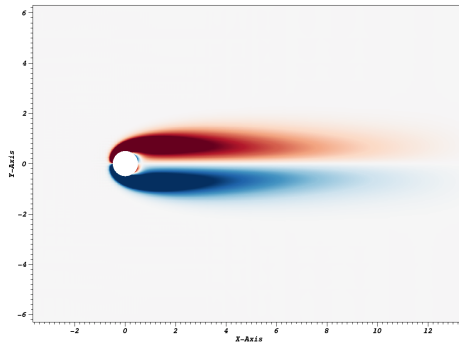


Numerical Simulation of Compressible Flows with Immersed Boundaries Using Discontinuous Galerkin Methods



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Bachelor thesis by Simone Stange
Prof. Dr.-Ing. habil. Martin Oberlack
Betreuer: Dr.-Ing Björn Müller





- 1 Introduction and Fundamentals
 - Introduction
 - The Discontinuous Galerkin Method
 - The Immersed Boundary Method
- 2 Verification of BoSSS for Inviscid Flows
 - Robustness
 - Convergence
- 3 Evaluation of BoSSS for Viscid Flows
 - Theory
 - Simulations
- 4 Conclusion and Outlook



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kurzes blabla



compressible flow

ideal gas mit γ $Ma = \text{def}$, $0.2 Re$, Pr



2d

conserved flow variables density, momentum, energy

dimensionless variables

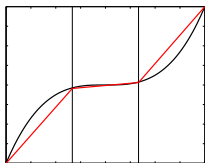
gleichung, aufgeteilt in temporal derivative, convective fluxes, viscous fluxes

time discretisation durch Runge-Kutta erster Ordnung -> expliziter Euler

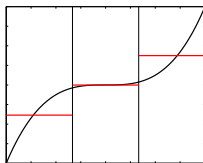
The Discontinuous Galerkin Space



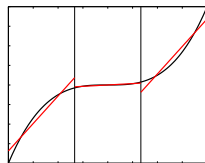
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(a) First order FEM



(b) Zeroth order DG (FVM)



(c) First order DG

Abbildung: Comparison of FEM, FVM and DG

DG space discretisation Vorgehen, Bildchen, fluxes

The Immersed Boundary Method



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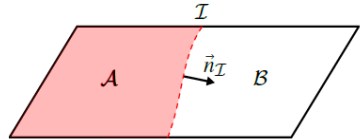
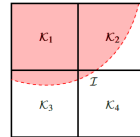
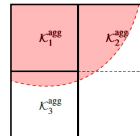


Abbildung: Cut cell with physical (red) and void region (white) [4]

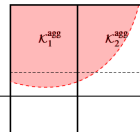
regions mit Bild, Aufteilung Integrale mass matrix rk time discretisation formel cell agglomeration



(a) Initial mesh partitioning



(b) Cell agglomeration with small
agglomeration threshold





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Problem Specification



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Gitter, Bild, domain, level set, isentropic inviscid flow mit gleichung $\rightarrow s=0$



shift, degree 1 bis 3, aggro 0.5, 64 mal 64 cells Parameter, was wird getan

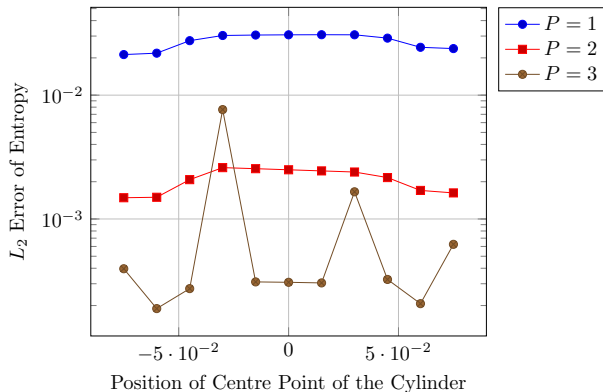


Abbildung: Convergence Plot

Ergebnisse, Plot, komischer punkt wird angeschaut

Comvergence Study – Preparation



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Parameter, was wird getan

Convergence Study – Evaluation



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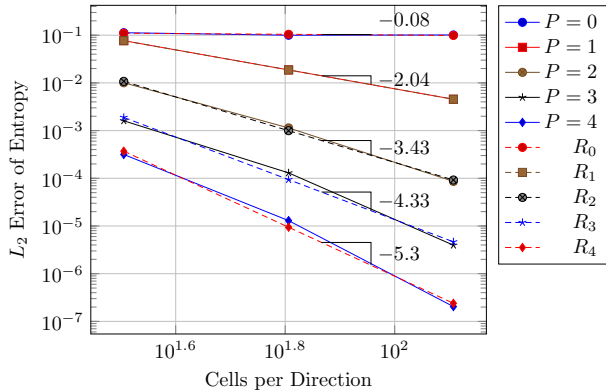


