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Summary Sheet

Building a virtual Hong Kong in metaverse

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1 Introduction

1.1 Background

Nowadays, *metaverse* has become a heated topic and a symbol of development in virtual technology. It refers to a three-dimensional virtual world, especially in online role-playing games such as *Second Life*, *Minecraft* and *Roblox*. In this system, people can build virtual items according to their own needs and complete basic communication with others such as buying and selling items from others as well as sharing information of their creations. In other words, this is a society which only depends on the instructions of game players. Using this technology, we can simulate the society by uploading the data given and create the items which exist in daily life to predict the future development of this system.

In the three games mentioned above, players use limited basic blocks and their own imagination to build their own virtual world. It can be seen that the type of basic blocks is very important. They must meet the needs of construction to the greatest extent, and at the same time, the number of types and size should be appropriate so that players can easily understand the function of each blocks and make full use of them.

Now Hong Kong is also confronted with the problem of how to improve its urban construction without imposing policies on the real city. On this occasion, creating a virtual Hong Kong by using metaverse is key to this challenge. We can create simple elements in this virtual world which fit the reality so that government can observe the effect of their policies by giving basic instructions in this virtual city. In this way, there will be no loss in the real world due to strategic mistakes because all of the mistakes actually happen in real life. City construction in Hong Kong can be easier and more efficient.

1.2 Problem Restatement

To build a virtual city and make sure that it can be used in daily thing, we need to figure out its basic elements and find out the computing and storage resources needed to maintain a virtual Hong Kong. So our work is divided into 2 parts:

- Build the basic blocks that satisfy the needs of citizens and can be seen in a real city. We will explain the functions of each block and how it can be planted in the virtual city.
- Calculate the fitting degree of basic blocks to make sure our virtual city can simulate Hong Kong.
- Describe the computing and storage resources required in our design by calculating the speed at which it update the state of moving objects(such as pedestrians and cars) and how much bytes of storage it needs to maintain a virtual city.

1.3 General Assumptions

- **The ground of Hong Kong can be regarded as a plain.**

Though we all know the earth is an ellipsoid, Hong Kong is so small that we can regard its ground as a plain. Also, the buildings in Hong Kong are generally not high. So we can neglect factors of ground inclination.

- **The data will be updated non automatically when serious natural disasters such as typhoons and hurricanes destroy buildings.**

We divide the shifts in location and shape of blocks into two types: small-scale shifts such as car driving and large-scale shifts such as decay of buildings. The latter happen rarely, so the data can be uploaded non automatically.

2 Model A

2.1 Model Overview

In this model, we will mainly discuss the basic block sets in this society. We divide the blocks into two parts: how to describe the location and features of the blocks and how to make sure our block fit the constructions in real Hong Kong. There are two kinds of blocks in this model: blocks which have shapes and blocks which have entity. Later we will discuss the relationship between them.

When we take everyday life into consideration, we will find that what we need to build is divided into two parts:

- **Transportation vehicles**

In Hong Kong, there are four types of transport: rail transit, air transport, transport on sea and road transport.

- **Buildings**

These buildings consists of building blocks and are seen as static objects.

- **Pedestrians**

It's common to see pedestrians walking in Hong Kong.

In this way, we can build a basic structure of our virtual city.

2.2 Notation

f(block)	properties of the block
V	volume of the block
ρ_1	continuity of lines in patterns
ρ_2	density of lines in patterns
L	dimension of lines in patterns
α_{radius}	a certain proportion which determines L
r	radius of the dots in patterns
θ_1	angle with O_x
θ_2	angle with O_y
k	a special property of each block

2.3 Creating the Blocks

In our model, we use a coordinate system to describe the absolute location of each blocks which can enable us to quickly track the route of each moving block. Also, we use a matrix to describe the key properties which will be introduced later.

We use a shape set to describe the geometric features of blocks. There are several kinds of geometry.

Type 0 is hexahedron, which is shown in the picture below. $\alpha, \beta, \gamma, a, b, c, \theta_1, \theta_2$ can be introduced to describe its shape. Also, k is introduced to describe its dimension. It means that, when $k=0$, it's a pyramid while when $k=1$, it's a parallelepiped.

