Winning Characteristics in the Olympics

Noah Obuya and Tamya Davidson

```
library(tidyverse)
-- Attaching packages ------ tidyverse 1.3.2 --
v ggplot2 3.3.6 v purrr 0.3.4
v tibble 3.1.8 v dplyr 1.0.9
v tidyr 1.2.0 v stringr 1.4.1
       2.1.2 v forcats 0.5.2
v readr
-- Conflicts ----- tidyverse_conflicts() --
x dplyr::filter() masks stats::filter()
x dplyr::lag() masks stats::lag()
  library(tidymodels)
-- Attaching packages ----- tidymodels 1.0.0 --
         1.0.1 v rsample 1.1.0
1.0.0 v tune 1.0.1
v broom
v dials
v infer 1.0.3 v workflows 1.1.0 v modeldata 1.0.1 v workflowsets 1.0.0 v parsnip 1.0.2 v yardstick 1.1.0
v recipes
            1.0.2
-- Conflicts ----- tidymodels_conflicts() --
x scales::discard() masks purrr::discard()
x dplyr::filter() masks stats::filter()
x recipes::fixed() masks stringr::fixed()
x dplyr::lag()
                 masks stats::lag()
x yardstick::spec() masks readr::spec()
x recipes::step() masks stats::step()
* Dig deeper into tidy modeling with R at https://www.tmwr.org
```

```
library(MASS)
Attaching package: 'MASS'
The following object is masked from 'package:dplyr':
    select
  library(nnet)
  library(car)
Loading required package: carData
Attaching package: 'car'
The following object is masked from 'package:dplyr':
    recode
The following object is masked from 'package:purrr':
    some
  library(lme4)
Loading required package: Matrix
Attaching package: 'Matrix'
The following objects are masked from 'package:tidyr':
    expand, pack, unpack
  library(glmnet)
Loaded glmnet 4.1-6
```

library(formatR)

```
Rows: 271116 Columns: 15
-- Column specification ------
Delimiter: ","
chr (10): name, sex, team, noc, games, season, city, sport, event, medal
dbl (5): id, age, height, weight, year

i Use `spec()` to retrieve the full column specification for this data.
i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

Introduction and Data

Research Question

What are the most influential characteristics (between sex, age, height, weight, and country) when it comes to predicting gold medals in the Summer Olympics, and do these characteristics change over the course of a decade?

We chose Olympics data from TidyTuesday's github repository (https://github.com/rfordatascience/tidytuesday 07-27/readme.md). The data were collected by scraping www.sports-reference.com and was created in May 2018. The data contains 271,116 observations of 15 variables. The variables of interest in our research include sex, age, height, weight, noc (country), year, season, and medals (Gold, Silver, Bronze). Based on these variables, we will answer the question of what are the most influential variables that influence an athlete receiving a gold medal, and do these variables change over time. From the data set we will only observe the more recent Olympic games (including the years 2004, 2008, 2012, 2016), and we will analyze our research question through subsets of the data. There are many NA values corresponding to medals, and because this is our variable of interest we will drop all NA values corresponding to medals. After doing this we are left with a case study of 39,783 observations of 15 variables. The motivation behind this project is to analyze what athletes can do to better prepare for the Olympic games, and see which factors are more influential than others.

Variables of Interest

Exploratory Data Analysis

In 2004, the number of bronze medals handed out to individuals was 676 which was 33.8% of the total medals, the number of silver medals was 660 which was 33% of the total medals , and the number of gold medals was 664 which was 33.2% of the total medals .

In 2008, the number of bronze medals handed out to individuals was 706 which was 34.7% of the total medals, the number of silver medals was 665 which was 32.7% of the total medals, and the number of gold medals was 664 which was 32.6% of the total medals.

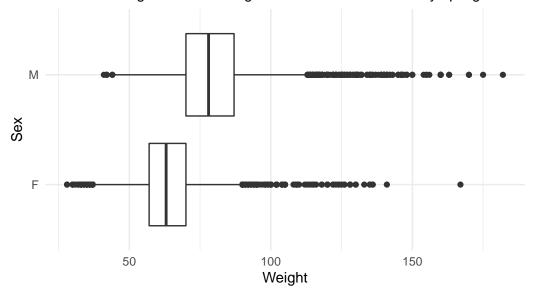
In 2012, the number of bronze medals handed out to individuals was 669 which was 35% of the total medals, the number of silver medals was 624 which was 32.6% of the total medals, and the number of gold medals was 622 which was 32.4% of the total medals.

In 2016, the number of bronze medals handed out to individuals was 700 which was 34.8% of the total medals, the number of silver medals was 652 which was 32.3% of the total medals, and the number of gold medals was 662 which was 32.8% of the total medals.

```
ggplot(olympics , mapping = aes(x = weight , y = sex )) +
  geom_boxplot() +
  theme_minimal() +
  labs(x = "Weight", y = "Sex", title = "Distribution of weights of athletes by sex", subt
```

Distribution of weights of athletes by sex

Men have a higher median weight than women across all olympic games



As we can see from the boxplots above, the distribution of weight for men and women athletes competing in the olympics are both skewed to the right, while it appears that the men are skewed heavier. We were interested in the one female athlete who is considered an outlier because her weight is above 150. We have found the athlete to be Olha Vasylivna Korobka who actually got a silver medal in the 2008 summer games in weight lifting. (Code shown below).

