

Convergence of the MLE

Some more theorems about convergence

Continuous mapping theorem:

Slutsky's theorem:

Convergence of the MLE

Intermediate steps

Using results we have previously derived, argue that:

$$+ \quad \frac{1}{n} \ell_n''(\theta) \xrightarrow{p} -\mathcal{I}_1(\theta)$$

$$+ \quad \frac{1}{\sqrt{n}} \ell_n'(\theta) \xrightarrow{d} N(0, \mathcal{I}_1(\theta))$$

Regularity conditions