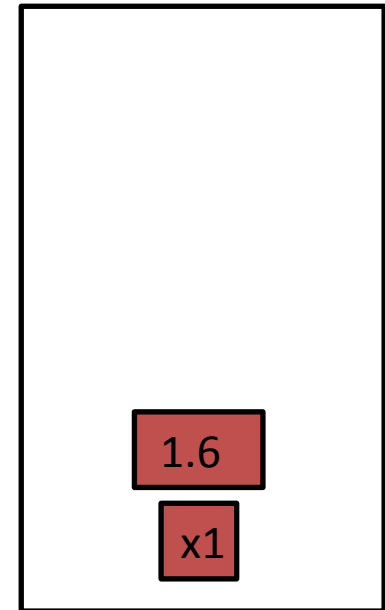
=



1.6 = x1



Assignment



Stack

Pi = 3.141594...

e = 2.701828...

Enviroment

X1 = 1.6

Stack

Pi = 3.141594...
e = 2.701828...

Enviroment

**No more input.
Pop the top of the stack to the
enviroment**

X1 = 1.6

Stack

Pi = 3.141594...

e = 2.701828...

x1= 1.6

Enviroment

X1 = 1.6

Stack



Pi = 3.141594...

e = 2.701828...

x1 = 1.6

Enviroment



Done!



Stack

Demo

Questions