DiffTrace: Efficient Whole-Program Trace Analysis and Diffing

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***Abstract*— Abstract to be written**
***Index Terms*—diffing, tracing, debugging**

I. Introduction

BEGIN Ganesh

Debugging high performance computing code remains a challenge at all levels of scale. Conventional HPC debuggers [**?**], [**?**], [**?**] excel at many tasks such as examining the execution state of a complex simulation at a detailed level and allowing the developer to re-execute the program close to the point of failure. However, they do not provide a good understanding of why a program version that worked earlier failed upon upgrade or feature addition. Innovative solutions are needed to highlight the salient differences between two executions in a manner that makes debugging easier as well as more systematic. A recent study conducted under the auspices of the DOE [**?**] provides a comprehensive survey of existing debugging tools. It classifies them under *four* software organizations (serial, multithreaded, multi-process, and hybrid), *six* method types (formal methods, static analysis, dynamic analysis, nondeterminism control, anomaly detection, and parallel debugging), and lists a total of 30 specific tools. Despite this abundance of tools and approaches, many significant problems remain to be solved before debugging *can be approached by the HPC community as a collaborative activity* so that HPC developers can share their solutions and extend a common framework **Need more build-up; will do later.**

In this paper, we provide our fundamentally fresh look at debugging. We point out three significant problems that we have addressed in our work, and provide our preliminary solutions backed up by case studies. While our work has not (yet) addressed the situations in which millions of threads and thousands of processes run for days and produce an error, we strongly believe that we can get there only through a series of *rigorous* approaches that overcome key limitations found in conventional debugging approaches in a step-by-step manner, accompanied by careful measurements of the merits of the new approach. The main contribution of this paper is the first such critical measurements of our proposed approach.

a) Problem-1: Need to Generalize Approaches for Outlier Detection:: Almost all debugging approaches seek to find outliers ("unexpected executions") amongst thousands of running processes and threads. The approach taken by most existing tools is to look for symptoms in a specific bug-class that they cover. Unfortunately, this approach calls for a programmer having a good guess of what the underlying problem might be, and to then pick the right set of tools to deploy. If the guess is wrong, the programmer has no choice but to refine their guess and look for bugs in another class, re-executing the application and hoping for better luck with another tool. This iterative loop of re-execution followed by applying a best-guess tool for the suspected bug class can potentially consume large amounts of execution cycles and also waste an expert developer's time.

Solution to Problem-1: Whole Program Tracing for Debugging: In this setting, our first contribution is a debugging approach in which the application is not merely run with a single symptom-specific tool attached as described earlier. Instead, we collect *whole program traces* of function calls and returns, using a PIN-based function call tracing facility called ParLoT that we have developed and previously reported [**?**]. We store these traces for potential examination by multiple tools and approaches. The advantage of whole program binary tracing supported in ParLoT is that we can collect function calls at *any desired level of abstraction*. For instance, if the programmer wants to cover activities at the MPI level, the OpenMP level and perhaps even lower levels (e.g., the MPI library or the OpenMP runtime), they can do so using ParLoT.

Clearly, the more APIs at which function calls are recorded, the more burdensome trace collection becomes. However, the advantage is that correspondingly more tools can then be applied to the collected traces. There is always a sweet-spot in this trade-off space, depending on the particular debugging situation. However, our fundamental insight is that *given the inevitability of heterogeneous programming* (the use of multiple concurrency models), it is important to be collecting traces from a few related APIs at a time, so that one can study bugs in one of the concurrency models or a bug resulting from a bad cross-model interaction from a *single run of the program*.

In our research, we have thus far demonstrated the advantage of ParLoT with respect to collecting both MPI and OpenMP traces from a *single run of a hybrid MPI/OpenMP program*. We demonstrate that from this single type of traces, it is possible to pick out MPI-level bugs or OpenMP-level bugs.

While we have not covered all these combinations in our work so far, the main contribution claimed is the ability to cover multiple APIs while debugging, and without re-executions or guess-work.

While this approach to whole-program tracing may sound extremely computation intensive, we employ novel on-the-fly compression techniques within ParLoT. In our previous study [**?**], we report compression efficiencies exceeding 16,000. This allows us to bring out the function call traces without significantly burdening the memory subsystem or I/O networks in the HPC cluster.

b) Problem-2: Need to Generalize Approaches for Outlier Detection:: Given that outlier detection is central to debugging, it is important to be employing efficient representations of the traces collected from threads and processes so that one can compute *distances* between these traces more systematically, without involving human reasoning in the loop. The representation must also be versatile enough to be able to "Diff" the traces[1] with respect to *an extensible number of vantage points*. These vantage points could be diffing with respect to process level activities, diffing with respect to thread-level activities, a combination thereof, or even finite sequences of process/thread calls (say, to locate *changes* in caller/callee relationships).

Solution to Problem-2: Use of Concept Lattices in Debugging: In DiffTrace, we employ *concept lattices* to amalgamate the collected traces. Concept lattices have previously been employed in HPC to perform structural clustering of process behaviors [**?**] to present performance data more meaningfully to users. The authors of that paper employ the notion of *Jaccard distances* to cluster performance results that are closely related to process structures (determined based on caller/callee relationships).

In DiffTrace, we employ incremental algorithms for building and maintaining concept lattices from the ParLoT-collected traces. In addition to Jaccard distances, in our work we also perform hierarchical clustering of traces and provide a tunable threshold for outlier detection. We believe that these uses of concept lattices and more refinement approaches for outlier detection are new in HPC debugging.

c) Problem-3: Loop Detection:: Most programs spend most of their time in loops. Therefore it is important to employ state-of-the-art algorithms for loop extraction from execution traces. It is also important to be able to diff two executions with respect to changes in their looping behaviors.

Solution to Problem-3: Rigorous Approaches to Loop Analysis: In DiffTrace, we employ the notion of NLRs (what does it stand for?) for extracting loops. Each repetitive loop structure is given an identifier, and nested loops are expressed as repetitions of this identifier exponentiated (as with regular expressions). This approach to summarizing loops can help manifest bugs where the program does not hang or crash, but nevertheless run differently in a manner that informs the developer engaged in debugging.

[1]Hence the name of our tool, **DiffTrace**.

To summarize, the key contributions of this paper are the following [[fix the section numbers later]]:

- A method to organize function call traces collected from processes and threads into concept lattices, and a method to detect loops from dynamic traces (Section **??**).
- Details of the algorithms employed in DiffTrace (Section **??**).
- Experimental studies on a heterogeneous program called Iterated Local Champion Search (ILCS, Section **??**).
- Strengths and limitations of DiffTrace, plans for future work (Section **??**).

END Ganesh

[[Ganesh and Saeed have written some text before for the intro which is available in v0/intro.tex (also available but commented in current file). Current version is based on our discussion on May 8th]]

- Importance of whole program diffing : understand changes, debug (DOE REPORT [1])
- Efficient tracing supports selective monitoring at multiple levels
  - Bugs not there at a predictable API level
  - Prior work (ParLoT) supports whole program tr.
- Dissimilarity is important to know: bugs, changes during porting,...
- Key enablers of meaningful diffing:
  - Formal concepts (novel contrib to debugging)
  - Loop detection (loop diffing can help)
- Importance, given the growing heterogeneity

** TODO: Highlights of results obtained as a result of the above thinking should be here. This typically comes before ROADMAP of paper.

In summary, this paper makes the following main contributions:

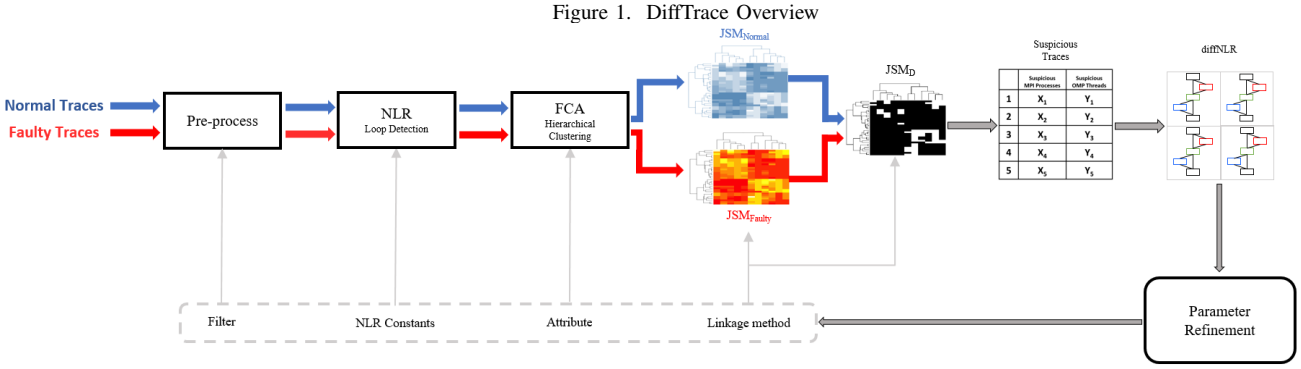
- A tunable tracing and trace-analysis tool-chain for HPC application program understanding and debugging
- A variation of the NLR algorithm to compress traces in lossless fashion for easier analysis and detecting (broken) loop structures
- An FCA-based clustering approach to efficiently classify traces with similar behavior
- A tunable ranking mechanism to highlight suspicious trace instances for deeper study
- A visualization framework that reflects the points of differences or divergence in a pair of sequences.

