

# AWE: A Mac-Layer Encounter Protocol for a Wildlife Tracking System

*Abstract—*

## I. INTRODUCTION

## II. BACKGROUND AND RELATED WORK

*Encounternet* [1]

## III. SYSTEM MODEL

In this paper, we study the encounter problem in a wildlife tracing system. We call individual animals as *agents*, and *peers* are referred as other agents that distinguish from a specific one. The definition of the *Encounter process* is formulated as follows.

**Definition 1:** Encounter is defined as the process that an agent detects and records message from other peer(s) if they keep at least  $T_0$  slots of close proximity  $\Delta \leq D$  in the wildlife tracking system.

In the following, we describe the system model for theoretical analysis in this paper.

### A. Communication Model

In the wildlife tracing system *Encounternet*, the encounter process is a common biological behavior and happens when more than one agents gather closely, constituting a single clique of size  $k$  ( $k \geq 2$ ). Note that,  $k$  is not known to each agent and the whole clique composes a sing-hop network for communication due to the proximity.

Each agent is equipped with a tag containing radio. An agent that has its radio on can choose to be in the *Transmit* state or the *Listen* state:

- **Transmit state:** an agent transmits (broadcasts) a message containing its ID on the channel;
- **Listen state:** an agent listens on the channel to receive messages from peers.

Suppose time is divided into slots of equal length  $t_0$ , which is assumed to be sufficient to finish a complete communication process (one agent transmits a message including its ID and a peer receives the message).

An agent transmit successfully in a time slot if and only if it is the only one transmitting and all the other peer(s) will receive its message and record its ID. Otherwise the channel is detected as *idle* if there is no transmission and *busy* if there are simultaneous messages.

In the wildlife tracing system *Encounternet*, on the one hand, each agent (animal) is equipped with an energy-restricted tag; on the other hand, encounter process happens occasionally, and it is a waste of energy if transmitting while there is no encounter with other peer(s). Thus in order to keep

a balance between the energy consumption and the efficiency of encounter process, we introduce the duty cycle mechanism.

**Duty cycle mechanism.** An agent has the capability to turn off the radio to save energy for most of the time, and may only be active (transmitting or receiving) during a fraction  $\theta$  of the time.

Incorporating the duty cycle mechanism, in each time slot an agent  $u_i$  is able to adopt an action as:

$$s_i^t = \begin{cases} \text{Sleep} & \text{sleep with probability } (1 - \theta_i) \\ \text{Transmit} & \text{transmit with probability } \theta_i p \\ \text{Listen} & \text{listen with probability } \theta_i(1 - p) \end{cases}$$

**Duty cycle** is defined as the fraction of time an agent turns its radio on, which is formulated as:

$$\theta_i = \frac{|\{t : 0 \leq t < t_0, s_i(t) \in \{\text{Transmit}, \text{Listen}\}\}|}{t_0}.$$

**Collision detection mechanism.** A listening agent can distinguish whether the channel is *idle* or *busy*, apart from successful receiving a message.

### B. Problem formulation

We formulate the problem in this paper as follows:

**Problem 1:** We define an encounter problem as to design a protocol to guarantee all the agents in the clique can receive message from each other at least once if they encounter for at least  $T$  ( $T \leq T_0$ ) time slots (i.e.,  $T$  is the upper bound of the protocol).

We look into the problem and find the key challenge is the uncertainty of dynamic movements of agents. Despite the dynamicity in this real system, when  $T_0$  is short enough relative to the time required for an agent to move a step (a short distance) in reality (e.g., less than 1 second), we can make a reasonable assumption that the communication connectivity of the agents is stable during each  $T_0$  time slots.

## IV. ADAPTIVE WILDLIFE ENCOUNTER PROTOCOL

In this section, we present our Adaptive Wildlife Encounter (AWE) protocol. The pseudo-code of the protocol is given in Algorithm 2 and Algorithm 3.

AWE consists of two stages: detecting stage and connecting stage.

