

# Package ‘clustMixType’

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**Title** k-Prototypes Clustering for Mixed Variable-Type Data

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**Imports** RColorBrewer

**Suggests** testthat

**Description** Functions to perform k-prototypes partitioning clustering for mixed variable-type data according to Z.Huang (1998): Extensions to the k-Means Algorithm for Clustering Large Data Sets with Categorical Variables, Data Mining and Knowledge Discovery 2, 283-304, <DOI:10.1023/A:1009769707641>.

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cindex\_kproto

*Validating k Prototypes Clustering: Cindex***Description**

Calculating the Cindex for a k-Prototypes clustering with k clusters or computing the optimal number of clusters based on the Cindex for k-Prototype clustering.

**Usage**

```
cindex_kproto(object = NULL, data = NULL, k = NULL, S_sort = NULL,
...)
```

**Arguments**

object	Object of class kproto resulting from a call with kproto(..., keep.data=TRUE)
data	Original data; only required if object == NULL.
k	Vector specifying the search range for optimum number of clusters; if NULL the range will set as 2:sqrt(n). Only required if object == NULL.
S_sort	for internal purposes only
...	Further arguments passed to <a href="#">kproto</a> , like: <ul style="list-style-type: none"> <li>• nstart: If &gt; 1 repetitive computations of kproto with random initializations are computed.</li> <li>• lambda: Factor to trade off between Euclidean distance of numeric variables and simple matching coefficient between categorical variables.</li> <li>• verbose: Logical whether information about the cluster procedure should be given. Caution: If verbose=FALSE, the reduction of the number of clusters is not mentioned.</li> </ul>

**Details**

$$Cindex = \frac{S_w - S_{min}}{S_{max} - S_{min}}$$

For  $S_{min}$  and  $S_{max}$  it is necessary to calculate the distances between all pairs of points in the entire data set ( $\frac{n(n-1)}{2}$ ).  $S_{min}$  is the sum of the "total number of pairs of objects belonging to the same cluster" smallest distances and  $S_{max}$  is the sum of the "total number of pairs of objects belonging to the same cluster" largest distances.  $S_w$  is the sum of the within-cluster distances.

The minimum value of the index is used to indicate the optimal number of clusters.

**Value**

For computing the optimal number of clusters based on the Cindex for k-Prototype clustering the output contains:

k_opt	optimal number of clusters
indices	calculated indices for $k = 2, \dots, k_{max}$

For computing the Cindex-value for a given k-Prototype clustering the output contains:

index	calculated index-value
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**Author(s)**

Rabea Aschenbruck

**References**

- Charrad, M., Ghazzali, N., Boiteau, V., Niknafs, A. (2014): NbClust: An R Package for Determining the Relevant Number of Clusters in a Data Set. *Journal of Statistical Software*, Vol 61, Issue 6. [www.jstatsoft.org](http://www.jstatsoft.org).

**See Also**

Other clustervalidation indices: [dunn\\_kproto](#), [gamma\\_kproto](#), [gplus\\_kproto](#), [mcclain\\_kproto](#), [ptbiseriial\\_kproto](#), [silhouette\\_kproto](#), [tau\\_kproto](#)

**Examples**

```
# generate toy data with factors and numerics

n <- 10
prb <- 0.99
muk <- 2.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k prototypes
kpres <- kproto(x, 4)
```

```
# calculate cindex-value
cindex_value <- cindex_kproto(object = kpres)

# calculate optimal number of cluster
k_opt <- cindex_kproto(data = x, k = 3:5, nstart = 5, verbose=FALSE)
```

---

clprofiles

*Profiling k-Prototypes Clustering*


---

## Description

Visualization of a k-prototypes clustering result for cluster interpretation.

## Usage

```
clprofiles(object, x, vars = NULL, col = NULL)
```

## Arguments

object	Object resulting from a call of resulting kproto. Also other kmeans like objects with object\$cluster and object\$size are possible.
x	Original data.
vars	Optional vector of either column indices or variable names.
col	Palette of cluster colours to be used for the plots. As a default RColorBrewer's <code>brewer.pal(max(unique(object\$cluster)), "Set3")</code> is used for $k > 2$ clusters and lightblue and orange else.

## Details

For numerical variables boxplots and for factor variables barplots of each cluster are generated.