```
olympics %>%
    filter(sex == "F") %>%
    filter(weight > 150)
# A tibble: 1 x 15
     id name
                  sex
                          age height weight team noc
                                                        games year season city
 <dbl> <chr>
                  <chr> <dbl> <dbl> <dbl> <chr> <chr> <chr> <chr> <dbl> <chr>
1 62843 Olha Vas~ F
                           22
                                 181
                                        167 Ukra~ UKR
                                                        2008~
                                                               2008 Summer Beij~
# ... with 3 more variables: sport <chr>, event <chr>, medal <chr>
```

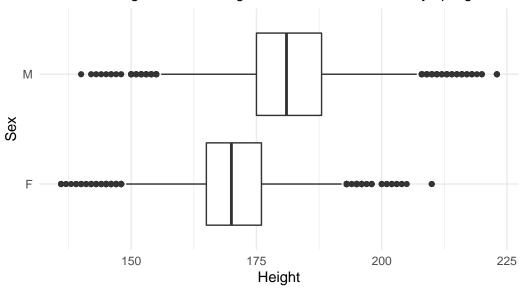
Height vs Sex BoxPlots

```
ggplot(olympics , mapping = aes(x =height , y = sex )) +
geom_boxplot() +
```

```
theme_minimal() +
labs(x = "Height", y = "Sex", title = "Distribution of heights of athletes by sex", subt
```

Distribution of heights of athletes by sex

Men have a higher median height than women across all olympic games



Similar to the results that we saw in the boxplots comparing distributions of weights between men and women, we can see that men also have a higher median height than women who have completed in the Olympics.

We chose to use all years when analyzing the distribution of heights and weights because over the course of our time frame (2004 - 2016) there have been many rule changes about allowed and not allowed substances, and analyzing these two variables through all of the years can give us a better idea of distributions.

Now that we have analyzed the data and got some idea of the distribution of specific parameters of interest, we are interested in analyzing which variables are the biggest factor in predicting gold medals for Summer Olympic games, and whether or not these variables (and their influence) change over time.

Logistic Regression

First we will fit a logistic regression model that predicts the probability of receiving a gold medal (for the purpose of this model, we will use the goldMedal? column that gives us a 1 if someone received a gold medal for their event, and gives us a 0 if someone did not receive

a gold medal (they received either gold or silver) this is due to the characteristics of logistic regression and how it works best when predicting a binary outcome.)

# A tibble: 147 x 5					
	term	estimate	std.error	statistic	p.value
	<chr></chr>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
1	(Intercept)	-15.0	624.	-0.0241	0.981
2	sexM	0.0535	0.0319	1.67	0.0942
3	age	0.00165	0.00257	0.640	0.522
4	height	0.00201	0.00201	0.999	0.318
5	weight	0.000230	0.00148	0.156	0.876
6	nocALG	13.9	624.	0.0223	0.982
7	nocANZ	0.00897	764.	0.0000117	1.00
8	nocARG	13.9	624.	0.0222	0.982
9	nocARM	12.7	624.	0.0204	0.984
10	nocAUS	13.6	624.	0.0217	0.983
# .	with 137	more rows			

The expected log odds of someone achieving a gold medal if their sex is male is 0.0535 times higher than if someone is a female when holding all other variables constant. For every one year increase in age, the expected log odds of someone achieving a gold medal is expected to increase by .00164 when all other variables are held constant. For every one unit increase in height, we expect the logs odds of someone achieving a gold medal to increase by approximately 0.0020 when all other variables are held constant. For every one unit increase in weight, we expect the log odds of someone achieving a gold medal to increase by approximately 0.00022 when all other variables are held constant. For each respective noc, the expected log odds of someone achieving a gold medal to [increase or decrease] by X when all other variables are held constant.

Ordinal Regression

Re-fitting to get Hessian

```
# A tibble: 148 x 5
  term
           estimate std.error statistic coef.type
   <chr>>
              dbl>
                        <dbl>
                                   <dbl> <chr>
 1 sexM
          0.0227
                     0.0167
                                  1.36
                                         coefficient
2 age
          0.00128
                     0.00134
                                  0.957
                                         coefficient
3 height 0.00126
                                  1.20
                     0.00105
                                         coefficient
4 weight 0.0000409
                     0.000771
                                  0.0531 coefficient
```