- **Stage 1: detecting stage.** In this stage, an agent attempts to detect whether there are nearby peers, regardless of who they are.

- **Stage 2: connecting stage** In this stage, an agent attempts to identify the nearby peer(s) and record their IDs to its log.

Initially, each agent starts from the detecting stage. In the detecting stage, an agent turns its radio to the *sleep* state most of the time, and switches to *transmit* state or *listen* state at intervals. In the connecting stage, agents only switch between *transmit* state and *listen* state.

The key idea of AWE is that, any single agent keeps in detecting stage to reduce ineffective energy consumption. When encounter happens, it detects the existence of nearby peers and turns to the connecting stage to identify those peers (or a peer) and record the encounter process to its log. After the encounter process is finished, the agent turns back to the detecting stage.

*Remark 1:* In the AWE protocol, there is no need to synchronize the stage between agents and AWE still works in this case. The proof of correctness will be presented in section V.

In the following subsections, we describe the operations of these two stages in detail.

#### A. Detecting stage

In the detecting stage, energy efficiency is achieved by the duty cycle mechanism, e.g., denote the predefined duty cycle for all the agents is  $\theta$ , the tag radio of each agent will work  $\theta T_0$  time slots in every period of  $T_0$ . However, it is very ineffective when two agents encounter and one is in *sleep* state while the other is transmitting or listening.

To technically achieve synchronizing the time that agents turn on the radio, we first introduce the Relax Difference Set (RDS). We use the RDS technique to guarantee that every encounter pair of agents turn on the radio in the same time slot at least once in each round  $T_0$ .

RDS is an efficient tool to construct cyclic quorum systems. The definition is:

*Definition 2:* A set  $R = \{a_1, a_2, \dots, a_k\} \subseteq Z_T$  (the set of all non-negative integers less than  $T$ ) is called a RDS if for every  $d \neq 0 \pmod{T}$ , there exists at least one ordered pair  $(a_i, a_j)$  such that  $a_i - a_j \equiv d \pmod{T}$ , where  $a_i, a_j \in D$ .

We now give an example to explain how RDS works to help synchronization, as depicted in Figure ?? (TBD). Suppose the duty cycle is set as 0.4, i.e., there are 4 active slots in every 10 time slots. it is easy to show that  $R = \{1, 2, 3, 6\}$  is a RDS under  $Z_{10}$ :

$$\begin{aligned} 2 - 1 &= 1, & 3 - 1 &= 2, & 6 - 3 &= 3, & 6 - 2 &= 4, \\ 6 - 1 &= 5, & 2 - 6 &= 6 \pmod{10}, & \dots, & \dots, \end{aligned}$$

In every round of 10 time slots, for any  $i = \{0, 1, \dots, 9\}$ , if  $i \in R$ , then the agent turns on its radio in the  $i^{th}$  slot in this round; otherwise it turns to the *sleep* state. Consider any two agents in the detecting stage: if the time drift between their time rounds is  $\delta$ , there exists at least one ordered pair  $(a_i, a_j)$  in  $R$  such that  $a_i - a_j \equiv \delta \pmod{10}$ . That is, in each period  $T_0$ , any two agents at least once turn on the radio in the same time slot.

---

#### Algorithm 1 RDS Construction Algorithm

---

```

1:  $R := \emptyset; \lambda := \lceil \sqrt{T} \rceil, \mu := \lceil \frac{\lceil \sqrt{T} \rceil}{2} \rceil;$ 
2: for  $i = 1 : \lambda$  do
3:    $R := R \cup i;$ 
4: end for
5: for  $j = 1 : \mu$  do
6:    $R := R \cup (1 + j * \lambda);$ 
7: end for
```

---

It has been proved that any RDS must have cardinality  $|R| \geq \sqrt{T}$  [2]. We present a linear algorithm to construct a RDS with cardinality  $\lceil \frac{3\sqrt{T}}{2} \rceil$  under  $Z_T$  in Alg. 1.

We show the correctness of the construction formally.

