# STA303: Methods of Data Analysis II Course guide

Prof. Liza Bolton

Winter 2022

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## 1

# How to use this course guide

This course guide has been created using bookdown. You can download a PDF version of the whole guide with the download button above (down arrow into a tray). You can also put the website into dark mode and changed the font style, if you find s different display preferable.

If you would like a PDF copy of the slides, you can 'Print to PDF' in your browser. Shortcut: Cmd+P or Ctrl+P, and select 'Save as PDF' (or similar).

#### 1.0.1 Communication policy reminder

All content and logistics questions must be asked on Piazza. Personal or private course matters should be emailed to sta303@utoronto.ca. Quercus mail or emails sent directly to teaching team members will not be answered. If you've missed an assessment due to illness or emergency, please fill out the appropriate form.

# STA303/1002 syllabus

# 2.1 Key information

Winter 2022, half year, half credit course

**Instructor**: Prof. Liza Bolton (she/her)

Head TA: Amin Banihashemi (he/him)



sta 303 @utoronto.ca



Synchronous class meetings Wednesdays L0101 12:10–1:00 p.m. L0201 3:10–4:00 p.m.

Prof. office hours will take place in the hour after class.

TA office hours will be announced on Quercus.

#### 2.1.1 Delivery

- This course will be run completely online until January 31, 2022. After that, *optional* in person components will be offered, subject to public health guidance.
- In person attendance is NOT required.
- Synchronous attendance is not required but some knowledge basket (see assessments) components are only available synchronously.
- All assessments will be completed online.

#### 2.1.2 Pre-requisities

STA302H1/STAC67H3/STA302H5 (or for STA1002, STA1001H1)

It is Department policy to strictly enforce pre-requisites This is not up to the teaching team. You will be removed from the course if you do not meet the prerequisite course requirements. Please **reach out to the UG stats team (ug.statistics@utoronto.ca)** with any questions abour enrolment orbook an appointment during their office hours.

# Start here!

#### 3.1 Introductions

Hi folks,

Welcome to STA303! We're excited you're joining us on this statistical voyage. I look forward to introducing myself to you in our first class on Wednesday, but for now, there is are basic introductions below for me and our Head TA Amin. Feel free to skip to How this course works, I know there is a lot to read in the module!

Looking forward to a great semester! See you in class on Wednesday.

#### 3.1.1 Professor Liza Bolton, Instructor

Email: sta303@utoronto.ca (Put "[Prof. Bolton]" in the subject line to the email me directly)

**Pronouns:** she/her

Before moving (back) to Canada in 2019, I had lived more than half my life in New Zealand. (I still mention New Zealand a lot in class...) My current research areas are in statistics education and online learning, as well as health disparities across ethnic groups. I used to run a small consulting company and called myself a Data Ambassador. Why? Well, lots of people are consultants. I even did an internship in management consulting once upon a time. But it wasn't a satisfying title for what I wanted my work with people to look like. I wanted something that focused on the communication and interpersonal side, not just high quality and appropriate analysis. People who aren't confident in their ability to analyse their own data need a go-between, someone who can be an ambassador for their data! While I don't do consulting any more, I love helping students build their technical and professional skills so they can go out into the world and be excellent ambassadors for data themselves.

Last movie I cried in: Kiki's Delivery Service

Favourite food: Corn. Popped, on the cob, in a chip, Mmmmm.

Book most often given as a gift: A Matter of Fact: Talking Truth in a Post-Truth World by Jess Berentson-Shaw

#### 3.1.2 Amin Banihashemi, Head TA

Email: sta303@utoronto.ca (Amin will often be the one responding to your emails)

**Pronouns:** he/him

I'm a fourth-year PhD student at the Institute of Medical Science. I have been a TA for STA130 in DoSS for the past 3 years and this is my second semester as Head TA of STA303.

My area of research is clinical Neuroscience, something I am passionate about. I analyze images of brain and eye structures in neurodegenerative diseases. I investigate possible associations of these structures with each other and

8 3. START HERE!

with the ability to remember well and carry out goal-oriented tasks successfully. I love creating reproducible statistical analysis workflows in R. I also like audiobooks, candlelight, and apple pie (which I make myself!)

\includegraphics[width=10d0%]{images/headers/map}

#### 3.2 How this course works

This course is organized into five two-week modules of learning + two one week assessment-focus weeks.

All course material will be made available through this course site in Quercus (any links to outside sites will be found here). Take a moment to familiarize yourself with some of the tools and content areas found in the left navigation bar. You can move through content in a module by selecting the "Next" button at the bottom right of the page. You can also visit the Module section in the left navigation menu so see all the available modules and their contents.

All times listed are 'Toronto time', i.e. Eastern Time. Note that Daylight Savings Time begins Sunday, March 13, 2022. You may find this time converter helpful: https://www.timeanddate.com/worldclock/meeting.html

#### 3.2.0.1 In most modules there be will be:

- A weekly module released on Monday morning.
- A quiz based on the content released in the module due on Tuesday at 6:00 p.m ET.
  - Special note for the Week 1 quiz: this quiz is available until January 26 at 6:00 p.m. ET. (with no penalty) because I know there is a lot to get used to in the first week.
- A synchronous class on Wednesday at 12:00 p.m. ET (L0101) and 3:00 p.m. ET (L0201).
  - Both sessions will be the same, you only need to attend one.
  - Please review the steps for attending a class.
  - Synchronous classes will be recorded. You're expected to watch the recording if you cannot attend live.
     They will be posted on the course overviewpage.
- Weekly writing Create phase due Thursday at 6:00 p.m. ET.
- Weekly writing Assess phase due Friday at 6:00 p.m. ET.
- Weekly writing Reflect phase due (next) Monday at 6:00 p.m. ET.
- · Office hours.
  - Prof office hours will occur after the Tuesday synchronous classes, i.e. 11:10–12:00 p.m ET and 3:00–4:00 p.m., in the same Zoom call.
  - TA office hours: will begin in Week 2 (TBC) and the schedule will be updated here.

#### 3.2.0.2 Students joining off the waitlist

You don't have to submit missed quizzes or writing activities or alert me that you joined the course late, these will be covered by the associated 'best of' policies. See the Syllabus for more information.

If you have a *friend* on the waitlist, they can sign up to receive materials here.

### 3.3 Hours expectations

While everyone has different work styles and learning needs, I want to provide some guidance around how I expect this course to look for students.

Plan to be doing 6–8 hours of work on STA303 each week. In a two-week module, this may be comprised of:

- 2-4 hours on videos and readings
- 1–3 hours of attending synchronous class or reviewing the recording and activities
- 1–2 hours on knowledge basket assessments
- 2–6 hours on other assessments
- Remaining time attending reading announcements, office hours, checking Piazza, revision, etc.

#### 3.3.1 Module flow

#### 3.3.2 Communication

- Our course discussion board on Piazza is to be used for all content and administration questions. Only sensitive or personal issues/questions should be sent to sta303@utoronto.ca. We reserve the right not to respond to emails that should be Piazza posts.
  - Please ensure all course-related emails include your **UTORID**.
- There are several important forms that you may need if you miss an assessment due to illness or emergency or wish to request a regrade of an assessment.
- I will use Quercus announcements to share course information and updates. Please make sure you read these. I may also occasionally email or Querus message you about things that relate specifically to you.

#### 3.3.3 To do now

Press the next button below to continue through this module. In the following pages you will:

- Read the Syllabus.
- Join the Piazza discussion board.
- Understand the tools we will be using in this course.
- [Optional] Introduce yourself in the Introductions discussion board.
- Learn about some of the services and supports available to you as a U of T student.
- Make sure you have a U of T Zoom account https://utoronto.zoom.us/.

Header photo by Andrew Stutesman.

# Assessments

# Assessment overview

There are two special elements of assessment/grade calculation in this course that are important to be aware of in planning your approach to it.

- Two roads diverged in a yellow wood<sup>1</sup>: You can opt for Path A or Path B to get your final mark. I will calculate your marks along both paths and then assign you the higher of the two as your final mark.
- A-tisket, a-tasket<sup>2</sup>, fill up your **knowledge basket**<sup>3</sup>:
  - Personalize which of these assessments you do based on your interests and skills you want to develop.
  - You can 'max out' your basket: just keep putting grades in until you get to 10% (Path A) or 5% (Path B).

Assessment	Path A	Path B	STA1002 ONLY	Due dates
Mini-portfolio	5	0	0	Feb 3
Portfolio	20	25	25	Feb 7
Mini-mixed assessment	5	0	0	Mar 9
Mixed assessment	20	25	25	Mar 16
Final project	45	45	50	Apr 7 (5% pt bonus)   Apr 11 (no bonus
Knowledge basket	5	5	0	Multiple
Total	100	100	100	

## 4.1 Graduate student modification (1002H)

There is no difference in the grading scheme or assessment for graduate students enrolled in STA1002, other than an additional 'path' to your final grade where you may opt out of the 'basket' assessments, if you wish. This only applies to graduate students enrolled in STA1002, not to any students enrolled in STA303.

You don't need to advise me of your choice, I will calculate you mark all three ways above and give you the highest of those marks.

<sup>&</sup>lt;sup>1</sup>The Road Not Taken, by Robert Frost. But, dear traveller, you can in fact take both roads and then get whichever gives you the better mark. https://www.poetryfoundation.org/poems/44272/the-road-not-taken

<sup>&</sup>lt;sup>2</sup>A-tisket, a-tasket by Ella Fitzgerald, https://www.youtube.com/watch?v=1bgFkeDLpSI

 $<sup>^3</sup>$  "Whaowhia te kete mātauranga" is a Māori proverb meaning "Fill up the basket of knowledge". Mātauranga is specifically traditional Māori knowledge. You can listen to the pronunciation here https://www.massey.ac.nz/student-life/m%C4%81ori-at-massey/te-reo-m%C4%81ori-and-tikanga-resources/te-reo-m%C4%81ori-pronunciation-and-translations/whakatauk%C4%AB-m%C4%81ori-proverbs/

# Mini-portfolio

Information	Note
Name	Mini-portfolio
Type (Main, mini or	Mini
basket)	
Value	5% (Path A)
	0% (Path B)
Due	2022-02-03
Submission instruction	Submission: Via peerScholar, click the button at the bottom of this page to load it.
Accommodations and	An extension for this assessment due to illness or personal emergency can be requested
extension policy	through the Illness/personal emergency declaration form.

