

# STA286 Lecture 01

Neil Montgomery

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admin

## contact, notes

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date format	YYYY-MM-DD – <i>All Hail ISO8601!!!</i>
instructor	Neil Montgomery
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office	BA8137
office hours	W11-1
website	portal (announcements, grades, suggested exercises, etc.)
github	<a href="https://github.com/sta286-winter-2017">https://github.com/sta286-winter-2017</a> (lecture material, code, etc.)

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Lecture notes and other course timing matters will be organized by *lecture number* and not *lecture date*, due to two lecture sections.

## evaluation, book, tutorials

what	when	how much
midterm 1	TBA	25%
midterm 2	TBA	25%
exam	TBA	50%

The book is Walpole, R.E., Myers, R.H., Myers, S.L., Ye, K., 2012. *Probability & statistics for engineers & scientists*. 9th edition.

I will suggest exercises from this book each week. Your TA will work through some of them in tutorial each week.

**Tutorials start TBA.**

## software

The course begins and ends with data analysis, with a long stretch of probability theory in the middle.

Data analysis requires a computer. Also, some concepts can be illustrated using simulation, which also requires a computer.

We will be using R. It's pretty good at data analysis.

language	interpreter	integrated development environment
R	R	RStudio

Some detailed instructions and suggestions for installation and configuration appear on the course website.

I will try to impart some data analysis workflow wisdom throughout the course. Some already appears in the detailed instructions.

MATLAB SUCKS!

what is a dataset?

## most datasets are rectangles

Columns are the *variables*.

The top row has the names of the variables; possibly chosen wisely.

Rows are the *observations* of measurements taken on *units*.

There are no averages, no comments (unless in a “comment” variable), no colors, no formatting, no plots, no capes!



not a dataset

Irrelevant commentary				
HUGE TITLE ACROSS THREE MERGED LINES				
Some God-forsaken Date Format	Column Title Which Is Very Long And Has Spaces And @\$#^ Special Characters!			
	time2		status	
	November 12 2003	2.575817169	27.43610042	censored
	November 12 2003	7.405809497	29.34394097	censored
	November 12 2003	0.372988356	27.33832542	censored
	November 12 2003	3.195281626	12.87646771	pr_fail
	November 12 2003	6.555084512	13.83875584	censored
	<b>November 12 Average</b>	<b>4.020996232</b>	<b>22.16671807</b>	
	November 13 2003	0	11.64588809	censored
	November 13 2003	5.371449791	15.38626237	tx_fail
November 13 2003	3.928454966	11.40722991	censored	
November 13 2003	4.90945976	20.55325312	censored	
November 13 2003	0	19.44576571	censored	
<b>November 13 Average</b>	<b>2.841872903</b>	<b>15.68767984</b>		

Neil:  
Hey Bob, check out this  
cell! It's yellow!

not a dataset

ASSETNUM	MOVEDATE_1	FROM_LOCATION1	TO_LOCATION1	MOVEDATE_2	FROM_LOCATION2	TO_LOCATION2	MOVEDATE_3	FRC
0201011	2005-12-16	NO_LOCATION	RSREPAIR					
0209679	2006-01-16	NO_LOCATION	RSREPAIR	2006-01-30	RSREPAIR	DN4VNCR	2014-02-14	DN:
0209680	2005-05-17	NO_LOCATION	RSREPAIR	2005-08-03	RSREPAIR	WY172UCR	2013-11-08	WY
0209709	2005-05-20	NO_LOCATION	WY92WEPR	2011-10-07	WY92WEPR	RSREPAIR	2013-11-08	RSR
0209711	2011-10-07	WY91WEPR	RSREPAIR	2013-11-08	RSREPAIR	WY174VNCR		
0209714	2003-12-15	NO_LOCATION	RSREPAIR					
0209720	2011-10-07	WY95WEPR	RSREPAIR	2013-06-25	RSREPAIR	WY70ASPR		
0209722	2011-10-07	WY106WEPR	RSREPAIR	2013-06-27	RSREPAIR	WY144BSUSR		
0209728	2011-10-07	WY94WEPR	RSREPAIR	2013-11-08	RSREPAIR	WY143NWCPR		
0209729	2006-01-16	NO_LOCATION	RSREPAIR	2006-01-30	RSREPAIR	DN12ASRA	2014-04-04	DN:
0209737	2005-01-11	NO_LOCATION	DN15NWCRB	2006-03-21	DN15NWCRB	RSREPAIR	2006-03-31	RSR
0209739	2011-10-07	WY144WEPR	RSREPAIR	2013-12-09	RSREPAIR	WY178TPR		
0209740	2011-10-07	WY143WEPR	RSREPAIR	2012-09-12	RSREPAIR	DNSPARE	2014-05-30	DN:
0209741	2006-01-16	NO_LOCATION	RSREPAIR	2006-01-30	RSREPAIR	DN10BHR	2014-09-05	DN:

## an oil readings dataset (wide version)

```
## # A tibble: 612 × 17
```

```
##       Ident      Date WorkingAge   TakenBy    Fe    Al    Cu
##       <chr>      <dtm>      <dbl>     <chr> <dbl> <dbl> <dbl>
## 1  448576 1999-05-10 19:00:00      243 EMPL_0917    13     5    14
## 2  448576 1999-07-26 19:00:00      569 EMPL_0917    18     6    25
## 3  448576 1999-09-29 19:00:00      830 EMPL_9375    26     6    35
## 4  448576 1999-10-08 19:00:00      862 EMPL_0917    15     9    14
## 5  448576 1999-11-02 19:00:00      946 EMPL_9375    14     4    19
## 6  448576 1999-12-09 19:00:00     1088 EMPL_0917    18     5    23
## 7  448576 1999-12-27 19:00:00     1157 EMPL_9375    24     8    25
## 8  448576 2000-01-14 19:00:00     1238 EMPL_9375    27     9    34
## 9  448576 2000-02-15 19:00:00     1376 EMPL_9375    16     8    17
## 10 448576 2000-03-11 19:00:00     1492 EMPL_0917    20     8    20
## # ... with 602 more rows, and 10 more variables: Cr <dbl>, Si <dbl>,
## #   Pb <dbl>, Ph <dbl>, Ca <dbl>, Zn <dbl>, Mg <dbl>, Mo <dbl>,
## #   Sn <dbl>, Na <dbl>
```

## oil readings with Ident and TakenBy properly treated

```
## # A tibble: 612 × 17
```

```
##       Ident      Date WorkingAge   TakenBy    Fe    Al    Cu
##       <fctr>      <dtm>      <dbl>    <fctr> <dbl> <dbl> <dbl>
## 1  448576 1999-05-10 19:00:00      243 EMPL_0917    13     5    14
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```

## oil readings dataset (long version)

