

Negative binomial regression

Recap: negative binomial regression

$$Y_i \sim NB(r, p_i)$$

$$\log(\mu_i) = \beta^T X_i$$

- + $\mu_i = \frac{p_i r}{1 - p_i}$
- + Note that r is the same for all i
- + Note that just like in Poisson regression, we model the average count
 - + Interpretation of β s is the same as in Poisson regression

In R

```
library(MASS)
```

```
m2 <- glm.nb(cigsPerDay ~ male + age + education +  
              diabetes + BMI, data = smokers)
```

```
...
```

```
##           Estimate Std. Error z value Pr(>|z|)  
## (Intercept)  2.877771    0.123477  23.306 < 2e-16 ***  
## male        0.459148    0.027641  16.611 < 2e-16 ***  
## age        -0.007010    0.001731  -4.050 5.12e-05 ***  
## education2  0.024518    0.032534   0.754  0.451  
## education3  0.009252    0.040802   0.227  0.821  
## education4 -0.027732    0.044825  -0.619  0.536  
##  
## (Dispersion parameter for Negative Binomial(3.2981) fami  
...
```

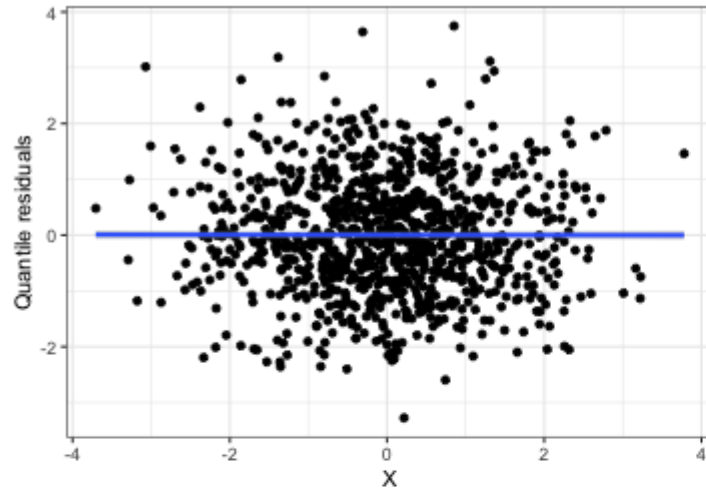
$$\hat{r} = 3.3$$

Class activity

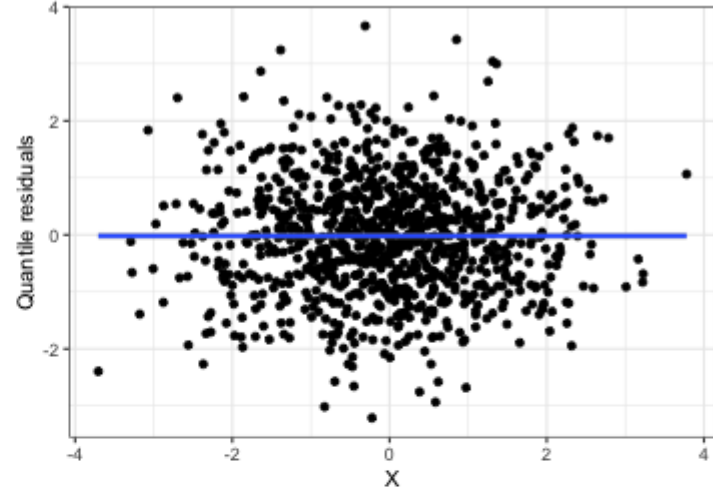
https://sta712-f22.github.io/class_activities/ca_lecture_27.html

