

DAYANANDA SAGAR COLLEGE OF ENGINEERING
(An Autonomous Institute Affiliated to VTU, Belagavi)
 Shavige Malleshwara Hills, Kumaraswamy Layout, Bengaluru-560078
Department of Telecommunication Engineering
Internal Assessment Test - I

Course: MIMO Communication
 Course Code: TE814
 Semester: VIII 'A' & 'B'

Date: 24/02/2020
 Maximum marks: 50
 Duration: 90 Min

Note: Answer 5 full questions.

- 1 a) A _____ which process the redundancy received signals
 i) Combiner ii) Equalizer iii) PCM iv) All of mentioned
- b) Diversity is used to combat
 i) Fading ii) Co channel interference iii) Error burst iv) all of mentioned
- c) Diversity techniques may exploit the _____ propagation, resulting in a diversity gain
 i) Single path ii) Multipath iii) Narrow path iv) Fading path
- d) The path loss exponent of the free space environment i.e. when only line of sight exists , no scatters is
 i) 2 ii) 3 iii) 6 iv) None of the above
- e) In _____ combiner, the first fully received and valid data packet will be immediately further processed, whereas the later arriving redundant packets will be immediately discarded after reception.
 i) Max-Ratio ii) Equal gain iii) Scanning/Switching iv) Selection
- f) Space diversity means using different physical parts for the signal, at a _____ frequency
 i) Multiple ii) Single iii) Co channel iv) Orthogonal
- g) _____ order means how many degrees of freedom you can have in your design
 i) Rank ii) Selection iii) Diversity iv) Uplink/Downlink
- h) The multipath spread is basically the _____ difference between the shortest and the longest paths that the transmitted signal goes through
 i) Time ii) Frequency iii) Both time and frequency iv) None of the above
- i) If the channel is said to be frequency selective fading channel, then it exhibits _____ interference
 i) Intersymbol interference ii) No Intersymbol interference iii) Both a and b iv) none of the above
- j) Channel capacity , which is defined as the _____ rate at which we can transmit information with an arbitrary _____ probability of error
 i) Maximum, High ii) Maximum, Low iii) Minimum, Low iv) None of the above
- 2 a) Define Channel Fading. Also discuss the wireless propagation mechanism
 b) Describe about Soft Decision Decoding and Hard Decision Decoding.
- 3 a) Focus on Capacity of Noisy Channel.
 b) Analyze the information Rate of Noisy Channel.
- 4 Discuss the classification in Channel Fading
 (OR)
- 5 Elaborate Diversity Techniques in Wireless Communication
- 6 Discuss Beamforming technique with Smart Antennae
 (OR)
- 7 Briefly explain demodulation of signal from set of received signals in MIMO.

Solution Scheme

Subject: MIMO Comm.

Code: TE814

Sem 8th A 4 B

Date: 24/02/2020

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Q1.

(a) (i) Combiner — (i)

(b) all of mentioned — (iv)

(c) Multipath — (ii)

(d) 2 — (i)

(e) Selection — (iv)

(f) Single — (ii)

(g) ~~Rank~~ Diversity — (iii)

(h) Time — (i)

(i) Intersymbol Interference (i)

(j) Maximum, Low

1x10

Q2. (a) Channel Fading (2)

The time variation of received signal power due to changes in transmission medium or path is known as fading. Fading depends on atmospheric conditions and path obstacles.

Wireless channels, signals are received through multiple paths. There is significant time variations caused by the relative motion of transmitter and receiver. Electromagnetic waves travel through three different mechanisms:

- Reflection
- Refraction
- Scattering

(3)

2.b) Soft Decision Coding / Hard Decision Decoding

- | | |
|---|---|
| 1) Difficult to Implement | HDD is relatively simple to Implement |
| 2) Gives the best performance | 2) Does not give the best performance. |
| 3) Receiver is complex | 3) Receiver is simple. |
| 4) Channel decoder directly works with the matched filter output to perform max likelihood decoding | 4) Max likelihood decoder picks the codeword closest to the received sequence in Hamming distance sense as the decoder output |
| 5) Here code constraints are used considered | 5) Tentative Hard decisions are made based on matched filter or correlator outputs without using code constraints. (5) |

2.a) Capacity of Noisy Channel

N = message

Q3 a

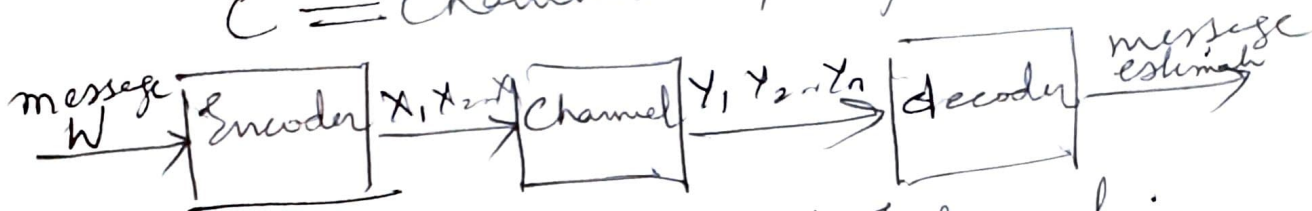
$W = \text{message}$

$n = \text{no of channel}$

$X_1, X_2, \dots = \text{Input channel}$

$Y_1, Y_2, \dots = \text{Output channels}$

$C = \text{Channel Capacity}$



$I(\cdot; \cdot) \rightarrow \text{Mutual Information}$

$$C = \lim_{n \rightarrow \infty} \frac{1}{n} \max_{p(x_1, \dots, x_n)} I(X_1, X_2, \dots, X_n; Y_1, Y_2, \dots, Y_n)$$

$$C = \max_{p(x)} I(X, Y)$$

$$C = \log(1 + P)$$

(5)