```
5 nocALG 5.89
                     0.0254
                                232.
                                         coefficient
6 nocANZ 4.77
                     0.00141
                             3373.
                                         coefficient
7 nocARG 5.94
                     0.0768
                                 77.3
                                         coefficient
8 nocARM 5.41
                     0.0217
                                249.
                                         coefficient
9 nocAUS 5.80
                     0.0364
                                160.
                                         coefficient
10 nocAUT 5.85
                     0.0691
                                 84.7
                                         coefficient
# ... with 138 more rows
```

height weight nocALG sexM age 1.022939e+00 1.001284e+00 1.001258e+00 1.000041e+00 3.609319e+02 1.179668e+02 nocARMnocAUS nocAUT nocAZE nocBAH 3.808297e+02 2.242517e+02 3.312331e+02 3.486949e+02 2.188170e+02 3.807950e+02 nocBAR nocBDI nocBEL nocBER nocBLR nocB0T 9.992425e-01 8.015282e+02 3.151169e+02 9.918638e-01 2.523201e+02 3.960174e+02 nocBRA nocBRN nocBUL nocCAN nocCHI nocCHN 3.213881e+02 4.087391e+02 2.831901e+02 4.004654e+02 1.526940e+02 4.380718e+02 nocCIV nocCMR nocCOL nocCRC nocCRO nocCUB 3.952125e+02 1.901743e+03 2.488254e+02 2.770645e+02 4.555103e+02 4.534841e+02 nocCYP nocCZE nocDEN nocDJI nocDOMnocECU 3.916621e+02 3.093963e+02 4.215064e+02 9.904270e-01 6.314113e+02 7.862872e+02 nocEGY nocERI nocESP nocEST nocETH nocEUN 1.901097e+02 1.027824e+00 3.368914e+02 3.155498e+02 4.014900e+02 5.128218e+02 nocFIN nocGAB nocFRA nocFRG 1.720031e+04 2.888531e+02 3.462567e+02 3.323209e+02 3.874859e+02 3.824089e+02 nocGEO nocGER. nocGHA nocGRE nocGRN 4.701884e+02 2.482348e+02 3.875267e+02 9.115933e+01 3.616318e+02 7.812284e+02 nocHKG nocGUY nocHAT nocHUN nocGUA nocTNA 3.949911e+02 1.013035e+00 3.917255e+02 4.013889e+02 4.038941e+02 3.872837e+02 nocIND nocIOA nocIRI nocIRL nocISL nocISR 4.019611e+02 2.172336e+02 3.498324e+02 4.168905e+02 3.345285e+02 1.100025e+02 nocITA nocJAM nocJOR nocJPN nocKAZ 3.905083e+02 3.571072e+02 3.775851e+02 1.567645e+04 3.289852e+02 3.211689e+02 nocKEN nocKGZ nocKOR nocKOS nocKSA nocKUW 4.367505e+02 1.458709e+02 4.183413e+02 1.606087e+04 1.004137e+02 9.791206e-01 nocLAT nocLIB nocLIE nocLTU nocLUX nocMAR 2.696198e+02 1.985573e+02 2.809772e+02 1.229116e+02 5.974742e+02 2.712552e+02 nocMAS nocMDAnocMEX nocMGL nocMKDnocMNE 2.676303e+02 1.571235e+02 3.556825e+02 2.005172e+02 9.981059e-01 4.019868e+02 nocMRI nocNAMnocNED nocNGR 4.079326e+02 9.977590e-01 3.910636e+02 3.799121e+02 2.869115e+02 3.803270e+02 nocNZI. nocPAK nocPAN nocPAR. 4.114726e+02 4.134593e+02 4.964070e+02 2.310660e+02 3.911467e+02 4.015484e+02

```
nocPOL
      nocPHI
                               nocPOR
                                             nocPRK
                                                          nocPUR
1.609344e+02 2.836537e+02 2.858389e+02 2.949953e+02 1.881955e+02 1.004130e+02
                   nocRSA
                                             nocSCG
                                                          nocSEN
      nocROU
                                nocRUS
                                                                       nocSGP
3.150833e+02 3.340651e+02 3.873419e+02 3.006391e+02 3.848809e+02 2.575954e+02
                   nocSRB
                                nocSRI
                                             nocSUD
                                                          nocSUI
                                                                       nocSUR
      nocSLO
2.266431e+02 2.526747e+02 4.075605e+02 3.863946e+02 3.085770e+02 3.926000e+02
                  \mathtt{nocSWE}
                               nocSYR
                                             nocTAN
                                                          nocTCH
4.148622e+02 3.431885e+02 3.936583e+02 3.903963e+02 2.811018e+02 3.877919e+02
                  nocTJK
                               nocTOG
                                             nocTPE
                                                          nocTT0
3.358591e+02 2.766558e+02 1.001161e+00 2.664786e+02 2.629928e+02 2.763449e+02
      nocTUR
                   nocUAE
                                nocUGA
                                                          nocURS
                                             nocUKR
4.637544e+02 3.876200e+02 3.973555e+02 2.741526e+02 4.942570e+02 5.386796e+02
      nocUSA
                   nocUZB
                                nocVEN
                                             nocVIE
                                                          nocWIF
                                                                       nocYUG
5.686591e+02 2.926607e+02 1.769305e+02 5.413833e+02 1.003835e+00 4.604019e+02
3.891662e+02 1.342010e+03
```

Variable Selection

[1] 0.003098408

plot(m_lasso_cv)

145 144 128 121 108 82 37 12 2 Mean-Squared Error 0.665 0.650 -8 **-7** -6 -9 -5 -3 -2 $\text{Log}(\lambda)$

