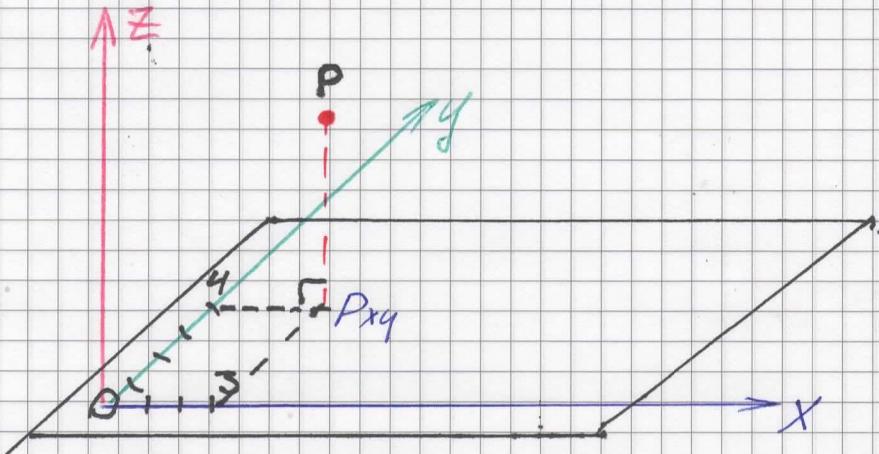


Introduction to vectors

- 1) Draw a right-handed coordinate system and locate the points:

a) $P(3, 4, 5)$

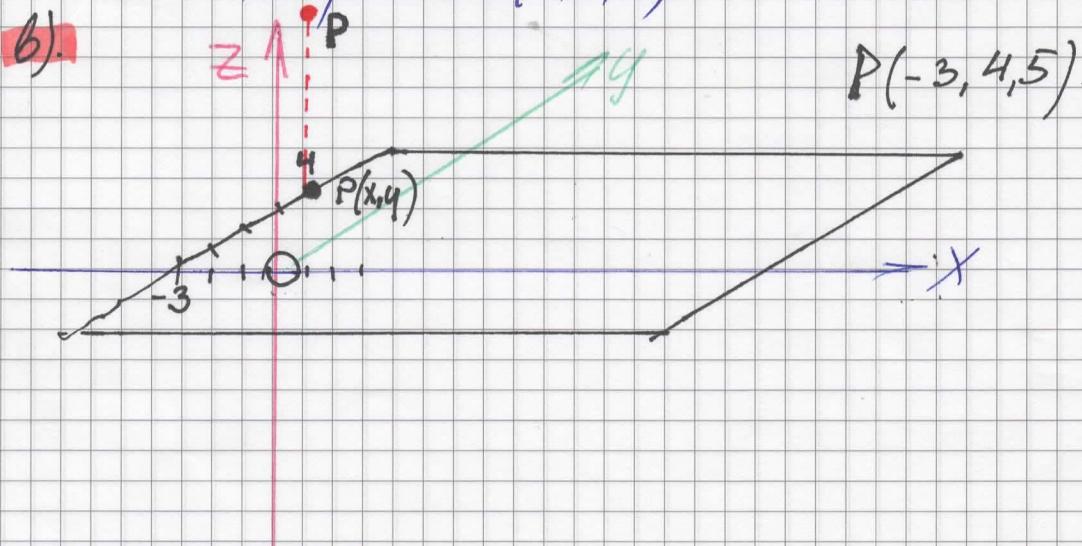
Draw a plane defined by xy -axis



Locate $P(x, y) = P(3, 4)$ which is projection of P on plane xy .

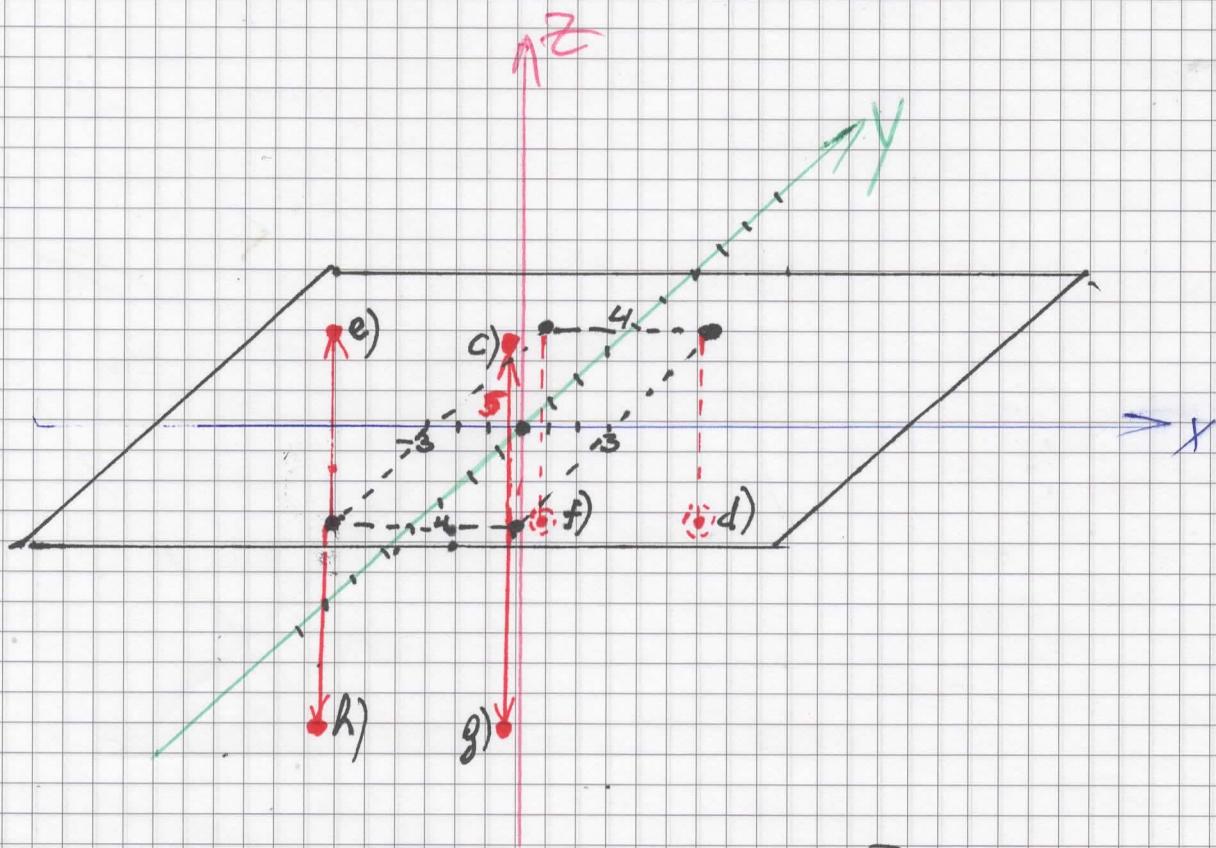
Lift $P(x, y)$ for 5 measurement units over the xy -plane under right angle (90°) to get $P(3, 4, 5)$