The rest of the paper is as follows:
- Sec 2: Background
- Sec 3: Components
- Sec 4: Case Study: ILCS
- Sec 5: Related Work
- Sec 6: Concluding Remarks

II. DiffTrace Overview

The general idea is to utilize ParLOT [2] traces for studying HPC application behaviors towards fault detection and

Figure 1. DiffTrace Overview



localization. ParLOT collects whole-program function calls and returns via dynamic binary instrumentation [3], and incrementally compresses them on-the-fly. ParLOT instruments and encodes functions within the binary to unique integers at two major levels: *main image* only contains functions from the source-code and included APIs and *all images* that cover system and library functions as well. Upon termination of the application, ParLOT flushes out per-thread trace files containing compressed sequence of executed function IDs. The compression mechanism of ParLOT significantly reduces the time, memory and disk overhead, leaves the majority of the system bandwidth for the application. With the mindset of "*pay a little upfront to dramatically reduce the number of overall debug iterations*", ParLOT well overcomes the challenge of whole-program *trace collection* and leaves the *trace analysis* for offline post-mortem analysis, saving HPC resources.

In this paper, we introduce DiffTrace, a tool-chain (figure 1) that provides infrastructures for *iterative and configurable search space reduction* of HPC traces. Considering a "successful" termination of the application as *normal behavior*, DiffTrace systematically reduces the search space to detect a *abnormal behavior* when an application crashes, time outs or produces a corrupted answer. Each abnormal behavior is a potential *error* cause or a manifestation of a *fault*. However, faults in HPC applications may occur or influence the program behavior at different locations and granularities, due to high and hybrid level of parallelism. Also typical HPC applications spend most of their execution time in a main loop until a convergence or over timesteps, and a fault may get triggered or causing problems after some iteration. Thus DiffTrace gives the HPC developers the capability of going through the pipeline of trace processing multiple times, each time putting a flash-light on various aspects of the applications' dynamic behavior, gradually collecting evidence about what went wrong that made the program fails.

The work-flow of DiffTrace starts with *pre-processing* traces. ParLOT traces are highly compressed and often contain functions that might no be interesting from a certain point of analysis. DiffTrace decompresses and prunes traces (systemically), providing cleaner traces for later phases.

Loops in source codes reflect themselves as a sequence of

Figure 2. Simplified MPI implementation of Odd/Even Sort

	Main Function	oddEvenSort()
1	`int main(){`	`oddEvenSort(rank, cp){`
2	`  int rank,cp;`	`  ...`
3	`  MPI_Init()`	`  for (int i=0; i < cp; i++)`
4	`  MPI_Comm_rank(..., &rank);`	`  {`
5	`  MPI_Comm_size(..., &cp);`	`   int ptr = findPtr(i, rank);`
6	`  // initialize data to sort`	`   ...`
7	`  int *data[data_size];`	`   if (rank % 2 == 0) {`
8	`  ...`	`    MPI_Send(..., ptr, ...);`
9	`  oddEvenSort(rank, cp);`	`    MPI_Recv(..., ptr, ...);`
10	`  ...`	`   } else {`
11	`  MPI_Finalize();`	`    MPI_Recv(..., ptr, ...);`
12	`}`	`    MPI_Send(..., ptr, ...);`
13		`   }`
14		`   ...`
15		`  }`
16		`}`

repetitive patterns, resulting in often-long but redundant traces. A "nested loop recognition" mechanism then mines loops from traces as "*a measure of progress*" per thread, and also a lossless abstraction to ease the rest of trace analysis. The control flow of events in parallel architectures often follow a *regular pattern* such as SPMD, odd-even and master/slave. This characteristic often makes all traces of a single execution tend to fall into just *a few* "conceptually/behaviorally equivalent classes". Adapted from the work by Webber et al [42], we have applied *formal concept analysis* (FCA)[14] techniques to reduce the trace search space into a few classes of traces, and also using the *concept lattice* (CL) data structure as the *model* of execution for further analysis. To reveal the impact of the fault, DiffTrace then measures the similarity between the equivalent classes of faulty traces against the corresponding bug-free traces. The basic idea is to find out which traces (and consequently processes/threads) are falling into a different class (i.e., cluster) when the fault is introduced. Based on the observed similarity of two clusterings, DiffTrace suggests top suspicious traces that are suffering the most from the fault for further analysis, and clearly reflects the actual points of differences of the suspicious trace versus its corresponding normal trace.

During the rest of this section, we explain each component of DiffTrace in details on collected traces (ParLOT-main) of execution of a MPI implementation of odd/even sort (figure 2. Odd/Even sort is a variant of the bubble-sort operates in two alternate phases: *Phase-even* where even processes

Table I
PRE-DEFINED FILTERS

Category	Sub-Category	Description
Primary	Returns	Filter out all returns
	PLT	Filter out the ".plt" function calls for external functions/procedures that their address needs to be resolved dynamically from Procedure Linkage Table (PLT)
MPI	MPI All	Only keep functions that start with "MPI_"
	MPI Collectives	Only keep MPI collective calls (MPI_Barrier, MPI_Allreduce, etc)
	MPI Send/Recv	Only keep MPI_Send, MPI_Isend, MPI_Recv, MPI_Irecv and MPI_Wait
	MPI Internal Library	Keep all inner MPI library calls
OMP	OMP All	Only keep OMP calls (starting with GOMP_)
	OMP Critical	Only keep OMP_CRITICAL_START and OMP_CRITICAL_END
	OMP Mutex	Only keep OMP_Mutex calls
System	Memory	Keep any memory related functions (memcpy, memchk, alloc, malloc, etc)
	Network	Keep any network related functions (network, tcp, sched, etc)
	Poll	Keep any poll related functions (poll, yield, sched, etc)
	String	Keep any string related functions (strlen, strcpy, etc)
Advanced	Custom	Any regular expression can be captured
	Everything	Does not filter anything

exchange (compare and swap) values with right neighbors and *Phase-odd* where odd processes exchange values with right neighbors. The for loop in line 4 of `oddEvenSort()` iterates over phases of the algorithm and based on the phase, the appropriate partner for each rank is getting discovered by the function `findPtr()` (line 6). The odd/even ranks then exchange their chunks of data (lines 9-13) and a set of sort, merge and copy operations would be performed on received data by each rank (which are replaced by `...` in line 15 for simplicity).

According to MPI Standard , MPI_Send is a *blocking send* used the *standard* communication mode in which MPI *may* buffer outgoing messages and the send call may complete before a matching receive is invoked. On the other hand, buffer space may be unavailable, or MPI may choose not to buffer outgoing messages, for performance reasons. In this case, the send call will not complete until a matching receive has been posted, and the data has been moved to the receiver. So based on the MPI implementation, a swap of order in line 11-12 of figure 7 code might end up causing a deadlock. This section ends with showing that DiffTrace can extract evidences from traces to justify and locate the cause of such deadlocks and other faults.

A. Pre-processing

Using ParLOT decoder, each trace needs to get decompressed for further analysis. Supporting the iterative approach of DiffTrace which is exploring different aspects of traces one at a time, corresponding function names of each function ID in traces are checked with some pre-defined (table VIII) or custom regular expressions (i.e., *filters*). In case of a match, DiffTrace would keep that function ID for later phases, otherwise that function ID would not be stored in the current iteration of DiffTrace.

Table II shows pre-processed traces (T_i) of odd/even sort execution with 4 processes. T_i is the trace that stores dynamic function calls of process i.