#### 5.0.1 Instructions

You can pull the template for this assessment into your U of T JupyterHub

The cover page must have:

- A title and subtitle
- Your name
- Date (assessment submission date is fine)

You can change the colour of this cover to any colour you would like by replacing 6C3082 in the YAML above (line 11) to another hex code. You could use this tool to help you: <a href="https://htmlcolorcodes.com/color-picker/">https://htmlcolorcodes.com/color-picker/</a>

In the **introduction** section, write a brief summary of the skills you have demonstrated in this portfolio. Think of it like a cover letter for this document. It should appropriate for a fairly general audience, imagine a future employer reading this. Your introduction should be not be longer than 300 words

#### Final advice: KNIT EARLY AND OFTEN!

#### 5.0.2 Prompt

Read the below job ad and write about the skills you would need to apply. The skills can be those highlighted in grey, as well as those not highlighted. Write on at least 2 soft skills and 2 analytic skills. The ad targets those with a MSc/PhD or those with 2+ years of experience, but imagine this requirement is not there.

1. Soft skills. What soft skills relating to communicating and working with others does the company seek?

- 1. In what way do you already possess two of these skills?
- 2. What evidence do you have of possessing one or two of these skills?
- 2. **Analytic skills.** What analytic skills relating to software use and performing data analysis does the company seek?
  - 1. In what way do you already possess two of these skills?
  - 2. What evidence do you have of possessing one or two of these skills?
- 3. Connection to studies. As part of the coursework of STA303, you proposed an activity related to your professional development. At the end of the course, you will provide evidence of completing this activity and then reflect on what you did.
  - 1. How does the evidence produced from your professional development activity help you in applying to this job ad?
  - 2. What other skills can you develop and what evidence can you accumulate during the remainder of your education to be ready for a similar job ad?

Structure your answer under three headings: 'Soft skills', 'Analytics skills' and 'Connection to studies'. Write your answers in full sentences, with appropriate paragraphing. No introduction or conclusion is required.

Word count: 300–500 words



Figure 5.1: Yelp logo

#### 5.0.2.1 Data Scientist (Remote)

Category Data Science & Analytics

Location Toronto, Ontario, Canada

**Department** Engineering and Product

At Yelp, it's our mission to connect people with great local businesses. Yelp's unique dataset contains billions of interactions between users and local business around the globe, from a user reviewing a neighborhood coffee shop to requesting a repair quote with a photo of a leaky faucet. Data Scientists at Yelp work to make sense of these interactions to deliver impactful analyses and products to our users, business partners and the general public.

The Data Science team performs analyses, builds models, and designs experiments that directly impact Yelp's business and users. Our centralized team is the most wide-ranging consumer of data at Yelp, adept at tasks from modeling content growth and user behavior to sharing insights about the health of local economies. With varied backgrounds and expertise, we strive for learning and growth in a collaborative environment.

We'd love to have you apply, even if you don't feel you meet every single requirement in this posting. At Yelp, we're looking for great people, not just those who simply check off all the boxes.

This opportunity is fully remote and does not require you to be located in any particular region. We welcome applicants from throughout Canada.

#### We Are Looking For:

5. MINI-PORTFOLIO

• 3+ years of experience as a data scientist or MS/PhD and 2+ years of industry experience in a quantitative role.

- Fluency with SQL and Python or R for data analysis.
- Solid understanding of statistical inference, experimental design and analysis.
- Enthusiasm for clean code and sharing reproducible results.
- Communication skills to work with partners on engineering, product and business teams.
- An eye for great data visualization with Matplotlib, Plotly, ggplot, or Tableau.
- If you don't have 2+ years of industry experience in a quantitative role, please take a look at our College Data Scientist roles instead!

#### Where You Come In:

- Define key metrics to track Yelp's performance and inform product decisions.
- Assess and frame questions from partners into actionable deliverables.
- Design, execute, and analyze complex experiments impacting millions of users.
- Devise and evaluate models for diverse business needs, such as identifying growth opportunities, personalizing user experience, and matching consumers to businesses.
- Own analyses start-to-finish and communicate key insights to stakeholders.
- Share your technical skills to develop and maintain high-quality, reusable analysis tools.

#### #LI-Remote

At Yelp, we believe that diversity is an expression of all the unique characteristics that make us human: race, age, sexual orientation, gender identity, religion, disability, and education — and those are just a few. We recognize that diverse backgrounds and perspectives strengthen our teams and our product. The foundation of our diversity efforts are closely tied to our core values, which include "Playing Well With Others" and "Authenticity."

We're proud to be an equal opportunity employer and consider qualified applicants without regard to race, color, religion, sex, national origin, ancestry, age, genetic information, sexual orientation, gender identity, marital or family status, veteran status, medical condition or disability.

We are committed to providing reasonable accommodations for individuals with disabilities in our job application process. If you need assistance or an accommodation due to a disability, you may contact us at accommodations-recruiting@yelp.com or 415-969-8488.

Note: Yelp does not accept agency resumes. Please do not forward resumes to any recruiting alias or employee. Yelp is not responsible for any fees related to unsolicited resumes.

Accessed from Yelp® on Feb 28, 2021, 15:15 PM

https://www.yelp.careers/us/en/job/YELPUS97AE2C833B0240318A66253960395242EXTERNALENUS/Data-Scientist-Remote

Large logo from Wikipedia https://en.wikipedia.org/wiki/Yelp#/media/File:Yelp\_Logo.svg

#### 5.1 Portfolio

# Knowledge basket: Writing and peer feedback

The module writing and peer feedback activities have three stages.

- Create phase due the first Friday of the module at 3:03 p.m. ET
  - Spend ~30 minutes writing a paragraph response to the prompt
- Assess phase due second Tuesday of the module at 3:03 p.m. ET
  - Read two peer's pieces and provide feedback
- Reflect phase due second Friday of the module at 3:03 p.m. ET
  - Read the feedback received from your peers
  - Rate the usefulness on a 3-point scale

These assessments can be used to make up your knowledge basket. They are also useful in helping you prepare for your portfolio writing samples and final project writing.

Warning: MAKE SURE YOU CLICK SUBMIT! Check that each phase is showing as submitted. Student occasionally have stuggled with this in peerScholar's interface.

## 6.1 Module 1 writing task

Information	Note
Name	Module 1 writing task
Type (Main, Mini or Basket)	Basket
Value	$0.5\% \ (0.2\% - 0.2\% - 0.1\%)$ Completion
Due	Create Friday, January 14, 2022 at 3:03 p.m ET;
	Assess Tuesday, January 18, 2022 at 3:03 p.m ET;
	Reflect Friday, January 21, 2022 at 3:03 p.m ET;
Submission instructions	Submission: Via peerScholar
	Untimed survey, marked for completion
Late submissions, accommodations, and extension policy	No late submissions, accommodations, or extensions.

#### 6.1.1 Instructions

Answer the following questions to help me get to know the class. Some of the questions might seem a little random, but I'm hoping to use them for some future class activities.

(Some questions are from factfulnessquiz.com, you are not being marked on correctness, so please answer to the best of your ability without looking anything up.)

## 6.2 Pre-knowledge check

Information	Note
Name	Pre-knowledge check
Type (Main, Mini or Basket)	Basket
Value	0.5% for completion + $0.5%$ for a score of $80%$ + OR active attendance at the prerequisite knowledge workshop $2022-02-02$
Due	Thursday, January 20, 2022 at 3:03 p.m ET (Workshop: Wednesday, February 2, 2022 in class time)
Submission instructions	Submission: Via Quercus survey 60 minutes, 1 attempt, no pausing
Late submissions, accommodations, and extension policy	No late submissions, accommodations, or extensions.

#### 6.2.1 Instructions

Answer the pre-knowledge check quiz questions to the best of your ability. In Quercus, you will see two assignment entries, one for the quiz and for storing your final score that takes into account completion of the quiz and the 80%+ score or workshop engagement/attendance.

#### 6.2.1.1 Grade structure

- Completion of the quiz (all questions attempted) will earn you 0.5%.
- If you score 80% or more on the quiz, you earn an additional 0.5%.
- If you do not score 80% or more, you can still earn this additional 0.5% by attending and actively engaging with the workshop on Wednesday, February 2, 2022 in class time.
- The maximum points to earn here is 1% (i.e., you cannot get BOTH the 80%+ and workshop attendance bonuses)

# Knowledge basket: Professional development task



Image source: https://www.nsta.org/q-if-tree-falls-forest-and-theres-no-one-around-hear-it-does-it-make-sound

If a tree falls in a forest, and there's no one around to hear it, does it make a sound? Or, more relevant to this course, if you do a data analysis and can't share it with anyone in helpful ways, did youreally do anything? With this in mind, you will have the opportunity to choose an area of relevant professional development to pursue over the course of the semester. This could include technical skills that make you better at collaborating with others (version control, Git, GitHub), creating things others will find useful (an R package) or practising communication (oral or written).

There is a 1% **proposal** due fairly early in the semester, and then the final submission of **evidence** of, and **reflection** on, your activity is worth 3% and due toward the end of the semster.

Example professional development tasks include:

- Learning how to set up and use Git and GitHub (this might come in handy if collaborating on the final project with a group)
- Setting up a personal profile website (a bit like a digital CV, GitHub provides free hosting for simple sites)
- Participating in weekly TidyTuesday activities
- Writing a stats blog
- Developing an R package and sharing it on GitHub
- A public speaking based activity like a debating society or Toastmasters
- Conducting a series of interviews with industry professional or academics and publishing videos/write-ups

• Create a wildly successful stats memes TikTok à la Chelsea Parlett-Pelleriti (okay, maybe not this one...but she's well worth checking out)

Note: the task must be related to **communication or collaboration in some way**. For example, 'learning SQL' would not be sufficiently directly related to communication or collaboration, but developing an R package and sharing it with others requires communication (writing the documentation) and is a great way to contribute to the collaborative and supportive R community. If you are not sure, please ask!

You will use the SMART goals framework (see image below) when setting out your proposal. The more thought you put into this upfront, the easier collecting evidence and reflecting on your progress will be at the end. More information will be available on the respective assessment pages when they go live.

### 7.1 Professional development proposal

Information	Note
Name	Professional development proposal
Type Main, Mini or Basket	Basket
Value	1%
Due	2022-01-13 3:03 p.m. ET
Submission instructions	Submission: PDF via Markus
Late submissions, accommodations, and extension policy	An extension can be requested up to 48 hours before
	the due date through the extension request form.
	In the case of a personal illness/emergency, a
	declaration can be made, but must be submitted no more than 3 days after the due date.

#### 7.1.1 Instructions

There is a general overview of this task on the professional development overview page.

