

ANOVA

sn

2024-05-20

1. Null Hypothesis: There is no difference between any of the groups.

2. $F = \text{between-group variability} / \text{within-group variability}$

3. Types of ANOVA:

1-way ANOVA: 1 factor (e.g. effect of 3 doses of a drug on heart rate)

2-way ANOVA: 2 factors (e.g. effect of age and sex on salary)

3-way ANOVA: 3 factors (e.g. effect of age, sex and education on salary)

4. Assumptions for ANOVA:

i.Independent random sampling

ii.Normality of residuals (distances from group mean)

`model <- aov(grade ~ attendance * previous_grades, data = class)`

* is for model with interaction; + is for model without interaction

`method1:hist(resid(model), main = "residuals")`

`method2:plot(model, 2)`

`method3:Shapiro-Wilk test`

iii.Equality of Variances

`plot(model, 1)`

5. ANOVA test

```
summary(model)
```

6. What groups exactly are different?

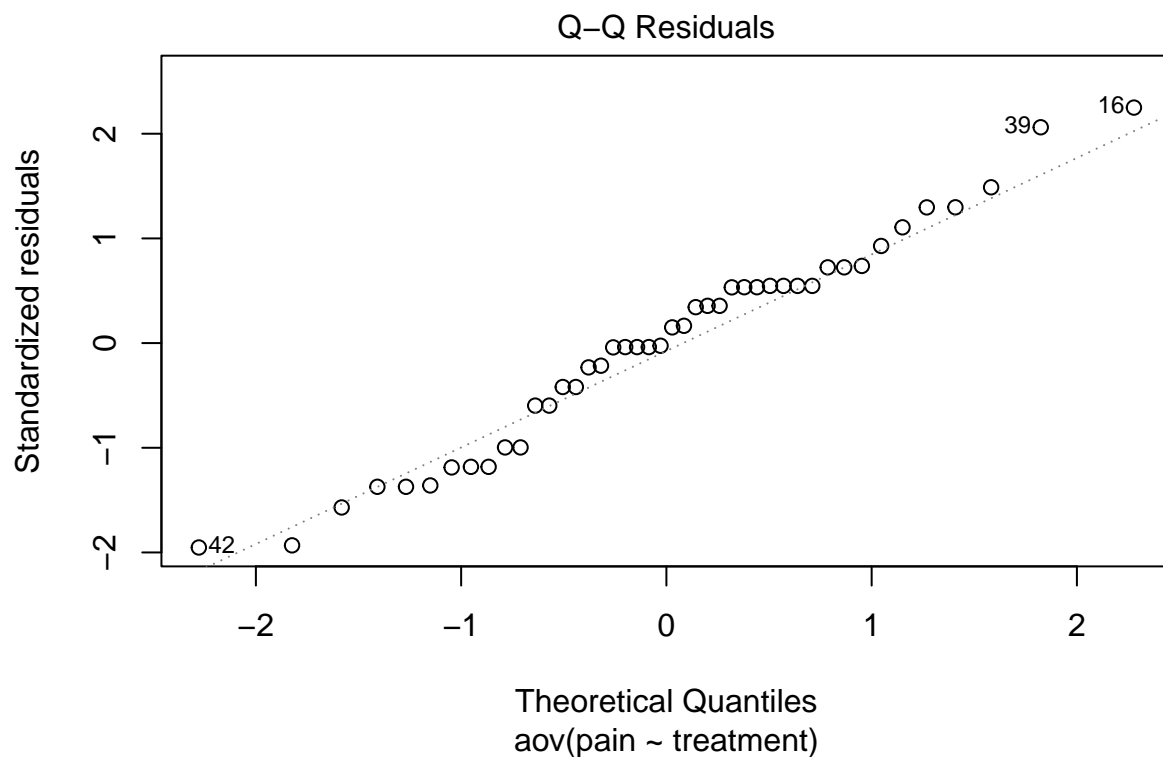
```
TukeyHSD(model)
```

P1. Drug trial dataset

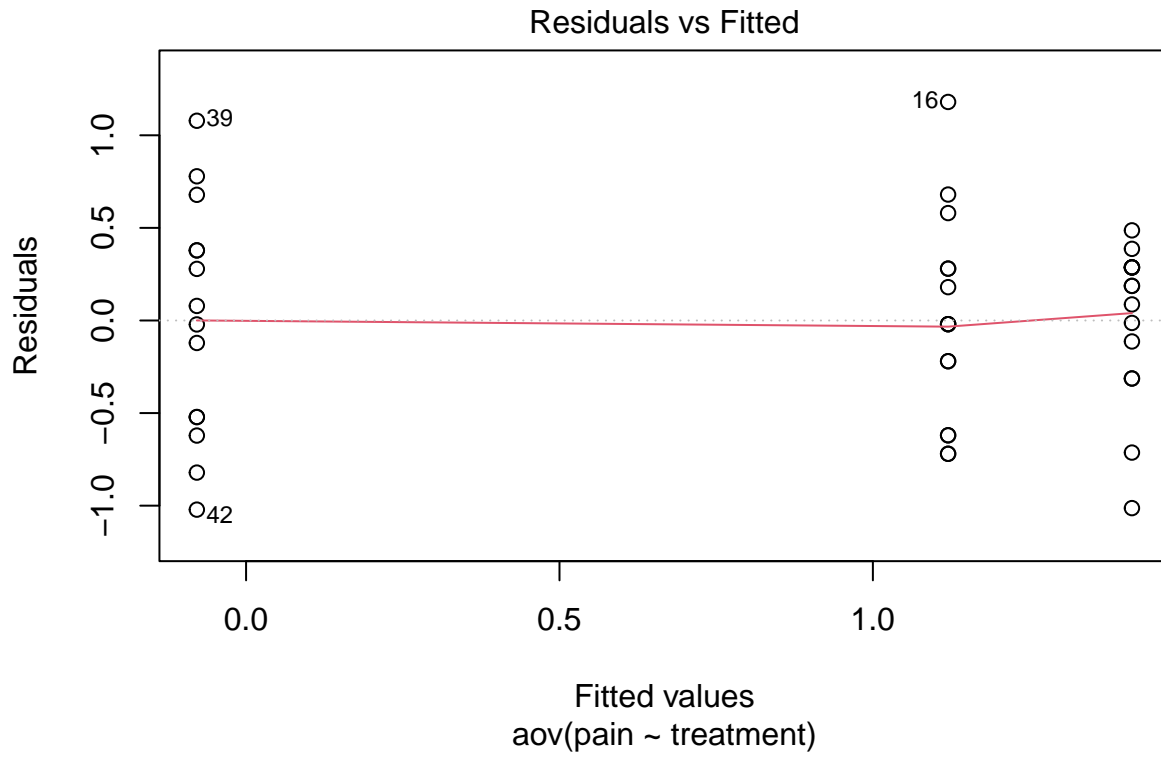
H0: There is no effect of treatment types on pain.

HA: At least one of those factors (placebo or drugA or drugB) influences pain.

```
# 1.Independent random sampling:yes  
# 2.Normality of residuals:yes  
drugmodel = aov(pain~treatment, data = trial)  
plot(drugmodel, 2)
```



```
# 3.Equality of Variances:yes  
plot(drugmodel, 1) # "Residuals vs Fitted" plot, looking for similar heights of "columns"
```



```
#perform ANOVA
summary(drugmodel)
```

```
##           Df Sum Sq Mean Sq F value    Pr(>F)
## treatment   2  17.92   8.960    30.4 8.01e-09 ***
## Residuals  41   12.09   0.295
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
#Run a post-hoc test
TukeyHSD(drugmodel)
```