```
## # A tibble: 7,956 × 6
```

##	Ident	Date	WorkingAge	TakenBy	element	ppm
##	<fctr>	<dtm>	<dbl>	<fctr>	<chr>	<dbl>
## 1	448576	1999-05-10 19:00:00	243	EMPL_0917	Fe	13
## 2	448576	1999-07-26 19:00:00	569	EMPL_0917	Fe	18
## 3	448576	1999-09-29 19:00:00	830	EMPL_9375	Fe	26
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## #	... with 7,946 more rows					

## the main questions

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  - ▶ were the units chosen randomly from a population?
  - ▶ were the units randomly assigned into groups?
- ▶ what are the (joint) *distributions* of the data?

random sample, experiment, observational data

Sometimes the data come from a *random sample* from a larger *population*, in which case statements about the sample can apply to the population using laws of probability.

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Sometimes data come from an *experiment* where units are randomly assigned to different *levels* of one or more *factors*, in which cause cause-and-effect can be inferred using laws of probability.

Often the data are just some records of what happened. Grander inferences might be made, but only on a subject-matter basis.

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through a process called *exploratory data analysis*

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    - ▶ Categories can have an inherent order
    - ▶ “Likert scale” (strongly disagree coded as 1 and so on. . . )
- ▶ Numerical variables could be discrete (counting something) or continuously measured.

numerical summaries of dataset variables — definitions first  
with examples after

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The dataset is often called the “sample” (no matter where the data came from).

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For a particular numerical variable in the sample with observations:

$$\{x_1, x_2, \dots, x_n\}$$

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$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$



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Could be sensitive to extreme observations.

## sample medians, sample percentiles

Order the observations:

$$x_{(1)} \leq x_{(2)} \leq \cdots \leq x_{(n)}$$

A number that divides the observations into two groups is called a *sample median*. For example:

$$\tilde{x} = \begin{cases} x_{((n+1)/2)} & : n \text{ odd} \\ \left( x_{(n/2)} + x_{(n/2+1)} \right) / 2 & : n \text{ even} \end{cases},$$

which is harder to write out than it is to understand.

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which is harder to write out than it is to understand.

A *sample  $p^{th}$  percentile* has  $p\%$  of the data below or equal to it. Special cases include (sample. . .): quartiles, quintiles, deciles, and indeed the median itself.

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Very (too?) simple measure: *sample range* which is just  $x_{(n)} - x_{(1)}$ .

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Adding them up just gives 0, so instead consider positive functions such as:

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Summing up over all the observations gives the *sum of absolute deviations* (aka SAD) and the *sample variance* respectively. Notation and formula:

$$s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$$

## sample standard deviation

$s^2$  is essentially the average squared deviation. (More on  $n - 1$  later in the course.)

The sample variance is good for theory but has an inconvenient unit. More practical is the *sample standard deviation*:

$$s = \sqrt{s^2}$$

## numerical summaries for categorical variables

The oil readings data has one categorical variable, the Ident variable which is just a serial number.