Q3(b) Information Rate of Noisy Channel

$$C = \lim_{n \rightarrow \infty} \frac{1}{n} \max_{p(x_1, x_2, \dots, x_n)} I(X_1, \dots, X_n; Y_1, \dots, Y_n)$$

Maximum mutual Information

For memoryless channels i.e if the output-input relationship can be written as

$$p(y_1, y_2, \dots, y_n | x_1, x_2, \dots, x_n) = \prod_{i=1}^n p(y_i | x_i)$$

$$C = \max_{p(x)} I(X; Y) \Rightarrow \text{mutual Information}$$

$$I(X; Y) = E \left[\log \frac{P(X, Y)}{P(X)P(Y)} \right]$$

$E \rightarrow$ expectation is over joint density of X and Y

(5)

Q 4.1. Classification of channel Fading

Path Loss Fading :- It is Large scale fading.
We can write received Power P_r as

$$P_r = \frac{c}{d^n} P_t$$

d → Separation between transmitter and receiver.

P_t → Transmitted power.

c → constant

n → Path loss exponent in range of 2 to 6.

Shadowing :- It is Large scale fading.
Here received Signal strength is averaged over a long period of time of order of few seconds or minutes.

$$P_r \text{ dBm} = \bar{P}_r \text{ dBm} + X_\sigma \text{ dB}$$

dBm, X_σ → Zero mean random variable.

X_σ has $SD = \sigma$

$\sigma = SD$ can be 3 dB - 12 dB.

(2)

Flat Frequency ~~Fading~~ Selective Fading

$$B.W = W.$$

B_c = coherence B.W

If Signal Bandwidth W is significantly smaller than the coherence B.W B_c of channel, all frequency components see the same effective channel, i.e. $C(f; t)$ for the frequency range of interest will be independent of f .

$$y_i(t) = C(0;t) \int_{-\infty}^{\infty} x_L(f) e^{j2\pi f t} df$$

$$= C(0;t) x_L(t)$$

$W \ll B_c \Rightarrow$ multipath spread of channel is significantly smaller than signal time duration.

\rightarrow No Inter Symbol Interference between consecutive symbols.

\rightarrow Different frequency components undergo different channel fades. (2)

Flat Frequency fading

$W > B_c$; $C(0;t) \approx C(0, \infty T) = \text{constant}$
 $T_m > T_s \Rightarrow$ Symbol time is smaller than signal time.

\rightarrow All frequency components of signal undergo same channel fades. (2)

Slow Fading / Fast Fading

Slow Fading

\rightarrow Symbol duration T_s is significantly smaller than coherence time of channel.
 \rightarrow Channel remains the same over entire symbol period.

Fast Fading

\rightarrow Symbol duration T_s is greater than coherence time of channel (2)
 \rightarrow Channel differs over same symbol period

Rayleigh Fading

Rayleigh Fading

channel coefficient has zero mean.
channel gain has absolute value Rayleigh
 $C = \text{Complex Gaussian Random variable}$

Rician Fading

Channel gain has non zero mean
 $C = \text{multiplicative term} = \text{Complex Gaussian Random variable}$

Q5 Diversity techniques in

Diversity techniques collectively refer to methods of improving this performance by effectively transmitting the same information multiple times where each replica sees a different ideally independent channel.

Frequency Diversity

Space Diversity

Time Diversity

Transmit Diversity

Receive Diversity

Channel Coding

Explanations

Q6. Beam Forming Techniques with Smart Antennas
Consider a scenario of small number of local scatterers and comm by

any. In such scenario multiple antenna elements can be employed at transmitter in order to provide directionality for electromagnetic waves, hence improving the effective SNR of channel.

A fundamental approach is the transmission of same signal from each of antenna elements with a certain gain and phase shift.

This can be implemented Analog or Digital. Digital Beam forming is more flexible.

Different techniques can be used to find suitable coefficients and of antenna beam, from feedback.

Coefficients can be computed to make effective antenna pattern have main beam in this required direction.

Also Interference suppression can be accomplished using beam forming.

Q 7. Demodulation from Signal received from set of MIMO

Maximum Ratio Combining

Assun channel coefficients are perfectly available at receiver.

Maxi Likelihood decision rule on symbol transmitted is

$$\hat{x} = \arg \max_{j=1, 2, \dots, M} P(y_1, y_2, \dots, y_L / h_1, h_2, \dots, h_L, x_j) \text{ page-7.}$$

$P(\cdot|\cdot) \rightarrow$ conditional joint Pdf.
 Since channel gains, transmitted signal, received signal are independent. (4)

$$\hat{x} = \underset{j=1,2,\dots,M}{\operatorname{argmin}} \operatorname{Re} \left\{ \left(\sum_{l=1}^L h_l^* y_l \right) x_j^* \right\} - \frac{1}{2} \sqrt{P \left(\sum_{l=1}^L |h_l|^2 \right)} |x_j|^2$$

SNR of L branch diversity with MRC is the sum of instantaneous SNRs of each branch. Hence error probabilities and outage will be reduced.

Selection Combining :-

Works with branch with best channel condition for any given transmission i.e. highest SNR branch is picked. (2)

Equal Gain Combining :-

- Signals of all branches are co-phased by multiplying with $e^{-j\angle h_l}$ using baseband notation.
- Signals summed together to form equivalent channel output. (2)

Switch and Stay Combining :-

We use particular branch for demodulation until SNR of it falls below threshold; then the other branch which has largest SNR is chosen and maintained till it also falls below threshold. This procedure is carried. (2)