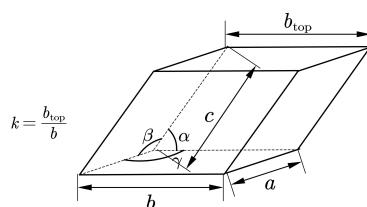


Fig.3 An example of parallelepiped

Type 1 is ellipsoid. a, b, c is introduced to determine its shape.

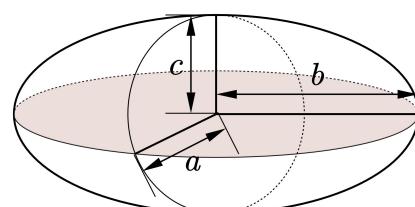


Fig.4 An example of ellipsoid

Type 2 is elliptic column platform. This time, $a, b, h, \alpha, \beta, k$ is introduced to describe its shape.

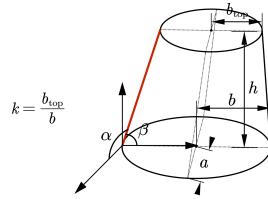


Fig. 5 An example of elliptic column platform

Secondly, we need to describe the color and patterns on the blocks. We use three primary colors(red, blue and yellow) to describe the color of blocks. For most of the patterns are made up of lines, we use ρ_1 and ρ_2 to describe the features of these patterns.

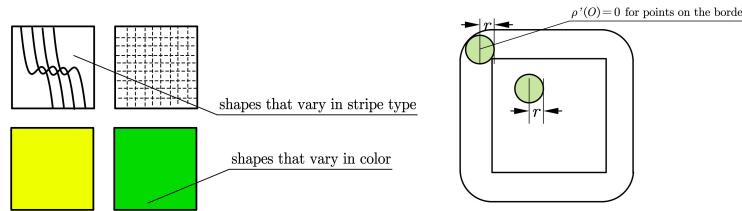


Fig.1&2 Patterns on the blocks

According to the picture, we can know the correct definition of r and L . We use α_{radius} to determine the proportion of this dimension.

$$r \stackrel{\text{def}}{=} L \times \alpha_{radius} \quad (2.1)$$

So, when we draw several circles with O as the center(O refers to every spot in the surface), we can find that:

$$\rho'(o) = \frac{\text{Line Area}}{\pi r^2} \quad (2.2)$$

They can be defined as the formulae below.

$$\rho_1 \stackrel{\text{def}}{=} \frac{\max_{\text{Surface}} \rho'(o) - \min_{\text{Surface}} \rho'(o)}{L} \quad (2.3)$$

$$\rho_2 \stackrel{\text{def}}{=} \frac{\iint_{\text{Surface}} \rho'(x, y) d\sigma}{S(\text{Surface})} \quad (2.4)$$

So, when we combine all the properties together, we can get the matrix:

$$f(\text{block}) = \begin{pmatrix} V \\ (\rho_1, \rho_2) \\ (R, G, B) \\ \text{vectors in the shape set} \end{pmatrix}$$

(In this part, vectors refer to their determining factors of the block's shape)

3 Calculating the Fitting Degree

3.1 Problem Overview

In this part, we will discuss the fitting degree of our blocks. Calculations will be focused on its shape. Blocks will be divided into different parts and using computing technology, we can compare basic properties mentioned in the last part with items in reality. In this part, Q-learning is introduced to facilitate calculations.

3.2 Notation

F_1	the fitting degree in volume
F_2	the fitting degree in lines
F_3	the fitting degree in color
F_4	the fitting degree in shape
ϕ	the fitting degree of the whole block
$Overlap_{Cluster}$	the degree in which blocks and items overlap
$Excessive_{Cluster}$	the degree in which blocks vary with items
$\Delta\rho_1$	change in continuity
$\Delta\rho_2$	change in density
Δ_e	the maximum color difference distinguishable by human eyes
Δ_{color}	color difference of blocks
I	definition of shape
Δ_{shape}	shape difference of blocks