```
## # A tibble: 5 × 17
```

```
##   Ident      Date WorkingAge TakenBy   Fe   Al   Cu
##   <fctr>    <dtm>      <dbl>   <fctr> <dbl> <dbl> <dbl>
## 1 448576 1999-05-10 19:00:00    243 EMPL_0917    13     5    14
## 2 448576 1999-07-26 19:00:00    569 EMPL_0917    18     6    25
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## # ... with 10 more variables: Cr <dbl>, Si <dbl>, Pb <dbl>, Ph <dbl>,
## #   Ca <dbl>, Zn <dbl>, Mg <dbl>, Mo <dbl>, Sn <dbl>, Na <dbl>
```



## tables of counts (or proportions)

A categorical variable could also be called a *factor* variable with *levels*, and to tabulate the frequency of each level is the way to summarize.

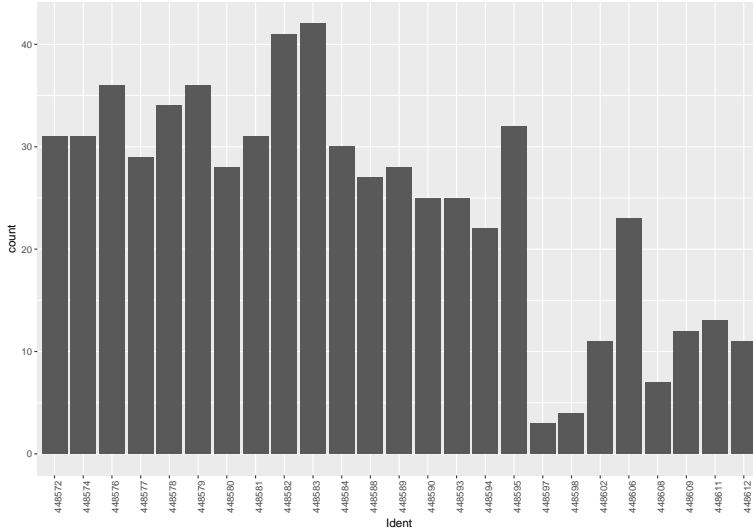
```