B. Nested Loop Representation

HPC applications often spend most of their times in *loops*. Function calls within each loop body reflect themselves as *repetitive patterns* in ParLOT traces, leaving often long traces

Table II
THE GENERATED TRACES FOR ODD/EVEN EXECUTION WITH FOUR PROCESSES

T_0	T_1	T_2	T_3
...	...	...	...
main	main	main	main
MPI_Init	MPI_Init	MPI_Init	MPI_Init
MPI_Comm_Rank	MPI_Comm_Rank	MPI_Comm_Rank	MPI_Comm_Rank
MPI_Comm_Size	MPI_Comm_Size	MPI_Comm_Size	MPI_Comm_Size
...	...	...	...
oddEvenSort	oddEvenSort	oddEvenSort	oddEvenSort
...	...	...	...
findPtr	findPtr	findPtr	findPtr
MPI_Send	MPI_Recv	MPI_Send	MPI_Recv
MPI_Recv	MPI_Send	MPI_Recv	MPI_Send
...	...	...	...
findPtr	findPtr	findPtr	findPtr
MPI_Send	MPI_Recv	MPI_Send	MPI_Recv
MPI_Recv	MPI_Send	MPI_Recv	MPI_Send
...	...	...	...
MPI_Finalize	MPI_Finalize	MPI_Finalize	MPI_Finalize

Figure 3. Trace NLRs

T0	T1	T2	T3
MPI_Init()	MPI_Init()	MPI_Init()	MPI_Init()
MPI_Comm_Rank()	MPI_Comm_Rank()	MPI_Comm_Rank()	MPI_Comm_Rank()
MPI_Comm_Size()	MPI_Comm_Size()	MPI_Comm_Size()	MPI_Comm_Size()
L0 ^ 2	L1 ^ 4	L0 ^ 4	L1 ^ 2
MPI_Finalize()	MPI_Finalize()	MPI_Finalize()	MPI_Finalize()

of redundant entries. Inspired by ideas from detection of repetitive patterns in strings [51] and other data structures[50], we have adapted the Nested Loop Recognition (NLR) algorithm from Ketterlin et al[13] to detect repetitive patterns in ParLOT traces (details of NLR algorithm are in section XX). Detecting such patterns "measures progress" per trace and reflects the delayed or unfinished/broken loops, potentially caused by a fault.

For example, the loop in line 3 of `oddEvenSort()` (figure 2) iterates 4 times in execution with 4 processes. Thus each T_i contains 4 consecutive occurrence of either `MPI_Send() - MPI_Recv()` (even Ts) or `MPI_Recv() - MPI_Send()` (odd Ts). By keeping only MPI functions and converting each T_i to its equivalent NLR (Nested Loop Representation), table II can be reduced to figure 3. **L0** (pair of MPI_Send - MPI_Recv) and **L1** (pair of MPI_Recv - MPI_Send) are two main body loops that have been detected among pre-processed filters. Note that, since first and last processes have only one-way communication with their neighbors, T_0 and T_3 iterates over the loop half of other processes.

connect this section to next

C. Hierarchical Clustering via FCA

Underlying parallel software architecture of HPC applications often follow a *regular pattern* with respect to sequences of executed functions. Considering this characteristic, per-thread individual function call traces can be classified into *a few equivalent groups* based on the *conceptual structure of trace contents*(i.e., sequence of functions). Such classification would distinguish naturally different threads (e.g., MPI processes from OpenMP threads in hybrid MPI+OpenMP applications), reduce the search space into just a few representative classes of traces and ease the process of detecting outlier

Figure 4. Formal Concept Definition

For subsets A ⊆ G of objects and subsets B ⊆ M of attributes, one defines two derivation operators as follows:
A' = {m ∈ M | (g,m) ∈ I for all g ∈ A}, and dually
B' = {g ∈ G | (g,m) ∈ I for all m ∈ B}.
Applying either derivation operator and then the other constitutes two closure operators:
A ↦ A'' = (A')' for A ⊆ G (extent closure), and
B ↦ B'' = (B')' for B ⊆ M (intent closure).

Definition of a formal concept: a pair (A,B) is a formal concept of a context (G, M, I) provided that:
$A \subseteq G$, $B \subseteq M$, $A' = B$, and $B' = A$.
Equivalently and more intuitively, (A,B) is a **formal concept** precisely when:

- every object in A has every attribute in B,
- for every object in G that is not in A, there is some attribute in B that the object does not have,
- for every attribute in M that is not in B, there is some object in A that does not have that attribute.

traces. In addition, the set of per-thread traces should be studied as "a whole" since there is a strong conceptual and causal relation among threads/processes. In order to integrate all collected traces into a *single model of execution* and forming "equivalent classes of traces", we have adapted the idea of *Structural Clustering* [42] by applying *formal concept analysis* (FCA)[14] techniques to ParLOT traces.

A *formal context* is a triple $K = (G, M, I)$, where G is a set of **objects**, M is a set of **attributes**, and $I \subseteq G \times M$ is an incidence relation that expresses *which objects have which attributes*. Table II-C) shows the formal context of odd/even sort pre-processed traces.

In this context, attributes are trace entries (function calls or detected loop bodies) without involving their frequency (e.g., loop counts). However, any set of attributes can be extracted from traces (table YY). Definition of formal concept (needed?) figure 4 :

A *concept lattice* can be derived from a *formal context* by specifying *formal concepts* (figure 4) and a *partial order* on them. Concept lattices are represented as a directed acyclic graph where concepts are nodes and the order on them determines the edges. Figure 5 shows the concept lattice of the formal context in The formal context in table II-C shows that all traces has the functions MPI_Init(), MPI_Comm_size(), MPI_Comm_rank() and MPI_Finalize(). Even traces have the loop *L0* and odd traces have the loop *L1*. The resulting concept lattice from this context is shown in figure 5 and reads as:

- The top node indicates that all traces share MPI_Init(), MPI_Comm_size(), MPI_Comm_rank() and MPI_Finalize().
- The bottom node signifies that none of the traces share all attributes.
- The middle nodes show that T_0 and T_2 are different from T_1 and T_3

We have used concept lattices to obtain pair-wise *similarity scores* among traces. The similarity metric that we have used is *Jaccard Index*, also known as *Intersection over Union*. For any

Table III
FORMAL CONTEXT OF ODD/EVEN SORT EXAMPLE

	MPI_Init()	MPI_Comm_Size()	MPI_Comm_Rank()	L0	L1	MPI_Finalize()
Trace 0	×	×	×	×		×
Trace 1	×	×	×		×	×
Trace 2	×	×	×	×		×
Trace 3	×	×	×		×	×

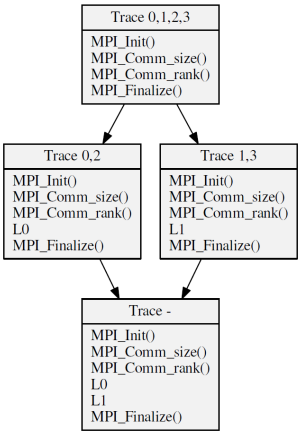


Figure 5. Sample Concept Lattice from Obj-Atr Context in tableII-C

pair of (T_i, T_j), number of attributes in the Lowest Common Ancestor (LCA) node of T_i and T_j is the number of attributes that T_i and T_j have in common (intersection). The sum of the number of attributes of nodes in the path from each T_i and T_j to their LCA is the union. Figure 6 shows the heatmap of full pair-wise Jaccard Similarity Matrix (JSM) obtained from the concept lattice in figure 5. DiffTrace uses obtained JSMs as *linkage* function to form equivalent classes of traces by hierarchical clustering. In the next phase of DiffTrace, we show how the differences of two hierarchical clustering from two executions (faulty vs. normal) can reveal which traces has been changed the most by the fault.

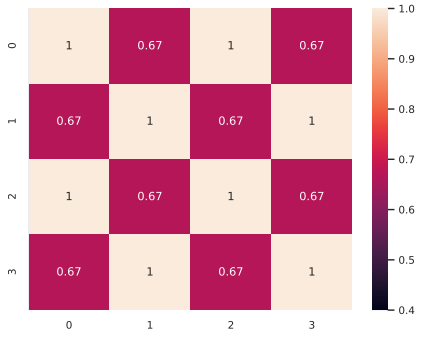


Figure 6. Pair-wise Jaccard Similarity Matrix (JSM) of MPI processes in Sample code

Figure 7. A line change in oddEvenSort (left) that might cause a deadlock in oddEvenSort_DL (right)

	oddEvenSort()	oddEvenSort_DL()
1	`oddEvenSort(rank, cp){`	`oddEvenSort_DL(rank, cp){`
2	`...`	`...`
3	`for (int i=0; i < cp; i++)`	`for (int i=0; i < cp; i++)`
4	`{`	`{`
5	`int ptr = findPtr(i, rank);`	`int ptr = findPtr(i, rank);`
6	`...`	`...`
7	`if (rank % 2 == 0) {`	`if (rank % 2 == 0) {`
8	`MPI_Send(..., ptr, ...);`	`MPI_Send(..., ptr, ...);`
9	`MPI_Recv(..., ptr, ...);`	`MPI_Recv(..., ptr, ...);`
10	`} else {`	`} else {`
11	`MPI_Recv(..., ptr, ...);`	`MPI_Send(..., ptr, ...);`
12	`MPI_Send(..., ptr, ...);`	`MPI_Recv(..., ptr, ...);`
13	`}`	`}`
14	`...`	`...`
15	`}`	`}`
16	`}`	`}`