*Lemma 1:* Set  $R = \{r_0, r_1, \dots, r_{\lambda+\mu-1}\}$  constructed in Alg. 1 is a RDS, where  $|R| = \lambda + \mu = \lceil \sqrt{N} \rceil + \lceil \frac{\lceil \sqrt{N} \rceil}{2} \rceil \approx \lceil \frac{3\sqrt{N}}{2} \rceil$ .

*Proof:* Obviously, if there exists one ordered pair  $(a_i, a_j)$  satisfying  $a_i - a_j \equiv d \pmod{N}$ , an opposing pair  $(a_j, a_i)$  exists such that  $a_j - a_i \equiv (N - d) \pmod{N}$ . Thus we only need to find at least one ordered pair  $(a_i, a_j)$  for each  $d \in [1, \lfloor N/2 \rfloor]$ .

In the construction,  $\lambda$  in Line 1 is the smallest integer satisfying  $\lambda^2 \geq N$ . Every  $d$  in range  $[1, \lfloor N/2 \rfloor]$  can be represented as:  $d = 1 + j \times \lambda - i$ , where  $1 \leq j \leq \mu, 1 \leq i \leq \lambda$ . Thus, there exists  $a_j = 1 + j \times \lambda$  from Line. 3 and  $a_i = i$  from Line. 6 satisfying  $a_j - a_i \equiv d$ . Then, the lemma can be derived. ■

---

#### Algorithm 2 Detecting Algorithm

---

```

1:  $T_0 := \lceil \frac{9}{4\theta^2} \rceil; \omega_0 := \frac{1}{2}; t := 0;$ 
2: Invoke Alg. 1 to construct  $R = \{r_0, r_1, \dots, r_{\lceil \frac{3\sqrt{T}}{2} \rceil}\}$  under  $Z_T$ ;
3: while True do
4:   if  $(t + 1) \in R$  then
5:     Generate a random float  $\rho \in (0, 1)$ ;
6:     if  $\rho < \omega_0$  then
7:       Transmit a beacon;
8:     else
9:       Listening;
10:    if Detects energy (a beacon or a collision by multiple beacons) then
11:      Turn to Connecting Stage;
12:    end if
13:  end if
14: else
15:   Sleep;
16: end if
17:  $t := (t + 1) \% T_0;$ 
18: end while
```

---

Based on the RDS, we present the operations in the detecting stage as Alg. 2. An agent turns on its radio according to the RDS sequence and in each active slot it transmits a beacon with probability  $\omega_0$  and listen with probability  $1 - \omega_0$ . As discussed before, the aim of this stage

is to detect nearby peer(s) as fast as possible (if exists), and either successful transmission or detecting collisions activate the agent to the connecting stage. Here we fix the transmitting probability as  $\omega_0 = \frac{1}{2}$  since it is the optimal probability for two-agent encounter, the most common case in the *Encounternet* system (??Not sure).

*Remark 2:* Though  $\omega_0 = \frac{1}{2}$  is not the optimal probability in multi-agent encounter cases, the probability that an agent detects a peer in a time slot grows as the number of agents increases. This is because a new agent will not interrupt but help other agents to detect peers if it is in *transmit* state in a time slot.

### B. Connecting stage

In the connecting stage, agents attempt to identify the nearby peers and record the encounter to its log. A successful identification happens only if the agent is listening and exactly one peer is transmitting.

---

#### Algorithm 3 Connecting Algorithm

---

```

1:  $t := 0; \omega_t := \zeta;$ 
2: while True do
3:   In the first sub-slot:
4:   Transmit a message containing ID with probability  $\omega_t$ 
     and listen with probability  $1 - \omega_t$ ;
5:   In the second sub-slot:
6:   if the agent is in listen state in the first sub-slot then
7:     if receive a message successfully then
8:       Record the source ID and transmit a beacon;
9:        $\omega_{t+1} := \frac{\omega_t}{2};$ 
10:    else if channel is idle then
11:       $\omega_{t+1} := \min\{2 \cdot \omega_t, \zeta\};$ 
12:    end if
13:  else
14:    if detect energy then
15:      Turn to the quiet state : keep listening in all the
        rest time slots of this round;
16:    else
17:       $\omega_{t+1} := \frac{\omega_t}{2};$ 
18:    end if
19:  end if
20:   $t := (t + 1);$ 
21:  if  $t == \hat{T}$  then
22:    if no peer is found in this round then
23:      Turn to Detecting Stage;
24:    else
25:       $t := 0; \omega_t := \zeta;$ 
26:    end if
27:  end if
28: end while

