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Assignment - Vector-3

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1

1

1

CONTENTS

I Problem

II Solution

III Code Link 1

IV Figure

I. PROBLEM

In each of the following, find the value of 'k', for which the points are collinear.

(i)
$$(7, -2)$$
, $(5, 1)$, $(3, k)$

(ii) (8, 1), (k, -4), (2, -5)

II. SOLUTION

(i) Given

$$\mathbf{A} = \begin{pmatrix} 7 \\ -2 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 5 \\ 1 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 3 \\ k \end{pmatrix} \tag{1}$$

Then

$$\left(\mathbf{A} - \mathbf{B}\right) = \begin{pmatrix} 2\\ -3 \end{pmatrix} \tag{2}$$

$$\left(\mathbf{A} - \mathbf{C}\right) = \begin{pmatrix} 4\\2k \end{pmatrix} \tag{3}$$

Forming the collinearity matrix

$$\begin{pmatrix} 2 & -3 \\ 4 & 2k \end{pmatrix} \stackrel{R_1 \to R_1 - 1}{\longleftrightarrow} = \begin{pmatrix} 1 & -2 \\ 4 & 2k \end{pmatrix} \tag{4}$$

$$k = 4 \tag{5}$$

(ii) Given

$$\mathbf{A} = \begin{pmatrix} 8 \\ 1 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} k \\ -4 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 2 \\ -5 \end{pmatrix}$$
 (6)

Then

$$\left(\mathbf{A} - \mathbf{B}\right) = \begin{pmatrix} -8k \\ -5 \end{pmatrix} \tag{7}$$

$$\left(\mathbf{A} - \mathbf{C}\right) = \begin{pmatrix} 6\\6 \end{pmatrix} \tag{8}$$

Forming the collinearity matrix

$$\begin{pmatrix} -8k & -5 \\ 6 & 6 \end{pmatrix} \stackrel{R_1 \to R_1 + 8}{\longleftrightarrow} = \begin{pmatrix} k & 3 \\ 6 & 6 \end{pmatrix} \qquad (9)$$

 $k = 3 \tag{10}$

III. CODE LINK

https://github.com/sssurajit/fwc/blob/main/vector/vector-3/codes/vector.py

Execute the code by using the command **python3 vector.py**

IV. FIGURE

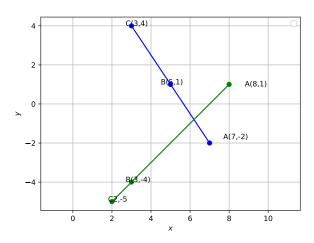


Fig. 1