```
m_best <- glmnet(x, y, alpha = 1, lambda = best_lambda)
m_best$beta</pre>
```

147 x 1 sparse Matrix of class "dgCMatrix" s0

(Intercept) sexM0.0068664920 0.0001888558 age height 0.0007798195 weight ${\tt nocALG}$ nocANZ-0.4312942616 ${\tt nocARG}$ nocARM-0.2075725595 nocAUS -0.0619561290 nocAUT-0.0050631105 nocAZE-0.2740426879 ${\tt nocBAH}$ ${\tt nocBAR}$ -0.4155635845 ${\tt nocBDI}$ 0.1778569347 nocBEL-0.0607687848 nocBER-0.4196495465

nocBLR	-0.2204886764
nocBOT	•
nocBRA	-0.0726397838
nocBRN	
nocBUL	-0.1654722668
nocCAN	0.0440867793
\mathtt{nocCHI}	-0.4411521348
nocCHN	0.1040796797
nocCIV	
nocCMR	0.7580256494
nocCOL	-0.1712833020
nocCRC	
nocCRO	0.1159548552
nocCUB	0.1253675138
nocCYP	
nocCZE	-0.0739127003
nocDEN	0.0663801357
nocDJI	-0.4152565196
nocDOM	0.1663496151
nocECU	0.1765738086
nocEGY	-0.2954310637
nocERI	-0.3979599685
nocESP	-0.0413497077
nocEST	-0.0095118328
nocETH	
nocEUN	0.2000844142
nocFIJ	0.8932562676
nocFIN	-0.1483812577
nocFRA	-0.0247624195
nocFRG	-0.0493914268
nocGAB	
nocGBR	0.0135141722
nocGDR	0.1579942587
nocGEO	-0.1672990819
nocGER	0.0251224460
nocGHA	-0.5624961948
nocGRE	
nocGRN	0.1679027268
nocGUA	
nocGUY	-0.4079533024
nocHAI	
nocHKG	
nocHUN	0.0502709174

nocINA	
nocIND	0.0107005070
nocIOA	-0.1079476779
nocIRI	•
nocIRL	•
nocISL	•
nocISR	-0.4638446002
nocISV	•
nocITA	-0.0023116760
\mathtt{nocJAM}	
nocJOR	0.5120223216
nocJPN	-0.0638289249
nocKAZ	-0.0333834716
nocKEN	0.0716622241
nocKGZ	-0.2968054319
nocKOR	0.0680575919
nocKOS	0.5304491775
nocKSA	-0.5094857278
${\tt nocKUW}$	-0.5726641823
nocLAT	-0.1384473323
nocLIB	-0.0670768253
nocLIE	-0.0011425182
nocLTU	-0.5813761445
nocLUX	0.0728723378
nocMAR	-0.0945010962
${\tt nocMAS}$	-0.1205251094
${\tt nocMDA}$	-0.3820612317
nocMEX	•
${\tt nocMGL}$	-0.3156370166
${\tt nocMKD}$	-0.4141035135
nocMNE	•
nocMOZ	•
nocMRI	-0.4109598168
nocNAM	•
nocNED	0.0023071590
nocNGR	-0.1215946731
nocNIG	•
nocNOR	0.0588295991
nocNZL	0.0493248605
nocPAK	0.1693918111
nocPAN	•
nocPAR	•
nocPER	•