```

---

The collision detection (CD) mechanism is incorporated in this stage to increase of efficiency. This mechanism enables the listening agent to notify its transmitting peers of the transmission outcomes, and hence they take measures to reduce the collisions.

Each time slot is divided into two sub-slots and every  $\hat{T}$  complete time slots consists of a round. Agents execute transmission or reception in the first sub-slot, and maintain the EncounterList and reply a beacon in the second sub-slot (if receive a message successfully in the first sub-slot). The algorithm in detecting stage is formulated as Alg. 3.

As discussed in section IV,  $\hat{T}$  is relatively short in real world, thus the communication connectivity stays stable in a round. However, due to the movements of agents, the communication connectivity may change from round to round, so all the parameters will be initialized at the beginning of each round and adaptively adjusted later according to the transmission outcome.

Since the number of the nearby peers is unknown to each agent, the transmitting probability is initially set as  $\zeta$ , which is a pre-defined constant. In the first sub-slot of each time slot  $t$ , an agent transmit a message containing ID with probability  $\omega_t$  and listen with probability  $1 - \omega_t$ .

In the second sub-slot:

- 1) The agent is in *listen* state in the first sub-slot:
  - if the agent receives a message successfully, it decodes and records the source ID in the message, and transmits a beacon (a bit is OK) as an acknowledgement on the channel in the second sub-slot;
  - if the channel is idle, this means there is a chance to transmit successfully and it multiplies its transmitting probability by a factor 2 (no larger than  $\zeta$ ).
  - if the agent detects collisions, it does nothing.
- 2) The agent is in *transmit* state in the first sub-slot:
  - if the agent detects energy (beacon or collisions) in this sub-slot, this means its previous message has been successfully received by its nearby peers, and it keeps listening in all the rest time slots of this round, which is called *quiet* state.
  - if the agent detects nothing in this sub-slot, it means its previous message failed to propagate due to simultaneous transmitting. Thus it divides its transmitting probability by a factor 2.

In the end of a complete round, if there is no peer detected in this whole round, which indicates the encounter process is finished, the agent turns to the detecting stage .

### V. ANALYSIS OF THE AWE PROTOCOL

In this section, we prove that with a clique of  $k$  agents, AWE protocol guarantees each agent can record all the peers in  $O(k)$  slots with high probability. Formally, this conclusion is derived from the following theorem.

*Theorem 1:* Consider an encounter process of  $k$  agents :

- (1) An agent in detecting stage will switch to the connecting stage in  $O(f(\theta))$  slots with high probability.
- (2) When all the agents are in the connecting stage, each agent can successfully transmit once and turn to *quiet* state in  $O(k)$  slots with high probability.

We prove the first conclusion in Theorem 1 in Section V-C, and the second conclusion in Section V-A. Finally, We explain

how the AWE protocol deal with the dynamic movements of agents and record a duration encounter process in Section ??.

#### A. Time bound for detecting stage

When encounter happens, an agent in detecting stage will switch to connecting stage very soon. We derive this conclusion from the following lemma.

**Lemma 2:** An agent in detecting stage will switch to the connecting stage in  $\frac{\ln \eta}{\ln(\frac{1}{2} + \frac{1}{2k})} \lceil \frac{9}{4\theta^2} \rceil$  slots with high probability.

*Proof:* Consider two agents encounter at a time and one turn to the connecting stage first. Then the other will switch to the connecting stage very soon since the prior one in connecting stage increases its transmission probability (because there is no duty cycle in the connecting stage) to let other peers detect it.