## Author(s)

<gero.szepannek@web.de>

## Examples

```
# generate toy data with factors and numerics

n <- 100
prb <- 0.9
muk <- 1.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)
```

```

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k-prototyps
kpres <- kproto(x, 4)
clprofiles(kpres, x)

# in real world clusters are often not as clear cut
# by variation of lambda the emphasize is shifted towards factor / numeric variables
kpres <- kproto(x, 2)
clprofiles(kpres, x)

kpres <- kproto(x, 2, lambda = 0.1)
clprofiles(kpres, x)

kpres <- kproto(x, 2, lambda = 25)
clprofiles(kpres, x)

```

---

dunn\_kproto

Validating *k* Prototypes Clustering: Dunn index

---

## Description

Calculating the Dunn index for a k-Prototypes clustering with *k* clusters or computing the optimal number of clusters based on the Dunn index for k-Prototype clustering.

## Usage

```
dunn_kproto(object = NULL, data = NULL, k = NULL, ...)
```

## Arguments

object	Object of class kproto resulting from a call with kproto(..., keep.data=TRUE)
data	Original data; only required if object == NULL.
k	Vector specifying the search range for optimum number of clusters; if NULL the range will set as 2:sqrt(n). Only required if object == NULL.
...	Further arguments passed to <a href="#">kproto</a> , like: <ul style="list-style-type: none"> <li>nstart: If &gt; 1 repetitive computations of kproto with random initializations are computed.</li> </ul>

- `lambda`: Factor to trade off between Euclidean distance of numeric variables and simple matching coefficient between categorical variables.
- `verbose`: Logical whether information about the cluster procedure should be given. Caution: If `verbose=FALSE`, the reduction of the number of clusters is not mentioned.

## Details

$$Dunn = \frac{\min_{1 \leq i < j \leq q} d(C_i, C_j)}{\max_{1 \leq k \leq q} diam(C_k)}$$

The following applies: The dissimilarity between the two clusters  $C_i$  and  $C_j$  is defined as  $d(C_i, C_j) = \min_{x \in C_i, y \in C_j} d(x, y)$  and the diameter of a cluster is defined as  $diam(C_k) = \max_{x, y \in C_k} d(x, y)$ . The maximum value of the index is used to indicate the optimal number of clusters.

## Value

For computing the optimal number of clusters based on the Dunn index for k-Prototype clustering the output contains:

<code>k_opt</code>	optimal number of clusters
<code>indices</code>	calculated indices for $k = 2, \dots, k_{max}$

For computing the Dunn index-value for a given k-Prototype clustering the output contains:

<code>index</code>	calculated index-value
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## Author(s)

Rabea Aschenbruck

## References

- Charrad, M., Ghazzali, N., Boiteau, V., Niknafs, A. (2014): NbClust: An R Package for Determining the Relevant Number of Clusters in a Data Set. *Journal of Statistical Software*, Vol 61, Issue 6.

## See Also

Other clustervalidation indices: [dunn\\_kproto](#), [gamma\\_kproto](#), [gplus\\_kproto](#), [mcclain\\_kproto](#), [ptbiserical\\_kproto](#), [silhouette\\_kproto](#), [tau\\_kproto](#)

## Examples

```
# generate toy data with factors and numerics

n <- 10
prb <- 0.99
muk <- 2.5
clusid <- rep(1:4, each = n)
```

```

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k prototypes
kpres <- kproto(x, 4)

# calculate index-value
dunn_value <- dunn_kproto(object = kpres)

## Not run:
# calculate optimal number of cluster
k_opt <- dunn_kproto(data = x, k = 3:5, nstart = 5, verbose = FALSE)

## End(Not run)

```

---

gamma\_kproto

Validating *k* Prototypes Clustering: Gamma index

---

## Description

Calculating the Gamma index for a k-Prototypes clustering with *k* clusters or computing the optimal number of clusters based on the Gamma index for k-Prototype clustering.

## Usage

```
gamma_kproto(object = NULL, data = NULL, k = NULL, dists = NULL,
...)
```

## Arguments

object	Object of class kproto resulting from a call with kproto(..., keep.data=TRUE)
data	Original data; only required if object == NULL.
k	Vector specifying the search range for optimum number of clusters; if NULL the range will set as 2:sqrt(n). Only required if object == NULL.
dists	for internal purposes only

...

