Assignment - Vector-4



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I. PROBLEM

Determine the ratio in which the line 2x+y-4=0 divides the line segment joining the points A(2,-2) and B(3,7).

II. SOLUTION

Symbol	Value
A	$\begin{pmatrix} 2 \\ -2 \end{pmatrix}$
В	$\begin{pmatrix} 3 \\ 7 \end{pmatrix}$
С	4
n	$\begin{pmatrix} 2 \\ 1 \end{pmatrix}$

TABLE I: Parameters

Given equation

$$\begin{pmatrix} 2 & 1 \end{pmatrix} \mathbf{x} = 4 \tag{1}$$

Using section formula

Let the ratio be k:1 (3)

$$\mathbf{n}^{\mathsf{T}}\mathbf{P} = c \tag{4}$$

(2)

$$\implies \mathbf{n}^{\top} \left(\frac{k\mathbf{B} + \mathbf{A}}{k+1} \right) = c$$
 (5)

$$\implies \mathbf{n}^{\top} (k\mathbf{B} + \mathbf{A}) = c(k+1)$$
 (6)

$$\implies \mathbf{n}^{\top} k \mathbf{B} + \mathbf{n}^{\top} \mathbf{A} = c \left(k + 1 \right) \tag{7}$$

$$\implies k\mathbf{n}^{\mathsf{T}}\mathbf{B} + \mathbf{n}^{\mathsf{T}}\mathbf{A} = c(k+1)$$
 (8)

$$\implies k\mathbf{n}^{\mathsf{T}}\mathbf{B} - ck = -\mathbf{n}^{\mathsf{T}}\mathbf{A} + c \qquad (9)$$

$$\implies k \left(\mathbf{n}^{\top} \mathbf{B} - c \right) = c - \mathbf{n}^{\top} \mathbf{A}$$
 (10)

$$\implies k = \frac{c - \mathbf{n}^{\mathsf{T}} \mathbf{A}}{\mathbf{n}^{\mathsf{T}} \mathbf{B} - c} \tag{11}$$

$$\implies k = \frac{4-2}{13-4} \tag{12}$$

$$\implies k = \frac{2}{9} \tag{13}$$

III. CODE LINK

https://github.com/sssurajit/fwc/blob/main/vector/vector-4/codes/vector.py

Execute the code by using the command **python3 vector.py**

IV. FIGURE

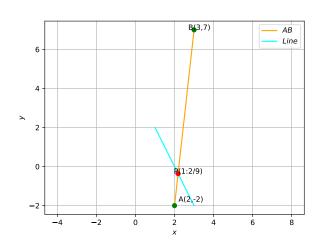


Fig. 1