# **Comparing estimators**

## **Example**

Suppose  $X_1, \ldots, X_n \stackrel{iid}{\sim} Uniform[0, \theta]$ . Some possible estimates:

What properties might I want an estimator  $\hat{\theta}$  to possess?

# Bias, Variance and MSE

#### **Example**

Suppose  $X_1,\ldots,X_n\stackrel{iid}{\sim}N(\mu,\sigma^2)$ . Previously, we considered

$$\widehat{\sigma}^2 = rac{1}{n} \sum_{i=1}^n (X_i - \overline{X})^2 \hspace{0.5cm} s^2 = rac{1}{n-1} \sum_{i=1}^n (X_i - \overline{X})^2$$

and we showed that  $\mathbb{E}\widehat{\sigma}^2=rac{n-1}{n}\sigma^2$ ,  $\mathbb{E}(s^2)=\sigma^2$ , and  $rac{(n-1)s^2}{\sigma^2}\sim\chi^2_{n-1}$ .

Calculate the MSE of both  $\widehat{\sigma}^2$  and  $s^2$ .

### **Best unbiased estimators**