Further arguments passed to `kproto`, like:

- `nstart`: If  $> 1$  repetitive computations of `kproto` with random initializations are computed.
- `lambda`: Factor to trade off between Euclidean distance of numeric variables and simple matching coefficient between categorical variables.
- `verbose`: Logical whether information about the cluster procedure should be given. Caution: If `verbose=FALSE`, the reduction of the number of clusters is not mentioned.

## Details

$$Gamma = \frac{s(+)-s(-)}{s(+)+s(-)}$$

Comparisons are made between all within-cluster dissimilarities and all between-cluster dissimilarities.  $s(+)$  is the number of concordant comparisons and  $s(-)$  is the number of discordant comparisons. A comparison is named concordant (resp. discordant) if a within-cluster dissimilarity is strictly less (resp. strictly greater) than a between-cluster dissimilarity.

The maximum value of the index is used to indicate the optimal number of clusters.

## Value

For computing the optimal number of clusters based on the Gamma index for k-Prototype clustering the output contains:

<code>k_opt</code>	optimal number of clusters
<code>indices</code>	calculated indices for $k = 2, \dots, k_{max}$

For computing the Gamma index-value for a given k-Prototype clustering the output contains:

<code>index</code>	calculated index-value
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## Author(s)

Rabea Aschenbruck

## References

- Charrad, M., Ghazzali, N., Boiteau, V., Niknafs, A. (2014): NbClust: An R Package for Determining the Relevant Number of Clusters in a Data Set. *Journal of Statistical Software, Vol 61, Issue 6*.

## See Also

Other clustervalidation indices: [dunn\\_kproto](#), [dunn\\_kproto](#), [gplus\\_kproto](#), [mcclain\\_kproto](#), [ptbiserial\\_kproto](#), [silhouette\\_kproto](#), [tau\\_kproto](#)



**Examples**

```
# generate toy data with factors and numerics

n <- 10
prb <- 0.99
muk <- 2.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k prototypes
kpres <- kproto(x, 4)

# calculate index-value
gamma_value <- gamma_kproto(object = kpres)

# calculate optimal number of cluster
k_opt <- gamma_kproto(data = x, k = 3:5, nstart = 5, verbose = FALSE)
```

gplus\_kproto

*Validating k Prototypes Clustering: Gplus index***Description**

Calculating the Gplus index for a k-Prototypes clustering with k clusters or computing the optimal number of clusters based on the Gplus index for k-Prototype clustering.

**Usage**

```
gplus_kproto(object = NULL, data = NULL, k = NULL, dists = NULL,
...)
```

**Arguments**

object	Object of class kproto resulting from a call with kproto(..., keep.data=TRUE)
data	Original data; only required if object == NULL.

k	Vector specifying the search range for optimum number of clusters; if NULL the range will set as 2:sqrt(n). Only required if object == NULL.
dists	for internal purposes only
...	Further arguments passed to <a href="#">kproto</a> , like: <ul style="list-style-type: none"> <li>• nstart: If &gt; 1 repetitive computations of kproto with random initializations are computed.</li> <li>• lambda: Factor to trade off between Euclidean distance of numeric variables and simple matching coefficient between categorical variables.</li> <li>• verbose: Logical whether information about the cluster procedure should be given. Caution: If verbose=FALSE, the reduction of the number of clusters is not mentioned.</li> </ul>

## Details

$$Gplus = \frac{2 \cdot s(-)}{\frac{n(n-1)}{2} \cdot \left(\frac{n(n-1)}{2} - 1\right)}$$

Comparisons are made between all within-cluster dissimilarities and all between-cluster dissimilarities.  $s(-)$  is the number of discordant comparisons and a comparison is named discordant if a within-cluster dissimilarity is strictly greater than a between-cluster dissimilarity.

The minimum value of the index is used to indicate the optimal number of clusters.

## Value

For computing the optimal number of clusters based on the Gplus index for k-Prototype clustering the output contains:

k_opt	optimal number of clusters
indices	calculated indices for $k = 2, \dots, k_{max}$

For computing the Gplus index-value for a given k-Prototype clustering the output contains:

index	calculated index-value
-------	------------------------

## Author(s)

Rabea Aschenbruck

## References

- Charrad, M., Ghazzali, N., Boiteau, V., Niknafs, A. (2014): NbClust: An R Package for Determining the Relevant Number of Clusters in a Data Set. *Journal of Statistical Software*, Vol 61, Issue 6.