```
nocPHI
             -0.3730526477
{\tt nocPOL}
             -0.1626057356
nocPOR
             -0.0777091724
nocPRK
             -0.0879716815
nocPUR
             -0.2589679442
nocQAT
             -0.5130270254
nocROU
             -0.0921154883
nocRSA
             -0.0036787346
nocRUS
             0.0206940917
nocSCG
             -0.0746484288
nocSEN
nocSGP
             -0.0890302958
nocSL0
             -0.2545363154
             -0.2065315467
nocSRB
nocSRI
nocSUD
{\tt nocSUI}
             -0.0965895098
nocSUR
              0.0126252158
nocSVK
nocSWE
             -0.0295020394
nocSYR
nocTAN
nocTCH
             -0.1719166349
{\tt nocTGA}
{\tt nocTHA}
nocTJK
nocTOG
             -0.4110503792
nocTPE
             -0.1715835368
nocTT0
             -0.1281211019
nocTUN
             -0.0434936490
nocTUR
              0.1046955361
{\tt nocUAE}
nocUGA
nocUKR
             -0.1682745796
nocURS
              0.2012641195
nocURU
              0.1491175915
nocUSA
              0.3020235759
nocUZB
             -0.0621028917
             -0.3382137505
nocVEN
nocVIE
              0.0411318346
{\tt nocWIF}
             -0.7094396716
              0.1363231897
nocYUG
nocZAM
```

Subset selection object
Call: regsubsets.formula(medals ~ sex + age + height + weight + noc,
 data = olympics_ord, nbest = 1, nvmax = 5, really.big = T)
146 Variables (and intercept)

	•	1
	Forced in	Forced out
sexM	FALSE	FALSE
age	FALSE	
height	FALSE	FALSE
weight	FALSE	FALSE
${\tt nocALG}$	FALSE	FALSE
${\tt nocANZ}$	FALSE	FALSE
${\tt nocARG}$	FALSE	FALSE
${\tt nocARM}$	FALSE	FALSE
${\tt nocAUS}$	FALSE	FALSE
${\tt nocAUT}$	FALSE	FALSE
${\tt nocAZE}$	FALSE	FALSE
${\tt nocBAH}$	FALSE	FALSE
nocBAR	FALSE	FALSE
${\tt nocBDI}$	FALSE	FALSE
${\tt nocBEL}$	FALSE	FALSE
nocBER	FALSE	FALSE
${\tt nocBLR}$	FALSE	FALSE
${\tt nocBOT}$	FALSE	FALSE
${\tt nocBRA}$	FALSE	FALSE
${\tt nocBRN}$	FALSE	FALSE
${\tt nocBUL}$	FALSE	FALSE
${\tt nocCAN}$	FALSE	FALSE
${\tt nocCHI}$	FALSE	FALSE
${\tt nocCHN}$	FALSE	FALSE
${\tt nocCIV}$	FALSE	FALSE
${\tt nocCMR}$	FALSE	FALSE
${\tt nocCOL}$	FALSE	FALSE
nocCRC	FALSE	FALSE
nocCRO	FALSE	FALSE
nocCUB	FALSE	FALSE
nocCYP	FALSE	FALSE
nocCZE	FALSE	FALSE
nocDEN		
nocDJI		
nocDOM	FALSE	FALSE

nocECU	FALSE	FALSE
nocEGY	FALSE	FALSE
nocERI	FALSE	FALSE
nocESP	FALSE	FALSE
nocEST	FALSE	FALSE
nocETH	FALSE	FALSE
nocEUN	FALSE	FALSE
nocFIJ	FALSE	FALSE
nocFIN	FALSE	FALSE
nocFRA	FALSE	FALSE
nocFRG	FALSE	FALSE
nocGAB	FALSE	FALSE
nocGBR	FALSE	FALSE
nocGDR	FALSE	FALSE
nocGEO	FALSE	FALSE
nocGER	FALSE	FALSE
\mathtt{nocGHA}	FALSE	FALSE
nocGRE	FALSE	FALSE
nocGRN	FALSE	FALSE
\mathtt{nocGUA}	FALSE	FALSE
nocGUY	FALSE	FALSE
nocHAI	FALSE	FALSE
nocHKG	FALSE	FALSE
nocHUN	FALSE	FALSE
nocINA	FALSE	FALSE
nocIND	FALSE	FALSE
nocIOA	FALSE	FALSE
nocIRI	FALSE	FALSE
nocIRL	FALSE	FALSE
nocISL	FALSE	FALSE
nocISR	FALSE	FALSE
nocISV	FALSE	FALSE
nocITA	FALSE	FALSE
nocJAM	FALSE	FALSE
nocJOR	FALSE	FALSE
nocJPN	FALSE	FALSE
nocKAZ	FALSE	FALSE
nocKEN	FALSE	FALSE
nocKGZ	FALSE	FALSE
nocKOR	FALSE	FALSE
nocKOS	FALSE	FALSE
nocKSA	FALSE	FALSE
\mathtt{nocKUW}	FALSE	FALSE

FALSE	FALSE
FALSE	FALSE
	FALSE

