

<Invertible Transformations>

$Ax=b \iff x=A^{-1}b$

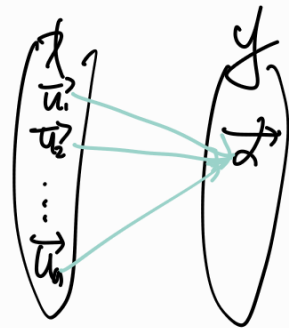
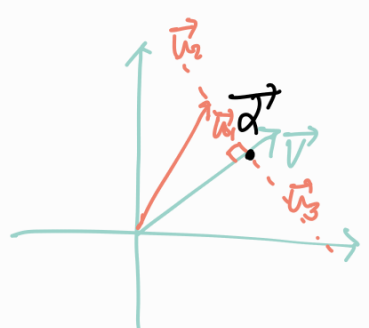
\mathbb{R} : 1차원 공간
 \mathbb{R}^2 : 2차원 "
 \mathbb{R}^3 : 3차원 "

역변환을 하겠다!

$$\begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix}^{-1} = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix}$$

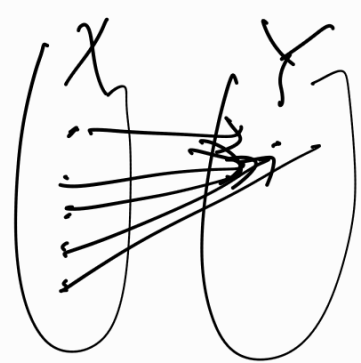
<Inverse>

$a \circledast x = e \implies x = a^{-1}$



$Ax=b$
 $0^{-1} = \frac{1}{0}$

None Invertible Transformations
! : 대역이 아님.



$a \circ a^{-1} = I \rightsquigarrow$ 항등원 = I
 $\implies a \circ a^{-1} = I$

$A \circ A^{-1} = I$

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} d & -b \\ -c & a \end{pmatrix} = \begin{pmatrix} ad-bc & -ab+ab \\ dc-dc & ad-bc \end{pmatrix} = (ad-bc) \cdot I$$

$$= \underbrace{\begin{pmatrix} a & b \\ c & d \end{pmatrix}}_A \circ \underbrace{\frac{1}{ad-bc} \begin{pmatrix} d & -b \\ -c & a \end{pmatrix}}_{A^{-1}} = I$$

\implies If) $ad-bc=0$ 이면
None Invertible

$\neq 0$, Invertible