Example professional development tasks include:

- Learning how to set up and use Git and GitHub (this might come in handy if collaborating on the final project with a group)
  - Possible resource: https://happygitwithr.com/
- Setting up a personal profile website (a bit like a digital CV, GitHub provides free hosting for simple sites)
  - Possible resource: http://jmcglone.com/guides/github-pages/
  - Possible resource: https://uoft-doss-issc.github.io/website-workshop/
- Participating in weekly TidyTuesday activities
  - Possible resource: https://github.com/rfordatascience/tidytuesday
- Writing a stats blog
- Developing an R package
  - Possible resource: https://r-pkgs.org/index.html
- A public speaking based activity like a debating society or Toastmasters
- Conducting a series of interviews with industry professional or academics and publishing videos/write-ups

- Create a wildly successful stats memes TikTok à la Chelsea Parlett-Pelleriti (okay, maybe not this one...but she's well worth checking out)
- 1. Choose a professional development task that you can devote at least 5–10 hours to over the next several weeks.
- 2. Work through the SMART goals framework to describe what you will do. The more thought you put into this upfront, the easier collecting evidence and reflecting on your progress will be at the end. More information will be available on the respective assessment pages when they go live.
- 3. Explain WHY the goal is a good choice for you and your career/further education path ('Relevant' criteria).

#### 7.1.2 Submission requirements

Your proposal should be:

- typed (not handwritten)
- one page<sup>1</sup>
- single-spaced
- size 12 font
- margins should be no larger than 1 inch
- saved as a PDF

With these specifications, your proposal will be approximately 500 words.

#### 7.1.3 Rubric

<sup>&</sup>lt;sup>1</sup>References, if relevant, may be included on a second page, but a simple hyperlink may also be sufficient. References are not required.

Component	Missing 0%	Poor 25%	Adequate 50%	Good 75%	Excellent 100%	Points
Specific	There is no goal stated.	Goal is too generic and poorly specified.	Goal is stated but it is not specific. At least one resource may or may not be listed.	Goal is specific but no/unclear resource is mentioned.	Goal is specific. At least one resource that will be used to help is mentioned.	1
Measurable	There is no measure for attaining the goal.	Minimal evidence of consideration for measuring progress towards the goal or success.	Definition of success lacks clarity. Measures of progress may or may not be listed.	What success will look like is clearly defined but there no/unclear statement of measure of progress.	Both definition of success and a measure of progress are clearly defined.	1
Attainable	There is no explanation for how the goal is to be attained.	Inappropriate scope, not believable that the goal is attainable.	Some issues with the scope of the goal, may not be attainable. Understanding of the steps and potential problems very limited.	Goal has a mostly appropriate scope but may lack some clarity around steps to take and potential problems.	Goal has an appropriate scope, and a strong understanding of the steps to take and potential problems is shown.	1
Relevant	Goal is not related to communication or collaboration appropriate for statisticians/data-related roles AND no discussion of why this goal was chosen.	Goal is not related to communication or collaboration appropriate for statisticians/data-related roles but some discussion of why this goal was chosen OR goal is appropriate, but no discussion of personal relevance.	Goal is tenuously related to communication or collaboration appropriate for statisticians/data-related roles but good discussion of why this goal was chosen OR goal is appropriate, but limited discussion of personal relevance.	Goal is related to communication or collaboration appropriate for statisticians/data-related roles AND there is a reasonable discussion of personal relevance.	Goal is related to communication or collaboration appropriate for statisticians/data-related roles AND there is a clear discussion of personal relevance.	2
Time-bound	There is no timeline or evidence of consideration of time-bounding the goal.	Minimal evidence of consideration time-bounding the goal.	Timeline is not listed according to days/weeks or dates. Time for delays and troubleshooting may or may not have been considered.	Timeline is listed based on days/weeks or dates. No/unclear time for delays and troubleshooting is considered.	Timeline is listed based on days/weeks or dates. Time for delays and troubleshooting is considered.	1
Structure	There is no structure, very difficult to follow.	Minimal evidence of an attempt to structure the proposal logically.	Some structure but difficult to follow.	The organization follows some logical structure.	Well organized, follows a logical structure.	1
Writing mechanics	No response OR response is largely unintelligible.	Considerable writing and grammatical issues that completely obscure the meaning OR lots of slang and inappropriate word choice.	Multiple sections are difficult to read but it is otherwise understandable.	Slight difficulty in understanding one or two sections.	Can read and follow along with minimal effort. Some grammatical or word choice errors are allowable, but they must not obstruct meaning.	2
Conclusion	There is no concluding sentences.	Minimal evidence of a concluding statement.	The conclusion is weak not well supported.	A conclusion is present but does not completely summarise the central idea.	There is a clear central idea that is well summarised in a concluding sentences.	1

#### 7.1.4 Checklist

Before submitting your proposal, check the following:

- Your goal is specific. (Specific)
- At least one resource you will use to help you is identified. (Specific)
- It is clear how you will define success. (Measurable)
- It is clear how you will measure your progress. (Measurable)
- Your goal has an appropriate scope and is attainable. (Attainable)
  - This is shown through a description of the steps you'll need to take and what potential problems you
    might face. Related to timeline below.
- The goal is related to communication and/or collaboration appropriate for a statistician/data-related role. (Relevant)
- It is clear why this goal is relevant to you personally. (Relevant)
- The steps you want to complete can be completed in 7 weeks. (Attainable and Time-bounded)
- A timeline with dates/weeks for the required steps is included. (Time-bounded)
- The timeline shows some accommodation for troubleshooting/delays. (Time-bounded)
- There is a clear concluding sentence or sentences that wrap(s) up the proposal.
- You have proofread your proposal and made sure the structure is logical and there are not intrusive grammatical or word choice errors.
- You have written in full sentences.
- Your submission is typed (not handwritten), one page, single-spaced with size 12 font and the margins are no larger than 1 inch.
- Your final version is saved as a PDF.

# 7.1.5 Things to keep in minds as you start working towards your professional development goal

- Track your time
  - A time sheet should be part of your evidence submission
- Create a work log document or file to store screenshots in, make notes of tasks you've completed
  - This will make writing your reflection much easier

#### 7.1.6 Example smart goal

Note: This is *not* a collaboration/communication goal, but provides some examples of how to approach a SMART goal. Where there are ellipses ("...") we are suggesting there would be more of the same, but this example should be enough to give you the idea. You should *not* use ellipses in this way in your own proposal.

#### 7.1.6.1 Specific

Goal: "Climb to the peak of Mount Robson over 2 weeks in January and write one blog post for my website about the journey."

Bad example: "Climb a mountain and write about it." Which mountain? What type of writing and with what purpose?

Resources: "I will need climbing equipment, my camera, notebook ..."

#### 7.1.6.2 Measurable

Defining success: "Reach the peak of Mount Robson and return and write at least 1 blog entry with a picture about the journey, all in 2 weeks."

Bad example: "Climbed Mount Robson." Needs more details about what this success looks like. Walk up a few metres and turn back? Relates to time-bounded also.

Measuring my progress: "I will measure my progress by how many steps of my goals I have accomplished and the altitude of my climb relative to the elevation of Mount Robson (3,954 m). I will have taken a picture"

#### 7.1.6.3 Attainable

You have or can you learn the required skills: "I am sufficiently fit to make this climb safely and have climbed a similar mountain recently. I have a camera and am currently taking an online course on blogging."

Possible steps I need to take:

- 1. Arrive at Mount Robson Visitors Center with my climbing plan.
- 2. Climb until ... on first day.

6. Write one blog entry with one picture.

Bad example: "Make progress with my goal by 7% each day." Not useful to you, what does 7% actually mean here? Will it really be the same amount of progress every day?

Potential problems:

1. Weather might be bad, and I may have to delay my climb by a few days.

Bad example: "Something might not work." What? In what way? Could you solve it?

#### 7.1.6.4 Relevant:

Personal relevance: "The climbing experience will help me learn new skills like ... which will help me work towards becoming a professional climbing quide."

Bad example: "Seems like fun."

#### 7.1.6.5 Time-bounded:

"A 2-week journey from Jan 25th:Days 1-3to climb;Days4-6return;5 days for delays;3days to rest."



Specific	Measurable	Attainable	Relevant	Time-Bound
Make sure your goals are focused and identify a tangible outcome. Without the specifics, your goal runs the risk of being too vague to achieve. Being more specific helps you identify what you want to achieve. You should also identify what resources you are going to leverage to achieve success.	You should have some clear definition of success. This will help you to evaluate achievement and also progress. This component often answers how much or how many and highlights how you'll know you achieved your goal.	Your goal should be challenging, but still reasonable to achieve. Reflecting on this component can reveal any potential barriers that you may need to overcome to realize success. Outline the steps you're planning to take to achieve your goal.	This is about getting real with yourself and ensuring what you're trying to achieve is worthwhile to you. Determining if this is aligned to your values and if it is a priority focus for you. This helps you answer the why.	Every goal needs a target date, something that motivates you to really apply the focus and discipline necessary to achieve it. This answers when. It's important to set a realistic time frame to achieve your goal to ensure you don't get discouraged.

Source: Canadian Management Center, https://cmcoutperform.com/setting-smart-goals

## 7.2 Professional development evidence and reflection

You may wish to use the provided template to complete this task. This is not required to get full marks, but we believe this will be a helpful structure for you to ensure you have addressed all parts of the task.

#### 7.2.1 Templates

- $\bullet$  template.docx
- template.Rmd, template\_rmd.zip

#### 7.2.2 Reflection and evidence components

#### 7.2.2.1 Activity, alignment and lessons

**Activity**: Describe what you did and what you learned. Be **specific** but you don't need a step-by-step guide or dates, save that for your timesheet. Assume your reader has *not* read your proposal and that you are introducing your goal and plan to them for the first time. (It may help to imagine how you might explain this task and your progress in a job interview.)

#### 7.2.2.1.1 Examples

- I wrote 4 blog posts on .... The first one was on ... One unanticipated activity I had to do was ...
- This task helped me learn how to write for general audience...
- Through this task I improved my...

**Alignment**: How well did your activity and progress align with your proposal?

#### **7.2.2.1.2** Examples

- My plan changed as my goal was not specific enough. I think the reason for this is ... I can set realistic goals next time by ...
- Most of my attainable steps and potential problems were correctly identified because ....
- This is a good method which I will use again when I need to ...
- My way of measuring progress worked because ... This is useful for next time because ...

Lessons: What did you learn from using the SMART goal-setting experience?

#### **7.2.2.1.3** Examples

- An interesting thing I learned from the SMART goal-setting exercise was that ...
- I prefer to modify the format of SMART goals to match my work habits by ...