## # A tibble: 25 × 3
##   Ident      n proportion
##   <fctr> <int>      <dbl>
## 1  448572    31 0.05065359
## 2  448574    31 0.05065359
## 3  448576    36 0.05882353
## 4  448577    29 0.04738562
## 5  448578    34 0.05555556
## 6  448579    36 0.05882353
## 7  448580    28 0.04575163
## 8  448581    31 0.05065359
## 9  448582    41 0.06699346
## 10 448583    42 0.06862745
## # ... with 15 more rows
```



graphical summaries

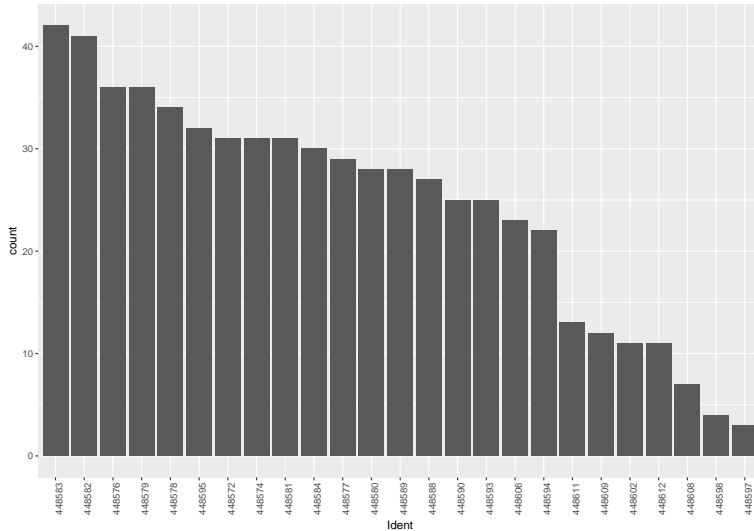
## barchart

A barchart is a table of counts, in graphical form.

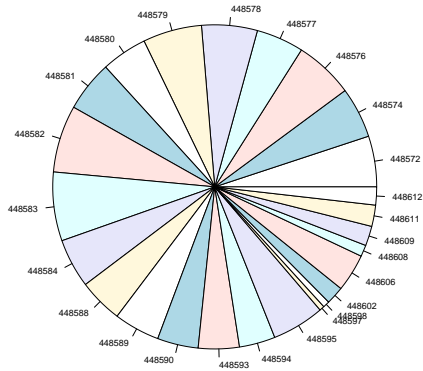


# “Pareto” chart

Ordered by count.



piecharts are problematic

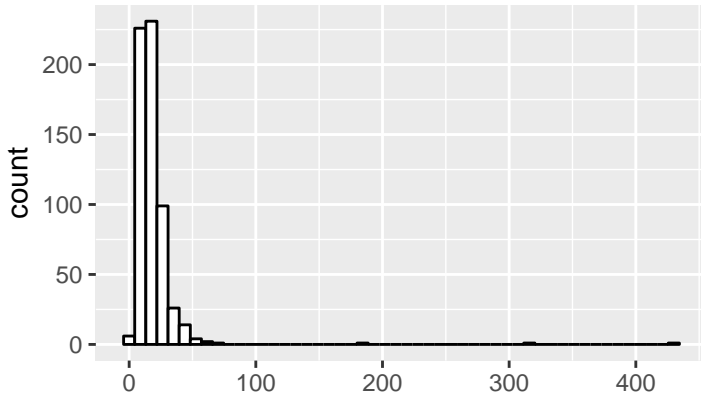


## histograms

A histogram is a special case of a barchart.

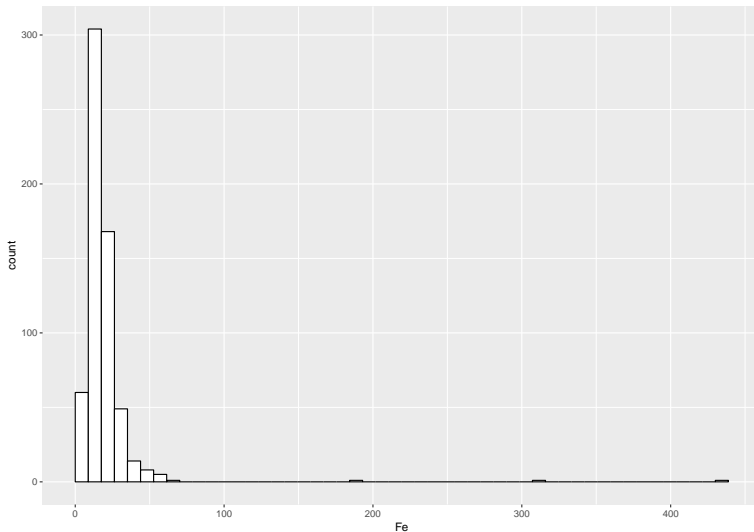
