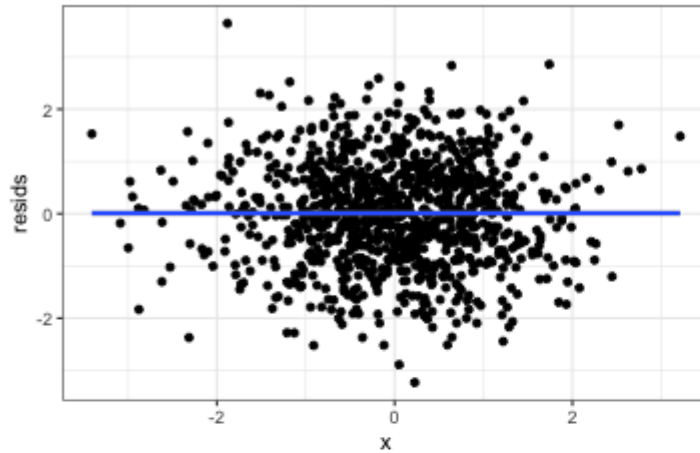


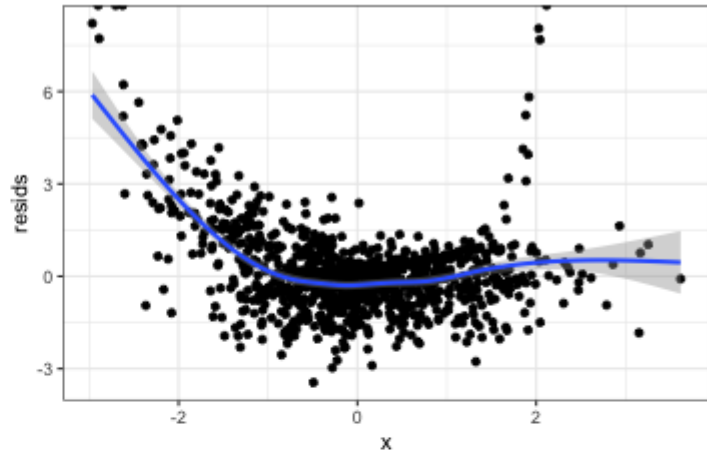
ZIP models

Recap: Assessing the shape assumption

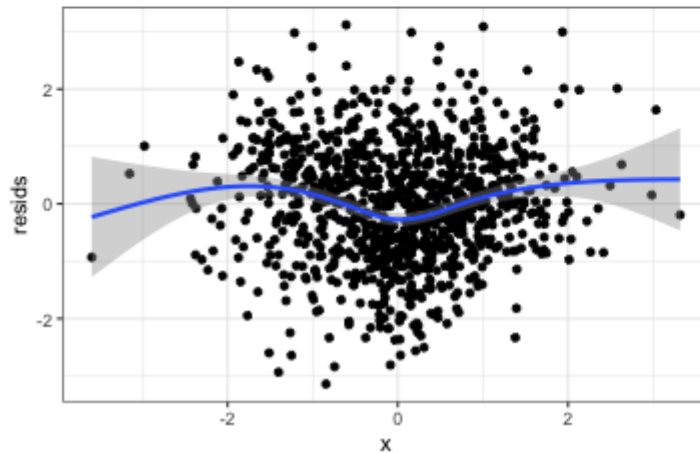
All assumptions satisfied



Poisson shape assumption violated



Logistic shape assumption violated



Logistic component vs. Poisson component

Class activity

https://sta712-f22.github.io/class_activities/ca_lecture_33.html

Class activity

$$\log\left(\frac{\alpha_i}{1 - \alpha_i}\right) = \gamma_0 + \gamma_1 \textit{EducationSome}_i + \gamma_2 \textit{EducationCollege}_i + \gamma_3 \textit{EducationAdv}_i + \gamma_4 \textit{Diabetes}_i + \gamma_5 \textit{Age}_i$$

$$\log(\lambda_i) = \beta_0 + \beta_1 \textit{EducationSome}_i + \beta_2 \textit{EducationCollege}_i + \beta_3 \textit{EducationAdv}_i + \beta_4 \textit{Diabetes}_i + \beta_5 \textit{Age}_i$$

Research question: for smokers, does the number of cigarettes smoked per day depend on age?

What are the null and alternative hypotheses?

Class activity

$$\log\left(\frac{\alpha_i}{1 - \alpha_i}\right) = \gamma_0 + \gamma_1 \textit{EducationSome}_i + \gamma_2 \textit{EducationCollege}_i + \gamma_3 \textit{EducationAdv}_i + \gamma_4 \textit{Diabetes}_i + \gamma_5 \textit{Age}_i$$

$$\log(\lambda_i) = \beta_0 + \beta_1 \textit{EducationSome}_i + \beta_2 \textit{EducationCollege}_i + \beta_3 \textit{EducationAdv}_i + \beta_4 \textit{Diabetes}_i + \beta_5 \textit{Age}_i$$

Research question: is there a relationship between age and whether someone is a smoker?

What are the null and alternative hypotheses?

Wald tests

Research question: is there a relationship between age and whether someone is a smoker?

```
m1 <- zeroinfl(cigsPerDay ~ education + diabetes +  
               age | education + diabetes + age,  
               data = heart_data)  
summary(m1)
```

```
...  
## Zero-inflation model coefficients (binomial with logit link):  
##           Estimate Std. Error z value Pr(>|z|)  
## (Intercept) -2.49673    0.20977 -11.902  <2e-16 ***  
## education2  -0.06100    0.07840  -0.778    0.4366  
## education3   0.17141    0.09362   1.831    0.0671 .  
## education4   0.03547    0.10749   0.330    0.7414  
## diabetes     0.26063    0.20854   1.250    0.2114  
## age          0.05071    0.00395  12.838  <2e-16 ***  
...
```

Class activity

$$\log\left(\frac{\alpha_i}{1 - \alpha_i}\right) = \gamma_0 + \gamma_1 \textit{EducationSome}_i + \gamma_2 \textit{EducationCollege}_i + \gamma_3 \textit{EducationAdv}_i + \gamma_4 \textit{Diabetes}_i + \gamma_5 \textit{Age}_i$$

$$\log(\lambda_i) = \beta_0 + \beta_1 \textit{EducationSome}_i + \beta_2 \textit{EducationCollege}_i + \beta_3 \textit{EducationAdv}_i + \beta_4 \textit{Diabetes}_i + \beta_5 \textit{Age}_i$$

Research question: Is there a relationship between education level and the number of cigarettes smoked?

What are the null and alternative hypotheses?

Likelihood ratio test

```
m1 <- zeroinfl(cigsPerDay ~ education + diabetes +  
              age | education + diabetes + age,  
              data = heart_data)  
m2 <- zeroinfl(cigsPerDay ~ education + diabetes  
              | education + diabetes,  
              data = heart_data)
```

```
2*(m1$loglik - m2$loglik)
```

```
## [1] 242.281
```

```
pchisq(242.281, df=6, lower.tail=F)
```

```
## [1] 1.828386e-49
```