#### **7.2.2.2** Evidence

Provide links and/or copy/paste a screenshot of a blog, website, Github repository, Rmd document, ... Provide commentary on what the image/link is and what it demonstrates. I.e., Describe what we should be seeing and understanding from what you've included and how it relates to your goals.

#### 7.2.2.2.1 Examples

- The screenshot shows ... which is evidence of partially completing [goal] ...
- The provided link goes to ... which relates to [goal] ...
- Notice that there are separate buttons on the website for each of the ...

#### 7.2.2.3 Timesheet

Include a timesheet that briefly describes how you used your time (no specific format required, but something like the below is fine). Hours spent can be approximate.

Describe what you learned from filling your timesheet. This can be short and could include how you'd track your time differently in future, what you noticed about your work habits from tracking your time

**7.2.2.3.1 Examples** About ...% of my time was spent preparing, maybe because the task was new. This means for future tasks that are new I need to consider ....

The timesheet can be better suited to my work habits if ...

Week	Week starts on (Monday)	Time spent (Hrs)	Activity (Brief description of what was done, e.g. what you read, what you tried on GitHub or state.)
5	Feb 7	1.5	Example: Worked through chapters 1 & 2 of
6	Feb 14	0	Example: No progress this week
	Feb 21		Reading week
7	Feb 28	1	Example: Set up postcard home page and pushed to GitHub
8	Mar 7	2	Example: Wrote one blog entry about
9	Mar 14	1.5	Example: Fixed coding error that[reason for error] by [fix]
10	Mar 21	2	Example: Edited the video on [topic] using [software]

#### 7.2.3 Recommended structure

You do not *have* to set out your writing in this way to get full marks, but we believe this will be a helpful structure for you to ensure you have addressed all parts of the task.

#	Section heading	Format
1	Activity, alignment and lessons ~3 paragraphs:	
		• activity,
		• alignment,
2 3	Evidence Timesheet	<ul> <li>SMART lessons</li> <li>Selected screenshots of work done, links,</li> <li>Fill provided template or create your own</li> </ul>
		• 1-3 sentences of what you learned

#### **7.2.4** Rubric

Points

Activity description	Missing	Limited description of task, insufficient detail to understand the scope of activity.	Some description of the activity, but too general and/or would require the reader to have some previous knowledge of the goal/activity chosen to fully under it.	Mostly clear description of activity but lacking some specificity or does not fully introduce the task for a reader with no previous knowledge of the tasks.	Clear and specific description of the activity undertaken.  Appropriately introduced for a reader with no background knowledge of the task.	2
Alignment	Missing	Limited description of alignment with original proposal. Lacks specifics and clear reasoning.	Some description of alignment with original proposal, though lacking reflective depth.	Reflection on alignment with proposal provides some specific details and reasoning for changes/successes.	Reflection on alignment with proposal is insightful and specific, detailing what went to plan/what didn't and any changes that needed to be made, as appropriate.	2
SMART goal-setting lessons	Missing	Limited description of lessons learned from the SMART goal setting approach.	Some description of lessons learned from the SMART goal setting approach, though lacking reflective depth.	Reflection on lessons learned from the SMART goal setting approach provides some specific details	Reflection on lessons learned from the SMART goal setting approach is insightful and specific.	2
Evidence	Missing	Insufficient evidence provided. No explanation or relation to goal was not clear.	Some evidence provided but aspects of explanation/commentary were not clear and/or the relationship to the goal not well described.	Evidence provided with commentary and the relationship to the goal described.	Relevant evidence provided with clear commentary on what it demonstrated and how it related to the goal described.	1
Timesheet	Missing	Some hours or activity descriptions missing/insufficient. No description of what was learned from the time tracking activity.	Some hours or activity descriptions missing/insufficient. Some description of what was learned from the time tracking activity.	Timesheet complete but insufficient description of what was learned from the time tracking activity OR timesheet somewhat complete but good description of what was learned from the time tracking activity.	Timesheet complete and a clear and relevant description of what they learned from the time tracking activity.	1
Structure	Missing	Minimal evidence of an attempt to structure logically.	Some structure but difficult to follow.	The organization follows some logical structure. Paragraphs either don't have topic sentences or have unrelated ideas.	Well organized, follows a logical structure. Paragraphs have topic sentences and contain related ideas.	1
Writing mechanics	Missing	Considerable writing and grammatical issues that completely obscure the meaning OR lots of slang and inappropriate word choice.	Multiple sections are difficult to read but it is otherwise understandable.	Slight difficulty in understanding one or two sections.	Can read and follow along with minimal effort. Some grammatical or word choice errors are allowable, but they must not obstruct meaning.	1

Adequate 50%

Good~75%

Excellent 100%

Component

Missing 0%

Poor 25%

# Knowledge basket: Other

## 8.1 'Getting to know you' survey

Information	Note
Name	'Getting to know you' survey
Type (Main, Mini or Basket)	Basket
Value	0.1%
Due	Thursday, January 13, 2022 at 3:03 p.m ET
Submission instructions	Submission: Via Quercus survey
	Untimed survey, marked for completion
Late submissions, accommodations, and extension policy	No late submissions, accommodations, or extensions.

#### 8.1.1 Instructions

Answer the following questions to help me get to know the class. Some of the questions might seem a little random, but I'm hoping to use them for some future class activities.

(Some questions are from factfulnessquiz.com, you are not being marked on correctness, so please answer to the best of your ability without looking anything up.)

## 8.2 Pre-knowledge check

Information	Note
Name	Pre-knowledge check
Type (Main, Mini or Basket)	Basket
Value	0.5% for completion + $0.5%$ for a score of $80%$ + OR active attendance at the prerequisite knowledge workshop $2022-02-02$
Due	Thursday, January 20, 2022 at 3:03 p.m ET (Workshop: Wednesday, February 2, 2022 in class time)
Submission instructions	Submission: Via Quercus survey 60 minutes, 1 attempt, no pausing
Late submissions, accommodations, and extension policy	No late submissions, accommodations, or extensions.

#### 8.2.1 Instructions

Answer the pre-knowledge check quiz questions to the best of your ability. In Quercus, you will see two assignment entries, one for the quiz and for storing your final score that takes into account completion of the quiz and the 80%+ score or workshop engagement/attendance.

#### 8.2.1.1 Grade structure

- Completion of the quiz (all questions attempted) will earn you 0.5%.
- If you score 80% or more on the quiz, you earn an additional 0.5%.
- If you do not score 80% or more, you can still earn this additional 0.5% by attending and actively engaging with the workshop on Wednesday, February 2, 2022 in class time.
- The maximum points to earn here is 1% (i.e., you cannot get BOTH the 80%+ and workshop attendance bonuses)

# Modules

# Module 1

#### 9.1 Instructor information

Prof. Liza Bolton

Course email: sta303@utoronto.ca

Help hours: During the second half of Wednesday classes: 11:10—12:00 p.m. ET and 4:10—5:00 p.m. ET

Please do not email my individual email with STA303 questions or use Quercus mail. It makes it harder to keep track of and address your questions. Sending me messages on three different platforms will NOT speed up my response. I will not respond messages that don't follow the course communication policy.

You can see the latest version of my email autoresponder here.

## 9.2 Upward management tips

'Upward management' is basically managing your manager. <sup>1</sup> If you make their life easier and help them be more effective, this should also make your life easier and is a good investment in your own career and skills building.

While our course isn't a business, some of the basic parts of this concept apply well to your time at univeristy AND can set you up for success in graduate studies and your future career.

But why should you put effort into upward managing me? Well, while I will always seek to treat all students fairly and to listen to your feedback, YOU can make this easier or harder for me, and thus make this course better or worse for yourselves.

For example, if I have to use all my time and energy following up on unclear emails for more information and dealing with students who haven't followed instructions etc. etc....I won't have that energy to put into writing TeamUp! activities to give you extra practice and opportunities to earn bonus points.

#### 9.2.1 Communicate using the tools your manager prefers.

- In business, this means knowing who likes face-to-face vs email, or whether your manager would rather receive an instant message than an email for a quick question.
- In STA303, this means:
  - Using Piazza for all course admin and content questions.
  - Using the appropriate forms for accommodations and regrade requests.

<sup>&</sup>lt;sup>1</sup>I used to haaaate this concept because I learned it while doing a consulting internship at a large international professional services firm and I really struggled with my manager.

- Emailing sta303@utoronto.ca for private issues not otherwise covered by the other tools,
   e.g. emailing me your Accommodation Serivces letter, requesting an extension to an assessment that conflicts with essential travel.
- Asking questions in office hours.

#### 9.2.2 Write good emails (when emails are appropriate)

- In business, this might mean:
  - Choosing who should be the main recipients vs CCed/BCCed.
  - Ensuring your contact details are clear in your signature.
  - Make sure the subject line is informative and short
  - Making the text of the email as clear and concise as possible.
  - Use proper grammar and punctuation.
  - Don't use emoji in formal emails. If in doubt, leave 'em out.
- In STA303, this looks like:
  - Everything in the right-hand column, plus the following.
  - Starting an email with "Hi Prof. Bolton," or "Hi Liza,".2
  - Sign off the email with your **preferred name** (i.e. what should I call you when I reply) and if your have different official name, include that and your UTORid below your name.
  - Subject line including [Prof. Bolton] or [TA name] if your email is for a specific person.

#### 9.2.3 Understand your manager's goals.

- In business, this might look like understanding their KPIs and how you can help make sure these are met.
- In STA303, most of my goals are for you, like that you learn useful statistical skills, improve your writing skills etc. I also personally want to improve as an instructor and have fun talking about somethign I love.
  - You can help me with these goals by working on this course every week, trying your best, asking for help early and often, engaging with feedback gathering mechanisms and providing constructive feedback if something is not working.

# 9.2.4 Demonstrate self-management and resilience while also asking for help and flagging problems early.

- In business, this might look like:
  - Being proactive about addressing possible problems before they occur. Managers like a 'no surprises' policy.
  - Preparing a list of questions to cover in a meeting or to compile in an organised fashion into one email (instead of ten).
  - Searching for answers yourself before asking your manager and improving your strategies for finding available information.
- In STA303, this looks like:
- Putting in a little effort into find answers before posting on Piazza/asking in class. (Have you searched Piazza? have you re-read/watched the assigned materials? have your checked the syllabus and recent announcements?)
- Come to office hours often, lists of questions very welcome!
- Getting in touch (or asking your registrar to) **early** if you might hate to miss a lot of class. It is usually easier to find a solution if I know things ahead of time, or as soon as possible after.

 $<sup>^2</sup>$  "Dear Madam" and "To my esteemed professor" make me uncomfortable.