Abbildung: Convergence Plot

Ergebnisse, Plot



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Theory – Differentiation into Flow Regimes

- ▶ $40 - 50 < Re < 190$: laminar vortex shedding,
- ▶ $190 < Re < 260$: 3D wake-transition regime,

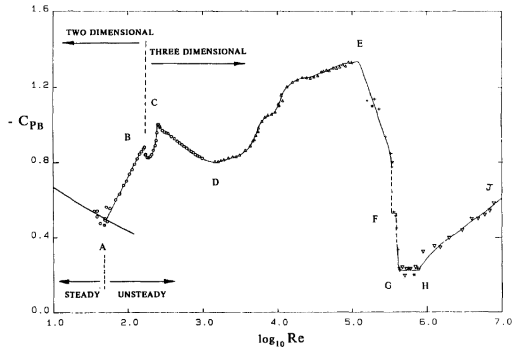


Abbildung: Base Suction Coefficient over Reynolds Numbers [4]

laminar steady regime Bild

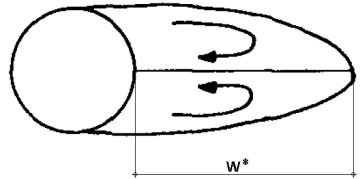


Abbildung: Recirculation Area [4]

Bild

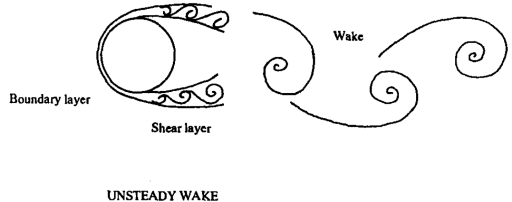


Abbildung: Kármán Vortex Street [4]

Karman vortex street frequency /strouhal



simulation parameter gitter cD , CL , W^* , St

Simulation at $Re = 20$ I

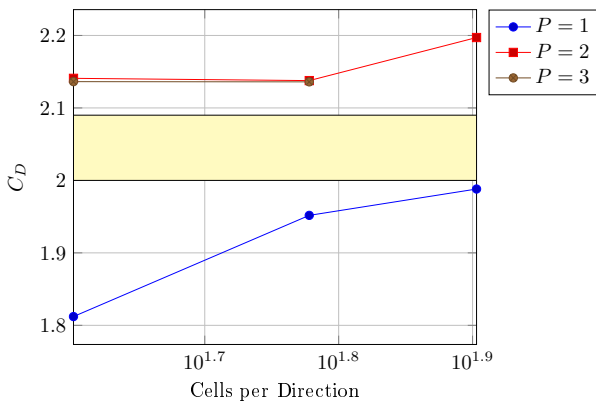


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Re = 20	Source	2D/3D	W^*	C_D
Numerical – Incompressible	Dennis and Chang	2D	0.94	2.05
	Fornberg	2D	0.91	2.00
	Linnick and Fasel	2D	0.93	2.06
Experimental	Coutanceau and Bouard	-	0.93	-
	Tritton	-	-	2.09
Numerical – Compressible	Brehm, Hader and Fasel ($Ma = 0.1$)	3D	0.96	2.02
	Ayers	2D	0.975	2.06
	Present Results:	2D	0.928	2.136

Simulation at Re = 20 II

- ▶ hier
- ▶ kommt
- ▶ beschreibung hin



Simulation at $Re = 40$ I



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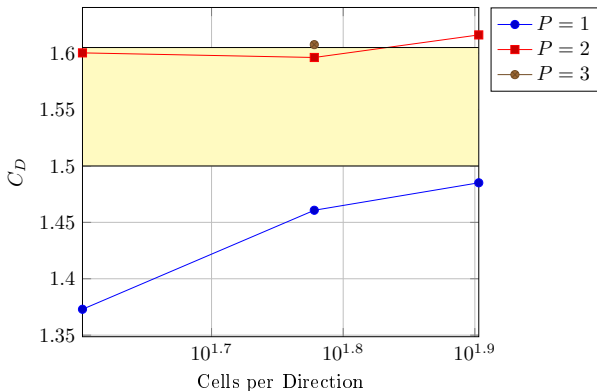
Re = 40	Source	2D/3D	W^*	C_D
Numerical – Incompressible	Dennis and Chang	2D	2.35	1.52
	Fornberg	2D	2.24	1.50
	Linnick and Fasel	2D	2.28	1.54
Experimental	Coutanceau and Bouard	-	2.13	-
	Tritton	-	-	1.59
Numerical – Compressible	Brehm, Hader and Fasel ($Ma = 0.1$)	3D	2.26	1.51
	Ayers	2D	2.250	1.605
	Present Results:	2D	2.201	1.608