## See Also

Other clustervalidation indices: [dunn\\_kproto](#), [dunn\\_kproto](#), [gamma\\_kproto](#), [mcclain\\_kproto](#), [ptbiserial\\_kproto](#), [silhouette\\_kproto](#), [tau\\_kproto](#)

## Examples

```
# generate toy data with factors and numerics

n   <- 10
prb <- 0.99
muk <- 2.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k prototypes
kpres <- kproto(x, 4)

# calculate index-value
gplus_value <- gplus_kproto(object = kpres)

# calculate optimal number of cluster
k_opt <- gplus_kproto(data = x, k = 3:5, nstart = 5, verbose = FALSE)
```

---

kproto

*k-Prototypes Clustering*


---

## Description

Computes k-prototypes clustering for mixed-type data.

## Usage

```
kproto(x, ...)

## Default S3 method:
kproto(x, k, lambda = NULL, iter.max = 100,
       nstart = 1, na.rm = TRUE, keep.data = TRUE, verbose = TRUE, ...)
```

**Arguments**

<code>x</code>	Data frame with both numerics and factors.
<code>...</code>	Currently not used.
<code>k</code>	Either the number of clusters, a vector specifying indices of initial prototypes, or a data frame of prototypes of the same columns as <code>x</code> .
<code>lambda</code>	Parameter $> 0$ to trade off between Euclidean distance of numeric variables and simple matching coefficient between categorical variables. Also a vector of variable specific factors is possible where the order must correspond to the order of the variables in the data. In this case all variables' distances will be multiplied by their corresponding lambda value.
<code>iter.max</code>	Maximum number of iterations if no convergence before.
<code>nstart</code>	If $> 1$ repetitive computations with random initializations are computed and the result with minimum tot.dist is returned.
<code>na.rm</code>	A logical value indicating whether NA values should be stripped before the computation proceeds.
<code>keep.data</code>	Logical whether original should be included in the returned object.
<code>verbose</code>	Logical whether information about the cluster procedure should be given. Caution: If <code>verbose=FALSE</code> , the reduction of the number of clusters is not mentioned.

**Details**

The algorithm like k-means iteratively recomputes cluster prototypes and reassigns clusters. Clusters are assigned using  $d(x, y) = d_{euclid}(x, y) + \lambda d_{simple\ matching}(x, y)$ . Cluster prototypes are computed as cluster means for numeric variables and modes for factors (cf. Huang, 1998). In case of `na.rm = FALSE`: for each observation variables with missings are ignored (i.e. only the remaining variables are considered for distance computation). In consequence for observations with missings this might result in a change of variable's weighting compared to the one specified by `lambda`. Further note: For these observations distances to the prototypes will typically be smaller as they are based on fewer variables.

**Value**

`kmeans` like object of class `kproto`:

<code>cluster</code>	Vector of cluster memberships.
<code>centers</code>	Data frame of cluster prototypes.
<code>lambda</code>	Distance parameter lambda.
<code>size</code>	Vector of cluster sizes.
<code>withinss</code>	Vector of within cluster distances for each cluster, i.e. summed distances of all observations belonging to a cluster to their respective prototype.
<code>tot.withinss</code>	Target function: sum of all observations' distances to their corresponding cluster prototype.
<code>dists</code>	Matrix with distances of observations to all cluster prototypes.

iter	Prespecified maximum number of iterations.
trace	List with two elements (vectors) tracing the iteration process: tot.dists and moved number of observations over all iterations.

**Author(s)**

<gero.szepannek@web.de>

**References**

- Szepannek, G. (2018): clustMixType: User-Friendly Clustering of Mixed-Type Data in R, *The R Journal* 10/2, 200-208.
- Z.Huang (1998): Extensions to the k-Means Algorithm for Clustering Large Data Sets with Categorical Variables, *Data Mining and Knowledge Discovery* 2, 283-304.