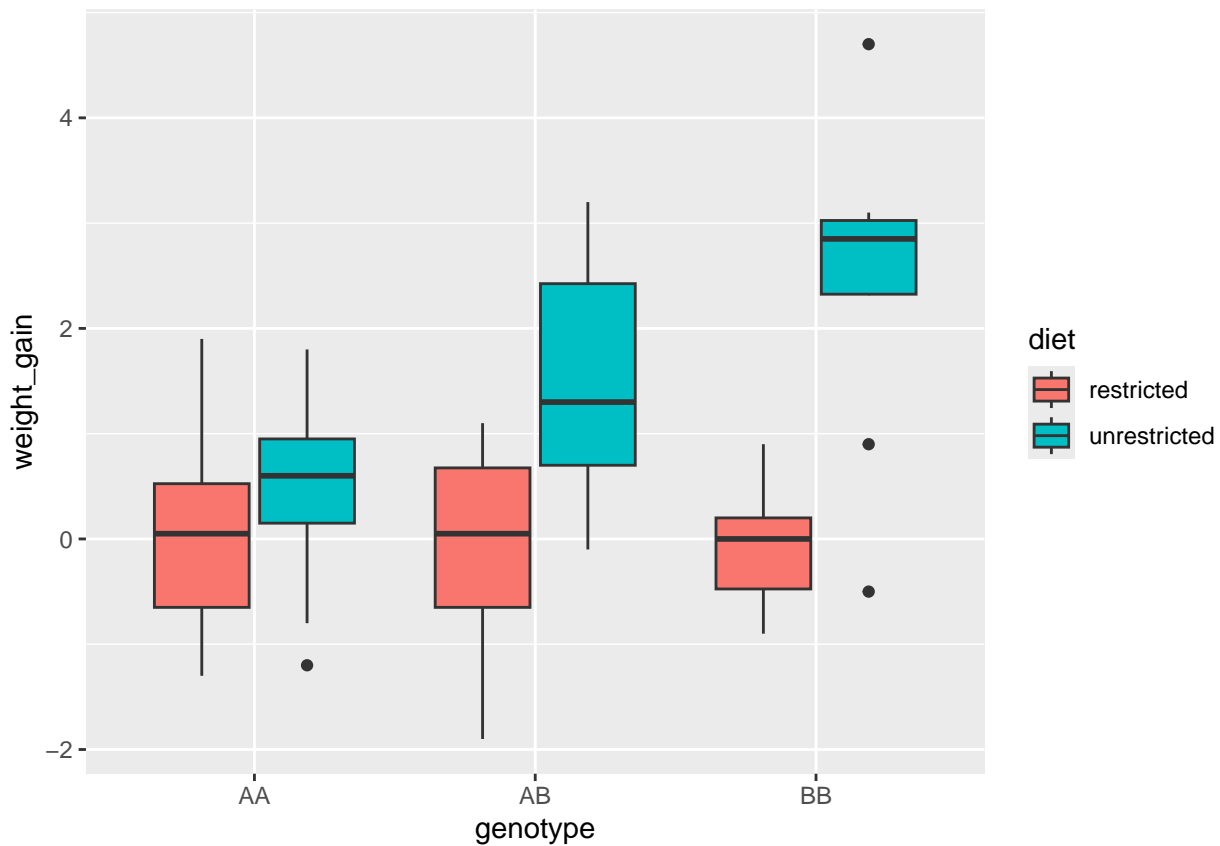
```
##    Tukey multiple comparisons of means
##    95% family-wise confidence level
##
## Fit: aov(formula = pain ~ treatment, data = trial)
##
## $treatment
##           diff           lwr           upr         p adj
## drugB-drugA -1.1985714 -1.6891632 -0.7079797 0.0000016
## placebo-drugA  0.2933333 -0.1887258  0.7753924 0.3110505
## placebo-drugB  1.4919048  1.0013130  1.9824965 0.0000000
```

P2. Weight loss in mice

H0: There is no effect of genotypes on weight_gain.

HA: At least one of those genotypes (AA or AB or BB) influences weight_gain.

