

QMM Assignment

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R Markdown

```

tbl <- matrix(c(22,14,30,600,100 ,
16,20,24,625,120,
80,60,70,"-","-" ), ncol=5, byrow=TRUE)
colnames(tbl) <- c("Warehouse 1", "Warehouse 2", "Warehouse 3","Production cost","Production Capacity")
rownames(tbl) <- c("Plant A", "Plant B","Monthly Demand")
tbl <- as.table(tbl)
tbl

##                               Warehouse 1 Warehouse 2 Warehouse 3 Production cost
## Plant A                  22          14          30          600
## Plant B                  16          20          24          625
## Monthly Demand           80          60          70          -
##                               Production Capacity
## Plant A                  100
## Plant B                  120
## Monthly Demand          -

```

The above transportation problem can be formulated in the LP format as below:

$$\begin{aligned} \text{Min } TC = & 22x_{11} + 14x_{12} + 30x_{13} \\ & + 16x_{21} + 20x_{22} + 24x_{23} \\ & + 80x_{31} + 60x_{32} + 70x_{33} \end{aligned}$$

Subject to the following major constrains and variables

Supply constraints:

$$x_{11} + x_{12} + x_{13} \leq 100$$

$$x_{21} + x_{22} + x_{23} \leq 120$$

Demand Constraints:

$$\begin{aligned}x_{11} + x_{21} &\geq 80 \\x_{12} + x_{22} &\geq 60 \\x_{13} + x_{23} &\geq 70\end{aligned}$$

Non-Negativity of the variables:

$$x_{ij} \geq 0$$

where

$$i = 1, 2, 3$$

and

$$j = 1, 2, 3$$

```
library(lpSolve)
```

```
## Warning: package 'lpSolve' was built under R version 4.1.3
```

```
# Set up cost matrix
```

```
cost_tbl <- matrix(c(622, 614, 630, 0,  
641, 645, 649, 0), ncol = 4, byrow = TRUE)
```

```
# Set Plant names
```

```
colnames(cost_tbl) <- c("Warehouse 1", "Warehouse 2", "Warehouse 3", "Dummy")  
rownames(cost_tbl) <- c("Plant A", "Plant B")  
cost_tbl
```

```
##          Warehouse 1 Warehouse 2 Warehouse 3 Dummy  
## Plant A       622        614        630      0  
## Plant B       641        645        649      0
```

```
#Set up constraint signs and right-hand sides (supply side)
```

```
row.signs <- rep("<=", 2)  
row.rhs <- c(100, 120)
```

```
#Demand (sinks) side constraints
```

```
col.signs <- rep(">=", 4)  
col.rhs <- c(80, 60, 70, 10)
```

```
#Run
```

```
lptrans_tbl <- lp.transport(cost_tbl, "min", row.signs, row.rhs, col.signs, col.rhs)
```

```
#Values of all 8 variables
```

```
lptrans_tbl$solution
```

```
##      [,1] [,2] [,3] [,4]  
## [1,]    0   60   40    0  
## [2,]   80    0   30   10
```

```
#Value of the objective function
```

```
lptrans_tbl$objval
```

```
## [1] 132790
```

```
#Getting the constraints value
```

```
lptrans_tbl$solution
```

```
##      [,1] [,2] [,3] [,4]
## [1,]     0   60   40    0
## [2,]    80    0   30   10
```

#In order to minimize the overall cost of production as well as shipping, the better approach is to produce 80 AEDs in Plant 2 - Warehouse1, 60 AEDs in Plant 1 - Warehouse2, 40 AEDs in Plant 1 - Warehouse3, 30 AEDs in Plant 2 - Warehouse3 in each plant which are distributed to each of the three wholesaler warehouses.

#As a result, we formulate the dual of the above transportation problem

#Since the primal was to be minimized so that the transportation cost the dual of it would be to maximize the value added(VA).

$$\text{Maximize VA} = 80W_1 + 60W_2 + 70W_3 - 100P_A - 120P_B$$

Subject to the following constraints

Total Profit Constraints

$$MR_1 - MC_1 \geq 622$$

$$MR_2 - MC_1 \geq 614$$

$$MR_3 - MC_1 \geq 630$$

$$MR_1 - MC_2 \geq 641$$

$$MR_2 - MC_2 \geq 645$$

$$MR_3 - MC_2 \geq 649$$

Where MR_1 = Marginal Revenue from Warehouse1

MR_2 = Marginal Revenue from Warehouse2

MR_3 = Marginal Revenue from Warehouse3

MC_1 = Marginal Cost from Plant1

MC_2 = Marginal Cost from Plant2

Economic Interpretation of the dual

$$MR_1 \leq MC_1 + 622$$

$$MR_2 \leq MC_1 + 614$$

$$MR_3 \leq MC_1 + 630$$

$$MR_1 \leq MC_2 + 641$$

$$MR_2 \leq MC_2 + 645$$

$$MR_3 \leq MC_2 + 649$$

#The above constraints are framed under the economic interpretation of the dual which technically follows the universal rule of profit maximization which are $MR \geq MC$ where “MR” is the Marginal Revenue and “MC” is the Marginal Cost.

$$MR_1 \leq MC_1 + 621 \quad i.e. \quad MR_1 \geq MC_1$$

#Marginal Revenue is mainly focused on the revenue generated for each additional unit sold relative to Marginal Cost (MC) i.e. The change in cost at Plant 1 along with an increase in the supply function should be greater than or equal to the revenue generated for each additional unit distributed to Warehouse 1.

#This approach is used in businesses to balance their production output with their costs to maximize profit by this process the businesses can avoid losses.