A numerical variable is split into classes and a barchart is made from the table of counts of obvservations within each class.

Histograms are done by the computer. Always play around with the number of classes.



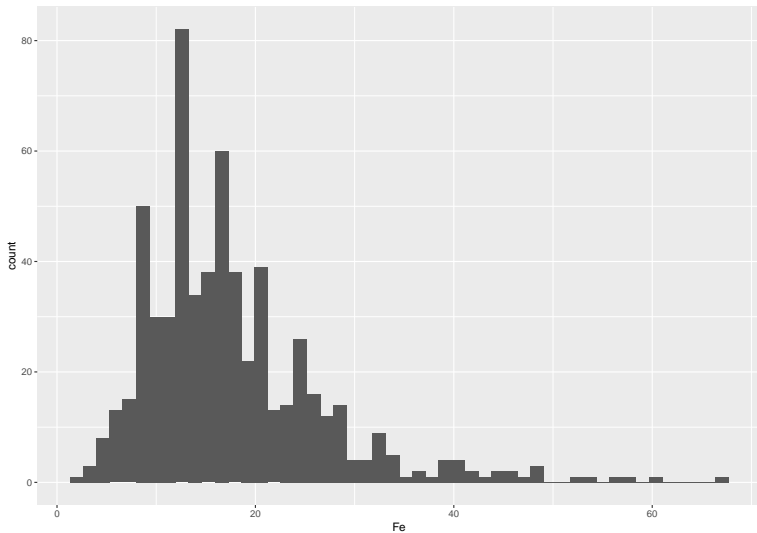
## histograms are hard to implement!

Better picture around 0. Possibly not important for EDA?

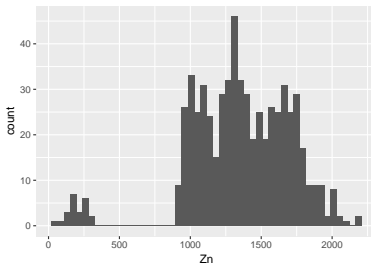
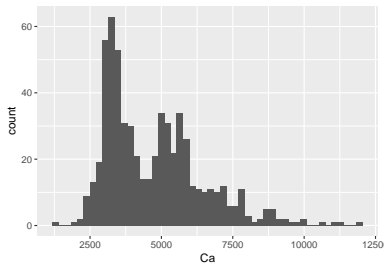
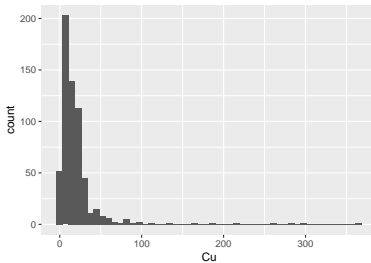
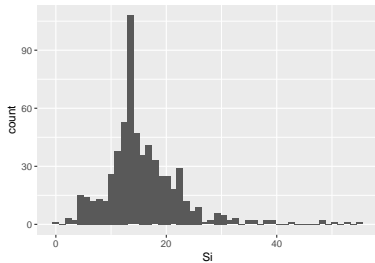




histogram without those really big values



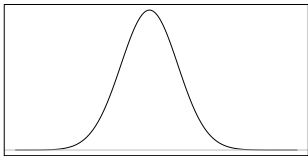
## a few more ppm histograms



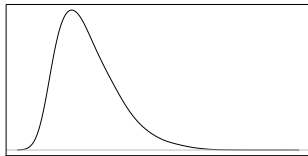