```
nocSWE
           FALSE
                       FALSE
nocSYR
           FALSE
                       FALSE
nocTAN
           FALSE
                       FALSE
{\tt nocTCH}
           FALSE
                       FALSE
nocTGA
           FALSE
                       FALSE
nocTHA
           FALSE
                       FALSE
nocTJK
           FALSE
                       FALSE
nocTOG
           FALSE
                       FALSE
nocTPE
           FALSE
                       FALSE
nocTT0
           FALSE
                       FALSE
nocTUN
           FALSE
                       FALSE
nocTUR
           FALSE
                       FALSE
nocUAE
           FALSE
                       FALSE
nocUGA
           FALSE
                       FALSE
nocUKR
           FALSE
                       FALSE
nocURS
           FALSE
                       FALSE
nocURU
           FALSE
                       FALSE
nocUSA
           FALSE
                       FALSE
{\tt nocUZB}
           FALSE
                       FALSE
nocVEN
           FALSE
                       FALSE
nocVIE
           FALSE
                       FALSE
nocWIF
           FALSE
                       FALSE
nocYUG
           FALSE
                       FALSE
nocZAM
           FALSE
                       FALSE
nocZIM
           FALSE
                       FALSE
1 subsets of each size up to 5
Selection Algorithm: exhaustive
Subset selection object
Call: regsubsets.formula(medals ~ sex + age + height + weight + noc,
    data = olympics_ord, nbest = 1, nvmax = 5, really.big = T)
146 Variables (and intercept)
       Forced in Forced out
sexM
           FALSE
                       FALSE
           FALSE
                       FALSE
age
height
           FALSE
                       FALSE
weight
           FALSE
                       FALSE
nocALG
           FALSE
                       FALSE
nocANZ
           FALSE
                       FALSE
           FALSE
nocARG
                       FALSE
nocARM
           FALSE
                       FALSE
nocAUS
           FALSE
                       FALSE
```

nocAUT	FALSE	FALSE
nocAZE	FALSE	FALSE
nocBAH	FALSE	FALSE
nocBAR	FALSE	FALSE
nocBDI	FALSE	FALSE
nocBEL	FALSE	FALSE
nocBER	FALSE	FALSE
nocBLR	FALSE	FALSE
nocBOT	FALSE	FALSE
nocBRA	FALSE	FALSE
nocBRN	FALSE	FALSE
nocBUL	FALSE	FALSE
${\tt nocCAN}$	FALSE	FALSE
${\tt nocCHI}$	FALSE	FALSE
\mathtt{nocCHN}	FALSE	FALSE
nocCIV	FALSE	FALSE
nocCMR	FALSE	FALSE
\mathtt{nocCOL}	FALSE	FALSE
nocCRC	FALSE	FALSE
nocCRO	FALSE	FALSE
nocCUB	FALSE	FALSE
nocCYP	FALSE	FALSE
nocCZE	FALSE	FALSE
nocDEN	FALSE	FALSE
nocDJI	FALSE	FALSE
nocDOM	FALSE	FALSE
nocECU	FALSE	FALSE
nocEGY	FALSE	FALSE
nocERI	FALSE	FALSE
nocESP	FALSE	FALSE
nocEST	FALSE	FALSE
nocETH	FALSE	FALSE
nocEUN	FALSE	FALSE
nocFIJ	FALSE	FALSE
nocFIN	FALSE	FALSE
nocFRA	FALSE	FALSE
nocFRG	FALSE	FALSE
${\tt nocGAB}$	FALSE	FALSE
nocGBR	FALSE	FALSE
\mathtt{nocGDR}	FALSE	FALSE
nocGEO	FALSE	FALSE
nocGER	FALSE	FALSE
\mathtt{nocGHA}	FALSE	FALSE

nocGRE	FALSE	FALSE
nocGRN	FALSE	FALSE
nocGUA	FALSE	FALSE
nocGUY	FALSE	FALSE
nocHAI	FALSE	FALSE
\mathtt{nocHKG}	FALSE	FALSE
nocHUN	FALSE	FALSE
nocINA	FALSE	FALSE
nocIND	FALSE	FALSE
nocIOA	FALSE	FALSE
nocIRI	FALSE	FALSE
nocIRL	FALSE	FALSE
nocISL	FALSE	FALSE
nocISR	FALSE	FALSE
nocISV	FALSE	FALSE
nocITA	FALSE	FALSE
${\tt nocJAM}$	FALSE	FALSE
nocJOR	FALSE	FALSE
nocJPN	FALSE	FALSE
nocKAZ	FALSE	FALSE
nocKEN	FALSE	FALSE
nocKGZ	FALSE	FALSE
nocKOR	FALSE	FALSE
nocKOS	FALSE	FALSE
nocKSA	FALSE	FALSE
nocKUW	FALSE	FALSE
nocLAT	FALSE	FALSE
nocLIB	FALSE	FALSE
nocLIE	FALSE	FALSE
nocLTU	FALSE	FALSE
nocLUX	FALSE	FALSE
${\tt nocMAR}$	FALSE	FALSE
nocMAS	FALSE	FALSE
${\tt nocMDA}$	FALSE	FALSE
nocMEX	FALSE	FALSE
${\tt nocMGL}$	FALSE	FALSE
${\tt nocMKD}$	FALSE	FALSE
nocMNE	FALSE	FALSE
nocMOZ	FALSE	FALSE
nocMRI	FALSE	FALSE
nocNAM	FALSE	FALSE
nocNED	FALSE	FALSE
nocNGR	FALSE	FALSE

FALSE
FALSE
F

```
nocUZB
             FALSE
                         FALSE
nocVEN
             FALSE
                         FALSE
nocVIE
            FALSE
                         FALSE
nocWIF
             FALSE
                         FALSE
nocYUG
             FALSE
                         FALSE
nocZAM
             FALSE
                         FALSE
nocZIM
             FALSE
                         FALSE
1 subsets of each size up to 5
Selection Algorithm: exhaustive
          sexM age height weight nocALG nocANZ nocARG nocARM nocAUS nocAUT
   (1)""
1
2
   (1)""
3
   (1)""
   (1)
4
                     11 11
                             11 11
                                     11 11
                                                                      11 11
                                                                              11 11
   (1)""
          nocAZE nocBAH nocBAR nocBDI nocBEL nocBER nocBLR nocBOT nocBRA nocBRN
   (1)""
                   11 11
                           11 11
                                   11 11
                                           11 11
                                                    11 11
                                                            11 11
1
                     11
                                   11 11
                                           11 11
                                                    11 11
                                                            11 11
                                                                            11 11
2
   (1)""
3
   (1)""
   (1)""
                   11 11
4
                   11 11
                                           11 11
                                                    11 11
5
   (1)""
          nocBUL nocCAN nocCHI nocCHN nocCIV nocCMR nocCOL nocCRC nocCRO nocCUB
                   11 11
                                   11 11
                                           11 11
                                                   11 11
                                                            11 11
                                                                            . .
1
   (1)
         11 11
                           11 11
                                           11 11
                                                            11 11
                                                                            11 11
2
   (1)""
                   11 11
                                   11 11
                                                    11 11
                                                                    11 11
   (1)""
                   11 11
                           11 11
                                           11 11
                                                    11 11
                                                                            11 11
3
4
   (1)""
   (1)""
                                   "*"
          nocCYP
                  nocCZE
                          nocDEN nocDJI
                                           nocDOM nocECU
                                                           nocEGY
                                                                   nocERI nocESP
                                                                                    nocEST
   (1)""
                   11 11
1
                                           11 11
                                                                            11 11
                   11 11
                           11 11
                                   11 11
                                                    11 11
          11 11
2
   (1)
                   11 11
                                                    11 11
3
   (1)""
4
   (1)""
                   11 11
                                           11 11
                                                    11 11
                                                            11 11
                                                                            11 11
                                                                            11 11
5
   (1)
          nocETH nocEUN nocFIJ nocFIN nocFRA nocFRG nocGAB nocGBR nocGDR nocGEO
                   11 11
   (1)""
1
2
   (1)""
                   11 11
                                   11 11
   (1)""
3
                   11 11
                                                                            "*"
   (1)""
                   11 11
                                           11 11
                                                    11 11
                                                            11 11
4
                                   11 11
                                                                            11 * 11
   (1)""
                   11 11
                           11 11
                                   11 11
                                           11 11
                                                    11 11
                                                            11 11
                                                                            "*"
                                                                                    11 11
5
          nocGER nocGHA nocGRE nocGRN nocGUA nocGUY nocHAI nocHKG nocHUN nocINA
   (1)""
                                   11 11
                                           11 11
                                                    11 11
                                                                            11 11
1
                                                                            11 11
2
   (1)""
```

nocUSA

FALSE

FALSE