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#### Recap of linear models 9.3

#### Why model? 9.4

- The goal of a model is to provide a (relatively) simple summary of a dataset.
- We can describe data AND make predictions.

#### 9.5Linear models

In a linear model,

$$y_i = \beta_0 + \beta_1 x_{1i} + \dots + \beta_p x_{pi} + \epsilon_i$$

The response is predicted by a linear function of explanatory (or predictor) variables plus an error term. a.k.a.

DATA = MODEL + ERROR

#### Linear regression assumptions 9.6

L: your model is Linear.

I: Errors are Independent (usually satisfied if observations are independent).

N: Errors are Normally distributed with expected value zero,  $E[\epsilon_i] = 0$ 

**E**: Equal/constant variance (homoscedasticity),  $var[\epsilon_i] = \sigma^2$ .

We can express "I N E" above as assuming the errors are i.i.d Normal with mean of zero and variance  $\sigma^2$ ,

$$\epsilon_i \sim N(0, \sigma^2)$$

#### What makes it a *linear* model? 9.7

A model is linear if it is linear in the parameters. That is, all the  $\beta$  enter the model in a linear way. It is totally fine if the predictor variables enter the model in a non-linear way.

#### 9.7.1Linear

- $\begin{array}{l} \bullet \quad y_i = \beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \epsilon_i \\ \bullet \quad y_i = \beta_0 + \gamma_1 \delta_1 x_{1i} + \beta_2 \exp(x_{2i}) + \epsilon_i \end{array}$

#### 9.7.2 NOT linear

- $\begin{array}{ll} \bullet & y_i = \beta_0 + \beta_1 x_i^{\beta_2} + \epsilon_i \\ \bullet & y_i = \beta_0 exp(\beta_1 x_{1i}) + \epsilon_i \end{array}$

Internally screaming "DON'T LET THE BETAS TOUCH" often helps me remember what is not linear. Additionally, don't let them do anything weird, like get exponentiated.

### 9.8 Optional refresher reading

#### 9.8.1 Brief discussion of assumptions with examples

Section 1.3 of Broaden your Statistical Horizons on the assumptions of OLS https://bookdown.org/roback/bookdown-bysh/ch-MLRreview.html#ordinary-least-squares-ols-assumptions [freely accessible]

#### 9.8.2 Fitting linear models in R

Section 1.6 of *Broaden your Statistical Horizons* on Mulitple linear regression (bootstrapping not assessed) https://bookdown.org/roback/bookdown-bysh/ch-MLRreview.html#multreg [freely accessible]

#### 9.8.3 Delicious mathematics

Chapter 1 of Wood, S. N. (2017). Generalized additive models: An introduction with r, second edition http://go.utlib.ca/cat/13435628 [you will need to log in to the U of T library for access]

#### 9.9 Common statistical tests as linear regression

#### 9.9.1 Introduction

Technical note: I have had to remove code answer checking, but if you get stuck the final 'Hint' is the solution. This is ungraded, so don't worry, just slightly inconvenient.

You have probably encountered several statistical tests in your studies so far.

#### 9.9.1.1 Parametric

E.g. one-sample t-tests, paired t-tests, two-sample t-tests, one-way ANOVA, two-way ANOVA Parametric tests make assumptions about the distribution of the population from which our sample data have been drawn.

#### 9.9.1.2 Non-parametric

#### E.g. Wilcoxon signed rank, Mann Whitney-U, Kruskal-Wallace

Non-parametric tests do not assume that our outcome is Normally distributed. They are sometimes called 'distribution-free', but note that this is because they have fewer assumptions than parametric tests, not because they have no assumptions at all.

#### 9.9.1.3 Aside: But why are there two types of tests?

Parametric tests are more **powerful**, i.e., they have a better chance of detecting an effect if there is one there to find. So why would you ever use a less powerful test? Well, with great power comes <del>great responsibility</del> more assumptions that must be valid to proceed.

There is a GIF in the web version. Not required content. https://tenor.com/view/spider-man-uncle-ben-with-great-power-comes-great-responsibility-its-true-just-saying-gif-24193883

Non-parametric tests are a great choice when your outcome is an ordinal variable, is ranks, or there are problematic outliers.

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For the purposes of this lesson, we're going to focus more on parametric tests, but also take a look at the corresponding non-parametric tests with the slight white lie that they are just ranked versions of their parametric companions. This approach is pretty good as long as you have a reasonable sample size.

Imagine this:

You're on a ship trying to spot land. **Parametric** tests are the crew member with the best eyesight, but they can be fussy and the conditions have to be right for them to work in or they will breakdown.

**Non-parametric** tests are the crew member with not quite as good eyesight, but they're more laid back about the conditions you make them work in.

In the following sections we'll explore several of these tests.

#### 9.9.2 One-sample t-test

I am assuming you've seen this in a 200-level statistics course or equivalent. Brief recap below.

#### 9.9.2.1 Use case

You want to know if it is believable that the population mean is a certain value (our 'hypothesized value' below).

#### 9.9.2.2 Assumptions

- 1. The data are continuous.
- 2. The data are normally distributed.
- 3. The sample is a simple random sample from its population. Each individual in the population has an equal probability of being selected in the sample

(Do these sound familiar from linear regression?)

#### 9.9.2.3 Hypotheses

$$H_0: \mu = \text{hypothesized val}$$
  
 $H_1: \mu \neq \text{hypothesized val}$ 

What are we doing? Finding the strength of evidence against the claim that the population mean is some hypothesized value.

The test statistic, t, is calculated as follows:

$$t = \frac{\bar{x} - \text{hypothesized val}}{s / \sqrt{n}}$$

We then compare this t value to the t-distribution with degrees of freedom df = n - 1 and find the area under the curve that represents the probability of values likes ours or more extreme.

#### 9.9.2.4 Example

Suppose existing research suggests that the average weight of penguins is 4000 grams. You want to see if this makes sense for your new penguins data.

$$H_0: \mu = 4000$$
  
 $H_1: \mu \neq 4000$ 

The penguins dataset is already loaded, you you don't have to run any libraries. Use the t.test() function run a one-sample t-test.

```
##
## One Sample t-test
##
## data: penguins$body_mass_g
## t = 4.6525, df = 341, p-value = 4.7e-06
## alternative hypothesis: true mean is not equal to 4000
## 95 percent confidence interval:
## 4116.458 4287.050
## sample estimates:
## mean of x
## 4201.754
```

#### 9.9.2.5 Now as a linear model

First, consider the following, what would a linear regression with no predictor variables and just an intercept tell you?

Create a linear regression model called mod1(replace the blank below) that is an 'intercept only model' with body\_mass\_g as the response.

```
##
## Call:
## lm(formula = body_mass_g ~ 1, data = penguins)
##
## Residuals:
##
      Min
               1Q Median
                                3Q
                                       Max
  -1501.8 -651.8 -151.8
##
                             548.2
                                   2098.2
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4201.75
                             43.36
                                     96.89
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 802 on 341 degrees of freedom
     (2 observations deleted due to missingness)
```

It turns out the estimate from this linear regression is the same as the sample mean.

```
mean(penguins$body_mass_g, na.rm = TRUE) #na.rm = TRUE removes missing values
```

```
## [1] 4201.754
```

Now, recall that with the t-test, we calculate our test statistic by subtracting the hypothesized value from the mean. Let's run the linear model again, but on the left-hand side of the formula, subtract the hypothesized value.

```
##
## Call:
## lm(formula = body_mass_g - 4000 ~ 1, data = penguins)
##
## Residuals:
## Min    1Q Median    3Q Max
## -1501.8 -651.8 -151.8    548.2    2098.2
##
## Coefficients:
```

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```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 201.75     43.36     4.652     4.7e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 802 on 341 degrees of freedom
## (2 observations deleted due to missingness)
```

Compare the results of this summary(mod2) and your earlier t-test. You should see that the t value, degrees of freedom and p-value are the same for both analyses.

Thus, our one sample t-test hypotheses,

 $H_0: \mu = \text{hypothesized val}$ 

 $H_1: \mu \neq \text{hypothesized val}$ 

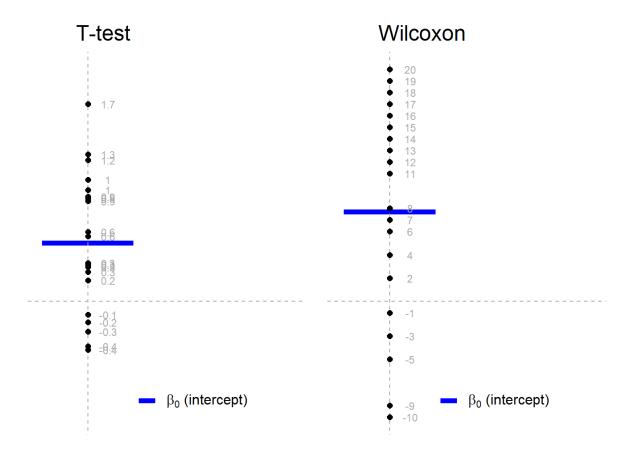
are equivalent to our linear regression hypotheses about the intercept,

 $H_0: \beta_0 = \text{hypothesized val}$ 

 $H_1: \beta_0 \neq \text{hypothesized val.}$ 

#### 9.9.2.6 Wilcoxon signed-rank test

While the linear regression approach to the one-sample t-test is exact, we can also approximate the Wilcoxon rank-sign test with linear regression. See below.



Note: The above is just example from some toy data, but aims to illustrate how a t-test is treating the data and how the Wilcoxon test is treating the data.

