

Wald tests and likelihood ratio tests

Wald tests for multiple parameters

Class activity

https://sta712-f22.github.io/class_activities/ca_lecture_11.html

- + Wald tests for the dengue data

Likelihood ratio tests

```
m1 <- glm(Dengue ~ WBC + PLT, data = dengue,  
          family = binomial)  
summary(m1)
```

```
...  
##              Estimate Std. Error z value Pr(>|z|)  
## (Intercept)  2.6415063  0.1213233   21.77  <2e-16 ***  
## WBC          -0.2892904  0.0134349  -21.53  <2e-16 ***  
## PLT          -0.0065615  0.0005932  -11.06  <2e-16 ***  
## ---  
##      Null deviance: 6955.8  on 5719  degrees of freedom  
## Residual deviance: 5399.7  on 5717  degrees of freedom  
## AIC: 5405.7  
...
```

What information replaces R^2 and R^2_{adj} in the GLM output?

Deviance

Definition: The *deviance* of a fitted model with parameter estimates $\hat{\beta}$ is given by

$$2\ell(\text{saturated model}) - 2\ell(\hat{\beta})$$

Comparing deviances

```
m1 <- glm(Dengue ~ WBC + PLT, data = dengue,  
          family = binomial)  
summary(m1)
```

...

```
##      Null deviance: 6955.8    on 5719  degrees of freedom
```

```
## Residual deviance: 5399.7    on 5717  degrees of freedom
```

```
## AIC: 5405.7
```

...

Comparing deviances

Full model: $\log\left(\frac{p_i}{1 - p_i}\right) = \beta_0 + \beta_1 WBC_i + \beta_2 PLT_i$

Reduced model: $\log\left(\frac{p_i}{1 - p_i}\right) = \beta_0$

$$G = 2\ell(\hat{\beta}) - 2\ell(\hat{\beta}^0)$$

Why is G always ≥ 0 ?

Comparing deviances

Full model: $\log\left(\frac{p_i}{1 - p_i}\right) = \beta_0 + \beta_1 WBC_i + \beta_2 PLT_i$

Reduced model: $\log\left(\frac{p_i}{1 - p_i}\right) = \beta_0$

$$G = 2\ell(\hat{\beta}) - 2\ell(\hat{\beta}^0) = 1556.1$$

If the reduced model is correct, how unusual is $G = 1556.1$?

Likelihood ratio test