**Examples**

```
# generate toy data with factors and numerics

n <- 100
prb <- 0.9
muk <- 1.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k-prototypes
kpres <- kproto(x, 4)
clprofiles(kpres, x)

# in real world clusters are often not as clear cut
# by variation of lambda the emphasize is shifted towards factor / numeric variables
kpres <- kproto(x, 2)
clprofiles(kpres, x)

kpres <- kproto(x, 2, lambda = 0.1)
clprofiles(kpres, x)

kpres <- kproto(x, 2, lambda = 25)
clprofiles(kpres, x)
```

lambdaest

*Compares Variability of Variables***Description**

Investigation of the variables' variances/concentrations to support specification of lambda for k-prototypes clustering.

**Usage**

```
lambdaest(x, num.method = 1, fac.method = 1, outtype = "numeric")
```

**Arguments**

x	Original data.
num.method	Integer 1 or 2. Specifies the heuristic used for numeric variables.
fac.method	Integer 1 or 2. Specifies the heuristic used for factor variables.
outtype	Specifies the desired output: either 'numeric', 'vector' or 'variation'.

**Details**

Variance (num.method = 1) or standard deviation (num.method = 2) of numeric variables and  $1 - \sum_i p_i^2$  (fac.method = 1) or  $1 - \max_i p_i$  (fac.method = 2) for factors is computed.

**Value**

lambda

Ratio of averages over all numeric/factor variables is returned. In case of outtype = "vector" the separate lambda for all variables is returned as the inverse of the single variables' variation as specified by the num.method and fac.method argument. outtype = "variation" directly returns these quantities and is not ment to be passed directly to kproto().

**Author(s)**

<gero.szepannek@web.de>

**Examples**

```
# generate toy data with factors and numerics

n <- 100
prb <- 0.9
muk <- 1.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)
```

```

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

lambdaest(x)
res <- kproto(x, 4, lambda = lambdaest(x))

```

mcclain\_kproto

*Validating k Prototypes Clustering: McClain index***Description**

Calculating the McClain index for a k-Prototypes clustering with k clusters or computing the optimal number of clusters based on the McClain index for k-Prototype clustering.

**Usage**

```
mcclain_kproto(object = NULL, data = NULL, k = NULL, ...)
```

**Arguments**

object	Object of class kproto resulting from a call with kproto(..., keep.data=TRUE)
data	Original data; only required if object == NULL.
k	Vector specifying the search range for optimum number of clusters; if NULL the range will set as 2:sqrt(n). Only required if object == NULL.
...	Further arguments passed to <a href="#">kproto</a> , like: <ul style="list-style-type: none"> <li>• nstart: If &gt; 1 repetitive computations of kproto with random initializations are computed.</li> <li>• lambda: Factor to trade off between Euclidean distance of numeric variables and simple matching coefficient between categorical variables.</li> <li>• verbose: Logical whether information about the cluster procedure should be given. Caution: If verbose=FALSE, the reduction of the number of clusters is not mentioned.</li> </ul>

**Details**

$$McClain = \frac{\bar{S}_w}{\bar{S}_b}$$

$\bar{S}_w$  is the sum of within-cluster distances divided by the number of within-cluster distances and  $\bar{S}_b$  is the sum of between-cluster distances divided by the number of between-cluster distances.

The minimum value of the index is used to indicate the optimal number of clusters.

**Value**

For computing the optimal number of clusters based on the McClain index for k-Prototype clustering the output contains:

k_opt	optimal number of clusters
indices	calculated indices for $k = 2, \dots, k_{max}$

For computing the McClain index-value for a given k-Prototype clustering the output contains:

index	calculated index-value
-------	------------------------

**Author(s)**

Rabea Aschenbruck

**References**

- Charrad, M., Ghazzali, N., Boiteau, V., Niknafs, A. (2014): NbClust: An R Package for Determining the Relevant Number of Clusters in a Data Set. *Journal of Statistical Software*, Vol 61, Issue 6.

**See Also**

Other clustervalidation indices: [dunn\\_kproto](#), [dunn\\_kproto](#), [gamma\\_kproto](#), [gplus\\_kproto](#), [ptbiserial\\_kproto](#), [silhouette\\_kproto](#), [tau\\_kproto](#)

**Examples**

```
# generate toy data with factors and numerics

n <- 10
prb <- 0.99
muk <- 2.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k prototypes
kpres <- kproto(x, 4)
```



```
# calculate index-value
mcclain_value <- mcclain_kproto(object = kpres)

# calculate optimal number of cluster
k_opt <- mcclain_kproto(data = x, k = 3:5, nstart = 5, verbose = FALSE)
```

---

predict.kproto	<i>Assign k-Prototypes Clusters</i>
----------------	-------------------------------------

---

## Description

Predicts k-prototypes cluster memberships and distances for new data.

