



# Assignment - 12.10.2.11

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## CONTENTS

<b>I</b>	<b>Problem</b>	1
<b>II</b>	<b>Solution</b>	1
<b>III</b>	<b>Code Link</b>	1
<b>IV</b>	<b>Figure</b>	1

### I. PROBLEM

Show that the vectors  $2\hat{i} + 3\hat{j} + 4\hat{k}$  and  $-4\hat{i} + 6\hat{j} - 8\hat{k}$  are collinear.

### II. SOLUTION

given

$$\mathbf{A} = \begin{pmatrix} 2 \\ 3 \\ 4 \end{pmatrix} \quad \mathbf{B} = \begin{pmatrix} -4 \\ 6 \\ -8 \end{pmatrix} \quad (1)$$

$$\begin{pmatrix} \mathbf{A}^\top \\ \mathbf{B}^\top \end{pmatrix} = 1 \quad (2)$$

$$\begin{pmatrix} \mathbf{A}^\top \\ \mathbf{B}^\top \end{pmatrix} = \begin{pmatrix} 2 & -3 & 4 \\ -4 & 6 & -8 \end{pmatrix} \quad (3)$$

Forming the collinearity matrix (4)

$$\begin{pmatrix} 2 & -3 & 4 \\ -4 & 6 & -8 \end{pmatrix} \xrightarrow{\frac{1}{2}R_1 \rightarrow R_1} \begin{pmatrix} 1 & -\frac{3}{2} & 2 \\ -4 & 6 & -8 \end{pmatrix} \quad (5)$$

$$\xrightarrow{-\frac{1}{4}R_2 \rightarrow R_2} \begin{pmatrix} 1 & -\frac{3}{2} & 2 \\ 1 & \frac{3}{2} & 2 \end{pmatrix} \quad (6)$$

$$\xrightarrow{R_2 - R_1 \rightarrow R_2} \begin{pmatrix} 1 & -\frac{3}{2} & 2 \\ 0 & 0 & 0 \end{pmatrix} \quad (7)$$

There is 1 nonzero in the row echelon form of the matrix, so the rank is 1. If rank of the matrix is 1 then the vectors are collinear.

### III. CODE LINK

<https://github.com/sssurajit/fwc/blob/main/vectors/12.10.2.11/codes/vector.py>

Execute the code by using the command  
**python3 vector.py**

## IV. FIGURE

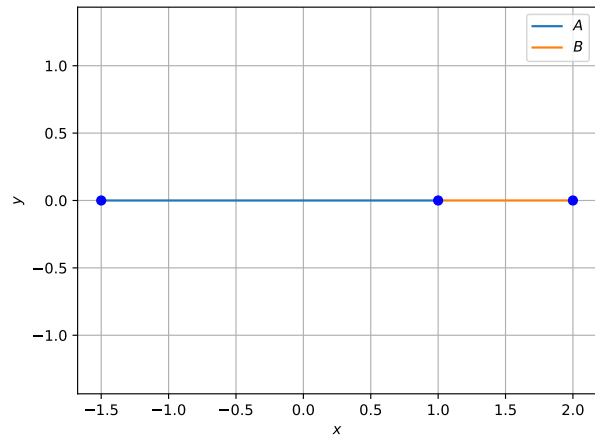


Fig. 1