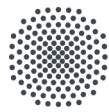


Robust Weighting and Matching Techniques for Causal Inference in Observational Studies with Continuous Treatment

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October 19, 2022

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Chapter 1

Chapter One Title

hello \mathbb{R}

Chapter 2

Convex Analysis

We begin by defining convex sets

Definition 1 A subset $\Omega \subseteq \mathbb{R}^n$ is called *CONVEX* if we have $\lambda x + (1 - \lambda)y \in \Omega$ for all $x, y \in \Omega$ and $\lambda \in (0, 1)$.

Clearly, the line segment $[a, b] := \{\lambda a + (1 - \lambda)b \mid \lambda \in [0, 1]\}$ is contained in Ω for all $a, b \in \Omega$ if and only if Ω is a convex set.

Next we define convex functions.

The concept of convex functions is closely related to convex sets.

The line segment between two points on the graph of a convex function lies on or above and does not intersect the graph.

In other words: The area above the graph of a convex function f is a convex set, i.e. the *epigraph* $\text{epi}(f) := \{(x, \alpha) \in \mathbb{R}^n \times \mathbb{R} \mid f(x) \leq \alpha\}$ is a convex set in \mathbb{R}^{n+1} .

Often an equivalent characterisation of convex functions is more useful.

Theorem 1 The convexity of a function $f : \mathbb{R}^n \rightarrow \overline{\mathbb{R}}$ on \mathbb{R}^n is equivalent to the following statement:

For all $x, y \in \mathbb{R}^n$ and $\lambda \in (0, 1)$ we have

$$f(\lambda x + (1 - \lambda)y) \leq \lambda f(x) + (1 - \lambda)f(y). \quad (2.1)$$