## “shapes” of “distributions”

To use a histogram, *glance* at it and look for any of the following (without getting fooled by plot artefacts):

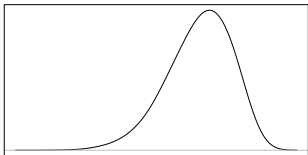
**Symmetric**



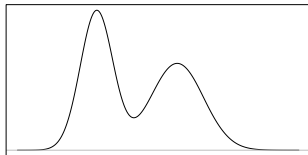
**Right skewed**



**Left skewed**

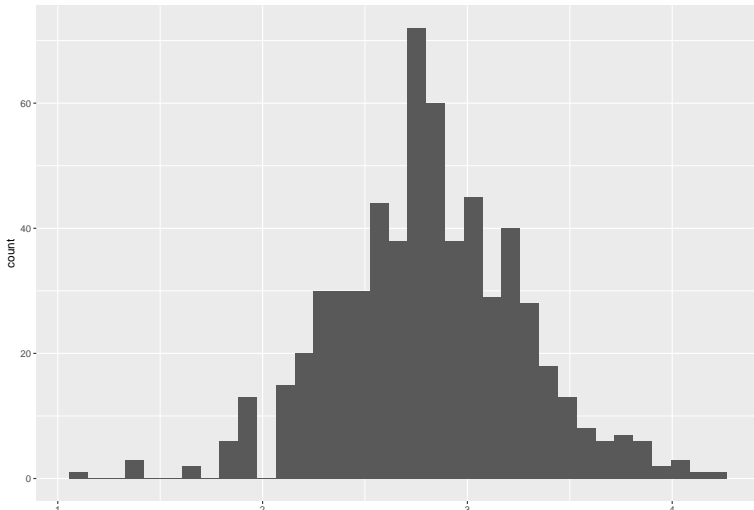


**Multimodal**



## transforming variables

Apply log or square root to a variable will change the shape of the empirical distribution, e.g. transform right-skewed to symmetric.



## boxplots

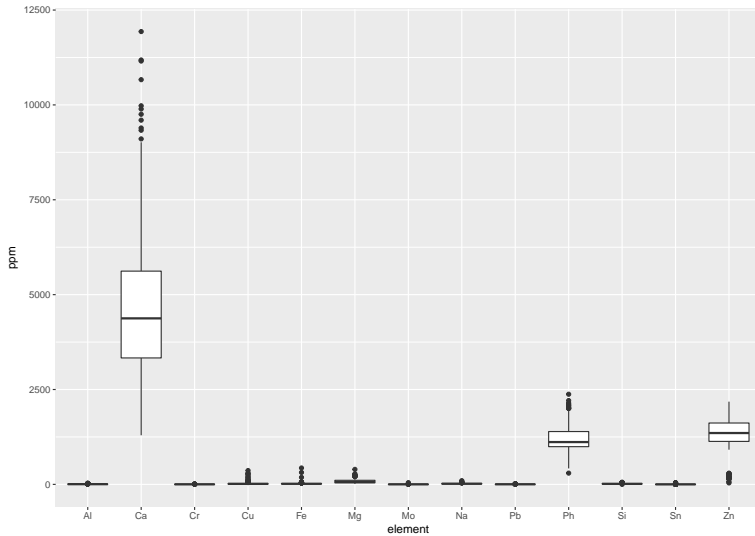
A special plot of these (or similar) five numbers:

min      25<sup>th</sup> percentile      median      75<sup>th</sup> percentile      max

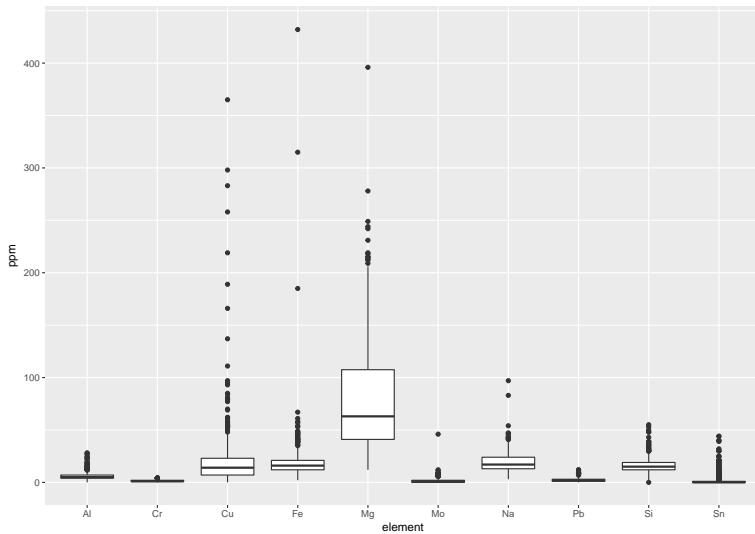
is called a *boxplot*. Often the extreme values are shown individually (see documentation for the (irrelevant) details.)