b).



- c) $(3, -4, 5)$ d) $(3, 4, -5)$ e) $(-3, -4, 5)$
 f) $(-3, 4, -5)$ g) $(3, -4, -5)$ h) $(-3, -4, -5)$

2.



2. Find components of vector $\vec{P_1P_2}$

a) $P_1(4, 8)$ $P_2(3, 7)$

$$\vec{P_1P_2} = (3-4, 7-8) = (-1, -1)$$

$$x = -1; y = -1$$

b) $P_1(3, -5)$ $P_2(-4, -7)$

$$\vec{P_1P_2} = (-4-3, -7-(-5)) = (-7, -2)$$

$$x = -7; y = -2$$

c) $P_1(-5, 0)$ $P_2(-3, 1)$ $\vec{P_1P_2} = (-3 - (-5), 1 - 0) = (2, 1)$

$$x = 2; y = 1$$

d) $P_1(3, -7, 2)$ $P_2(-2, 5, -4)$ $\vec{P_1P_2} = (-2-3, 5-(-7), -4-2)$
 $= (-5, 12, -6)$

$$x = -5$$

$$y = 12$$

$$z = -6$$

e) $P_1(-1, 0, 2) \quad P_2(0, -1, 0)$

$$\vec{P_1P_2} = (0 - (-1), -1 - 0, 0 - 2) = (1, -1, -2)$$

$$x = 1 \quad y = -1 \quad z = -2$$

③ Let $u = (-3, 1, 2) \quad v = (4, 0, -8) \quad w = (6, -1, -4)$
Find components

a) $v - w = (4, 0, -8) - (6, -1, -4)$

$$x = 4 - 6 = -2 \quad y = 0 - (-1) = 1 \quad z = -8 - (-4) = -4$$

b) $6u + 2v = 6 \cdot (-3, 1, 2) + 2 \cdot (4, 0, -8) = (-18, 6, 12) +$
 $+ (8, 0, -16) = (-10, 6, -4)$

$$x = -10 \quad y = 6 \quad z = -4$$

c) $-v + u = -(4, 0, -8) + (-3, 1, 2) = (-4, 0, 8) + (-3, 1, 2) =$
 $= (-7, 1, 10)$

$$x = -7 \quad y = 1 \quad z = 10$$

d) $5 \cdot (v - 4u) = 5 \cdot ((4, 0, -8) - 4 \cdot (-3, 1, 2)) = 5 \cdot (4, 0, -8) - 5 \cdot (-12, 4, 8) =$
 $= 5 \cdot (16, -4, -16) = (80, -20, -80)$

$$x = 80 \quad y = -20 \quad z = -80$$

e) $-3(v - 8w) = -3((4, 0, -8) - 8 \cdot (6, -1, -4)) =$

$$= -3 \cdot (-44, 8, 24) = (132, -24, -72)$$

$$x = 132 \quad y = -24 \quad z = -72$$

④ Find the norm of v

a) $v(4, -3) \quad |v| = \sqrt{4^2 + (-3)^2} = \sqrt{16+9} = \sqrt{25} = 5$

b) $v(2, 3) \quad |v| = \sqrt{4+9} = \sqrt{13} \approx 3,6$

c) $v(2, 2, 2) \quad |v| = \sqrt{4+4+4} = \sqrt{12} \approx 3,46$

d) $v(-7, 2, -1)$

$$|v| = \sqrt{49+4+1} = \sqrt{54} \approx 7,35$$

4

e) $v(2, 6, 1)$

$$|v| = \sqrt{4+36+1} = \sqrt{41} \approx 6,4$$

5. Find the distance between P_1 and P_2

a) $P_1(-3, 6)$ $P_2(-1, -4)$

$$\text{Distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \\ = \sqrt{2^2 + (-10)^2} = \sqrt{104} \approx 10,2$$

b) $P_1(7, -5, 1)$ $P_2(-7, -2, -1)$

$$\text{Distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2} = \\ = \sqrt{(-14)^2 + 3^2 + (-2)^2} = \\ = \sqrt{196 + 9 + 4} = \sqrt{209} \approx 14,46$$

c) $P_1(3, 3, 3)$ $P_2(6, 0, 3)$

$$\text{Dist.} = \sqrt{3^2 + (-3)^2 + 0^2} = \sqrt{18} \approx 4,24$$