```
# Function to get signed rank of each observation
signed_rank = function(x) sign(x) * rank(abs(x))
# The wilcoxon test function
wilcox.test(penguins$body_mass_g, mu = 4000)
##
##
   Wilcoxon signed rank test with continuity correction
##
## data: penguins$body_mass_g
## V = 34723, p-value = 0.0004829
## alternative hypothesis: true location is not equal to 4000
# Equivalent linear model
mod3 <- lm(signed_rank(penguins$body_mass_g-4000) ~ 1)</pre>
summary(mod3)
##
## Call:
## lm(formula = signed_rank(penguins$body_mass_g - 4000) ~ 1)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -334.63 -173.13 -22.13 187.87 305.37
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  36.63
                             10.53
                                     3.479 0.000569 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 194.7 on 341 degrees of freedom
     (2 observations deleted due to missingness)
```

[Optional] Check out the theory behind the rank transformation in section 3.0.2 https://lindeloev.github.io/tests-as-linear/#3 pearson and spearman correlation

### 9.9.2.7 Paired sample t-test and Wilcoxon matched pair

A paired t-test is equivalent to a one sample t-test if you just consider  $x_{\text{diff }i} = x_{1i} - x_{2i}$ , i.e.,  $x_{\text{diff }i}$  is the difference of the paired values for each observation, and proceed with  $x_{\text{diff }i}$  as you would in the one sample case. Likewise for the Wilcoxon

The R code (not evaluated here) would be as follows:

```
# Built-in Wilcoxon matched pairs
wilcox.test(x1, x2, paired = TRUE)

# Equivalent linear model:
summary(lm(signed_rank(x1 - x2) ~ 1))
```

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# 9.9.3 Dummy variables

Let's take a quick detour before we explore the next tests. We'll need to understand the concept of dummy variables and contrasts first.

### 9.9.3.1 The matrices we use for linear regression

Recall that we can express our linear regression in matrix form:

$$\mathbf{y} = X\beta + \varepsilon$$

where

$$\mathbf{y} = \begin{pmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{pmatrix},$$
 
$$\beta = \begin{pmatrix} \beta_0 \\ \beta_1 \\ \beta_2 \\ \vdots \\ \beta_p \end{pmatrix}, \quad \varepsilon = \begin{pmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \vdots \\ \varepsilon_n \end{pmatrix}$$

and

$$X = \begin{pmatrix} \mathbf{x}_1^\mathsf{T} \\ \mathbf{x}_2^\mathsf{T} \\ \vdots \\ \mathbf{x}_n^\mathsf{T} \end{pmatrix} = \begin{pmatrix} 1 & x_{11} & \cdots & x_{1p} \\ 1 & x_{21} & \cdots & x_{2p} \\ \vdots & \vdots & \ddots & \vdots \\ 1 & x_{n1} & \cdots & x_{np} \end{pmatrix}$$

We often talk about X as the **model matrix** (or design or regressor matrix) and it will be the focus of this section.

### 9.9.3.2 Getting our model matrix in R

Let's start by fitting a model with body\_mass\_g as the response and flipper\_length\_mm and species as the predictor variables.

(Note: Users of statistics use a lot of different words to refer to the same thing. Can you think of other terms people might use instead of *response* and *predictor*?)

```
##
## Call:
## lm(formula = body_mass_g ~ flipper_length_mm + species, data = penguins)
##
## Residuals:
##
      Min
               1Q Median
                                3Q
## -927.70 -254.82 -23.92 241.16 1191.68
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    -4031.477
                                 584.151 -6.901 2.55e-11 ***
## flipper_length_mm
                       40.705
                                   3.071 13.255 < 2e-16 ***
## speciesChinstrap
                                  57.731 -3.577 0.000398 ***
                    -206.510
```

```
## speciesGentoo 266.810 95.264 2.801 0.005392 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 375.5 on 338 degrees of freedom
## (2 observations deleted due to missingness)
## Multiple R-squared: 0.7826, Adjusted R-squared: 0.7807
## F-statistic: 405.7 on 3 and 338 DF, p-value: < 2.2e-16</pre>
```

Now we can use the model.matrix() function to extract the model matrix for mod4. I've applied head() to stop the entire thing being printed.

##		(Intercept)	flipper_length_mm	${\tt speciesChinstrap}$	speciesGentoo
##	1	1	181	0	0
##	2	1	186	0	0
##	3	1	195	0	0
##	5	1	193	0	0
##	6	1	190	0	0
##	7	1	181	0	0
##	8	1	195	0	0
##	9	1	193	0	0
##	10	1	190	0	0
##	11	1	186	0	0
##	12	1	180	0	0
##	13	1	182	0	0
##	14	1	191	0	0
##	15	1	198	0	0
##	16	1	185	0	0
##	17	1	195	0	0
##	18	1	197	0	0
##	19	1	184	0	0
##	20	1	194	0	0
##	21	1	174	0	0

You'll notice that even though we only had an intercept and two variables, we have four columns in our model matrix. You should also notice that R has given the columns helpful names, and that we have a column for the Chinstrap species and the Gentoo species, but not the Adelie species.

Further, recall that when we are working with a categorical variables we call the different values the variables can take "levels". I may also refer to these as factor variables, and talk about the "levels of the factor".

What R is doing is dropping the first level (alphabetically) of the categorical variable and then creating **dummy** variables for each of the other levels.

The dropped level becomes our **reference level** and this should be familiar from interpreting summary output in previous courses where you have conducted multiple linear regressions with categorical variables.

A dummy variable is also called an indicator variable, and it *indicates* whether or not the given observation takes that level or not. I.e., if the 40th penguin in this dataset had a 1 in the speciesGentoo column, then I know it is a Gentoo penguin, and that it won't have a 1 in the speciesChinstrap column because each penguin can only have one species.

More generally, the sum across the row of the dummy variables for one categorical variable will either be 0 (if that observation has the reference level) or 1 (not the reference level) but you will never have more than one 'one' amongst the dummies for a given categorical variable.

9.9.3.2.0.1 [Unassessed aside] Why do we have to drop one of the levels? You may recall that for the matrix calculations required to get our vector of  $\beta$ s, we need to be able to invert X our matrix. We can only invert

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matrices for which all the columns are linearly independent and if we have the intercept AND dummies for all the levels of the categorical variable, our matrix will be linearly dependent.

Additional optional discussion here.

#### 9.9.4 Two means

Back to tests!

Independent t-tests let you compare two means. I am assuming you've seen this in a 200-level statistics course or equivalent. Brief recap below.

#### 9.9.4.1 Use case

You want to know if it is believable that two independent groups have the same population mean.

### 9.9.4.2 Assumptions

- 1. The data are continuous.
- 2. The data are normally distributed (in each group).
- 3. Each group is a simple random sample from its population. Each individual in the population has an equal probability of being selected in the sample
- 4. The variances for the groups are equal.

Notice that these are the same assumptions as the one-sample t-test, but with the equality of variances assumption added.

### 9.9.4.3 Hypotheses

$$H_0: \mu_1 = \mu_2$$

$$H_1: \mu_1 \neq \mu_2$$

What are we doing? Finding the strength of evidence against the claim that the population means for both groups are the same. This differs from the one sample test because we have uncertainty about BOTH values here. Both are population parameters that we don't know.

The test statistic, t, is calculated as follows:

$$t = \frac{\bar{x_1} - \bar{x_2}}{\sqrt{s^2(\frac{1}{n_1} + \frac{1}{n_2})}}$$

We then compare this t value to the t-distribution with degrees of freedom  $df = n_1 + n_2 - 2$  and find the area under the curve that represents the probability of values likes ours or more extreme.

### 9.9.4.4 Example

Conduct an independent t-test to test if the mean of <code>body\_mass\_g</code> is the same for male and female penguins (<code>sex</code>). Add your code below. Note: you must set , <code>var.equal = TRUE</code> as one of the arguments for it two be the independent t-test. If you don't set this we are conducting a <code>Welch's t-test</code>. I won't be covering this, but it is covered in the source credited at the end of this activity.

```
##
## Two Sample t-test
##
## data: body_mass_g by sex
## t = -8.5417, df = 331, p-value = 4.897e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -840.8014 -526.0222
## sample estimates:
## mean in group female mean in group male
## 3862.273 4545.685
```

Now, based on what we've learned, write a linear model using the lm() function to do the same this as our independent t-test. Save the model as mod5.

```
##
## Call:
## lm(formula = body_mass_g ~ sex, data = penguins)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -1295.7 -595.7 -237.3
                            737.7 1754.3
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 3862.27
                            56.83 67.963 < 2e-16 ***
                683.41
                            80.01
                                    8.542 4.9e-16 ***
## sexmale
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 730 on 331 degrees of freedom
  (11 observations deleted due to missingness)
## Multiple R-squared: 0.1806, Adjusted R-squared: 0.1781
## F-statistic: 72.96 on 1 and 331 DF, p-value: 4.897e-16
```

Take a moment to match up parts of the outputs that are the same. There is a difference here in that the sign of the test statistics differs. That does not matter as out t-distribution is symmetrical and we're doing a two-tailed test.

### 9.9.4.5 Mann-Whitney U

Similar idea to before, except for this test it is just rank not signed rank.

```
# Wilcoxon / Mann-Whitney U (multiple names)
wilcox.test(body_mass_g ~ sex, data = penguins)

##
## Wilcoxon rank sum test with continuity correction
##
## data: body_mass_g by sex
## W = 6874.5, p-value = 1.813e-15
## alternative hypothesis: true location shift is not equal to 0
```

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```
# As linear model with our dummy-coded group_y2:
summary(lm(rank(body_mass_g) ~ sex, data = penguins))
```

```
##
## Call:
## lm(formula = rank(body_mass_g) ~ sex, data = penguins)
##
## Residuals:
##
      Min
               10 Median
                               3Q
                                      Max
## -183.68 -74.13 -16.63
                            91.32 162.87
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 128.630
                            6.948 18.512
                                             <2e-16 ***
                86.051
                            9.783
                                    8.796
                                             <2e-16 ***
## sexmale
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 89.25 on 331 degrees of freedom
     (11 observations deleted due to missingness)
## Multiple R-squared: 0.1895, Adjusted R-squared: 0.187
## F-statistic: 77.37 on 1 and 331 DF, p-value: < 2.2e-16
```

### 9.9.5 ANOVA

#### 9.9.5.1 Use case

You've probably seen 'ANOVA' in the context of model comparison, but it is also a popular test in psychology and other disciplines.

Let's look specifically at one-way ANOVA (or the F-test). It tests if all the means for several groups (more than 2) are the same or if at least one is different.

I hope this sounds a bit like the next evolution from the independent t-test...

 $(+ 1000 \text{ stats respect points to anyone who draws Pokemon-esque evolutions of these three tests...with regression as the mega-evolution...)$ 

#### 9.9.5.2 Assumptions

And it just so happens that the assumptions for the one-way ANOVA (also called the F-test) are EXACTLY the same as for the independent t-test

There is a GIF in the web version. Not required content. https://gifst.blogspot.com/2019/03/snl-hi-saturday-night-live-hey-kate.html

- 1. The data are continuous.
- 2. The data are normally distributed (in each group).
- 3. Each group is a simple random sample from its population. Each individual in the population has an equal probability of being selected in the sample
- 4. The variances for the groups are equal.

### 9.9.5.3 Hypotheses

$$H_0: \mu_1 = \mu_2 = \dots = \mu_k$$

 $H_1$ : at least one  $\mu$  differs from the others

#### 9.9.5.4 Example

Let's now look at body mass across species. Suppose we wanted to know if was believable that the means body mass in grams was the same across all three species. This is when we could fit a quick ANOVA to test this. The aov() allows us to do this.