Simulation at Re = 40 II



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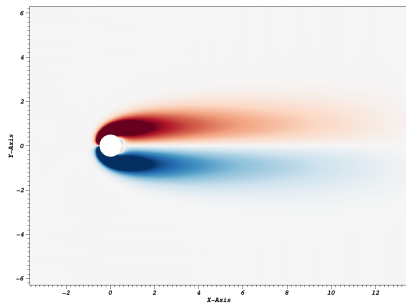


Comparison of $Re = 20$ and $Re = 40$

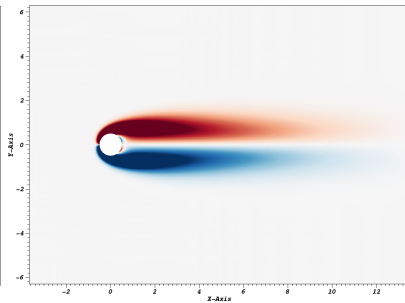


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	W^*	C_D
$Re = 20$	0.928	2.136
$Re = 40$	2.201	1.608



(a) $Re = 20$



(b) $Re = 40$

Simulation at $Re = 100$ I

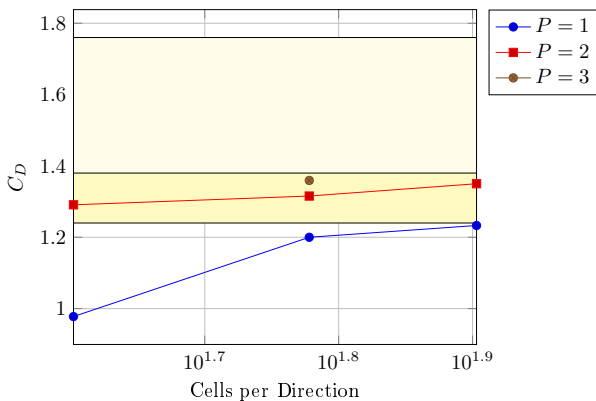


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Re = 100	Source	2D/3D	St	C_D	C_L
Numerical – Incompressible	Gresho, Chan, Lee, et al.	2D	0.18	1.76	-
	Linnick and Fasel ($\lambda = 0.056$)	2D	0.169	1.38 ± 0.010	± 0.337
	Linnick and Fasel ($\lambda = 0.023$)	2D	0.1696	1.34 ± 0.009	± 0.333
	Persillon and Braza	2D	0.165	1.253	-
	Saiki and Biringen	2D	0.171	1.26	-
	Persillon and Braza	3D	0.164	1.240	-
	Liu, Zheng and Sung	3D	0.165	1.35 ± 0.012	± 0.339
Experimental	Berger and Wille	-	0.16 – 0.17	-	-
	Clift, Grace and Weber	-	-	1.24	-
	Williamson	-	0.164	-	-
Numerical – Compressible	Brehm, Hader and Fasel ($Ma = 0.1$)	3D	0.165	1.32 ± 0.01	± 0.32
	Ayers	2D	0.167	1.371 ± 0.011	± 0.333
	Present Results:	2D	0.1669	1.3593 ± 0.00805	± 0.3291

Simulation at $Re = 100$ II

- ▶ hier
- ▶ kommt
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Simulation at $Re = 200$ I



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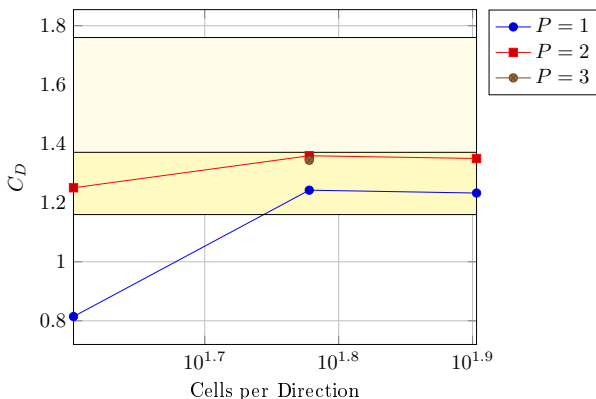
Re = 200	Source	2D/3D	St	C_D	C_L
Numerical – Incompressible	Belov, Martinelli and Jameson	2D	0.193	1.19 ± 0.042	± 0.64
	Gresho, Chan, Lee et al.	2D	0.21	1.76	-
	Linnick and Fasel ($\lambda = 0.056$)	2D	0.199	1.37 ± 0.046	± 0.70
	Linnick and Fasel ($\lambda = 0.023$)	2D	0.197	1.34 ± 0.044	± 0.69
	Miyake, Sakamoto, Tokunaga et al.	2D	0.196	1.34 ± 0.043	± 0.67
	Persillon and Braza	2D	0.198	1.321	-
	Saiki and Biringen	2D	0.197	1.18	-
	Persillon and Braza	3D	0.181	1.306	-
	Liu, Zheng and Sung	3D	0.192	1.31 ± 0.049	± 0.69
Experimental	Berger and Wille	-	0.18 – 0.19	-	-
	Clift, Grace and Weber	-	-	1.16	-
	Williamson	-	0.181	-	-
Numerical – Compressible	Brehm, Hader and Fasel ($Ma = 0.1$)	3D	0.192	1.3 ± 0.04	± 0.66
	Ayers	2D	0.201	1.371 ± 0.011	± 0.70
	Present Results:	2D	0.2002	1.344 ± 0.0462	± 0.6887

