Lecture 16: Asymptotic normality of the MLE

Convergence of the MLE

Intermediate steps

Using the WLLN and the CLT, argue that:

•
$$\frac{1}{n} \ell_n''(\theta) \stackrel{p}{\longrightarrow} -I_1(\theta)$$

•
$$\frac{1}{\sqrt{n}} \ell'_n(\theta) \stackrel{d}{\longrightarrow} N(0, I_1(\theta))$$

Putting everything together

Regularity conditions