3.3 Simulating the Shape

Firstly, we need to calculate the fitting degree of the block's shape. We separate the degree into two parts: $Overlap_{Cluster}$ and $Excessive_{Cluster}$. So we can the fitting degree shape can be described as:

$$F_1 = \frac{Overlap_{Cluster} - Excessive_{Cluster}}{V} \quad (3.1)$$

Secondly, we will discuss the fitting degree in patterns on blocks. It will be divided into lines, colors and shape. $\Delta\rho_1$ and $\Delta\rho_2$ is introduced to explain the relationship between blocks and items. So we can get the following formulae:

$$\Delta\rho_1 = |\rho_1(surface(Block)) - \rho_1(surface(Target))| \quad (3.2)$$

$$\Delta\rho_2 = |\rho_2(surface(Block)) - \rho_2(surface(Target))| \quad (3.3)$$

$$F_2 = e^{-(k_1\Delta\rho_1+k_2\Delta\rho_2)} \quad (3.4)$$

When we discuss the fitting degree in color, we identify Δ_e as the maximum color difference distinguishable by human eyes. So when we compare $(R_{Block}, G_{Block}, B_{Block})$ with $(R_{Target}, G_{Target}, B_{Target})$, it is clear that:

$$\Delta_{color} \stackrel{\text{def}}{=} \sqrt{\sum_{R,G,B} \frac{(R_{Block} - R_{Target})^2}{3}} \quad (3.5)$$

$$F_3 = e^{1-\frac{\Delta_{color}}{\Delta_e}} \quad (3.6)$$

(When $\Delta_{color} = \Delta_e$, the fitting degree is 100%.)

The last factor is shape. We assume that in calculation, the type the block belongs to must be consistent with the building's shape. It means that if the shape of block is consistent with the type in calculation, $I=1$. Otherwise $I=0$. So we can find that:

$$\Delta_{shape} = \sqrt{\frac{\sum_{x \in \text{attribute}_{\text{set}}(block)} |x_{Block} - x_{Target}|}{\text{attribute}_{\text{set}}}} \quad (3.7)$$

$$F_4 = e^{-\Delta_{shape}} \quad (3.8)$$

So when we combine all the factors together, we can get the complete fitting degree:

$$\phi = (F_1, F_2, F_3, F_4) \stackrel{\text{def}}{=} (V_v, V_{line}, V_c, V_{sh}) \quad (3.9)$$

$$\begin{aligned} & \left(\begin{array}{c} V_v \\ V_{st} \\ V_c \\ V_{sh} \end{array} \right) \times f(\text{Block}) = \left(\begin{array}{c} V_v \\ V_{st} \\ V_c \\ V_{sh} \end{array} \right) \times \\ & \left(\begin{array}{c} V \stackrel{\text{def}}{=} J_1 \\ (\rho_1, \rho_2) \stackrel{\text{def}}{=} J_2 \\ (R, G, B) \stackrel{\text{def}}{=} J_3 \\ (\alpha_1, \dots, \alpha_k) \stackrel{\text{def}}{=} J_4 \end{array} \right) \end{aligned}$$

$$\begin{aligned}
 &= \begin{pmatrix} V_v J_1 & & & \\ & V_{st} J_2 & & \\ & & V_c J_3 & \\ & & & V_{sh} J_4 \end{pmatrix} \\
 &\begin{pmatrix} V_{vV} & & & \\ & (V_{st}\rho_1, V_{st}\rho_2) & & \\ & & (V_c R, V_c G, V_c B) & \\ & & & (V_{sh}\alpha_1, \dots, V_{sh}\alpha_k) \end{pmatrix} \\
 &\stackrel{\text{def}}{=} f_{\text{same}}(\text{Block}, \text{Cluster})
 \end{aligned}$$

Finally, we can get the formula:

$$\alpha_{\text{fit}} = \frac{\sum_{\text{Block}} \frac{f_{\text{same}}(\text{Block}, \text{Cluster})}{f_{\text{same}}(\text{Block}, \text{Building})}}{\text{Properties of blocks}} (0\% \text{ } 100\%) \quad (3.10)$$

3.4 Combining the Degree of Each Block

After we come up with the 'same block' notion, we can actually calculate how much kinds of blocks it takes to construct the virtual world. Firstly, we need to try this on a smaller scale. Consider a single building. We've already got the 'same block' of each block of the building. However, the disparities of some blocks may only vary so little on the numerical scale that the difference is not detectable by the human eye. We define the difference between 'same block's as $\Delta_{\text{same}} = \dots$ (笔记第 4 页最下面红笔第一行公式), and suppose the least detectable value of this by naked eye equals $\delta_{\text{mathermeye}}$, which can be calculated with enough information or experiments.