Simulation at Re = 200 II



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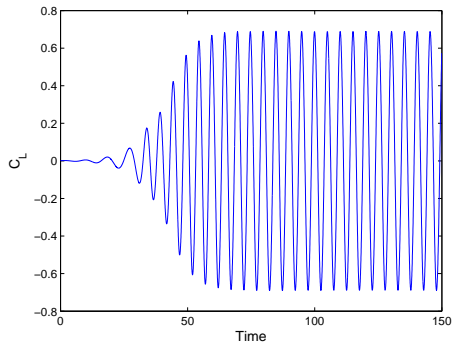
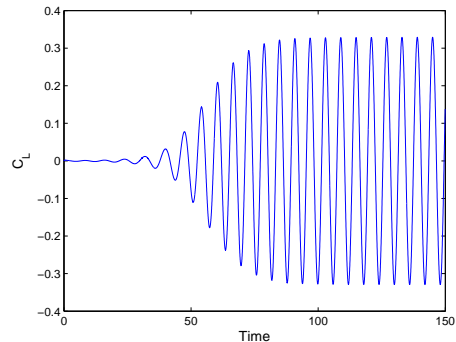
Simulation at $Re = 200$ III



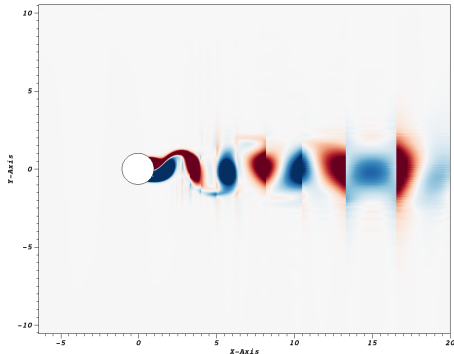
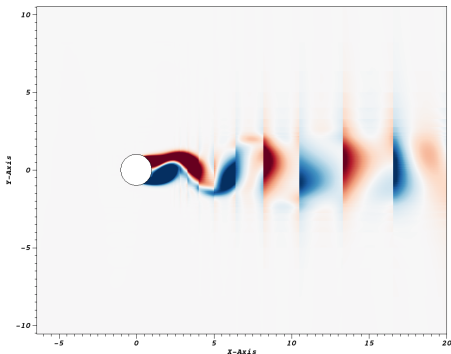
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re 200 tabelle, plot, lift over time, vorticity

Comparison of $Re = 100$ and $Re = 200$ I



Comparison of $Re = 100$ and $Re = 200$ II



	St	C_D	C_L
$Re = 100$	0.1669	1.359 ± 0.00805	± 0.3291
$Re = 200$	0.2002	1.344 ± 0.0462	± 0.6887



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Summary



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conclusion



future works

The End



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ende, fragen

- [1] [Müller, 2014] B. Müller
Methods for higher order numerical simulations of complex inviscid fluids with immersed boundaries
PhD thesis, TU Darmstadt, 2014.
- [2] [Ayers, 2015] L. F. Ayers
Validation of a discontinuous Galerkin based compressible CFD solver
Bachelor thesis, TU Darmstadt, 2015.
- [3] [Müller, 2016] B. Müller, S. Krämer-Eis, F. Kummer et al.
A high-order Discontinuous Galerkin method for compressible flows with immersed boundaries
International Journal of Numerical Methods in Engineering, 2016, submitted.



- [4] [Williamson, 1996] C. H. Williamson
Vortex dynamics in the cylinder wake
Annual review of fluid mechanics, 1996.



alle tabellen und graphen die man brauchen könnte in anhang