D. Detecting Suspicious Traces via DiffJSM

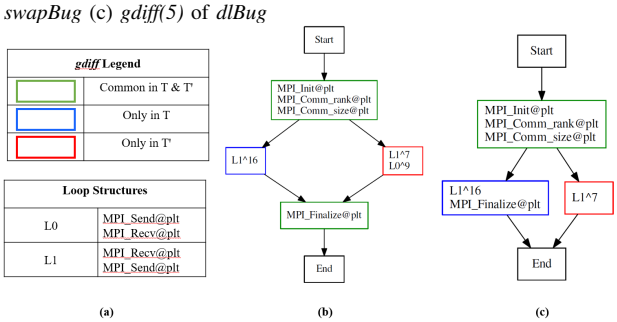
Up to this point, DiffTrace can narrow down the search space from numerous long traces to their equivalent JSM (i.e., clusters). As the original goal of DiffTrace implies, we are interested in detecting what has changed the most when a fault is introduced with respect to the "natural asymmetry" of the application. In other words, DiffTrace abstracts function call traces into JSMs which are reflections of asymmetry among traces. Now the hierarchical clustering based on the *DiffJSM*, the subtraction of the faulty JSM from its corresponding normal JSM, would put the trace(s) that changed the most in a separate cluster from the others (i.e., outlier). The obtained outlier traces are candidates of the potential cause of the change in the program behavior, thus a potential fault root cause or fault manifestation. However, a single iteration of DiffTrace (with a single set of parameters shown as dotted box in figure 1) might not reflect such asymmetries in the normal and faulty traces. Also different set of parameters might produce inaccurate suggestions (false positives).

We have used We have used the *B-score* similarity metric of two hierarchical clustering by Fowlkes et al [20] to and obtained the DiffJSM by subtra JSMs reflect the *asymmetry* of traces. Now the goal is to see which traces or which region of a trace is causing a *change* in the execution with respect to the application's *natural asymmetry*. proposed a similarity metric (B-score) for comparison of two hierarchical clustering. B-score of two JSMs is computed by counting the number of objects that happen to fall into a different cluster. DiffTrace first measures the B-score of faulty JSM with its corresponding normal JSM.

To clearly see what has changed in the actual (suspicious) trace of a faulty execution with its corresponding trace from the normal run, we have implemented a visualized version of

- Comparison of JSMs (i.e., hierarchical clusterings) would give insight about how a change (bug, library update, porting to new system) has changed the behavior of the program.
- Outlier detection via Diffing JSMs
  - the method by Fowlkes to measure the similarity score of two clusterings
  - detecting outlier(s) by detecting if an object (trace) falls into a different cluster
  - an illustration of the idea on odd/even - explaining a potential deadlock.
- introducing *gdiff*: bolds the actual points of differences in the outlier trace w.r.t. its corresponding normal trace
- sample gdiffs from odd/even example

Figure 8. (a) The legend of *gdiff* and the list of loop structures (b) *gdiff(5)* of *swapBug* (c) *gdiff(5)* of *dlBug*



1) Ranking Suspicious Traces:

- Select a set of parameters and let DiffTrace generate JSMs based on the parameters (from both buggy and bug-free).
- Calculate B-score and outliers for all possible combinations of parameters
- sort outliers (i.e., suggestions as suspicious traces that suffer the most from the change) based on their B-score, lower scores shows bigger change in JSMs, higher chance of showing the actual outlier.

"Diff" algorithm by Meyers [19] takes two sequences S_A and S_B and computes the minimal *edit* to convert S_A to S_B. This algorithm has been used in GNU `diff` to compare two text files and in git for efficiently keeping track of file changes. Since ParLOT preserves the order of function calls in the binary, each per thread trace T_i is totally ordered, thus *diff* can reflect the differences of a pair of Ts. *gdiff* is the graphical visualization of diff, aligning common and different blocks of a pair of sequences horizontally and vertically, making it easier for analyst to see the differences of a pair of sequences in a glance. For simplicity, our implementation of *gdiff* only takes one argument x as *the suspicious trace*

$gdiff(x) \equiv gdiff(T_x, T'_x)$

where T_x is the trace of thread/process x of a normal/successful execution and T'_x is the corresponding trace of faulty execution.

The for loop in line 4 of `oddEvenSort()` iterates over phases of the algorithm and based on the phase, the appropriate partner for each rank is getting discovered by the function `findPtr()` (line 6). The odd/even ranks then exchange their chunks of data (lines 9-13) and a set of sort, merge and copy operations would be performed on received data by each rank (which are replaced by `...` in line 15 for simplicity).

Execution of odd/even sort application with four processes (`mpirun -np 4`) while ParLOT trace collection is enabled on top of the application, would result in T_0, T_1, T_2 and T_3 (table II). This execution terminates successfully with expected results and the set of generated traces clearly reflects the expected behavior (control flow) of odd and even processes.

We have planted two artificial bugs (*swapBug* and *dlBug*) in the code in figure 2 and launched the code with 16 processes. *swapBug* swaps the order of MPI_Send and MPI_Recv in rank 5 after 7th iteration (of the loop in line 3 of `oddEvenSort`) simulating a potential deadlock and *dlBug* simulates an actual deadlock (e.g., infinite loop) in the same location (rank 5 after 7th iteration). Upon collection of ParLOT traces from execution above buggy versions, DiffTrace first decompresses traces and filters out all non-MPI functions. Then two major loops are detected, **L0** and **L1** (figure 8-(a)) that are supposed to occur 16 times in even and odd ranks, respectively. After analysis of CL models of execution, $x = 5$ has been suggested as the most affected trace by the artificial bugs. Figure 8-(b) shows the *gdiff*(5) of *swapBug* where T_5 iterates over the loop [MPI_Recv - MPI_Send] for 16 times (L1^16) after the MPI initilization while the order swap has well reflected in T'_x (L1^7 - L0^9). Both processes seem to be terminated fine by executing MPI_Finalize(). However, *gdiff*(5) of *dlBug* (figure 8-(c)) shows that while T_5 have executed MPI_Finalize and terminated well, T'_5 got stuck after executing L1 seven times and have never reached MPI_Finalize.

This example shows that our approach can locate the impacted part of each execution by a fault. Having a pre-understanding of *how the application should behave normally* would reduce the number of iterations by picking the right set of parameters on each pass.

Table IV
ILCSTSP.MC1-MC-6-N1.M.8.AUTO

Filter	Attributes	Link Method	Thresh	B-score	Top Procs (JSMD)	TOP Threads(JSMD)
01.mem.ompall.cust.0K10	sing.actual	average	4	0.308594		6.2 , 6.4 , 5.2 , 5.4 , 7.3 ,
11.mem.ompall.cust.0K10	sing.actual	average	4	0.308594		6.2 , 6.4 , 5.2 , 5.4 , 7.3 ,
01.mem.ompmutex.cust.0K10	sing.actual	weighted	4	0.321883		6.2 , 3.4 , 5.3 , 4.2 , 7.4 ,
11.mem.ompmutex.cust.0K10	sing.actual	weighted	4	0.321883		6.2 , 3.4 , 5.3 , 4.2 , 7.4 ,
11.plt.mem.mpi.ompcrit.cust.0K10	doub.actual	weighted	4	0.324427	3 ,	0.2 , 1.1 , 3.1 , 4.3 , 4.4 , 5.2 ,
01.plt.mem.mpi.ompcrit.cust.0K10	doub.actual	weighted	4	0.324427	3 ,	0.2 , 1.1 , 3.1 , 4.3 , 4.4 , 5.2 ,
01.mem.ompall.cust.0K10	doub.actual	weighted	4	0.33266	3 ,	6.4 , 7.1 , 3.4 , 4.3 , 4.4 , 5.2 ,
11.mem.ompall.cust.0K10	doub.actual	weighted	4	0.33266	3 ,	6.4 , 7.1 , 3.4 , 4.3 , 4.4 , 5.2 ,
01.mem.ompcrit.cust.0K10	sing.actual	weighted	4	0.354396	6 ,	7.2 , 7.4 , 3.4 , 4.2 , 4.3 , 4.4 ,
11.mem.ompcrit.cust.0K10	sing.actual	weighted	4	0.354396	6 ,	7.2 , 7.4 , 3.4 , 4.2 , 4.3 , 4.4 ,
11.plt.mem.mpi.ompcrit.cust.0K10	doub.actual	average	4	0.381646		3.3 , 2.4 ,