Now we consider  $k$  agents in the detecting stage at the beginning. For any pair of agents  $(u_i, u_j)$ , we can find an ordered pair  $(r_i, r_j)$  from the constructed RDS such that  $r_i - r_j \equiv \delta_{ij}$  (mode  $T_0$ ), where  $\delta_{ij}$  is the time drift. This indicates that any two peers can turn on their radios in the same slot at least once during every period of  $T_0$ . For a specific agent, the probability it detects a peer in a rounds of  $T_0$  is at least  $Pr \geq 1 - (\frac{1}{2} + \frac{1}{2k})$ . Hence it holds with high probability that an agent detects peer(s) in  $\frac{\ln \eta}{\ln(\frac{1}{2} + \frac{1}{2k})} \lceil \frac{9}{4\theta^2} \rceil$  slots, where  $\eta$  is small enough. ■

#### B. Time bound for connecting stage

Consider the connecting stage. We analyze the upper bound of slots for all the agents in the clique to transmit successfully. Note that, an agent transmitting successfully will be recorded by all the other peers in the clique, and then it switches to the *quiet* state. Denote  $S_t$  as the set of agents which have not switched to the *quiet* state in time slot  $t$ , and  $|S_t|$  is the cardinality. Thus the upper bound of the protocol is the maximum time slots for a clique to turn to  $|S_t| = 0$ .

In the following, we first show the upper bound of slots it takes from the beginning to  $|S_t| \leq \log k$  in Lemma 3. Then we show the upper bound it takes to  $|S_t| = 1$  in Lemma 13. Finally we present that it takes for all agents to successfully transmit (i.e.,  $|S_t| = 0$ ) in  $O(k)$  in Lemma 14.

**Lemma 3:** At time  $T_2 = T_1 + \gamma_1 \cdot k = O(k)$  it holds with high probability that  $|S_{T_2}| \leq \log k$ .

To prove this lemma, we need to introduce and prove some small lemmas at first. We review two useful lemmas as follows.

**Lemma 4:** Consider a set of  $l$  agents,  $u_1, u_2, \dots, u_l$ . For an agent  $u_i$ , it transmits with probability  $0 < \omega(u_i) < \frac{1}{2}$ . Let  $p_0$  denote the probability that the channel is idle in a time slot; and  $p_1$  denote the probability that there is exactly one transmission in a time slot. Then  $p_0 \cdot \sum_{i=1}^l \omega(u_i) \leq p_1 \leq 2 \cdot p_0 \cdot \sum_{i=1}^l \omega(u_i)$

**Lemma 5:** With  $a_i \in [0, \frac{1}{2}]$  for  $i = 0, 1, \dots$ , it holds that

$$4^{-\sum_i a_i} \leq \prod_i (1 - a_i) \leq e^{-\sum_i a_i}. \quad (1)$$

The proof of Lemma 4 can be referred to [3] and the proof of Lemma 5 can be referred to [4]. Based on these two lemmas, we get the following conclusion.

**Lemma 6:** For a time slot  $T > 0$  with  $|S_t| \geq \log k$ , if there exist constants  $\alpha_1, \alpha_2 \geq 1$  such that  $\alpha_1 \leq \sum_{u \in S_t} \omega_t(u) \leq \alpha_2$ , then with constant probability there is one active node switching to the *quiet* state in each time slot.

*Proof:* In each time slot, the channel is idle with probability at least  $4^{-2\alpha}$ , and there is exactly one transmission on the channel with probability at least  $\alpha \cdot 4^{-2\alpha}$ . By the Chernoff bound, it holds that with constant probability (given  $\alpha_1$  and  $\alpha_2$ ), there are one agent switch to the quiet state in each slot. ■

Next we show that after all the agents turn to the connecting stage, the summation of the total agents' transmission probabilities will go between  $\alpha_1$  and  $\alpha_2$  soon, where  $\alpha_1$  and  $\alpha_2$  are constants defined in Lemma 6.