Now all we need to do is to calculate the ideal number of blocks. Therefore, we use the K-means algorithm, where a cluster with a 'distance' of points less than δ_{eye} can be aggregated as one block. Running the following algorithm can help us get the number of blocks of a specific building. Repeat this on all buildings, and again use this algorithm, deriving the 'same same' blocks, the amount of which is what we want.

To further discuss the relationship between the fitting degree of each block, we use Q-Learning technology to help us realize the whole process. This can make calculations in the second model easier. The steps are shown below.

4 Model B

4.1 Model Overview

Now that we've figured out all the features of basic blocks and how to calculate its fitting degree, we need to calculate the running speed of our virtual society so that it can be put into real calculation. In this model, we fill focus on the byte required in different

Algorithm 1 Q-Learning algorithm

```

divide the whole area into several cubic parts
for part (i, j, k): # simulate the single part do
    initialize Q table # the potential benefits of the plan, a matrix
    initialize S # the set of actions to simulate the city with geometric forms, a list
    initialize  $\alpha$  # is the rate of learning while  $\gamma$  is the rate of declining. Both  $\alpha$  and  $\gamma$  are in the range of (0, 1).
    choose action A from S due to a policy from Q # A is a plan of fitting the blocks with geometric forms, choose the plan with the highest simulation level
    while not done: do
        take action A, observe R, S'
         $Q(S,A) \leftarrow Q(S,A) + [R + \max_a Q(S', a)Q(S,A)]$  # update the Q table and the status S
         $\leftarrow S'$ 
    end while
end for
for the borders of parts: do
    small adjustments to simulate the area better
end for

```

moving circumstances and different transportation devices. In addition, we will calculate its lagging index according to its updating speed.

4.2 Assumptions

- All the straps and lines have width.
- All the entities can be seen as a particle.

To fasten the calculating speed, we assume that all the entities' volume can be neglected. In other words, they can be seen as particles.

- There is a "middle" area between blocks and entities.

There are places that people can enter but cars cannot and certain areas that only special transportation vehicles can enter. To make it easier for calculation, a "middle" area is set between blocks and entities. **If the distance from one entity to a block is constant from any perspective, the measure of the area it has observed is constant.**

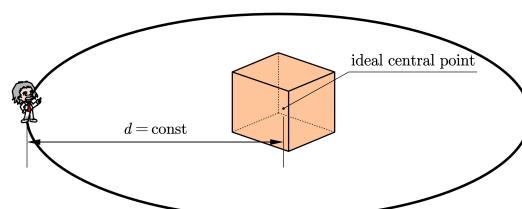


Fig. 6 Explanation of constant measure

- **Entities don't keep cars out.**

After observing the traffic condition in Hong Kong, we find out that there aren't much cars in Hong Kong. So we assume that the entities will not affect cars.

- **Only flights recorded in HKG is considered in this model.**

We find that most of the flights passing Hong Kong arrive or take off at HKG while there are no planned observed on Hong Kong's territory. Therefore, we assume that only flights recorded in HKG has an impact.

- **All the data are collected after the pandemic.**

To make sure that our calculation matches the latest information, all the data will be collected after the pandemic(2020).

- **Observation of planes can be identified as a two dimensional picture.**

Considering the assumptions above, there will be no planes flying over the HKG in this model, which means if a person wants to observe a plane, its flying route must be flush with line of sight.

- **We take the standard horizontal plane as the datum.**

4.3 Obtaining Data

As we need to build the virtual Hong Kong as real as possible, we need some data provided by the government to make the virtual Hong Kong look like Hong Kong in real life.

Firstly, we need the information of the buildings in Hong Kong, as we need to place the blocks in the virtual Hong Kong. Meanwhile, we need the data about Hong Kong's population and transportation to estimate how much calculation the virtual Hong Kong needs. This kind of data include data of Hong Kong's population, total amount of cars, total traffic volume and total area. These data can be gotten from the government. In addition, we need the data of human eye resolution to confirm an adequate resolution for the virtual Hong Kong. Fortunately, the data can be found from the Internet.