Table V
ILCSTSP.MC1-MC-2-2.M.8.AUTO

Filter	Attributes	Link Method	Thresh	B-score	Top Procs (JSMD)	TOP Threads(JSMD)
01.mem.ompall.cust.0K10	doub.actual	weighted	4	0.309391	3 ,	6.2 , 6.4 , 7.1 , 7.4 , 1.3 , 3.1 ,
11.mem.ompall.cust.0K10	doub.actual	weighted	4	0.309391	3 ,	6.2 , 6.4 , 7.1 , 7.4 , 1.3 , 3.1 ,
11.plt.mem.cust.0K10	doub.actual	weighted	4	0.318003	7 , 4 ,	1.3 , 2.2 , 3.3 , 3.4 , 4.2 , 4.3 ,
01.plt.mem.cust.0K10	doub.actual	weighted	4	0.318003	7 , 4 ,	1.3 , 2.2 , 3.3 , 3.4 , 4.2 , 4.3 ,
01.mem.ompall.cust.0K10	doub.actual	average	4	0.34462	7 , 3 ,	7.1 , 1.3 , 1.4 , 2.2 , 2.3 , 3.1 ,
11.mem.ompall.cust.0K10	doub.actual	average	4	0.34462	7 , 3 ,	7.1 , 1.3 , 1.4 , 2.2 , 2.3 , 3.1 ,
11.plt.mem.mpi.ompcrit.cust.0K10	doub.actual	average	4	0.350702	7 , 3 ,	6.2 , 6.3 , 7.2 , 2.4 , 3.3 , 4.2 ,
01.plt.mem.mpi.ompcrit.cust.0K10	doub.actual	average	4	0.350702	7 , 3 ,	6.2 , 6.3 , 7.2 , 2.4 , 3.3 , 4.2 ,
11.plt.mem.cust.0K10	doub.actual	weighted	3	0.357334	7 ,	2.2 , 3.3 , 3.4 , 4.3 , 4.4 ,
01.plt.mem.cust.0K10	doub.actual	weighted	3	0.357334	7 ,	2.2 , 3.3 , 3.4 , 4.3 , 4.4 ,
01.mem.ompall.cust.0K10	doub.actual	weighted	3	0.380481	3 ,	7.1 , 1.3 , 3.1 , 4.3 , 4.4 ,

III. CASE STUDY: ILCS

Table VI
ILCSTSP.AR2-WO-2-NN.M.8.AUTO

Filter	Attributes	Link Method	Thresh	B-score	Top Procs (JSMD)	TOP Threads(JSMD)
01.plt.cust.0K10	doub.actual	average	4	0.392446	6 ,	2.3 , 2.4 , 4.2 , 4.3 , 4.4 ,
11.plt.cust.0K10	doub.actual	average	4	0.392446	6 ,	2.3 , 2.4 , 4.2 , 4.3 , 4.4 ,
01.plt.cust.0K10	sing.log10	centroid	4	0.945946	0 ,	6.2 , 0.4 , 1.1 , 0.1 , 2.3 , 2.4 ,
01.plt.cust.0K10	sing.log10	median	4	0.945946	0 ,	6.2 , 0.4 , 1.1 , 0.1 , 2.3 , 2.4 ,
11.plt.cust.0K10	sing.log10	centroid	4	0.945946	0 ,	6.2 , 0.4 , 1.1 , 0.1 , 2.3 , 2.4 ,
11.plt.cust.0K10	sing.log10	median	4	0.945946	0 ,	6.2 , 0.4 , 1.1 , 0.1 , 2.3 , 2.4 ,
01.plt.cust.0K10	sing.log10	median	3	0.947368	0 ,	6.2 , 0.4 , 1.1 , 0.1 , 2.3 , 2.4 ,
11.plt.cust.0K10	sing.log10	median	3	0.947368	0 ,	6.2 , 0.4 , 1.1 , 0.1 , 2.3 , 2.4 ,
01.plt.cust.0K10	sing.log10	complete	3	1	0 ,	0.1 , 7.1 , 1.1 , 3.1 , 3.3 ,
01.plt.cust.0K10	sing.log10	complete	4	1	0 ,	0.1 , 7.1 , 1.1 , 3.1 , 3.3 ,
01.plt.cust.0K10	sing.log10	average	4	1	0 ,	0.1 , 7.1 , 1.1 , 3.1 , 3.3 ,

Table VII
ILCSTSP.BC2-WR-3-NN.M.8.AUTO

Filter	Attributes	Link Method	Thresh	B-score	Top Procs (JSMD)	TOP Threads(JSMD)
01.plt.cust.0K10	doub.actual	centroid	4	0.512309	2 ,	6.4 , 7.3 , 1.2 , 1.3 , 2.1 , 2.2 ,
11.plt.cust.0K10	doub.actual	centroid	4	0.512309	2 ,	6.4 , 7.3 , 1.2 , 1.3 , 2.1 , 2.2 ,
01.plt.cust.0K10	sing.actual	average	4	0.513221	7 ,	3.4 , 5.2 , 4.2 , 4.3 ,
11.plt.cust.0K10	sing.actual	average	4	0.513221	7 ,	3.4 , 5.2 , 4.2 , 4.3 ,
11.mpi.cust.0K10	sing.actual	median	4	0.544807	0 ,	0.1 , 6.4 , 7.3 , 7.4 , 1.3 , 0.2 ,
11.mpiall.cust.0K10	sing.actual	median	4	0.544807	0 ,	0.1 , 6.4 , 7.3 , 7.4 , 1.3 , 0.2 ,
01.mpiall.cust.0K10	sing.actual	median	4	0.544807	0 ,	0.1 , 6.4 , 7.3 , 7.4 , 1.3 , 0.2 ,
01.mpicol.cust.0K10	sing.actual	median	4	0.544807	0 ,	0.1 , 6.4 , 7.3 , 7.4 , 1.3 , 0.2 ,
11.mpicol.cust.0K10	sing.actual	median	4	0.544807	0 ,	0.1 , 6.4 , 7.3 , 7.4 , 1.3 , 0.2 ,
01.mpi.cust.0K10	sing.actual	median	4	0.544807	0 ,	0.1 , 6.4 , 7.3 , 7.4 , 1.3 , 0.2 ,
01.plt.cust.0K10	doub.actual	centroid	3	0.639268	2 ,	6.4 , 7.3 , 1.2 , 1.3 , 2.1 , 2.2 ,

Table VIII
ILCSTSP.BC1-WS-3-NN.M.8.AUTO

Filter	Attributes	Link Method	Thresh	B-score	Top Procs (JSMD)	TOP Threads(JSMD)
11.mpi.cust.0K10	sing.actual	weighted	4	0.385229	6 ,	6.2 , 6.3 , 6.4 , 7.2 , 7.3 , 7.4 ,
11.mpiall.cust.0K10	sing.actual	weighted	4	0.385229	6 ,	6.2 , 6.3 , 6.4 , 7.2 , 7.3 , 7.4 ,
01.mpiall.cust.0K10	sing.actual	weighted	4	0.385229	6 ,	6.2 , 6.3 , 6.4 , 7.2 , 7.3 , 7.4 ,
01.mpicol.cust.0K10	sing.actual	weighted	4	0.385229	6 ,	6.2 , 6.3 , 6.4 , 7.2 , 7.3 , 7.4 ,
11.mpicol.cust.0K10	sing.actual	weighted	4	0.385229	6 ,	6.2 , 6.3 , 6.4 , 7.2 , 7.3 , 7.4 ,
01.mpi.cust.0K10	sing.actual	weighted	4	0.385229	6 ,	6.2 , 6.3 , 6.4 , 7.2 , 7.3 , 7.4 ,
01.plt.cust.0K10	sing.actual	weighted	4	0.448188	7 , 3 ,	6.2 , 6.4 , 7.1 , 7.4 , 3.3 , 3.4 ,
11.plt.cust.0K10	sing.actual	weighted	4	0.448188	7 , 3 ,	6.2 , 6.4 , 7.1 , 7.4 , 3.3 , 3.4 ,
11.mpi.cust.0K10	sing.actual	weighted	3	0.465043	6 ,	6.2 , 6.3 , 6.4 , 7.2 , 7.3 , 7.4 ,
11.mpiall.cust.0K10	sing.actual	weighted	3	0.465043	6 ,	6.2 , 6.3 , 6.4 , 7.2 , 7.3 , 7.4 ,
01.mpiall.cust.0K10	sing.actual	weighted	3	0.465043	6 ,	6.2 , 6.3 , 6.4 , 7.2 , 7.3 , 7.4 ,

IV. Case Study: ILCS

A. Experimental Methodology

So far, we are able to collect whole-program execution traces, preprocess them (decompress, filter, detect loops, extract attributes) and inject each PT to concept lattice data structure. Concept lattices help us having a single model for the execution of HPC application with thousands of processes/threads. Concept lattices also classify PTs based on their Jaccard distance. Full pair-wise Jaccard distance matrix can be extracted from the concept lattice in linear time and reduces the search space from thousands of PTs to just a few equivalent classes of PTs. Studying JSM by itself helps the user to understand the program behavior as a whole, and how each process/thread behaving. However, comparing the JSM of the bug-free version of the application versus the buggy version would reveal insights about how the bug impacted the behavior of the application. In particular, we are interested to see how the bug changes the formation of equivalent classes of PTs. Inspired by a method for comparing two different clustering [20], we count the number of objects (PTs) in each cluster and see which PT(s) fall into different clusters once the bug is introduced. A set of candidate PTs then would be reported to the user for more in-depth study. Here is where we take advantage of diffNLR to see how does the bug changes the control flow of a candidate PT comparing to its corresponding PT of native run.