Class activity

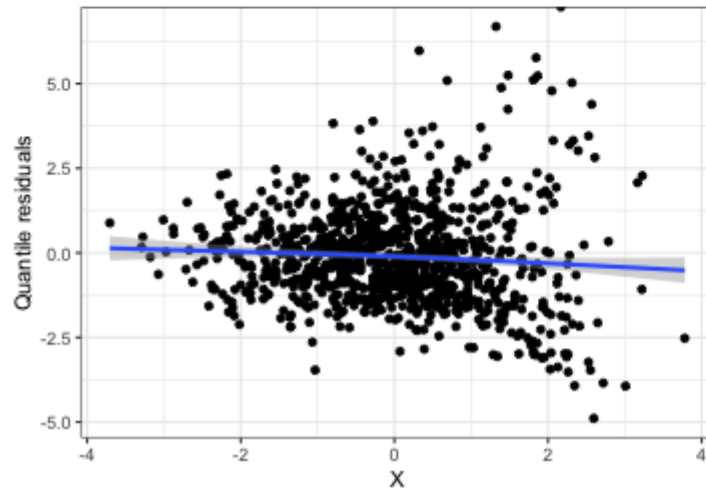
Poisson regression on Poisson data



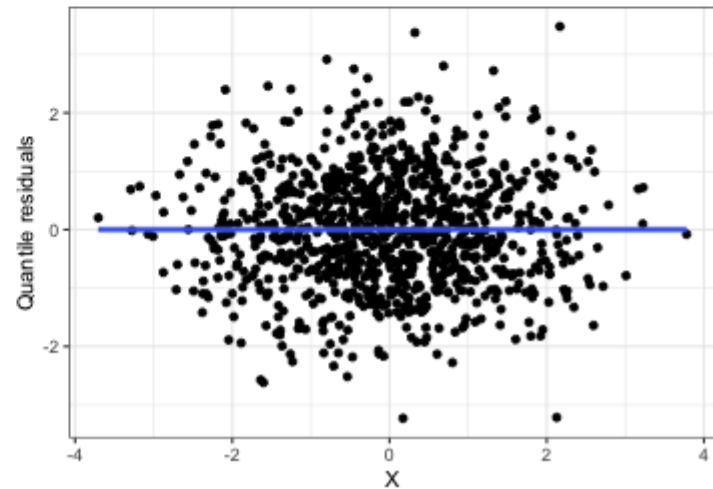
Negative binomial regression on Poisson data



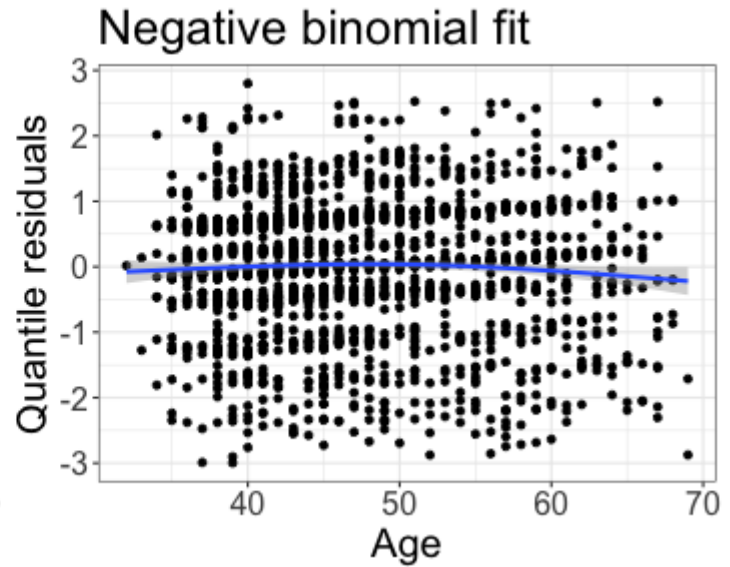
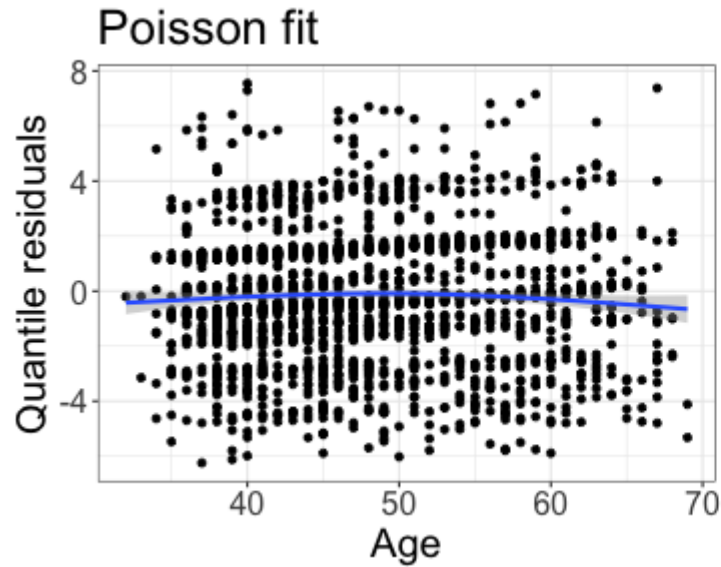
Poisson regression on negative binomial data



Negative binomial regression on negative binomial data



Poisson vs. negative binomial fits



Inference with negative binomial models

```
...  
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## male        0.459148    0.027641  16.611  < 2e-16 ***  
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## education4 -0.027732    0.044825  -0.619    0.536  
## diabetes   -0.010124    0.099126  -0.102    0.919  
## BMI        0.003693    0.003573   1.033    0.301  
...
```

How would I test whether there is a relationship between age and the number of cigarettes smoked, after accounting for other variables?

Inference with negative binomial models

```
...  
##           Estimate Std. Error z value Pr(>|z|)  
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## diabetes   -0.010124    0.099126  -0.102  0.919  
## BMI        0.003693    0.003573   1.033  0.301  
...
```

How would I test whether there is a relationship between education and the number of cigarettes smoked, after accounting for other variables?

Likelihood ratio test

```
m2 <- glm.nb(cigsPerDay ~ male + age + education +  
              diabetes + BMI, data = smokers)  
m3 <- glm.nb(cigsPerDay ~ male + age +  
              diabetes + BMI, data = smokers)  
m2$twologlik - m3$twologlik
```

```
## [1] 1.423055
```

```
pchisq(1.423, df=3, lower.tail=F)
```

```
## [1] 0.7001524
```