

Lecture 2

Agenda

- HW 1 released on course website, due next Friday
- Continuing intro to probability simulations
- Time permitting: start HW 1 in class
- Office hours (Manchester 329):
 - 3 - 4pm Monday
 - 1 - 2pm Thursday
- TA study session (Manchester 121): 7-8pm Thursday

Warm-up question

- A roulette wheel has 38 slots numbered 00, 0, and 1–36. Two are green, 18 are red, and 18 are black.
- If a gambler bets based on color, the return on a \$1 bet is \$2
- A gambler has \$50, and will continuously bet \$1 on red until they double their money (have \$100) or lose the money they came with
- What is the probability the gambler doubles their money?

Question: Without calculating probabilities, how could you design an experiment to estimate this probability?

Designing an experiment

Step 1: need a roulette wheel! (and money)
(38 slots, 2 g, 18 red, 18 black)

vector: $\underbrace{g, g}_2, \underbrace{r, r, \dots, r}_{18}, \underbrace{b, b, \dots, b}_{18}$

Step 2: spin the wheel!

Sample from our vector (roulette wheel)

Step 3: check result, and update our money

code? $\rightarrow \begin{cases} \text{if spin is red : money} = \text{money} + 1 \\ \text{if spin is not red : money} = \text{money} - 1 \end{cases}$

Step 4: keep spinning (loop!) until money = 100 or money = 0

Step 5: Repeat whole process many times!
(estimate a probability)
(for loop)

Step 1: representing the roulette wheel

```
1 wheel <- c(rep("green", 2), rep("black", 18), rep("red", 18))  
2 vector 2 g 18 b 18 r  
3 wheel
```

```
[1] "green" "green" "black" "black" "black" "black" "black" "black"  
"black"  
[10] "black" "black" "black" "black" "black" "black" "black" "black"  
"black"  
[19] "black" "black" "red" "red" "red" "red" "red" "red"  
"red"  
[28] "red" "red" "red" "red" "red" "red" "red" "red"  
"red"  
[37] "red" "red"
```

- rep repeats a value a specified number of times
- c() combines vectors into a single vector

Step 2: spin the wheel!

```
1 spin <- sample(wheel, size = 1)  
2  
3 spin
```

```
[1] "red"
```

if spin is red:

money = money + 1

if spin is not red:

money = money - 1

Step 3: change in money

```
1 money <- 50
2 spin <- sample(wheel, size = 1)
3
4 if(spin == "red"){
5   money <- money + 1
6 } else {
7   money <- money - 1
8 }
9
10 spin
```

```
[1] "black"
```

```
1 money
```

```
[1] 49
```

- if the result was red, gain a dollar
- otherwise, lose a dollar

Step 3: change in money

Another way of writing the conditional statement:

```
1 money <- 50
2 spin <- sample(wheel, size = 1)
3
4 money <- ifelse(spin == "red", money + 1, money - 1)
5
6 spin
```

[1] "black"

```
1 money
```

[1] 49

Handwritten annotations:

- Under `spin == "red"`: *condition to check*
- Under `money + 1`: *if condition is true*
- Under `money - 1`: *otherwise do this*
- An arrow points from the `spin` variable in line 6 to the `money` variable in the output box below, with the text *update money*.

Step 4: keep spinning

The gambler continues to bet until they have \$0 or \$100.

Question: Is a `for` loop appropriate for iterating the betting process?

`for` loop: repeats a chunk of code a fixed # of times

`while` loop: repeats code `while` a condition is true

Step 4: keep spinning

```
1 money <- 50 # starting money
2
3 while(money > 0 & money < 100){
4   spin <- sample(wheel, size = 1)
5   money <- ifelse(spin == "red", money + 1, money - 1)
6 }
7
8 money
```

repeat until either money == 0
or money == 100

[1] 0

false

- while loop: repeat the process until the condition is ~~true~~

(while condition is true)

code to
repeat
while
loop
runs

Step 5: repeat the process

```
1 set.seed(279)
2
3 nsim <- 1000      ← # simulations
4 results <- rep(NA, nsim) ← vector to store results
5
6 for(i in 1:nsim){ ← play the game nsim times
7   money <- 50 # starting money
8
9   while(money > 0 & money < 100){
10     spin <- sample(wheel, size = 1)
11     money <- ifelse(spin == "red", money + 1, money - 1)
12   }
13
14   results[i] <- ...money == 100
15 }
```

- What should I check at each iteration?

results[i] : ith entry in results vector

$\frac{\text{sum}(\text{results})}{\text{nsim}}$

or mean(results)

Step 5: repeat the process

```
1  set.seed(279)
2
3  nsim <- 1000
4  results <- rep(NA, nsim)
5
6  for(i in 1:nsim){
7    money <- 50 # starting money
8
9    while(money > 0 & money < 100){
10     spin <- sample(wheel, size = 1)
11     money <- ifelse(spin == "red", money + 1, money - 1)
12   }
13
14   results[i] <- money == 100
15 }
16
17 mean(results)
```

```
[1] 0.008
```