Table 9 shows different parameters that we can pre-process PTs with. Each combination of these parameters would result in a different concept lattice, thus different JSM and different clusterings. A table similar to X is created for each injected bug. Each row of the table is showing the set of parameters used to create JSMs. Then by calculating $|JSM(buggy) - JSM(bugfree)|$ we are interested to see which PT changes the most after the bug injected and falls into a single cluster. The object(s) in the cluster with the fewest members (below a threshold) are potential candidates of *threads that are manifesting the bug* and the diff(buggy,bug-free) is in our interest to see how does the bug changes its control flow.

B. Case Study: ILCS-TSP

Here is the ILCS framework pseudo-code. User needs to write `CPU_Init()`,`CPU_Exec()` and `CPU_Output()`.

```
.
int main(argc,argv){
 MPI_Init();
 MPI_Comm_size()
 MPI_Comm_rank(my_rank)
 //Figuring local number of CPUs
 MPI_Reduce() // Figuring global number of CPUs
 CPU_Init();
 //For storing local champion results
 champ[CPUs] = malloc();
 MPI_Barrier();
 #pragma omp parallel num_threads(CPUs+1)
 {
  rank = omp_get_thread_num()
  if (rank == 0){ //communication thread
   do{
    //Find and report the thread with
    //local champion, global champion
    MPI_AllReduce();
    //Find and report the process with
    //global champion
    MPI_AllReduce();
    //The process with the global champion
    //copy its results to bcast_buffer
    if (my_rank == global_champion){
     #pragma omp cirtical
     memcpy(bcast_buffer,local_champ)
    }
    //Broadcast the champion
    MPI_Bcast(bcast_buffer)
   } while (no_change_threshold);
   cont=0 // signal worker threads to stop
  } else{ // worker threads
   while(cont){
    //Calculate Seed
    local_result = CPU_Exec()
    if (local_result < champ[rank]){
     #pragma omp cirtical
     memcpy(champ[rank],local_result)
    }
   }
  }
 }
 //Find and report the thread with
 //local champion, global champion
 MPI_AllReduce();
 //Find and report the process with
 //global champion
 MPI_AllReduce();
 // The process with the global champion
 // copy its results to bcast_buffer
 if (my_rank == global_champion){
  #pragma omp cirtical
  memcpy(bcast_buffer,local_champ)
 }
 //Broadcast the champion
 MPI_Bcast(bcast_buffer)
 if(my_rank==0){
  CPU_Output(champ)
 }
 MPI_Finalize()
}
/* User code for TSP problem */

CPU_Init(){
 // Read In data from cities
 // Calculate distances
```

<table>
<tr><th colspan="10">Filters</th><th rowspan="2" colspan="2">CL Attributes</th><th rowspan="2">Clustering</th></tr>
<tr><th colspan="2">Prime</th><th colspan="2">General</th><th colspan="2">MPI</th><th colspan="2">OMP</th><th colspan="2">Other</th></tr>
<tr><th>Filter</th><th>Description</th><th>Filter</th><th>Description</th><th>Filter</th><th>Description</th><th>Filter</th><th>Description</th><th>Filter</th><th>Description</th></tr>
<tr><td>ret</td><td>Filter Returns</td><td>@plt</td><td>...@plt</td><td>mpi</td><td>MPI_...</td><td>ompcrit</td><td>OMP critical</td><td>Custom</td><td>Defining specific regex to filter</td><td colspan="2">Objects: Traces
Attributes: set of <atr:freq></td><td>single</td></tr>
<tr><td>.plt</td><td>Filter .plts</td><td>mem</td><td>Memory related malloc memcpy etc</td><td>mpiall</td><td>..MPI...
MPID...
PMPI...</td><td>ompmutex</td><td>OMP mutex</td><td>incEverything</td><td>Include whatever is not in the Filters</td><td>Single: set of single trace entries
atr: sing</td><td>No Frequency: only presence of attribute entries matters
freq:-</td><td>complete</td></tr>
<tr><td></td><td></td><td>net</td><td>Network related</td><td>mpicol</td><td>MPI collectives</td><td>ompall</td><td>OMP all functions</td><td></td><td></td><td>Double: set of 2-consecutive entries
atr: doub</td><td>Log10: log(freq) of each entry matters (for large frequency numbers
freq: log10(#atr)</td><td>average</td></tr>
<tr><td></td><td></td><td>poll</td><td>Poll Related poll, yield</td><td>mpisr</td><td>MPI send/recv</td><td></td><td></td><td></td><td></td><td></td><td>Actual: actual frequency of each entry matters
freq: #atr</td><td>weighted</td></tr>
<tr><td></td><td></td><td>str</td><td>String related stcpy strcmp etc</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>centroid</td></tr>
<tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>median</td></tr>
<tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>ward</td></tr>
</table>

Figure 9. Filters, Attributes and other Parameters used to pre-process ParLOT Traces (PTs)

```
  // Return data structure to store champion
}

CPU_Exec(){
  // Find local champions (TSP tours)
}

CPU_Output(){
  // Output champion
}
```

Table **??** describes the bug that I injected to ILCS-TSP

Table IX
INJECTED BUGS TO ILCS-TSP

ID	Level	Bugs	Description
1	MPI	allRed1wrgOp-1-all-x	Different operation (MPI_MAX) in only one process (buggyProc = 2) for MPI_ALLREDUCE() in Line 21
2		allRed1wrgSize-1-all-x	Wrong size in only one process (buggyProc = 2) for MPI_ALLREDUCE() in Line 21
3		allRed1wrgSize-all-all-x	Wrong Size in all processes for MPI_ALLREDUCE() in Line 21
4		allRed2wrgOp-1-all-x	Different operation (MPI_MAX) in only one (buggyProc) for first MPI_ALLREDUCE() – L277:ilcsTSP.c
5		allRed2wrgSize-1-all-x	Wrong size in only one (buggyProc) for first MPI_ALLREDUCE() – L277:ilcsTSP.c
6		allRed2wrgSize-all-all-x	Wrong Size in all processes for second MPI_ALLREDUCE() – L277:ilcsTSP.c
7		bcastWrgSize-1-all-x	Wrong Size in only one (buggyProc) of MPI_Bcast() – L290:ilcsTSP.c
8		bcastWrgSize-all-all-x	Wrong Size n all processes for MPI_Bcast() – L240:ilcsTSP.c
9	OMP	misCrit-1-1-x	Missing Critical Section in buggyProc and buggyThread – L170:ilcsTSP.c
10		misCrit-all-1-x	Missing Critical Section in buggyThread and all prcoesses – L170:ilcsTSP.c
11		misCrit-1-all-x	Missing Critical Section in buggyProc and all threads – L170:ilcsTSP.c
12		misCrit-all-all-x	Missing Critical Section in all procs and threads – L170:ilcsTSP.c
13		misCrit2-1-1-x	Missing Critical Section in buggyProc and buggyThread – L230:ilcsTSP.c
14		misCrit2-all-1-x	Missing Critical Section in buggyThread – L230:ilcsTSP.c
15		misCrit2-1-all-x	Missing Critical Section in buggyProc and all threads – L230:ilcsTSP.c
16		misCrit2-all-all-x	Missing Critical Section in all procs and threads – L230:ilcsTSP.c
17		misCrit3-1-all-x	Missing Critical Section in buggyProc and all threads – L280:ilcsTSP.c
18		misCrit3-all-all-x	Missing Critical Section in all procs and threads – L280:ilcsTSP.c
19	General	infLoop-1-1-1	Injected an infinite loop after CPU_EXEC() in buggyProc,buggyThread & buggyIter L164:ilcsTSP.c

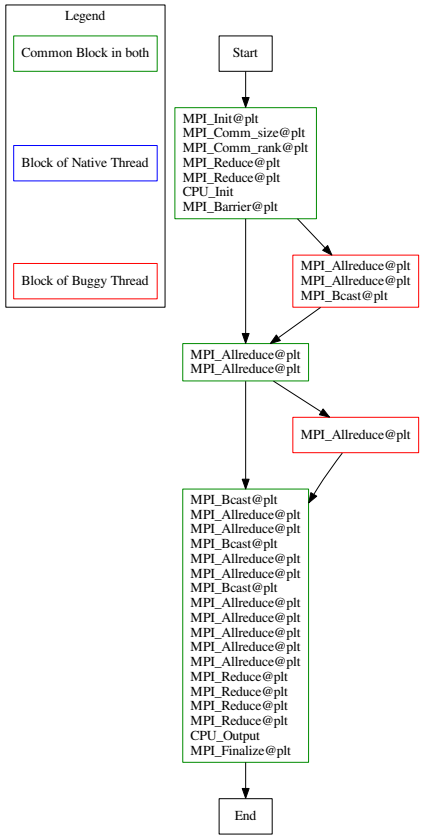


Figure 10. Bug1: diffNLR $PT_{0,0}$ - buggy vs. native

1) Bug1: Wrong Operation in MPI AllReduce(): We have injected a bug (row 1 table IX) where `MPI_Allreduce()` had been invoked with a wrong operation in one of the processes (P_2)(`MPI_MAX` instead of `MPI_MIN`).