That looks a lot like the output from calling summary on lm()...in fact, aov is just a wrapper for lm! Which means it has been linear regression the whole time.

### 9.9.5.5 We'll stop here and talk further about this particular topic in class this week.

Your next topic is reproducible examples (reprexes).

### 9.9.6 Credits

Credit to Jonas Kristoffer Lindeløv for the excellent resource this resource is based on. There are more examples there than we will cover in this course.

# Appendix

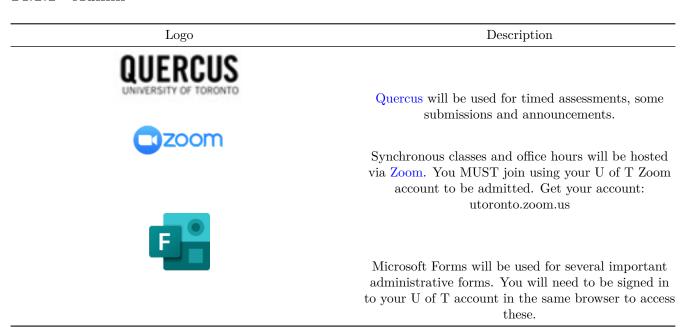
# Resources

### 14.1 Course tools overview

While we've tried to keep things as streamlined as possible, there are still several different tools we'll be using this semester. Your U of T login should work with all of them. The below PDF file provides an overview of how you'll be interacting with each one.

- At the bottom of the page is an embedded slideshow introducing you to the JupyterHub.
- You can always access Piazza from the Navigation Menu on the left.
- Instructions for setting up your U of T Zoom are on the Zoom page and links are in the Navigation menu and on the home page.

#### 14.1.1 Admin



# 14.2 Using RStudio with the JupyterHub

We will be using R through RStudio to conduct analyses in this course. If you have a local installation of R you are welcome to continue using that, but, for this course, you do not need to have R and RStudio installed.

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Instead, assessments and activities will be shared through the U of T JupyterHub. This gives you access to RStudio in your browser through your U of T login on any internet-connected device. It means you don't have to fight package installations and we can instead focus on the good stuff.

Please read through the following slides, experiment with the example sharing link, make sure you know how to knit an Rmd to pdf + export the pdf, and practice navigating and moving files.

Link: https://rstudio-with-jupyerhub-uoft.netlify.app.

# 14.3 Zoom, Zoom, Zoom, Zoom...

Access to STA303 synchronous meetings and office hours is restricted to our students.

Set up your U of T Zoom account

# 14.3.1 Make sure your Zoom is up to date

To participate fully, you will need Desktop client or mobile app: version 5.3.0 or higher. You can check your desktop client or mobile app version by following these instructions.

#### 14.3.2 Customize!

Once you have logged in, please customize your profile:

- Update your name to your **preferred name** (what you would like us to call you in class) Note: this may not be allowed with your U of T settings, so don't worry if this doesn't work.
- Add a **profile picture** (please make it a photo of YOU or an avatar that looks like you...we don't want Snoopy or Joe Biden<sup>1</sup> in class)

### 14.3.3 VPN

There is a University of Toronto VPN (UTORvpn) that you have access to as a student. It may help with video quality and access to U of T resources.

If you are based in mainland China, the Alibaba Cloud Enterprise Network (CEN)Links to an external site. service should help with your Quercus access.

### 14.3.4 Notes:

- 1. Please always use your real name and face for this course, and be cautious about changing them and your virtual background for other meetings. A joke background for a call with family or friends may not be appropriate for class.
- 2. For class meetings, the settings will always be that your camera and microphone are off to begin with so you have the control to check these things first.
- 3. We do ask that, when possible, you use your microphone in office hours, breakout groups and any other small group meetings and strongly prefer that you use your camera AND microphone. We trust you to make the best choice for your environment, comfort and learning.
- 4. You may get a "This meeting is for authorized participants only message". Choose the "Sign in with SSO" option to sign in.

<sup>&</sup>lt;sup>1</sup>Yes, these are real images students have used.

## 14.3.5 Changing your profile picture on Zoom and Quercus

Follow these instructions to add a profile picture (or bitmoji style avatar if you'd prefer) to Quercus and Zoom. I want this experience to be more social and less faceless. Please don't use photos of cartoon characters, etc. A good photo will be a close-up of your face so we can see who you are even when the photo is small.

## 14.3.6 What to do if you experience technical difficulties during class?

First, (if possible) send me a chat note that you're having technical difficulties and are working to resolve them.

**Second**, leave the meeting and re-enter. This often resets things and resolves the problem. Before entering the meeting, make sure all of your devices are properly plugged in and Bluetooth devices are connected.

If that doesn't fix things, exit the meeting again and update your Zoom Client. This is the Zoom software that should be on your computer. Here's a short video tutorial explaining how to update the software: <a href="https://www.youtube.com/watch?v=E7zERcVLUBM">https://www.youtube.com/watch?v=E7zERcVLUBM</a>.

After updating, enter the meeting again to see if this resolved your problems.

Our synchronous classes are recorded, so if your technology is just going catastrophically wrong, go get a cup of tea/coffee/water and relax, you can catch up with the recording when it is posted on Quercus.

# 14.3.7 What to do if your instructor or TA is experiencing technical difficulties on Zoom

**First**, check the **chat** to see if the instructor or the project mentor have said what is going on and what they are doing to fix things and follow any instructions they give.

**Second**, if they have disappeared completely, wait 10 minutes (or until the end of the meeting time, whichever comes first) before closing the call. (You can do other things in the meantime, but be ready to jump back in).

**Third**, expect to see an announcement on Quercus afterwards telling you what to do (e.g. it might be to watch a video I'll record later, to review some slides or perhaps there is nothing to do and i'll see you next time).

# 14.4 Student support services and resources

# 14.4.1 Mental health support

You may find yourself feeling overwhelmed, depressed, or anxious. Lots of people feel the same way. There is help available from mental health professionals 24 hours a day via online and phone-based services. Here are some that are available to U of T students:

- MySSP My Student Support Program 1-844-451-9700, or outside of Canada call 001-416-380-6578
- Good2Talk Student Helpline 1-866-925-5454, or text GOOD2TALK to 686868
- Distress Centres of Greater Toronto 416-408-4357, or text 45645

There is also the new Navi tool for U of T students, it is a chatbot and your questions are totally anonymous. http://uoft.me/navi

The student union are also curating a list here: https://www.utsu.ca/mental-health/

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# 14.4.2 General University resources

The following are some important links to help you with academic and/or technical service and support:

- Health & Wellness can help with appointments with a range of clinicians, nutrition, immunizations, sexual and reproductive health and much more. Many of their services continue to be available online.
- Arts & Sciences student resources through Sidney Smith Commons Online
- General student services and resources at Student Life
  - Tips for dealing with multi-choice questions (MCQs)
  - Book an appointment with a learning strategist (they can help you with strategies for MCQs also)
- Full library service through the University of Toronto Libraries
- Resources on academic support from the Academic Success Centre
- Learner support at the Writing Centre
- Information about Accessibility Services
- Quercus Information in the Canvas Student Guide
- Logistical and social support for international students at the Center for International Experience

Visit the A&S online resources for students page for resources available to support you through your online studies. If you have further questions, please email ask.artsci@utoronto.ca.

# 14.4.3 Financial support

A list of University financial supports, work-study opportunities, as well as provincial and federal government programs is available on the University's Financial Support & Funding Opportunity directory.

### 14.4.4 Arts & Science COVID19 FAQ

The Arts & Science Undergraduate FAQ page addresses frequently asked questions that are specific to undergraduate students taking courses with the Faculty of Arts & Science. On this page you will find information for:

Messages from Dean Woodin can be found on the A&S latest updates page.

# FAQs and Errata

# 15.1 Frequently asked questions

While Piazza is our main class question and answer board, this page will have some static Questions and Answers for frequently asked questions. Use Cmd + F (Mac) or Ctrl + F (PC) to search for keywords on this page.

Additionally, make sure you're familiar with the Syllabus. I've tried to explain as much as I could there.

### 15.1.1 Course admin

### 15.1.1.1 STA303 pre-requisites

I didn't take STA302 or an equivalent course, can I still take STA303?

No, sorry. We enforce pre-reqs strictly. This isn't up to me. You will be removed from the course. Please reach out to the UG stats team (ug.statistics@utoronto.ca) about questions of this nature.

- Book an appointment during their office hours.
- For grad courses, please email grad.statistics@utoronto.ca.

### 15.1.1.2 Recorded lectures

Where can I find recorded lectures and how soon can I expect them to be available?

Recorded lectures will be linked on the Course overview page. I aim to have the links up within 24 hours of class. They take some time to process.

#### 15.1.1.3 Sections

Do L0101 and L0201 cover the same materials?

Yes. The only difference is when your synchronous class is. See the below question in "Attending synchronous class".

### 15.1.1.4 Attending synchronous class

Can I attend the synchronous class for the other section?

Yes!\*

\*If the number of attendees is getting too close to the call cap of 300 (this is a Zoom license thing), preference will be given to those enrolled in the session and others will be asked to leave. Any Team Up! activity bonuses will also be applied-section/session does not matter.

Why can't I access the class/office hour Zoom meeting?

You must have and be signed in with your University of Toronto Zoom account. Use the 'SSO' (single sign-on) option.

"Will STA303/STA1002 be able to be completed online-only?" Yes.

- STA303 will be a flipped course, with content delivered online and opportunities for activities both in-person (subject to health advice) and online. All assessments will be completed and submitted online.
- If you are enrolled in an **in-person tutorial**, you will have an option to attend online instead.
- Synchronous attendance is NOT required to pass this course, but being able to attend (online) synchronously at the times in the timetable may make things easier for you.

"Where is your office?"/"Can I come see you in-person?" At this stage, I cannot offer in-person office hours nor student meetings in my office. Drop-ins are not currently allowed for any instructors or TAs in Statistical Sciences, unless they have told you they have organized another meeting space for this purpose.

## 15.1.2 Team Up!

### 15.1.2.1 Troubleshooting & FAQ advice from U of T CTSI

My screen seems to be lagging compared to those of my group members (eg. I'm not on the same question as the driver/members, the answer I chose does not appear on my group members' screens, etc.)

As long as you are logged in, you will receive your grade, so just continue to participate by communicating with your team. Almost always, your device will re-sync with the rest of your team's devices within a minute or two. If not, refresh your screen once. Repeatedly refreshing is not usually helpful!

I've been disconnected. Will my quiz progress be saved? Can I re-join my group?

Enter the Team Up! session again and you will automatically be put back into your group. Your progress will be saved, and you will return to the question you or your group was working on. This is true for the Driver as well as any team member.