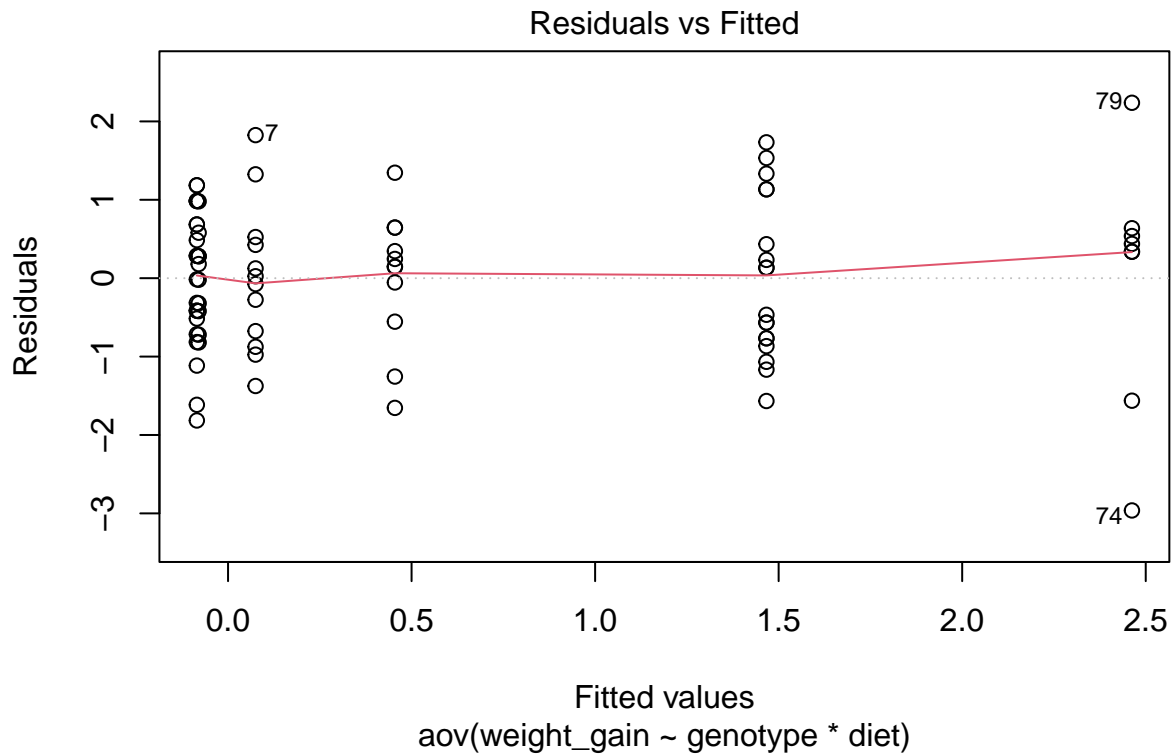
```
#visualise  
p <- ggplot(data = mouse, aes(x = genotype, y = weight_gain, fill = diet))  
p + geom_boxplot()
```



```
# prepare model  
mousemodel = aov(weight_gain~genotype * diet, data = mouse)  
  
#check normality of residuals:yes  
shapiro.test(resid(mousemodel))
```

```
##  
## Shapiro-Wilk normality test  
##  
## data:  resid(mousemodel)  
## W = 0.98974, p-value = 0.7851
```

```
#check equality of Variances:yes
plot(mousemodel, 1)
```



```
#perform ANOVA
summary(mousemodel)
```

```
##           Df Sum Sq Mean Sq F value    Pr(>F)
## genotype     2   6.40     3.20   3.276 0.04342 *
## diet         1  40.39    40.39  41.362 1.16e-08 ***
## genotype:diet 2   11.97     5.99   6.130 0.00346 **
## Residuals    73   71.29     0.98
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
#Run a post-hoc test
TukeyHSD(mousemodel)
```

```
## Tukey multiple comparisons of means
## 95% family-wise confidence level
##
## Fit: aov(formula = weight_gain ~ genotype * diet, data = mouse)
##
## $genotype
##           diff          lwr          upr          p adj
```

```

## AB-AA 0.3934783 -0.2311222 1.018079 0.2935392
## BB-AA 0.7934783 0.0494578 1.537499 0.0338875
## BB-AB 0.4000000 -0.2764864 1.076486 0.3387304
##
## $diet
##               diff          lwr          upr p adj
## unrestricted-restricted 1.432486 0.9884195 1.876552 0
##
## $'genotype:diet'
##               diff          lwr          upr          p adj
## AB:restricted-AA:restricted -0.1600000 -1.21611661 0.8961166 0.9977516
## BB:restricted-AA:restricted -0.1550000 -1.39340649 1.0834065 0.9991025
## AA:unrestricted-AA:restricted 0.3795455 -0.82776637 1.5868573 0.9401208
## AB:unrestricted-AA:restricted 1.3916667 0.31377217 2.4695612 0.0041690
## BB:unrestricted-AA:restricted 2.3875000 1.06735424 3.7076458 0.0000176
## BB:restricted-AB:restricted 0.0050000 -1.11518082 1.1251808 1.0000000
## AA:unrestricted-AB:restricted 0.5395455 -0.54615997 1.6252509 0.6937938
## AB:unrestricted-AB:restricted 1.5516667 0.61198003 2.4913533 0.0001032
## BB:unrestricted-AB:restricted 2.5475000 1.33756643 3.7574336 0.0000005
## AA:unrestricted-BB:restricted 0.5345455 -0.72918895 1.7982799 0.8167215
## AB:unrestricted-BB:restricted 1.5466667 0.40593036 2.6874030 0.0022395
## BB:unrestricted-BB:restricted 2.5425000 1.17056429 3.9144357 0.0000105
## AB:unrestricted-AA:unrestricted 1.0121212 -0.09478011 2.1190225 0.0925815
## BB:unrestricted-AA:unrestricted 2.0079545 0.66402047 3.3518886 0.0005552
## BB:unrestricted-AB:unrestricted 0.9958333 -0.23315548 2.2248221 0.1800034

```

#A allele is related to weight gain