::What is the runtime reaction to this bug:: Program terminated well without any error, crash, hang or throwing any exception. But the results might be corrupted. This might be a silent bug that diffTrace could reveal

The last row of table X is telling us that among all combinations of parameters (filters, attributes, etc.) PT 0 (ParLOT trace that belongs to thread 0 of process 0 got impacted the most after we inject the bug.

The target MPI_Allreduce() that we injected the bug to, finds the rank (i.e., process) that has the "champion" result among all of ranks using MPI_MIN operator. Then that champion rank copies its "champion results" to a global data-structure and broadcast the "champion results" to all other ranks for the next time step. However, since we changed the MPI_MIN to MPI_MAX in only one of the ranks, the true champion rank would get lost, instead a false champion rank (which turned to be rank 0 or $PT_{0,0}$) would broadcast its results as champion in the first time-step, causing a potential wrong answer.

Table X
BUG 1: WRONG MPI OPERATION IN ALLREDUCE() CANDIDATE TABLE

Filter	Attribute	K: # of diff Clusters	# Objects in each Cluster (CL i)	Candidate PT Outliers
11.mpi.cust.0K10	sing.orig	2	CL 0:34	-
			CL 1:6	-
11.mpi.cust.0K10	sing.orig	3	CL 0:34	-
			CL 1:5	{2 3 4 27 29 }
			CL 2:1	{22 }
11.mpi.cust.0K10	sing.orig	4	CL 0:3	{24 38 39 }
			CL 1:31	-
			CL 2:5	{2 3 4 27 29 }
			CL 3:1	{22 }
11.mpi.cust.0K10	sing.log10	2	CL 0:34	-
			CL 1:6	-
11.mpi.cust.0K10	sing.log10	3	CL 0:34	-
			CL 1:5	{2 3 4 27 29 }
			CL 2:1	{22 }
11.mpi.cust.0K10	sing.log10	4	CL 0:3	{24 38 39 }
			CL 1:31	-
			CL 2:5	{2 3 4 27 29 }
			CL 3:1	{22 }
11.mpi.cust.0K10	sing.actual	2	CL 0:34	-
			CL 1:6	-
11.mpi.cust.0K10	sing.actual	3	CL 0:34	-
			CL 1:5	{2 3 4 27 29 }
			CL 2:1	{22 }
11.mpi.cust.0K10	sing.actual	4	CL 0:3	{24 38 39 }
			CL 1:31	-
			CL 2:5	{2 3 4 27 29 }
			CL 3:1	{22 }
11.mpi.cust.0K10	doub.orig	2	CL 0:39	-
			CL 1:1	**{0}**
11.mpi.cust.0K10	doub.orig	3	CL 0:32	-
			CL 1:7	-
			CL 2:1	**{0}**
11.mpi.cust.0K10	doub.orig	4	CL 0:32	-
			CL 1:7	-
			CL 2:1	**{0}**
11.mpi.cust.0K10	doub.log10	2	CL 0:39	-
			CL 1:1	**{0}**
11.mpi.cust.0K10	doub.log10	3	CL 0:32	-
			CL 1:7	-
			CL 2:1	**{0}**
11.mpi.cust.0K10	doub.log10	4	CL 0:32	-
			CL 1:7	-
			CL 2:1	**{0}**
11.mpi.cust.0K10	doub.actual	2	CL 0:39	-
			CL 1:1	**{0}**
11.mpi.cust.0K10	doub.actual	3	CL 0:32	-
			CL 1:7	-
			CL 2:1	**{0}**
11.mpi.cust.0K10	doub.actual	4	CL 0:32	-
			CL 1:7	-
			CL 2:1	**{0}**
		TOP Suspicious Traces to check	**1-0 2-2 3-3**	-

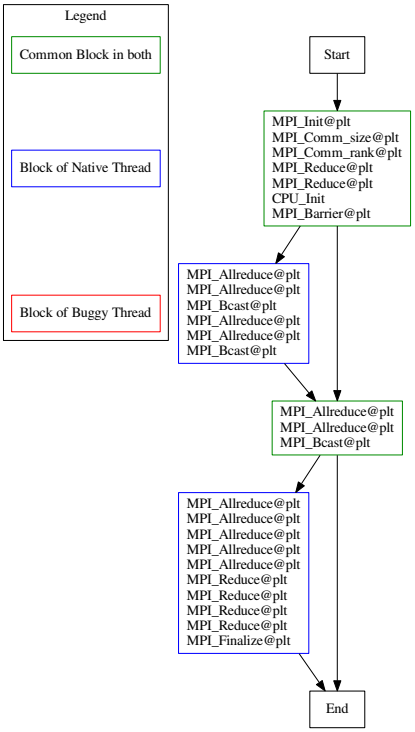


Figure 11. Bug2: diffNLR $PT_{3,0}$ - buggy vs. native

2) Bug2: Wrong Size in MPI AllReduce() (one process): We have injected a bug (row 2 table IX) where `MPI_Allreduce()` had been invoked with a wrong size. **::MORE EXPLANATIONS ABOUT WHAT THE BUG IS::**

Similar to table X, the same ranking system tells us to check $PT_{1,0}$ and $PT_{3,0}$. Note that the bug injected to only one process (P_3) to have the wrong size.)

::EXPLANATIONS OF OBSERVATIONS::