```
11 11
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                            11 11
                                                                                11 11
                                                                                         11 11
                                                                                                   11 11
3
   (1)""
4
   (1)""
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                            11 11
                                                                      11 11
                                                                                11 11
                                                                                          11 11
                                                                                                   11 11
    (1)""
                      11 11
                                         11 11
                                                   11 11
                                                             11 11
                                                                      11 11
                                                                                          11 11
5
            nocIND nocIOA nocIRI nocIRL nocISL nocISR nocISV nocITA nocJAM nocJOR
    (1)""
                                         11 11
                                                   11 11
                                                            11 11
                                                                      11 11
1
    (1)""
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                             11 11
2
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                            11 11
                                                                      11 11
                                                                                          11 11
                                                                                                   11 11
    (1)""
3
                                                             11 11
                                                                                          11 11
                                                                                                   11 11
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                                      11 11
                                                                                11 11
4
    (1)""
                                                            ......
5
    (1)""
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                                      11 11
                                                                                          11 11
                                                                                                   11 11
            nocJPN nocKAZ nocKEN nocKGZ nocKOR nocKOS nocKSA nocKUW nocLAT nocLIB
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                            11 11
                                                                      11 11
                                                                                          11 11
    (1)""
1
                      11 11
                                         11 11
                                                   11 11
                                                             11 11
                                                                      11 11
                                                                                11 11
                                                                                          11 11
2
    (1)""
    (1)""
                      11 11
3
    (1)""
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                             11 11
                                                                      11 11
                                                                                          11 11
                                                                                                   11 11
4
                                                   11 11
                                                             11 11
                                                                      11 11
                                                                                          11 11
                                                                                                   11 11
    (1)""
                      11 11
                                11 11
                                         11 11
            nocLIE nocLTU
                               nocLUX nocMAR nocMAS nocMDA nocMEX nocMGL nocMKD nocMNE
1
    (1)""
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                            11 11
                                                                      11 11
                                                                                11 11
                                                                                         11 11
                                                                                                   11 11
    (1)""
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                             11 11
                                                                      11 11
                                                                                11 11
                                                                                          11 11
                                                                                                   11 11
2
    (1)""
                                                   11 11
                                                             11 11
                                                                                          11 11
3
    (1)""
                      "*"
4
    (1)""
                      "*"
                                         11 11
                                                   11 11
5
            nocMOZ nocMRI nocNAM nocNED nocNGR nocNIG nocNOR nocNZL nocPAK nocPAN
                                                   11 11
                                                                      11 11
    (1)""
                      11 11
                                11 11
                                         11 11
                                                            11 11
                                                                                11 11
                                                                                         11 11
                                                                                                   11 11
1
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                             . .
                                                                      11 11
                                                                                . .
                                                                                          . .
                                                                                                   11 11
2
    (1)""
    (1)""
3
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                            11 11
                                                                      11 11
                                                                                11 11
                                                                                          11 11
                                                                                                   11 11
    (1)""
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                             11 11
                                                                      11 11
                                                                                11 11
                                                                                          11 11
                                                                                                   11 11
4
    (1)""
                                                   11 11
                                                                      11 11
                                                                                          11 11
5
            nocPAR nocPER nocPHI nocPOL
                                                  nocPOR nocPRK
                                                                     nocPUR
                                                                               nocQAT nocROU nocRSA
                                11 11
                                         11 11
                                                   11 11
                                                            11 11
                                                                      11 11
                                                                                          11 11
                                                                                                   11 11
                      11 11
    (1)""
1
                                                   11 11
                                                            11 11
                                                                      11 11
                                                                                          11 11
                                                                                                   11 11
2
    (1)""
                      11 11
                                11 11
                                         11 11
                                                                                11 11
                                                                                          11 11
                                                                                                   11 11
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                             11 11
                                                                      11 11
                                                                                11 11
3
    (1)""
                      11 11
                                                             11 11
                                                                                                   11 11
4
    (1)""
                                11 11
                                         11 11
                                                   11 11
                                                                      11 11
                                                                                11 11
                                                                                          11 11
    (1)""
                                                                                          11 11
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                             11 11
                                                                      11 11
                                                                                11 11
                                                                                                   11 11
5
            nocRUS nocSCG nocSEN nocSGP nocSLO nocSRB nocSRI nocSUD nocSUI nocSUR
    (1)""
                                                   11 11
                                                             11 11
                      11 11
                                         11 11
                                                                      11 11
1
                      11 11
                                         11 11
                                                   11 11
                                                             11 11
                                                                                11 11
2
    (1)""
    (1)""
                      11 11
                                         11 11
                                                   11 11
                                                            11 11
                                                                                11 11
                                                                                          11 11
3
    (1)""
                                                                                          11 11
4
                      11 11
                                         11 11
                                                   11 11
                                                             11 11
                      . .
                                                   11 11
                                                            11 11
                                                                      11 11
                                                                                          . .
                                                                                                   11 11
    (1)""
                                11 11
                                         11 11
                                                                                11 11
5
            nocSVK nocSWE nocSYR nocTAN nocTCH nocTGA nocTHA nocTJK nocTOG nocTPE
    (1)""
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                            11 11
                                                                      11 11
                                                                                11 11
                                                                                         11 11
                                                                                                   11 11
1
                      11 11
                                11 11
                                         11 11
                                                   11 11
                                                             11 11
                                                                      11 11
                                                                                11 11
                                                                                          11 11
                                                                                                   11 11
2
    (1)""
                                                                                          11 11
    (1)""
                      11 11
                                         11 11
```

