18.022 Recitation Quiz (with solutions) 13 November 2014

1. Integrate $f(x, y, z) = x^2 + y + z$ over the pentahedron with vertices (0, 0, 0), (1, 0, 0), (0, 2, 0), (1, 2, 0), (0, 0, 4) and (1, 0, 4).

Solution. We evaluate

$$\int_0^1 \int_0^2 \int_0^{4-2y} x^2 + y + z \, dz \, dy \, dx = \boxed{28/3}.$$