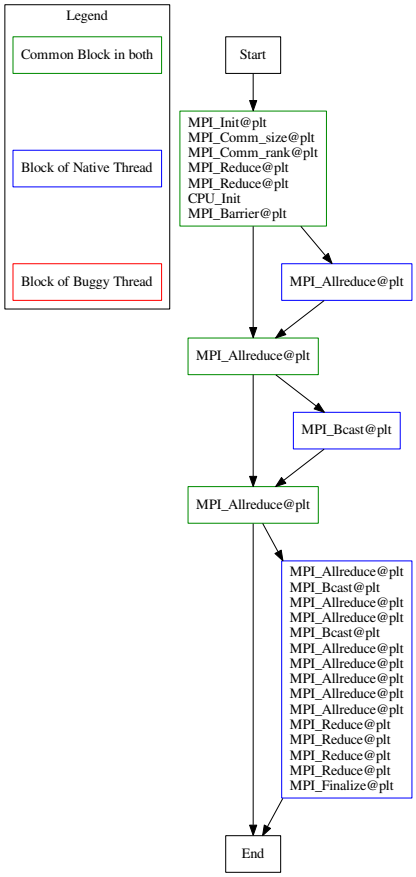


Figure 12. Bug2: diffNLR $PT_{1,0}$ - buggy vs. native

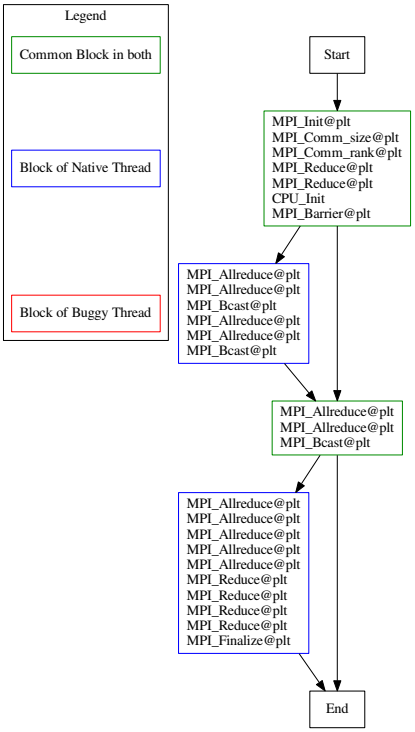


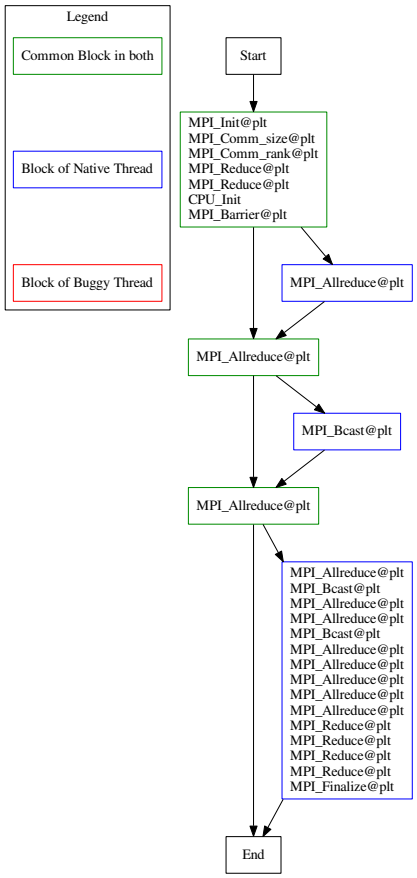
Figure 13. Bug2: diffNLR $PT_{3,0}$ - buggy vs. native

3) Bug3: Wrong Size in MPI AllReduce() (all processes): We have injected a bug (row 3 table IX) where `MPI_Allreduce()` had been invoked with a wrong size. **::MORE EXPLANATIONS ABOUT WHAT THE BUG IS::**

::What is the runtime reaction to this bug:: on node 3 (rank 3 in comm 0): Fatal error in PMPI_Bcast: Invalid root

Similar to table X, the same ranking system tells us to check $PT_{1,0}$ and $PT_{3,0}$. Note that the bug injected to only one process (P_3) to have the wrong size.)

::EXPLANATIONS OF OBSERVATIONS::



4) Bug4: Wrong Op in MPI AllReduce(): no effect!,program terminates fine: maybe all images show some reflection

5) Bug5: Wrong Size in next MPI AllReduce()(one process)::no effect, program terminates fine: maybe all images show some reflection

6) Bug6: Wrong Size in next MPI AllReduce()(all processes)::no effect,program terminates fine: maybe all images show some reflection

7) Bug7: Wrong Size in MPI Bcast()(one process)::: maybe all images show some reflection

8) Bug8: Wrong Size in next MPI Bcast()(all processes)::no effect,program terminates fine: maybe all images show some reflection

9) 3: Missing Critical Section one thread in on process: I planted the bug (missing critical section) in process 2

V. Related Work

A. Program Understanding

- Score-P [6]
- TAU [5]
- ScalaTrace: Scalable compression and replay of communication traces for HPC [21]
- Barrier Matching for Programs with Textually unaligned barriers [22]
- Pivot Tracing: Dynamic causal monitoring for distributed systems - Johnathan mace [23]
- Automated Charecterization of parallel application communication patterns [24]
- Problem Diagnosis in Large Scale Computing environments [25]
- Probablistic diagnosis of performance faults in large-scale parallel applications [26]
- detecting patterns in MPI communication traces - robert preissl [27]
- D4: Fast concurrency debugging with parallel differntial analysis - bozhen liu [28]
- Marmot: An MPI analysis and checking tool - bettina krammer [29]
- MPI-checker - Static Analysis for MPI - Alexandrer droste [30]
- STAT: stack trace analysis for large scale debugging - Dorian Arnold [7]
- DMTracker: Finding bugs in large-scale parallel programs by detecting anomaly in data movements [31]
- SyncChecker: Detecting synchronization errors between MPI applications and libraries - [32]
- Model Based fault localization in large-scale computing systems - Naoya Maruyama [33]
- Synoptic: Studying logged behavior with inferred models - ivan beschastnikh [34]
- Mining temporal invariants from partially ordered logs - ivan beschastnikh [35]
- Scalable Temporal Order Analysis for Large Scale Debugging - Dong Ahn [36]
- Inferring and asserting distributed system invariants - ivan beschastnikh - stewart grant [37]
- PRODOMETER: Accurate application progress analysis for large-scale parallel debugging - subatra mitra [38]
- Automaded : Automata-based debugging for dissimilar parallel tasks - greg [39]
- Automaded : large scale debugging of parallel tasks with Automaded - ignacio [8]
- Inferring models of concurrent systems from logs of their behavior with CSight - ivan [40]

B. Trace Analysis

- Trace File Comparison with a hierarchical Sequence Alignment algorithm [41]
- structural clustering : matthias weber [42]
- building a better backtrace: techniques for postmortem program analysis - ben liblit [43]
- automatically charecterizing large scale program behavior - timothy sherwood [44]

C. Visualizations

- Combing the communication hairball: Visualizing large-scale parallel execution traces using logical time - katherine e isaacs [45]
- recovering logical structure from charm++ event traces [46]
- ShiViz - Debugging distributed systems - [47]

D. Concept Lattice and LCA

- Vijay Garg - Applications of lattice theory in distributed systems
- Dimitry Ignatov [**?**] - Concept Lattice Applications in Information Retrieval
- [14] [18] [48] [15] [19]

E. Repetitive Patterns

- [49] [50] [51] [52] [53]

F. STAT

Parallel debugger STAT[7]

- STAT gathers stack traces from all processes
- Merge them into prefix tree
- Groups processes that exhibit similar behavior into equivalent classes
- A single representative of each equivalence can then be examined with a full-featured debugger like TotalView or DDT

What STAT does not have?

- FP debugging
- Portability (too many dependencies)
- Domain-specific
- Loop structures and detection

45	(7)11.mem.ompcrit.cust.0K10	sing.actual	1:(3_0,4_0):0.75	1:(2_1,3_1):0.00	1:(3_2,6_2):0.57	1:(1_3,2_3):0.89
			2:(2_0,3_0):0.75	2:(0_1,4_1):0.00	2:(3_2,5_2):0.57	2:(6_3,7_3):0.89
			3:(1_0,6_0):0.75	3:(0_1,5_1):0.00	3:(2_2,4_2):0.50	3:(4_3,6_3):0.50
46	(7)11.mem.ompcrit.cust.0K10	sing.log10	1:(3_0,4_0):0.75	1:(2_1,3_1):0.00	1:(0_2,2_2):0.33	1:(1_3,2_3):0.33
			2:(2_0,3_0):0.75	2:(0_1,4_1):0.00	2:(3_2,7_2):0.33	2:(6_3,7_3):0.33
			3:(1_0,6_0):0.75	3:(0_1,5_1):0.00	3:(3_2,6_2):0.33	3:(1_3,4_3):0.20
47	(7)11.mem.ompcrit.cust.0K10	sing.orig	1:(3_0,4_0):0.75	1:(2_1,3_1):0.00	1:(0_2,2_2):0.33	1:(1_3,2_3):0.33
			2:(2_0,3_0):0.75	2:(0_1,4_1):0.00	2:(3_2,7_2):0.33	2:(6_3,7_3):0.33
			3:(1_0,6_0):0.75	3:(0_1,5_1):0.00	3:(3_2,6_2):0.33	3:(1_3,4_3):0.20

Figure 14. Part of ranking table for MisCrit 1-1

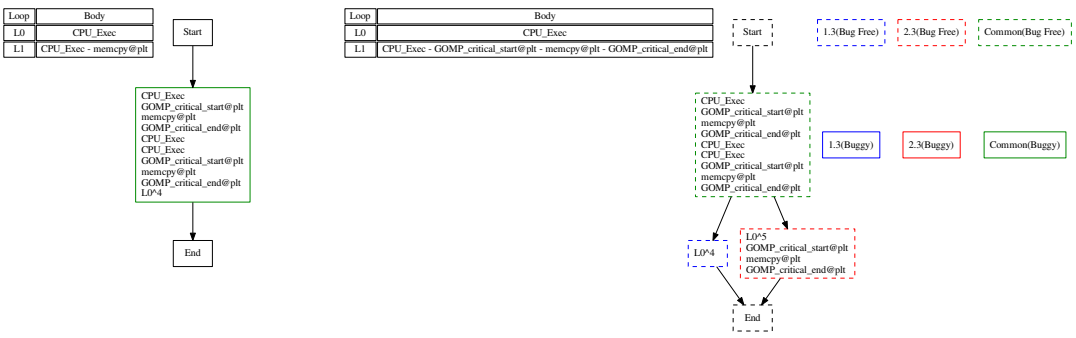


Figure 15. diffNLR of process 1 thread 3 and process 2 thread 3 buggy(missing critical section) vs. bug-free

VI. Concluding Remarks

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APPENDIX