```
4 (1)""
                  11 11
                          11 11
                                  11 11
                                          11 11
                                                  11 11
                                                          11 11
                                                                  11 11
                                                                          11 11
                                                                                  11 11
                                                  11 11
                                                                                  11 11
   (1)""
                  11 11
                          11 11
                                  11 11
                                          11 11
                                                          11 11
                                                                  11 11
                                                                          11 11
          nocTTO nocTUN nocTUR nocUAE nocUGA nocUKR nocURS nocURU nocUSA nocUZB
   (1)""
                                  11 11
                                          11 11
                                                  11 11
                                                          11 11
                                                                          "*"
1
                  11 11
2
   (1)""
                                                          "*"
                                                                          "*"
                  11 11
                                          11 11
                                                          11 * 11
                                                                          11 * 11
3
   (1)""
                  11 11
                          11 11
                                                                                  11 11
  (1)""
                                  11 11
                                          11 11
                                                  11 11
                                                          "*"
                                                                  11 11
                                                                          "*"
                  11 11
                          11 11
                                  11 11
                                          11 11
                                                  11 11
                                                          11 * 11
                                                                                  11 11
   (1)""
                                                                          "*"
          nocVEN nocVIE nocWIF nocYUG nocZAM nocZIM
   (1)""
                                          11 11
                                                  11 11
                  11 11
                          11 11
                                  11 11
1
  (1)""
                  11 11
                          11 11
                                  11 11
                                          11 11
                                                  11 11
2
   (1)""
                  11 11
                          11 11
                                  11 11
                                          11 11
                                                  11 11
3
  (1)""
                  11 11
                          11 11
                                  11 11
                                          11 11
4
   (1)""
                  11 11
                          11 11
                                  11 11
  m_all <- regsubsets(medals ~ sex + age + height + weight,</pre>
                       data = olympics_ord,
                       nbest = 1, nvmax = 5, really.big = T)
  m_all
Subset selection object
Call: regsubsets.formula(medals ~ sex + age + height + weight, data = olympics_ord,
    nbest = 1, nvmax = 5, really.big = T)
4 Variables (and intercept)
        Forced in Forced out
sexM
            FALSE
                         FALSE
age
            FALSE
                         FALSE
height
            FALSE
                         FALSE
            FALSE
                         FALSE
weight
1 subsets of each size up to 4
Selection Algorithm: exhaustive
   summary(m_all)
Subset selection object
Call: regsubsets.formula(medals ~ sex + age + height + weight, data = olympics_ord,
    nbest = 1, nvmax = 5, really.big = T)
4 Variables (and intercept)
        Forced in Forced out
            FALSE
                         FALSE
sexM
```

```
FALSE
                     FALSE
age
height
          FALSE
                     FALSE
          FALSE
weight
                     FALSE
1 subsets of each size up to 4
Selection Algorithm: exhaustive
         sexM age height weight
  (1)""""*"
                         11 11
2 (1)""
              "*" "*"
              "*" "*"
                        11 11
3 (1) "*"
              "*" "*"
4 (1) "*"
                        "*"
  summary(m_all)$cp
[1] 8.033983 2.634207 3.027055 5.000000
Final Model
  ordMod final <-
    polr(factor(medals) ~ sex + age + height , data = olympics_ord , method = "probit")
  tidy(ordMod_final) %>%
    mutate(estimate = round(estimate , 9))
Re-fitting to get Hessian
# A tibble: 5 x 5
 term
         estimate std.error statistic coef.type
  <chr>
                               <dbl> <chr>
            <dbl>
                     <dbl>
1 sexM
         -0.0196
                  0.0155
                              -1.27 coefficient
2 age
        -0.00336 0.00129
                              -2.60 coefficient
3 height 0.00304 0.000673
                               4.52 coefficient
```

0.163 scale

7.30 scale

4 1 2

5 2 3

0.0192

0.863

0.118

0.118