

# Sufficiency and minimal sufficiency

# Where we are and where we're going

## Recap: factorization theorem

## Example

Suppose  $X_1, \dots, X_n \stackrel{iid}{\sim} N(\mu, \sigma^2)$  with  $\mu$  and  $\sigma^2$  unknown. Let  $\theta = (\mu, \sigma^2)$ .

Use the factorization theorem to find a sufficient statistic for  $\theta$ .  
(The dimension of the statistic will be greater than 1).

# Sufficient statistics as partitions

# Minimal sufficient statistics