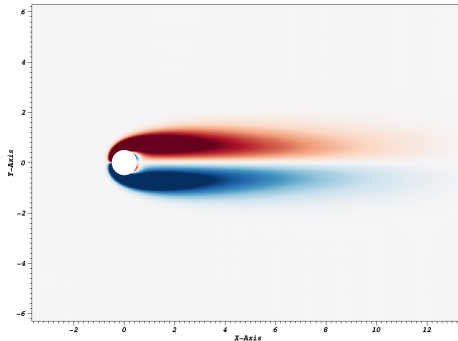


Numerical Simulation of Compressible Flows with Immersed Boundaries Using Discontinuous Galerkin Methods



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Bachelor thesis by Simone Stange
Prof. Dr.-Ing. habil. Martin Oberlack
Betreuer: Dr.-Ing Björn Müller





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 - Introduction
 - The Runge-Kutta Discontinuous Galerkin Method
 - The Immersed Boundary Method
- 2 Verification of BoSSS for Inviscid Flows
 - Robustness
 - Convergence
- 3 Evaluation of BoSSS for Viscid Flows
 - Theory
 - Simulations
- 4 Conclusion and Outlook



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kurzes blabla



compressible flow

ideal gas mit γ $Ma = \text{def}$, $0.2 Re$, Pr

Compressible Navier-Stokes Equation



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2d

conserved flow variables density, momentum, energy

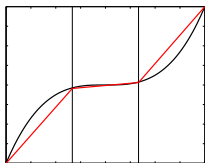
dimensionless variables

gleichung, aufgeteilt in temporal derivative, convective fluxes, viscous fluxes

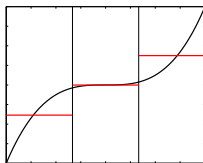
The Discontinuous Galerkin Space



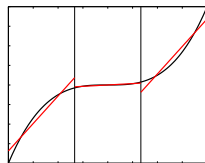
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(a) First order FEM



(b) Zeroth order DG (FVM)



(c) First order DG

Abbildung: Comparison of FEM, FVM and DG

DG space discretisation Vorgehen, Bildchen, fluxes

The Runge-Kutta Time Discretisation



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RK time discretisation Endformel, Tabelle, cfl criterion

The Immersed Boundary Method



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regions mit Bild, Aufteilung Integrale mass matrix rk time discretisation formel cell agglomeration



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Problem Specification



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Gitter, Bild, domain, level set, isentropic inviscid flow mit gleichung $\rightarrow s=0$

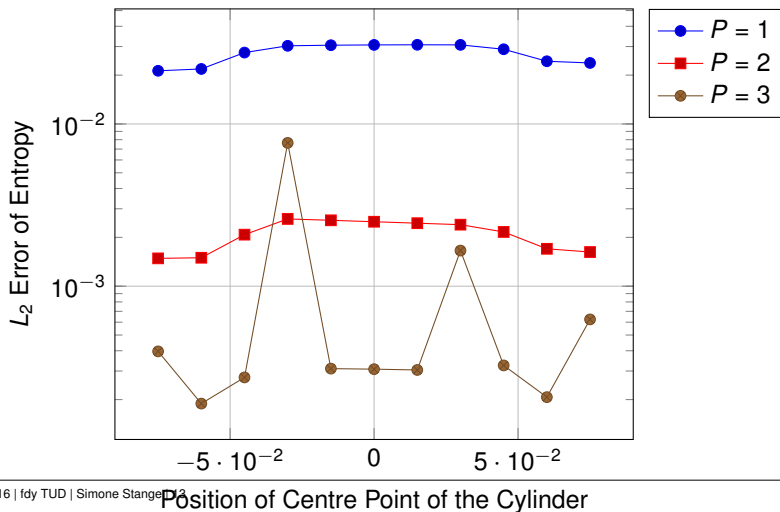
Robustness Study – Preparation



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shift, degree 1 bis 3, aggro 0.5, 64 mal 64 cells Parameter, was wird getan