4.4 Notation

α_{lagging}	lagging index
α_c	clarity index
P_{reload}	pixels needed for reload
P_{target}	pixels targeted for use
x	a variable related to reloading speed
y	a variable related to clarity degree
V_{reload}	reloading speed
V_{eye}	eye's reacting speed
C	clarity degree of blocks
C_{eye}	clarity degree of human eye
V_E	normal moving speed of an entity
L_E	dimension of an entity
S_E	measure of an entity
d	distance to the observer
N_E	number of pixels an entity require
ρ_E	density per unit area of an entity
δ_E	proportion of entities in observable area
r_g	observation range of man's eye
r_{street}	observation range of man's eye on streets

4.5 Calculating Local Speed

We need to calculate the reloading speed(V_{reload}). The process is divided into several parts.

First, we need to calculate the lagging index. The formula is shown below.(In this formula, V_{eye} refers to human eyes' reacting speed, which is about 16 Hz.)

$$x = \frac{V_{\text{reload}}}{V_{\text{eye}}} \quad (4.1)$$

$$\alpha_{\text{lagging}} = \begin{cases} 1 & , x \in (0, \infty) \\ 2 - e^{1-x} & , x \in \left[\ln \frac{e}{2}, 1 \right] \\ 0 & , x \in \left(0, \ln \frac{e}{2} \right) \end{cases} \quad (4.2)$$

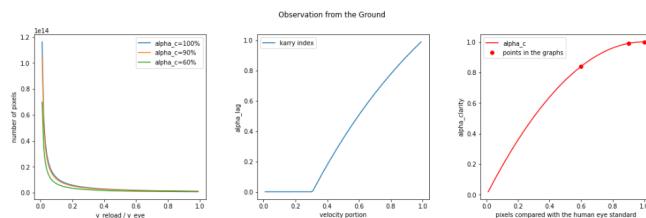


Fig. 7 Pattern of x

Secondly, we need to calculate the clarity index. In this part, we identify C as the clarity degree now and C_{eye} as the clarity degree human eyes can distinguish. According to research data, the clarity degree human eyes can distinguish is about 40960000. The index can be calculated by the formula below:

$$y = \frac{C}{C_{\text{eye}}} \quad (4.3)$$

$$\alpha_c = \begin{cases} 1 & , y \in (1, \infty) \\ -\left(\frac{4096}{4095}\right)^2 (y - 1)^2 = 1 & , y \in \left[\frac{1}{4096}, 1\right] \\ 0 & , y \in \left(0, \frac{1}{4096}\right) \end{cases} \quad (4.4)$$

(The bigger α_{clarity} is, the more comfortable people feel when looking at the virtual city.)

In addition, we need to find out the pixels required when a block move when it's uploaded. First we calculate how much pixels will be uploaded when the city is reloaded (for example, the observer walks a step).

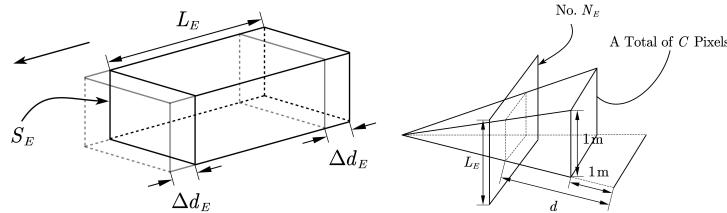


Fig. 9&10 State of observer when he moves

4.5.1 Observing From the Ground

When man observe from the ground, the range that man can observe is about 2 kilometers. So we can find that:

$$\Delta V_E = S_E \times \Delta d_E \quad (4.5)$$

$$N_E = \left(\frac{r - d}{r - 1}\right)^2 C \quad (4.6)$$

$$\frac{2\Delta d_E}{L_E} = 2\Delta d_E L_E C \left(\frac{r - d}{r - 1}\right)^2 \quad (4.7)$$