Best as *side-by-side* boxplots with more than one variable on the same scale.

## boxplot example - I

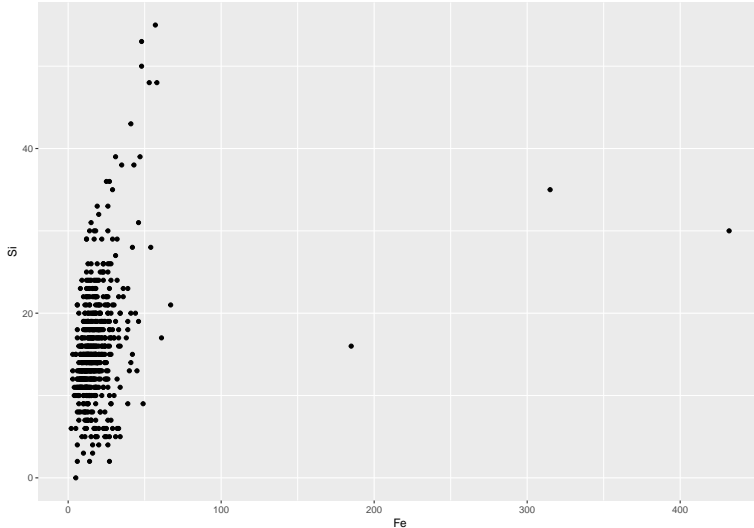


## boxplot example - II



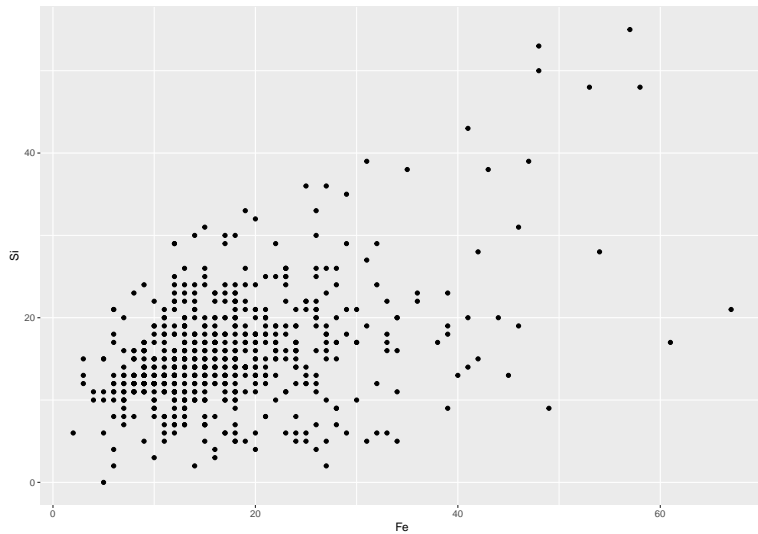
## scatterplot

A graphic for two numerical variables, e.g. Fe and Si

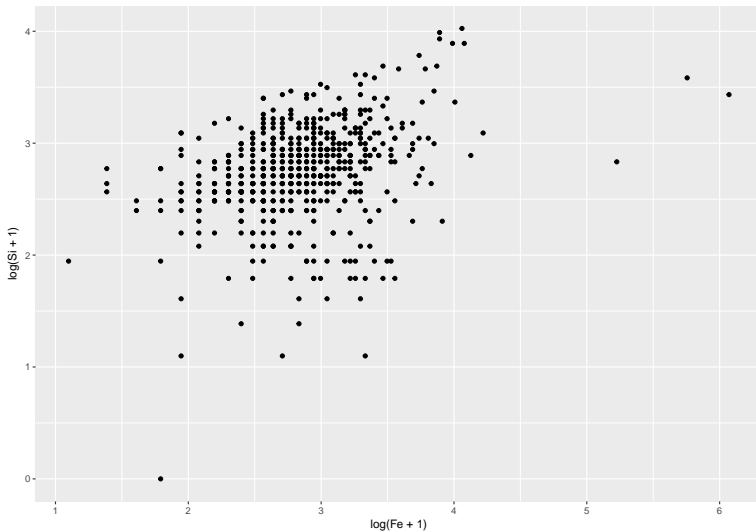




## Fe vs Si without the “outliers”

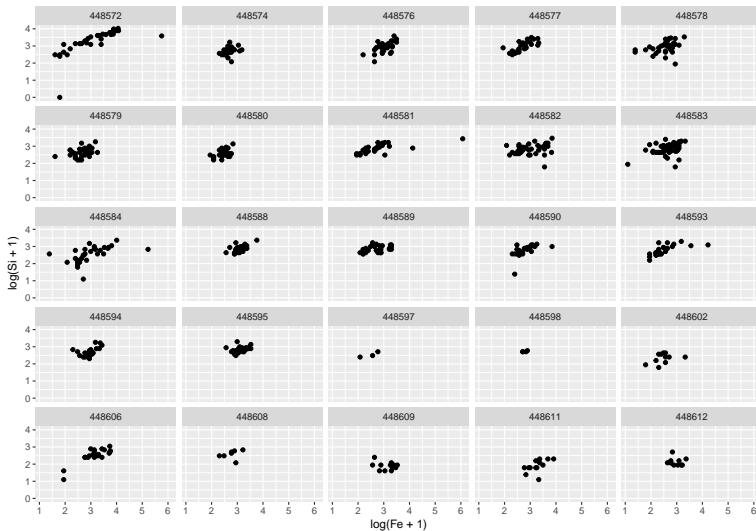


alternatively, on a log-log scale

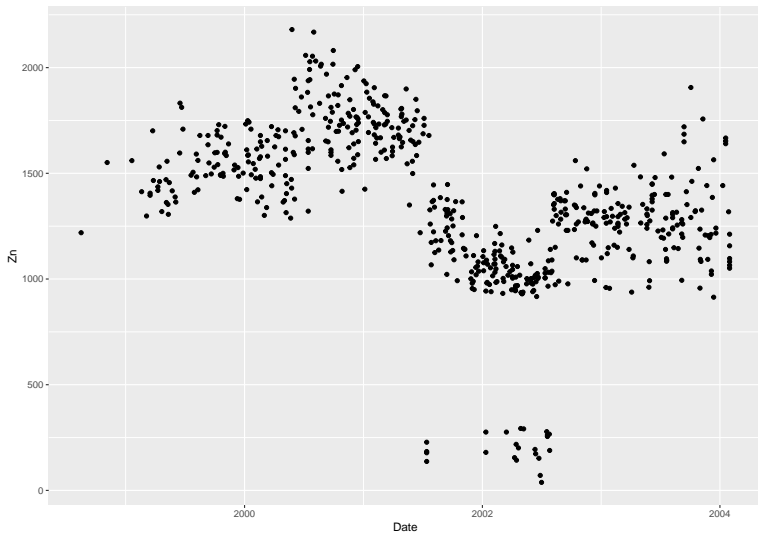


## “small multiples” through faceting

A powerful exploratory tool is to make a grid of small plots on subsets of the data.



what about that “Date” variable... (!)



# Fe versus Date, facet by Ident