**Lemma 7:** For a time slot with  $\sum_{u \in S_t} \omega_t(u) = \alpha$ , it holds that  $Pr[\sum_{u \in S_t} \omega_{t+1}(u) \leq \alpha \cdot \frac{3}{4}] \geq \frac{7}{8}$  for large enough  $\alpha$ .

*Proof:* The probability that there are more than one agents transmit in time slot  $t$  is at least  $1 - \exp\{-\alpha\}$  according to Equation (1). All the agents will halve their transmission probabilities if the channel is not idle in slot  $t$ . Denote  $X$  as the random variable that indicates the value of  $\sum_{u \in S_{t+1}} \omega_{t+1}(u)$ . We get,

$$Pr[X = \sum_{u \in S_t} \frac{\omega_t(u)}{2}] \geq 1 - \exp\{-\alpha\}$$

which is at least  $7/8$  when  $\alpha$  is large enough. Hence,

$$X \leq \frac{7}{8} \cdot \frac{1}{2} \cdot \alpha + \frac{1}{8} \cdot 2\alpha < \frac{3}{4} \cdot \alpha.$$

Therefore, it holds with high probability that for large  $\alpha$ ,  $Pr[\sum_{u \in S_t} \omega_{t+1}(u) \leq \alpha \cdot \frac{3}{4}] \geq \frac{7}{8}$ . Note that, we did not consider the effect when an agent turns to the *quiet* state, which only makes the summation decrease and hence is not harmful. ■

**Lemma 8:** There exists a constant  $\hat{\alpha}_2 > 1$ , such that among  $\gamma \log k$  slots (not necessarily consecutive) with  $\sum_{u \in S_t} \omega_t(u) \geq \hat{\alpha}_2$  and sufficiently large  $\gamma > 0$ , there are at least  $\frac{3}{4} \gamma \log k$  slots with  $\sum_{u \in S_{t+1}} \omega_{t+1}(u) < \frac{3}{4} \sum_{u \in S_t} \omega_t(u)$ , with probability  $1 - O(k^{-1})$ .

*Proof:* Let  $T := \gamma \log k$ , and  $X_t$  be the random variable that indicates the value of  $\sum_{u \in S_{t+1}} \omega_{t+1}(u) / \sum_{u \in S_t} \omega_t(u)$ . Then by Lemma 7, it holds that  $Pr[X_t \leq \frac{3}{4}] \geq \frac{7}{8}$ . Let  $Y_t$  be the binary random variable that takes value 1 if  $X_t \leq \frac{3}{4}$ . Note that given  $\sum_{u \in S_t} \omega_t(u) \geq \hat{\alpha}_2$ ,  $E[Y_t] \geq \frac{7}{8}$  always hold. Hence,  $E[\sum_{t=1}^T Y_t] \geq T \cdot \frac{7}{8}$ , and it holds that  $Pr[\sum_{t=1}^T Y_t \leq T \cdot \frac{3}{4}]$  by the Chernoff bound. That is with probability  $1 - O(k^{-1})$ , there are at least  $T \cdot \frac{3}{4}$  slots  $t$  with  $\sum_{u \in S_{t+1}} \omega_{t+1}(u) / \sum_{u \in S_t} \omega_t(u) \leq 3/4$ , which completes the proof. ■

**Lemma 9:** There exists a constant  $\hat{\alpha}_2 > 1$ , such that during any period of  $\gamma \log k$  slots with sufficiently large  $\gamma > 0$ , the probability that within the considered period there is a slot  $t$  with  $\sum_{u \in S_t} \omega_t(u) \leq \hat{\alpha}_2$  is  $1 - O(k^{-1})$ .