## Usage

```
## S3 method for class 'kproto'
predict(object, newdata, ...)
```

## Arguments

object	Object resulting from a call of kproto.
newdata	New data frame (of same structure) where cluster memberships are to be predicted.
...	Currently not used.

## Value

[kmeans](#) like object of class kproto:

cluster	Vector of cluster memberships.
dists	Matrix with distances of observations to all cluster prototypes.

## Author(s)

<gero.szepannek@web.de>

## Examples

```
# generate toy data with factors and numerics

n <- 100
prb <- 0.9
muk <- 1.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
```

```

x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k-prototyps
kpres <- kproto(x, 4)
predicted.clusters <- predict(kpres, x)

```

---

ptbiserial\_kproto

Validating *k* Prototypes Clustering: *Ptbiserial* index

---

## Description

Calculating the Ptbiserial index for a k-Prototypes clustering with *k* clusters or computing the optimal number of clusters based on the Ptbiserial index for k-Prototype clustering.

## Usage

```
ptbiserial_kproto(object = NULL, data = NULL, k = NULL, s_d = NULL,
  ...)
```

## Arguments

<code>object</code>	Object of class <code>kproto</code> resulting from a call with <code>kproto(..., keep.data=TRUE)</code>
<code>data</code>	Original data; only required if <code>object == NULL</code> .
<code>k</code>	Vector specifying the search range for optimum number of clusters; if <code>NULL</code> the range will set as <code>2:sqrt(n)</code> . Only required if <code>object == NULL</code> .
<code>s_d</code>	for internal purposes only
<code>...</code>	Further arguments passed to <code>kproto</code> , like: <ul style="list-style-type: none"> <li><code>nstart</code>: If <code>&gt; 1</code> repetetive computations of <code>kproto</code> with random initializations are computed.</li> <li><code>lambda</code>: Factor to trade off between Euclidean distance of numeric variables and simple matching coefficient between categorical variables.</li> <li><code>verbose</code>: Logical whether information about the cluster procedure should be given. Caution: If <code>verbose=FALSE</code>, the reduction of the number of clusters is not mentioned.</li> </ul>

## Details

$$Ptbiserial = \frac{(\bar{S}_b - \bar{S}_w) \cdot \left(\frac{N_w \cdot N_b}{N_t^2}\right)^{0.5}}{s_d}$$

$\bar{S}_w$  is the sum of within-cluster distances divided by the number of within-cluster distances and  $\bar{S}_b$  is the sum of between-cluster distances divided by the number of between-cluster distances.

$N_t$  is the total number of pairs of objects in the data,  $N_w$  is the total number of pairs of objects belonging to the same cluster and  $N_b$  is the total number of pairs of objects belonging to different clusters.  $s_d$  is the standard deviation of all distances.

The maximum value of the index is used to indicate the optimal number of clusters.

## Value

For computing the optimal number of clusters based on the Ptbiserial index for k-Prototype clustering the output contains:

k_opt	optimal number of clusters
indices	calculated indices for $k = 2, \dots, k_{max}$

For computing the Ptbiserial index-value for a given k-Prototype clustering the output contains:

index	calculated index-value
-------	------------------------

## Author(s)

Rabea Aschenbruck

## References

- Charrad, M., Ghazzali, N., Boiteau, V., Niknafs, A. (2014): NbClust: An R Package for Determining the Relevant Number of Clusters in a Data Set. *Journal of Statistical Software*, Vol 61, Issue 6.