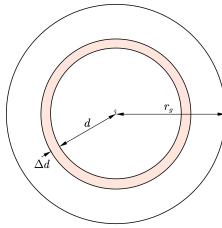


Fig. 8 An example of observing from the ground

Let us assume that there are $N_E = \pi r_g^2 \rho_E$ entities in this area. So in an area of which the radius is d ,

$$N_g = \pi d^2 \rho_E \quad (4.8)$$

$$\delta_E = \frac{N_g(d)}{N_g} = \left(\frac{r_g}{d}\right)^2 \propto d^2 \quad (4.9)$$

$$\frac{1}{r_g^2} [(d + \Delta_d)^2 - d^2] \xrightarrow{\Delta_d \rightarrow 0} \frac{2}{r_g^2} \Delta_d \quad (4.10)$$

$$\frac{2\Delta_d}{r_g} N_g \times P_{\text{Target}} = 2\Delta_d L_E C \frac{r - d}{r - 1} \quad (4.11)$$

$$(4.12)$$

So, when we sum all the pixels required together, we can get the following definition formula:

$$\begin{aligned} P_{\text{reload}} &= \lim_{\Delta d \rightarrow 0} \sum_{i=1}^{\lfloor \frac{r_g}{\Delta d} \rfloor} \left[\frac{2\Delta d}{r_g} \cdot N_g \cdot 2\Delta d L_E C \cdot \left(\frac{r_g - i\Delta d}{r_g - 1} \right)^2 \right] \\ &\stackrel{\text{def}}{=} A \cdot \lim_{\Delta d \rightarrow 0} \sum_{i=1}^{\lfloor \frac{r_g}{\Delta d} \rfloor} \Delta d \cdot \left(\frac{r_g - i\Delta d}{r_g - 1} \right)^2 \\ &= A \cdot \int_0^{r_g} \left(\frac{r_g - x}{r_g - 1} \right)^2 dx \\ &= \frac{4\pi r_g^4 \rho_E \Delta d L_E C}{3(r_g - 1)^2} \\ (A &= \frac{4N_g \Delta d L_E C}{r_g} = 4\pi r_g \rho_E \Delta d L_E C) \end{aligned}$$

4.5.2 Observing From the Air

When man observe from the sky, the average observing range r_a is about 1300 kilometer.

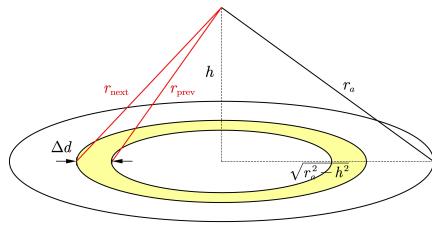


Fig. 11 An example of observing from the air

For entities in the marked part, for $\Delta_d \rightarrow 0$ ($\Delta_d \ll h$), we take r_{next} as the distance from the observer to all the entities in the ring. So we can get the formula:

Number of pixels within a Δd range

$$\begin{aligned}
 &= \frac{2\Delta d}{\sqrt{r_a^2 - h^2}} \cdot N_g \left(\sqrt{r_a^2 - h^2} \right) \cdot 2\Delta d E L E C \cdot \left(\frac{r_a - r_{\text{next}}}{r_a - 1} \right)^2 \\
 &= \frac{4\pi\sqrt{r_a^2 - h^2}\rho_E\Delta d E L E C}{(r_a - 1)^2} \cdot \Delta d (r_a - r_{\text{next}})^2, \text{ where } r_{\text{next}} = \sqrt{h^2 + (i\Delta d)^2} \\
 &\stackrel{\text{def}}{=} B \cdot \Delta d (r_a - r_{\text{next}})^2 \\
 &(B = \frac{4\pi\sqrt{r_a^2 - h^2}\rho_E\Delta d E L E C}{(r_a - 1)^2})
 \end{aligned}$$

$$r_{\text{next}} = \sqrt{h^2 + (i\Delta d)} \quad (4.13)$$

In conclusion, we can get a summarized formula:

$$\begin{aligned}
 P_{\text{reload}} &= \lim_{\Delta d \rightarrow 0} \sum_{i=1}^{\lfloor \frac{\sqrt{r_a^2 - h^2}}{\Delta d} \rfloor} B \Delta d \cdot \left(r_a - \sqrt{h^2 + (i\Delta d)^2} \right) \\
 &= \int_0^{\sqrt{r_a^2 - h^2}} B \cdot \left(r_a - \sqrt{h^2 + x^2} \right) dx \\
 &= B \left[x \left(h^2 + r_a^2 \right) + r_a \sqrt{h^2 + x^2} \cdot \left(-\frac{h \cdot \sinh^{-1}(\frac{x}{h})}{\sqrt{(\frac{x}{h})^2 + 1}} - x \right) + \frac{x^3}{3} \right] \Big|_0^{\sqrt{r_a^2 - h^2}} \\
 &= B \left[\sqrt{r_a^2 - h^2} \left(h^2 + r_a^2 \right) - r_a^2 \cdot \left(\frac{h \cdot \sinh^{-1}(\frac{\sqrt{r_a^2 - h^2}}{h})}{\frac{r_a}{h}} + \sqrt{r_a^2 - h^2} \right) + \frac{(r_a^2 - h^2)^{\frac{3}{2}}}{3} + r_a h^2 \sinh^{-1}(0) \right] \\
 &= \frac{4\pi\sqrt{r_a^2 - h^2}\rho_E\Delta d E L E C}{(r_a - 1)^2} \cdot \left(\sqrt{r_a^2 - h^2} \cdot h^2 - h^2 \cdot r_a \sinh^{-1} \left(\frac{\sqrt{r_a^2 - h^2}}{h} \right) + \frac{(r_a^2 - h^2)^{\frac{3}{2}}}{3} \right)
 \end{aligned}$$

4.5.3 Observing From Planes

The third condition is observing from planes, we abstract it as a regional calculation on the ground. The average observation range of human height is far less than r_a under

this circumstance. We find out the following formula:

$$P_{\text{Reload}} = \frac{4\pi L_{\text{airport}}^4 \Delta d_E L_E C}{3 (L_{\text{airport}} - 1)^2} \quad (4.14)$$

According to the data online, we find that L_{airport} is about 3452.5979 meter. So we find out that :

$$V_{\text{plane}} \approx 900 \text{m/s} \quad (4.15)$$

$$L_{\text{plane}} \sqrt[3]{58.82 \times 12.61 \times 17.39} \approx 23.452 \text{m} \quad (4.16)$$

$$\rho_{\text{plane}} = 0.163 \times 10^{-6} \text{m}^{-2} \quad (4.17)$$

$$(r_g \approx r_a >> L_{\text{airport}}) \quad (4.18)$$

4.5.4 Observing From Roads

Finally, we will consider the condition where observers walk on streets. To facilitate our calculation, we see the streets as straight lines which have width shown in the figure below.

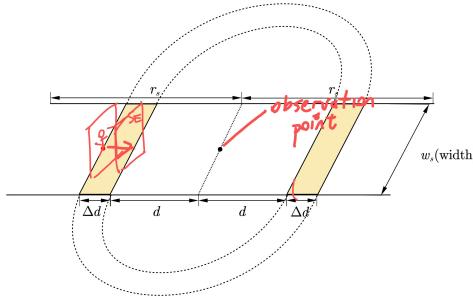


Fig.12 An example of observing from roads

From this picture, we can figure out the relationship of P_{reload} with other determining factors in the following formula:

$$\begin{aligned} P_{\text{reload}} &= \lim_{\Delta d \rightarrow 0} \sum_{i=1}^{\lfloor \frac{r_s}{\Delta d} \rfloor} \rho_E \Delta d \cdot W_s \cdot C \cdot \left(\frac{r_s - i \Delta d}{r_s - 1} \right)^2 \cdot \frac{S_E}{L_E} \cdot 2 \Delta d_E \\ &= \frac{2 \rho_E W_s C S_E \Delta d_E}{(r_s - 1)^2 L_E} \int_0^{r_s} x (r_s - x)^2 dx \\ &= \frac{r_s^4 \rho_E W_s C S_E \Delta d_E}{6(r_s - 1)^2 L_E} \end{aligned}$$

4.6 Calculating Speed(# undetermined)

When we calculate the byte required ro store this virtual city, we also need to find out how many times it calculate in one second.

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$$P_{\text{calc_cloud}} = V_{\text{reload}} \cdot u_E \cdot \left(2L_E^2 \cdot \Delta_{d_E}\right) \quad (4.19)$$

$$P_{\text{calc_local}} = V_{\text{reload}} \cdot \sum_{E \in entity} \left(\frac{r-d}{r-1}\right)^2 L_E C \quad (4.20)$$

References

- [1] EPSG:2326 Hong Kong 1980 Grid System, MapTiler Team
<https://epsg.io/2326>