*Proof:* Denote  $T := \gamma \log k$  and the period of  $T$  starts from slot  $t_0$ . By Lemma 8, with probability at least  $1 - O(n^{-1})$ , it holds that

$$\begin{aligned} \sum_{u \in S_{t_0+T}} \omega_{t_0+T}(u) &\geq \sum_{u \in S_{t_0}} \omega_{t_0}(u) \cdot \left(\frac{3}{4} \cdot \frac{3}{4} \cdot \frac{3}{4} \cdot 2\right)^{\frac{T}{4}} \\ &= \sum_{u \in S_{t_0}} \omega_{t_0}(u) \cdot \left(\frac{27}{32}\right)^{\frac{T}{4}}. \end{aligned}$$

Since  $\sum_{u \in S_{t_0+T}} \omega_{t_0+T}(u) < k$  and  $T = \gamma \log k$ , we know that  $\sum_{u \in S_{t_0+T}} \omega_{t_0+T}(u)$  is at most  $\hat{\alpha}_2$  for large enough  $\gamma$ . ■

**Lemma 10:** There exists a constant  $\hat{\alpha} \geq 0.01$  such that for any time  $t$  with  $\sum_{u \in S_t} \omega_t(u) = \hat{\alpha}$ , it holds that

$$\Pr\left[\sum_{u \in S_{t+1}} \omega_{t+1}(u) \geq \hat{\alpha} \cdot \frac{4}{3}\right] \geq \frac{7}{8}. \quad (2)$$

*Proof:* Denote  $X$  as the random variable that indicates the value of  $\sum_{u \in S_{t+1}} \omega_{t+1}(u)$ . The probability that there are no transmissions in time slot  $t$  is at least  $4^{-\hat{\alpha}}$ . Hence,

$$\Pr[X = \sum_{u \in S_t} 2 \cdot \omega_t(u)] \geq 1 - 4^{-\hat{\alpha}}$$

which is at least  $7/8$  when  $\hat{\alpha}$  is close to  $0.01$ . Hence,

$$X \geq \frac{7}{8} \cdot 2 \cdot \hat{\alpha} + \frac{1}{8} \cdot \frac{1}{2} \hat{\alpha} > \frac{4}{3} \cdot \hat{\alpha}.$$

Therefore, it holds with high probability that for small  $\hat{\alpha}$  close to  $0.01$ ,  $\Pr[\sum_{u \in S_t} \omega_{t+1}(u) \leq \hat{\alpha} \cdot \frac{4}{3}] \geq \frac{7}{8}$ . ■

**Lemma 11:** There exists a constant  $\hat{\alpha}_1 > 0$ , such that among  $\gamma \log k$  slots (not necessarily consecutive) with  $\sum_{u \in S_t} \omega_t(u) \leq \hat{\alpha}_1$  and sufficiently large  $\gamma > 0$ , there are at least  $\frac{3}{4} \gamma \log k$  slots with  $\sum_{u \in S_{t+1}} \omega_{t+1}(u) \geq \frac{4}{3} \sum_{u \in S_t} \omega_t(u)$ , with probability  $1 - O(k^{-1})$ .

*Proof:* Denote  $T := \gamma \log k$ ,  $X_t$  as the random variable that indicates the value of  $\sum_{u \in S_{t+1}} \omega_{t+1}(u) / \sum_{u \in S_t} \omega_t(u)$ , and  $Y_t$  to be the binary random variable that takes value 1 if  $X_t \leq \frac{4}{3}$ . Note that given  $\sum_{u \in S_t} \omega_t(u) \geq \hat{\alpha}_1$ ,  $E[Y_t] \geq \frac{7}{8}$  always hold. Hence,  $E[\sum_{t=1}^T Y_t] \geq T \cdot \frac{7}{8}$ , and it holds that  $\Pr[\sum_{t=1}^T Y_t \leq T \cdot \frac{3}{4}]$  by the Chernoff bound. That is with probability  $1 - O(k^{-1})$ , there are at least  $T \cdot \frac{4}{3}$  slots  $t$  with

**Lemma 12:** Let  $t_0$  be the first time slot in which  $\sum_{u \in S_t} \omega_t(u)$  drops below  $\hat{\alpha}_2$ . in the subsequent  $T := \tau \cdot \log k$  slots where  $\tau > 0$  and  $k$  is large enough, the following hold:

- (1) there are at least  $\frac{3}{4} \cdot T$  slots  $t$  with  $\sum_{u \in S_t} \omega_t(u) \leq \alpha_2$ , where  $\alpha_2 > \hat{\alpha}_2$  is a constant.
- (2) there are at least  $\frac{3}{4} \cdot T$  slots  $t$  with  $\sum_{u \in S_t} \omega_t(u) \geq \alpha_1 \cdot k$ , where  $\alpha_1 < \hat{\alpha}_1$  is a constant.

*Proof:* First we prove the conclusion (1). ■

With Lemma 6, 7, 8, 9, 10, 11 and 12, we now prove Lemma 3.

*Proof:* By Lemma 6, ■

Then we show that when the number of agents not switching to the *quiet* state is less than  $\log k$ , the process

accelerates to only one agent not in *quiet* state with high probability. This is formulated as the following lemma.

**Lemma 13:** At time  $T_3 := T_2 + \gamma_2 \cdot \log k = O(k)$  it holds with high probability that  $|S_{T_3}| = 1$ .

*Proof:* After  $T_2$  slots, it holds with high probability that  $|S_{T_2}| \leq \log k$ . Then it takes at most  $\gamma_2 \cdot \log k$  slots to keep  $\beta_1 \leq \sum_{u \in S_t} \omega_t^u \leq \beta_2$ , where  $\beta_1$  and  $\beta_2$  are two constants. Afterwards, there is a time slot  $T_3 := T_2 + \gamma_2 \cdot \log k$  such that  $|S_{T_3}| = 1$ , where  $\gamma_2 > 0$  is a large enough constant. Otherwise during the period from  $T_2$  to  $T_3$ , with high probability there are more than  $\log k$  agents switching to the *quiet* state. ■

Finally we need to prove the following lemma.

**Lemma 14:** For time  $T_3$  when there is only one agent not switching to *quiet* state, at time  $T_4 := 2 \cdot T_3 + \log k = O(k)$  it holds with high probability that this agent successes to transmit.

*Proof:* Since at time  $T_3$  there is only one agent still attempting to transmit, the transmission probability will get to  $\zeta$  at time  $2 \cdot T_3$  if it keeps listening. Note that if agent  $u$  transmit with probability  $\zeta$  for  $\log k$  slots, then with high probability there exist one time slot in which agent  $u$  successes to transmit. ■

According to the Lemma 3, 13 and 14, we get the upper bound  $O(k)$  of the AWE protocol with respect to the clique size  $k$ . Note that, since the round of each agent may not be synchronized, AWE requires an overlap of at least  $T_4$  time slots in a complete round between each agent. This can be easily solved as we set  $\hat{T} := 2 \cdot T_4$  in Algorithm 3.

## C. Time bound for connecting stage

## VI. EVALUATION

## VII. CONCLUSIONS

## REFERENCES

- [1] I. I. Levin, D. M. Zonana, J. M. Burt, and R. J. Safran, "Performance of encounter tags: Field tests of miniaturized proximity loggers for use on small birds," *Plos One*, vol. 10, no. 9, p. e0137242, 2015.
- [2] W.-S. Luk and T.-T. Wong, "Two new quorum based algorithms for distributed mutual exclusion," in *Distributed Computing Systems, 1997., Proceedings of the 17th International Conference on*. IEEE, 1997.
- [3] A. Richa, C. Scheideler, S. Schmid, and J. Zhang, "A jamming-resistant mac protocol for multi-hop wireless networks," in *Twenty-Seventh ACM Symposium on Principles of Distributed Computing*, 2010, pp. 45–54.
- [4] S. Daum, M. Ghaffari, S. Gilbert, F. Kuhn, and C. Newport, "Maximal independent sets in multichannel radio networks," in *ACM Symposium on Principles of Distributed Computing*, 2013, pp. 335–344.