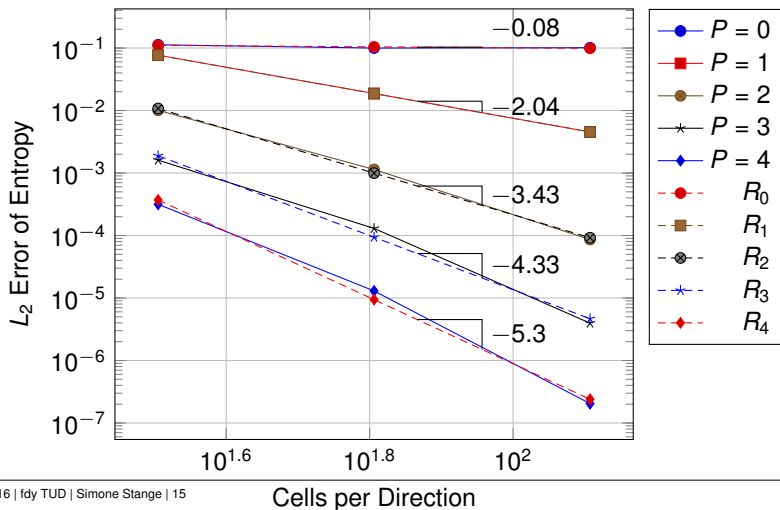
Robustness Study – Evaluation





Parameter, was wird getan

Convergence Study – Evaluation

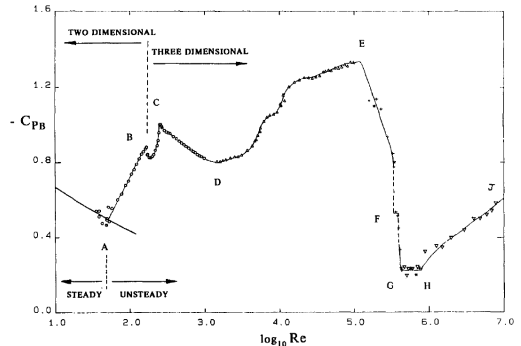




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Theory – Differentiation into Flow Regimes

- ▶ $40 - 50 < Re < 190$:
laminar vortex shedding,
- ▶ $190 < Re < 260$: 3d
wake-transition regime,



laminar steady regime Bild

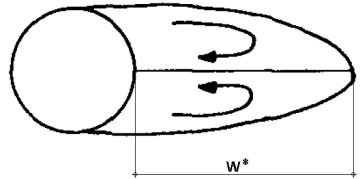


Abbildung: Wake Separation Length,
Taken from [?], Modified

Bild

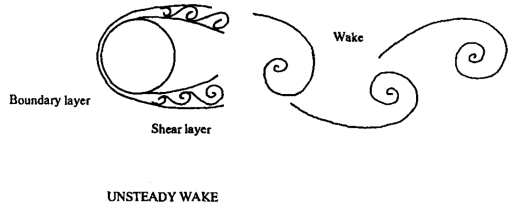


Abbildung: Kármán Vortex Street [?]

Karman vortex street frequency /strouhal

Simulation Properties



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simulation parameter gitter cD , CL , W^* , St

Simulation at $Re = 20$ I



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Re = 20	Source	2d/3d	W^*	C_D
Numerical – Incompressible	dennis1970numerical	2d	0.94	2.05
	fornberg1980numerical	2d	0.91	2.00
	linnick2005high	2d	0.93	2.06
Experimental	coutanceau1977experimental	-	0.93	-
	tritton1959experiments	-	-	2.09
Numerical – Compressible	brehm2015locally ($Ma = 0.1$)	3d	0.96	2.02
	ayers	2d	0.975	2.06
	Present Results:	2d	0.928	2.136

Tabelle: Comparison of Results for W^* and C_D , taken from [?], modified

Simulation at $Re = 40$



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Re = 40	Source	2d/3d	W^*	C_D
Numerical – Incompressible	dennis1970numerical	2d	2.35	1.52
	fornberg1980numerical	2d	2.24	1.50
	linnick2005high	2d	2.28	1.54
Experimental	coutanceau1977experimental	-	2.13	-
	tritton1959experiments	-	-	1.59
Numerical – Compressible	brehm2015locally (Ma = 0.1)	3d	2.26	1.51
	ayers	2d	2.250	1.605
	Present Results:	2d	2.201	1.608

Tabelle: Comparison of Results for W^* and C_D , taken from [?], modified

re 40 tabelle, plot, drag over time, vorticity

Simulation at $Re = 100$



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Re = 100	Source	2d/3d	St	C_D
Numerical – Incompressible	gresho1984modified	2d	0.18	1.76
	linnick2005high ($\lambda = 0.056$)	2d	0.169	1.38 ± 0.05
	linnick2005high ($\lambda = 0.023$)	2d	0.1696	1.34 ± 0.05
	FLM:14223	2d	0.165	1.25
	saiki1996numerical	2d	0.171	1.26
	FLM:14223	3d	0.164	1.24
	liu1998preconditioned	3d	0.165	1.35 ± 0.05
Experimental	berger1972periodic	-	0.16 – 0.17	-
	clift2005bubbles	-	-	1.24
13. April 2016 fdy TUD Simone Stange 28	williamson1996vortex	-	0.164	fdy -

Simulation at $Re = 200$



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Re = 200	Source	2d/3d	St	C_D
Numerical – Incompressible	belov1995new	2d	0.193	1.19 ± 0.04
	gresho1984modified	2d	0.21	1.76
	linnick2005high ($\lambda = 0.056$)	2d	0.199	1.37 ± 0.04
	linnick2005high ($\lambda = 0.023$)	2d	0.197	1.34 ± 0.04
	miyake1992numerical	2d	0.196	1.34 ± 0.04
	FLM:14223	2d	0.198	1.321
	saiki1996numerical	2d	0.197	1.18
	FLM:14223	3d	0.181	1.306
	liu1998preconditioned	3d	0.192	1.31 ± 0.04
Experimental	berger1972periodic	-	0.18 – 0.19	-
	clift2005bubbles	-	-	1.16
	williamson1996vortex	-	0.181	<u>fdy</u>



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Summary



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conclusion



future works

The End



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ende, fragen



bibliography



alle tabellen und graphen die man brauchen könnte in anhang