## See Also

Other clustervalidation indices: [dunn\\_kproto](#), [dunn\\_kproto](#), [gamma\\_kproto](#), [gplus\\_kproto](#), [mcclain\\_kproto](#), [silhouette\\_kproto](#), [tau\\_kproto](#)

## Examples

```
# generate toy data with factors and numerics

n <- 10
prb <- 0.99
muk <- 2.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
```

```

x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k prototypes
kpres <- kproto(x, 4)

# calculate index-value
Ptbiserial_value <- ptbiserial_kproto(object = kpres)

# calculate optimal number of cluster
k_opt <- ptbiserial_kproto(data = x, k = 3:5, nstart = 5, verbose = FALSE)

```

---

silhouette\_kproto

Validating *k* Prototypes Clustering: Silhouette index

---

## Description

Calculating the Silhouette index for a *k*-Prototypes clustering with *k* clusters or computing the optimal number of clusters based on the Silhouette index for *k*-Prototype clustering.

## Usage

```
silhouette_kproto(object = NULL, data = NULL, k = NULL, ...)
```

## Arguments

object	Object of class <code>kproto</code> resulting from a call with <code>kproto(..., keep.data=TRUE)</code>
data	Original data; only required if <code>object == NULL</code> .
k	Vector specifying the search range for optimum number of clusters; if <code>NULL</code> the range will set as <code>2:sqrt(n)</code> . Only required if <code>object == NULL</code> .
...	Further arguments passed to <code>kproto</code> , like: <ul style="list-style-type: none"> <li><code>nstart</code>: If <code>&gt; 1</code> repetitive computations of <code>kproto</code> with random initializations are computed.</li> <li><code>lambda</code>: Factor to trade off between Euclidean distance of numeric variables and simple matching coefficient between categorical variables.</li> <li><code>verbose</code>: Logical whether information about the cluster procedure should be given. Caution: If <code>verbose=FALSE</code>, the reduction of the number of clusters is not mentioned.</li> </ul>

**Details**

$$Silhouette = \frac{1}{n} \sum_{i=1}^n \frac{b(i) - a(i)}{\max(a(i), b(i))}$$

$a(i)$  is the average dissimilarity of the  $i$ th object to all other objects of the same/own cluster.  $b(i) = \min(d(i, C))$ , where  $d(i, C)$  is the average dissimilarity of the  $i$ th object to all the other clusters except the own/same cluster.

The maximum value of the index is used to indicate the optimal number of clusters.

**Value**

For computing the optimal number of clusters based on the Silhouette index for k-Prototype clustering the output contains:

k_opt	optimal number of clusters
indices	calculated indices for $k = 2, \dots, k_{max}$

For computing the Silhouette index-value for a given k-Prototype clustering the output contains:

index	calculated index-value
-------	------------------------

**Author(s)**

Rabea Aschenbruck

**References**

- Charrad, M., Ghazzali, N., Boiteau, V., Niknafs, A. (2014): NbClust: An R Package for Determining the Relevant Number of Clusters in a Data Set. *Journal of Statistical Software*, Vol 61, Issue 6.

**See Also**

Other clustervalidation indices: [dunn\\_kproto](#), [dunn\\_kproto](#), [gamma\\_kproto](#), [gplus\\_kproto](#), [mcclain\\_kproto](#), [ptbiseriial\\_kproto](#), [tau\\_kproto](#)

**Examples**

```
# generate toy data with factors and numerics

n <- 10
prb <- 0.99
muk <- 2.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)
```

```

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k prototypes
kpres <- kproto(x, 4)

# calculate index-value
silhouette_value <- silhouette_kproto(object = kpres)

# calculate optimal number of cluster
k_opt <- silhouette_kproto(data = x, k = 3:5, nstart = 5, verbose = FALSE)

```

summary.kproto

*Summary Method for kproto Cluster Result***Description**

Investigation of variances to specify lambda for k-prototypes clustering.

**Usage**

```

## S3 method for class 'kproto'
summary(object, data = NULL, pct.dig = 3, ...)

```

**Arguments**

object	Object of class kproto.
data	Optional data set to be analyzed. If <code>!(is.null(data))</code> clusters for data are assigned by <code>predict(object, data)</code> . If not specified the clusters of the original data are analyzed which is only possible if kproto has been called using <code>keep.data = TRUE</code> .
pct.dig	Number of digits for rounding percentages of factor variables.
...	Further arguments to be passed to internal call of <code>summary()</code> for numeric variables.

**Details**

For numeric variables statistics are computed for each clusters using `summary()`. For categorical variables distribution percentages are computed.

**Value**

List where each element corresponds to one variable. Each row of any element corresponds to one cluster.