How do I send my completed quiz results?

Click the large red "Submit to Quercus" button at the end of the Team Up! quiz.

Can we change our group driver?

You can request a driver change by pressing the red exclamation mark in the top right of your Team Up! quiz.

How is the driver for our group chosen, and how can the driver pass the group ID to others in remote classes?

Group members can decide who will be the Driver (ideally someone with a good internet connection). The Driver can pass the group ID to other members verbally through chat or microphone in breakout rooms.

The Driver of my group has to leave unexpectedly or their device has stopped functioning. How do we proceed with the auiz?

Request for a Driver Change using the red button at the top right of your Team Up! Session. This button only provides help for Driver Changes. You may also need to speak with your instructor or TA.

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# 15.2 Other

### 15.2.1 References

Can you (Prof. Bolton) write me a reference? I'm desperate!

Please read my personal policy here to get a sense of under what circumstances I could write for you, but basically, a good mark in one class is not sufficient and you need to have at least two 'activities' with me. If you believe you meet my basic criteria, you can request a reference from me here. I will then accept or decline based on the the information provided.

Do you (Prof. Bolton) have any research opportunities available?

### Research/work study/teaching assistant opportunities:

- See the Department website. The main round of TA recruitment occurs during the summer but there are occasionally emergency postings.
- Some information about opportunities with me on my website.
- Reading courses: STA496/497: Readings in Statistics must be registered for as part of special enrolment during July. I will not be taking on any further students.
  - If you're thinking about the future, I usually consider taking on a small number of STA497 students for a half-credit, year long version.
  - There is much more information about my past students, research interests and what a course with me might be like on my website: <a href="https://www.lizabolton.com/reading">https://www.lizabolton.com/reading</a> courses.html>.

# 15.3 Errata

ID	Location	Note

# Bits and pieces

# 16.1 Code to generate course art

```
# install.packages('readr')
# install.packages('tidyverse')
# install.packages("devtools")
# devtools::install_github("BlakeRMills/MetBrewer")
library(readr)
library(MetBrewer)
library(tidyverse)
course_code <- "STA303"
my_colours <- c(met.brewer("Cross", n = 8), met.brewer("Cross", n = 9))</pre>
set.seed(parse_number(course_code))
ngroup=17
names=paste("G_",seq(1,ngroup),sep="")
DAT=data.frame()
for(i in seq(1:30)){
  data=data.frame( matrix(0, ngroup , 3))
  data[,1]=i
  data[,2]=sample(names, nrow(data))
  data[,3]=prop.table(sample( c(rep(0,100),c(1:ngroup)) ,nrow(data)))
  DAT=rbind(DAT,data)
colnames(DAT)=c("Year", "Group", "Value")
DAT=DAT[order( DAT$Year, DAT$Group) , ]
ggplot(DAT, aes(x=Year, y=rev(Value), fill=Group )) +
  geom_area(alpha=1 )+
  theme_bw() +
  scale_fill_manual(values = my_colours)+
    text = element_blank(),
    line = element_blank(),
    title = element_blank(),
    legend.position="none",
```

```
panel.border = element_blank(),
  panel.background = element_blank(),
  plot.margin = margin(0, -2.7, 0, -2.7, "cm"))

ggsave(paste0(course_code, "-base.png"), width = 24, height = 2)
```

# 16.2 M1 supporting information on matrices (not assessed)

## 16.2.1 Background

### 16.2.1.1 Some true things about matrices

- The rank of a matrix is the number of linearly independent columns your matrix has.
- If the number of columns = the rank of the matrix all the columns are **linearly independent**. If the umber of columns is > the rank of the matrix, all the columns are *not* linearly independent.
- You can only **invert** a square matrix if all its columns are linearly independent. (Determinant non-zero).

Why do we care? In linear regression, to estimate  $\beta$ , our vector of coefficients, we calculate  $(X^TX)^{-1}X^TY$ . The elements of  $\beta$  can't be estimated if  $X^TX$  (a square matrix) isn't invertible.

Clarification to what I said in the tests activity: We usually perform regression with an intercept because we don't want to assume out line passes through the origin,  $\mathbf{0}$ . So, if there is an intercept, (column of 1s in the model matrix) we must convert every categorical variable with k levels into k-1 dummy variables to have the intercept and still satisfies linear independence. IF we ditch the intercept, we can have k dummies, but this is only usually useful in the specific case of ANOVA.

## 16.2.2 Example

```
## # A tibble: 12 x 2
##
  # Groups:
                species [3]
##
      body_mass_g species
##
            <int> <fct>
   1
              3900 Adelie
##
   2
              3700 Adelie
##
##
    3
              3450 Adelie
##
   4
              3175 Adelie
##
   5
              4500 Chinstrap
##
    6
              3850 Chinstrap
    7
##
              3650 Chinstrap
##
   8
              4550 Chinstrap
##
   9
              5150 Gentoo
## 10
              5000 Gentoo
##
              5700 Gentoo
  11
## 12
              4600 Gentoo
```

## # A tibble: 12 x 4

##		body_mass_g	species.Adelie	species.Chinstrap	species.Gentoo
##		<int></int>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
##	1	3900	1	0	0
##	2	3700	1	0	0
##	3	3450	1	0	0
##	4	3175	1	0	0
##	5	4500	0	1	0
##	6	3850	0	1	0

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##	7	3650	0	1	0
##	8	4550	0	1	0
##	9	5150	0	0	1
##	10	5000	0	0	1
##	11	5700	0	0	1
##	12	4600	0	0	1

#### 16.2.2.1 Classic regression, k-1 dummies (intercept)

```
##
## Call:
## lm(formula = body_mass_g ~ species, data = pengwings)
##
## Residuals:
##
      Min
               1Q Median
                                3Q
                                       Max
## -512.50 -310.94 -34.37 348.44 587.50
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
                                  206.8 17.199 3.42e-08 ***
## (Intercept)
                      3556.3
## speciesChinstrap
                      581.2
                                  292.4
                                          1.988 0.07809 .
                      1556.2
                                  292.4
## speciesGentoo
                                          5.322 0.00048 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 413.6 on 9 degrees of freedom
## Multiple R-squared: 0.7627, Adjusted R-squared:
## F-statistic: 14.46 on 2 and 9 DF, p-value: 0.001545
##
     (Intercept) speciesChinstrap speciesGentoo
## 1
               1
## 2
                                              0
                                0
               1
## 3
               1
                                0
                                              0
                                              0
## 4
               1
                                0
## 5
               1
                                1
                                              0
                                              0
## 6
               1
                                1
```

Does the rank of the model matrix equal the number of columns?

#### ## [1] TRUE

Okay, linearly independent, we're good to go!

### 16.2.2.2 Classic regression but trying to force k dummies (with an intercept)

```
##
## Call:
## lm(formula = body_mass_g ~ species.Adelie + species.Gentoo +
## species.Chinstrap, data = wider)
##
## Residuals:
## Min 1Q Median 3Q Max
## -512.50 -310.94 -34.38 348.44 587.50
##
```

```
## Coefficients: (1 not defined because of singularities)
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       4137.5
                                    206.8 20.010 9.04e-09 ***
                                    292.4 -1.988 0.07809 .
## species.Adelie
                       -581.2
                        975.0
## species.Gentoo
                                    292.4
                                            3.334 0.00874 **
## species.Chinstrap
                           NA
                                       NA
                                               NA
                                                         NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 413.6 on 9 degrees of freedom
## Multiple R-squared: 0.7627, Adjusted R-squared:
## F-statistic: 14.46 on 2 and 9 DF, p-value: 0.001545
##
      (Intercept) species.Adelie species.Gentoo species.Chinstrap
## 1
                1
                                1
                                               0
                                                                  0
## 2
                1
                                1
                                               0
                                                                  0
## 3
                1
                                1
                                               0
                                                                  0
## 4
                1
                                               0
                                                                  0
                                1
## 5
                1
                                0
                                               0
                                                                  1
## 6
                                0
                                               0
                1
                                                                  1
## 7
                1
                                0
                                               0
                                                                  1
## 8
                1
                                0
                                               Ω
                                                                  1
## 9
                                0
                                                                  0
                1
                                               1
## 10
                                0
                                                                  0
                1
                                               1
## 11
                1
                                0
                                               1
                                                                  0
                                0
                                                                  0
## 12
                                               1
                1
## attr(,"assign")
## [1] 0 1 2 3
## [1] 3
```

Does the rank of the model matrix equal the number of columns?

#### ## [1] FALSE

Not linearly independent. Why?

Well, this intercept column is a linear combination of the three species columns!

# 16.2.3 Regression NOT classic, actually ANOVA! (no intercept)

```
##
## Call:
## lm(formula = body_mass_g ~ 0 + species.Adelie + species.Gentoo +
##
       species.Chinstrap, data = wider)
##
## Residuals:
                1Q Median
##
      Min
                                3Q
                                       Max
## -512.50 -310.94 -34.38 348.44 587.50
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
```

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```
## species.Adelie
                                     206.8
                                             17.20 3.42e-08 ***
                        3556.2
## species.Gentoo
                        5112.5
                                     206.8
                                             24.73 1.39e-09 ***
## species.Chinstrap
                        4137.5
                                     206.8
                                             20.01 9.04e-09 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 413.6 on 9 degrees of freedom
## Multiple R-squared: 0.9932, Adjusted R-squared: 0.9909
## F-statistic: 435.8 on 3 and 9 DF, p-value: 4.659e-10
##
      species.Adelie species.Gentoo species.Chinstrap
## 1
                                                       0
##
  2
                    1
                                    0
                                                       0
## 3
                                    0
                                                       0
                    1
## 4
                    1
                                    0
                                                       0
## 5
                    0
                                    0
                                                       1
## 6
                    0
                                    0
                                                       1
## 7
                    0
                                    0
                                                       1
## 8
                    0
                                    0
                                                       1
                                                       0
## 9
                    0
                                    1
## 10
                    0
                                    1
                                                       0
## 11
                    0
                                                       0
                                    1
## 12
                    0
                                    1
                                                       0
## attr(,"assign")
## [1] 1 2 3
```

## [1] 3

Challenge question for +100 stats respect points: How do you interpret these coefficients?

Does the rank of the model matrix equal the number of columns?

```
## [1] TRUE
```

Great, back to being linearly independent.

# 16.2.4 Further reading (if you want it)

As I said at the beginning, I'm not planning to assess you on any of this. If you're interested in knowing more, or just think matrix algebra is delicious, I think this is a delightfully approachable walk through.  $\frac{1}{100} \frac{1}{100} \frac{1}{100}$