**Author(s)**

<gero.szepannek@web.de>

**Examples**

```
# generate toy data with factors and numerics

n <- 100
prb <- 0.9
muk <- 1.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

res <- kproto(x, 4)
summary(res)
```

---

tau\_kproto

Validating *k* Prototypes Clustering: Tau index

---

**Description**

Calculating the Tau index for a k-Prototypes clustering with k clusters or computing the optimal number of clusters based on the Tau index for k-Prototype clustering.

**Usage**

```
tau_kproto(object = NULL, data = NULL, k = NULL, dists = NULL, ...)
```

**Arguments**

object	Object of class kproto resulting from a call with <code>kproto(..., keep.data=TRUE)</code>
data	Original data; only required if <code>object == NULL</code> .
k	Vector specifying the search range for optimum number of clusters; if <code>NULL</code> the range will set as <code>2:sqrt(n)</code> . Only required if <code>object == NULL</code> .
dists	for internal purposes only
...	Further arguments passed to <a href="#">kproto</a> , like: <ul style="list-style-type: none"> <li>• <code>nstart</code>: If <code>&gt; 1</code> repetitive computations of kproto with random initializations are computed.</li> <li>• <code>lambda</code>: Factor to trade off between Euclidean distance of numeric variables and simple matching coefficient between categorical variables.</li> <li>• <code>verbose</code>: Logical whether information about the cluster procedure should be given. Caution: If <code>verbose=FALSE</code>, the reduction of the number of clusters is not mentioned.</li> </ul>

**Details**

$$Tau = \frac{s(+) - s(-)}{\left(\left(\frac{N_t(N_t-1)}{2} - t\right) \frac{N_t(N_t-1)}{2}\right)^{0.5}}$$

Comparisons are made between all within-cluster dissimilarities and all between-cluster dissimilarities.  $s(+)$  is the number of concordant comparisons and  $s(-)$  is the number of discordant comparisons. A comparison is named concordant (resp. discordant) if a within-cluster dissimilarity is strictly less (resp. strictly greater) than a between-cluster dissimilarity.

$N_t$  is the total number of distances  $\frac{n(n-1)}{2}$  and  $t$  is the number of comparisons of two pairs of objects where both pairs represent within-cluster comparisons or both pairs are between-cluster comparisons.

The maximum value of the index is used to indicate the optimal number of clusters.

**Value**

For computing the optimal number of clusters based on the Tau index for k-Prototype clustering the output contains:

k_opt	optimal number of clusters
indices	calculated indices for $k = 2, \dots, k_{max}$

For computing the Tau index-value for a given k-Prototype clustering the output contains:

index	calculated index-value
-------	------------------------

**Author(s)**

Rabea Aschenbruck



## References

- Charrad, M., Ghazzali, N., Boiteau, V., Niknafs, A. (2014): NbClust: An R Package for Determining the Relevant Number of Clusters in a Data Set. *Journal of Statistical Software*, Vol 61, Issue 6.

## See Also

Other clustervalidation indices: [dunn\\_kproto](#), [dunn\\_kproto](#), [gamma\\_kproto](#), [gplus\\_kproto](#), [mcclain\\_kproto](#), [ptbiseriial\\_kproto](#), [silhouette\\_kproto](#)

## Examples

```
# generate toy data with factors and numerics

n <- 10
prb <- 0.99
muk <- 2.5
clusid <- rep(1:4, each = n)

x1 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x1 <- c(x1, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x1 <- as.factor(x1)

x2 <- sample(c("A","B"), 2*n, replace = TRUE, prob = c(prb, 1-prb))
x2 <- c(x2, sample(c("A","B"), 2*n, replace = TRUE, prob = c(1-prb, prb)))
x2 <- as.factor(x2)

x3 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))
x4 <- c(rnorm(n, mean = -muk), rnorm(n, mean = muk), rnorm(n, mean = -muk), rnorm(n, mean = muk))

x <- data.frame(x1,x2,x3,x4)

# apply k prototypes
kpres <- kproto(x, 4)

# calculate index-value
tau_value <- tau_kproto(object = kpres)

# calculate optimal number of cluster
k_opt <- tau_kproto(data = x, k = 3:5, nstart = 5, verbose = FALSE)
```

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